

PROPOSING A NEW STRUCTURE TO THE ELECTROMAGNETIC WAVE - A NEW SOLUTION TO THE MAXWELL'S EQUATIONS IN VACUUM

V.A.Induchoodan Menon,
9, Readers' Row Houses, Gujarat University,
Ahmedabad-380009, Gujarat, India.
e-mail: induchoodanmenon@yahoo.co.in

Abstract

The author shows that the Maxwell's equations in vacuum have solutions which have helical structure in space while being circularly polarized at the same time. This goes against the universally accepted solutions which treat the electromagnetic wave as sinusoidal wave propagating along a linear path. He shows that the helical wave structure assumes that the fundamental state of the electromagnetic wave is the circularly polarized state and not the linearly polarized state. Since the photon is theorized to exist in a circularly polarized state, the proposed new solution is consistent with that picture. The author proposes a simple experiment using maser to confirm the veracity of the proposed helical structure.

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1 Introduction

We know that the beauty of the Maxwell's equations (given below) is that while they are very simple linear equations, all aspects of electromagnetism could be explained by them.

$$\begin{aligned} (i) \quad \nabla \cdot \boldsymbol{\xi} &= \rho/\epsilon_o, & (ii) \quad \nabla \times \boldsymbol{\xi} &= -\partial \mathbf{B}/\partial t, \\ (iii) \quad \nabla \cdot \mathbf{B} &= 0. & (iv) \quad c^2 \nabla \times \mathbf{B} &= \mathbf{j}/\epsilon_o + \partial \boldsymbol{\xi}/\partial t \end{aligned} \quad (1)$$

Since we propose to study the transmission of the electromagnetic (EM) waves in vacuum, we shall take the charge density, ρ and the electric current density \mathbf{j} as zero which gives

$$\begin{aligned} (i) \quad \nabla \cdot \boldsymbol{\xi} &= 0, & (ii) \quad \nabla \cdot \boldsymbol{\xi} &= -\partial \mathbf{B}/\partial t, \\ (iii) \quad \nabla \cdot \mathbf{B} &= 0. & (iv) \quad c^2 \nabla \times \mathbf{B} &= \partial \boldsymbol{\xi}/\partial t. \end{aligned} \quad (2)$$

We shall now solve these equations to see how the concept of the EM wave emerges from them. Subsequently we shall modify the approach suitably to arrive at the new solutions. We shall follow Feynman's insightful approach here in solving these equations in the conventional way [1]. We know that the first equation can be written as

$$\nabla \cdot \boldsymbol{\xi} = \frac{\partial \xi_x}{\partial x} + \frac{\partial \xi_y}{\partial y} + \frac{\partial \xi_z}{\partial z} = 0. \quad (3)$$

Here we assume that there are no variations with y and z , so that the last two terms could be taken as zero. Hence, we have

$$\frac{\partial \xi_x}{\partial x} = 0. \quad (3A)$$

This means that ξ_x is a constant in the x -direction. If we study Maxwell's equation (2.iv), assuming that just as in the case of the electric field, there is no variation in y and z directions in the magnetic field also, it can be seen that E_x is also a constant in time. Such a field could be conveniently taken as zero as we are interested in only dynamic fields. Therefore we may take $E_x = 0$. In other words, the electric field exists only in the y and z directions which are perpendicular to the direction of propagation. As a first step, for the sake of simplicity, we may assume that the electric field has a component only in the y -direction and obtain a solution on that basis. Later we may take up the case where the electric field has a component only in the z -direction. Then, the general solution could always be expressed as the superposition of the two cases.

Let us take the Maxwell's equation (2.ii) and equate the projections along the three coordinate axes separately to obtain

$$(\nabla \times \xi)_x = \frac{\partial \xi_z}{\partial y} - \frac{\partial \xi_y}{\partial z}; \quad (\nabla \times \xi)_y = \frac{\partial \xi_x}{\partial z} - \frac{\partial \xi_z}{\partial x}; \quad (\nabla \times \xi)_z = \frac{\partial \xi_y}{\partial x} - \frac{\partial \xi_x}{\partial y}. \quad (4)$$

Here $(\nabla \times \xi)_x$ will be zero because the derivatives with regard to y and z are zero. Note that from (3) we have already taken ξ_y as a constant while ξ_z is taken as zero. $(\nabla \times \xi)_y$ is zero because the first term which is a derivative of ξ_x is zero while the second term is zero for reasons already stated. The only component of $\text{curl} \xi$ which is not zero is $(\nabla \times \xi)_z$ which is equal to $\partial \xi_y / \partial x$. Setting the three components of $(\nabla \times \xi)$ equal to the corresponding components of $-\partial \mathbf{B} / \partial t$, we obtain

$$\frac{\partial B_x}{\partial t} = 0; \quad \frac{\partial B_y}{\partial t} = 0; \quad \frac{\partial B_z}{\partial t} = -\frac{\partial \xi_y}{\partial x}. \quad (5)$$

Since the x and y components of the magnetic field have zero time derivatives, they represent constant fields. If we study Maxwell's equation (2.ii), it can be seen that B_x is also a constant in time. Such a field could be conveniently taken as zero as we are interested in only dynamic fields. Therefore, we may take $B_x = 0$. The last equation in (5) shows that the electric field has only the y -component while the magnetic field has only the z -component. This means ξ and \mathbf{B} are perpendicular to each other.

Let us now take the last Maxwell's equation whose components can be written as

$$c^2 [\nabla \times \mathbf{B}]_x = c^2 \frac{\partial B_z}{\partial y} - c^2 \frac{\partial B_y}{\partial z} = \frac{\partial \xi_z}{\partial t}; \quad c^2 [\nabla \times \mathbf{B}]_y = c^2 \frac{\partial B_x}{\partial z} - c^2 \frac{\partial B_z}{\partial x} = \frac{\partial \xi_y}{\partial t};$$

$$c^2[\nabla \times \mathbf{B}]_z = c^2 \frac{\partial B_y}{\partial x} - c^2 \frac{\partial B_x}{\partial y} = \frac{\partial \xi_x}{\partial t}. \quad (6)$$

Out of these, only the term $\partial B_z / \partial x$ is not equal to zero. So these three equations gives us simply

$$-c^2 \frac{\partial B_z}{\partial x} = \frac{\partial \xi_y}{\partial t}. \quad (7)$$

Now taking partial differentiation with retard to t and using the last equation in (5), we obtain the wave equations

$$\frac{\partial^2 \xi_y}{\partial x^2} - \frac{1}{c^2} \frac{\partial^2 \xi_y}{\partial t^2} = 0 ; \quad \frac{\partial^2 B_z}{\partial x^2} - \frac{1}{c^2} \frac{\partial^2 B_z}{\partial t^2} = 0. \quad (8)$$

Similarly we can obtain the wave equation for ξ_z and B_y also as

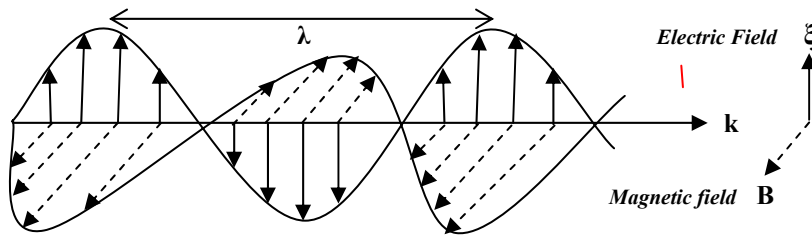
$$\frac{\partial^2 \xi_z}{\partial x^2} - \frac{1}{c^2} \frac{\partial^2 \xi_z}{\partial t^2} = 0 ; \quad \frac{\partial^2 B_y}{\partial x^2} - \frac{1}{c^2} \frac{\partial^2 B_y}{\partial t^2} = 0. \quad (8A)$$

We know the solutions for the wave equations are given by

$$\psi_y = \xi_y e^{-i(\omega t - kx)} ; \quad \psi_z = \xi_z e^{-i(\omega t - kx)}. \quad (9)$$

$$\psi_y' = B_y e^{-i(\omega t - kx)} ; \quad \psi_z' = B_z e^{-i(\omega t - kx)}.$$

where ω is the angular frequency and k is the wave vector. Combining both, the wave equation



The electric and the magnetic fields are perpendicular to each other and the direction of propagation. Note that the sinusoidal curve represents the field on the line of propagation.

Figure 1

in a general direction will be given by

$$\psi = \xi e^{-i(\omega t - \mathbf{k} \cdot \mathbf{r})}. \quad (9A)$$

Similarly, we may obtain the wave equation for the magnetic component also which may be written as

$$\psi' = \mathbf{B} e^{-i(\omega t - \mathbf{k} \cdot \mathbf{r})} . \quad (9B)$$

Note that the magnetic field will always be perpendicular to the electric field. Another important point to be kept in mind is that the solutions represent not a single wave, but a wave front which has its components of the electric field ξ_y and ξ_z (also the corresponding magnetic fields) constant along the y and z directions at any instant.

2 The New Solutions of Maxwell's Equations

We shall now look for the solution of the Maxwell's equations in a different way. Earlier in (3) we had taken $\partial \xi_y / \partial y = \partial \xi_z / \partial z = 0$, which lead us to the result, $\partial \xi_x / \partial x = 0$. The assumption, $\partial \xi_y / \partial y = \partial \xi_z / \partial z = 0$ means that at any instant, the electric field in the transverse directions is a constant one. In fact, to satisfy the condition of zero divergence for the electric field we need not take ξ_y and ξ_z as constants. We may as well take

$$\frac{\partial \xi_y}{\partial y} = - \frac{\partial \xi_z}{\partial z} . \quad (10)$$

Note that this relation when applied in (3) gives us the equation, $\partial \xi_x / \partial x = 0$. Let us examine the implications of such an assumption. The relation given in (10) shows that the electric field has a gradient along the y and z directions. But note that when ξ_y increases with y, ξ_z decreases with z.

The simplest way to interpret (10) is to assume ξ_y and ξ_z to be the field at a point which undergoes simple harmonic motion (SHM) along y and z directions simultaneously. We may attribute the field at the point to be directly proportional to the displacement from the x-axis. There are four ways of defining ξ_y , ξ_z , y and z so that (10) is satisfied. They are

$$\xi_y = \pm \alpha y \quad \text{and} \quad \xi_z = \mp \alpha z , \quad (11)$$

$$\text{where } y = R \cos[\omega t - kx] \quad \text{and} \quad z = \mp R \sin[\omega t - kx]. \quad (11A)$$

Of these four possibilities, right now we shall take up the first case given by the following set of equations for study.

$$\xi_y = \alpha y \quad \text{and} \quad \xi_z = -\alpha z , \quad (12)$$

$$\text{where } y = R \cos[\omega t - kx] \quad \text{and} \quad z = -R \sin[\omega t - kx]. \quad (12A)$$

Note that the helical wave defined by (12) and (12A) will be executing rotation in the clockwise direction. We may attribute to any point on the helical path a magnetic field which is perpendicular to the resultant of ξ_y and ξ_z at that point. This is to state that the point which is

executing the SHM has got electric and magnetic fields which are perpendicular to each other and also perpendicular to the x-axis. We may take

$$B_z = \alpha y \quad ; \quad B_y = \alpha z \quad . \quad (12B)$$

Note the difference between (12B) and (12). Here the B_z depends on y , not on z . Likewise, B_y depends on z , not y . Now we observe that for a given value of x , the locus of the point which has field components (ξ, \mathbf{B}) where $\xi = (\xi_y + \xi_z)$ and $\mathbf{B} = (B_y + B_z)$ will be a circle with radius R because we have

$$y^2 + z^2 = R^2 \quad . \quad (12C)$$

From (12) and (12B) one may get the impression that there is nothing to limit the magnitude of the electric and the magnetic fields. However, the fact the frequency of the SHMs in the transverse directions has to be equal to that of the wave propagation introduces a limit to the value of R to $1/k$. We shall be discussing this issue in detail in section 4.

Let us now proceed further with this line of reasoning. Let us now take equation (4)

$$\frac{\partial \xi_z}{\partial y} - \frac{\partial \xi_y}{\partial z} = -\frac{\partial B_x}{\partial t} \quad ; \quad \frac{\partial \xi_x}{\partial z} - \frac{\partial \xi_z}{\partial x} = -\frac{\partial B_y}{\partial t} \quad ; \quad \frac{\partial \xi_y}{\partial x} - \frac{\partial \xi_x}{\partial y} = -\frac{\partial B_z}{\partial t} \quad (13)$$

On the basis of (11), we observe that $\partial \xi_z / \partial y = \partial \xi_y / \partial z = 0$. Further, since $\xi_x = 0$ everywhere, its derivative will also be zero. This would leave us with

$$\frac{\partial B_x}{\partial t} = 0 \quad ; \quad \frac{\partial B_y}{\partial t} = \frac{\partial \xi_z}{\partial x} \quad ; \quad \frac{\partial B_z}{\partial t} = -\frac{\partial \xi_y}{\partial x} \quad . \quad (13A)$$

Let us now take the last Maxwell's equation whose components can be written as

$$\begin{aligned} c^2 [\nabla \times \mathbf{B}]_x &= c^2 \frac{\partial B_z}{\partial y} - c^2 \frac{\partial B_y}{\partial z} = \frac{\partial \xi_z}{\partial t} \quad ; \quad c^2 [\nabla \times \mathbf{B}]_y = c^2 \frac{\partial B_x}{\partial z} - c^2 \frac{\partial B_z}{\partial x} = \frac{\partial \xi_y}{\partial t} \quad ; \\ c^2 [\nabla \times \mathbf{B}]_z &= c^2 \frac{\partial B_y}{\partial x} - c^2 \frac{\partial B_x}{\partial y} = \frac{\partial \xi_x}{\partial t} \quad . \end{aligned} \quad (14)$$

Here unlike in the case of ξ_y and ξ_z , we have $\partial B_z / \partial y = \alpha = \partial B_y / \partial z$. This will make $[\nabla \times \mathbf{B}]_x = 0$. Of the remaining derivatives given in (14), only $\partial B_z / \partial x$ and $\partial B_y / \partial x$ will not be zero. Therefore (13) can be simplified to give

$$-c^2 \frac{\partial B_z}{\partial x} = \frac{\partial \xi_y}{\partial t} \quad ; \quad c^2 \frac{\partial B_y}{\partial x} = \frac{\partial \xi_z}{\partial t} \quad . \quad (14A)$$

Now using the above equation as well as (13A) and taking partial differentiation with retard to t and we obtain the wave equations

$$\frac{\partial^2 \xi_y}{\partial x^2} - \frac{1}{c^2} \frac{\partial^2 \xi_y}{\partial t^2} = 0; \quad \frac{\partial^2 B_z}{\partial x^2} - \frac{1}{c^2} \frac{\partial^2 B_z}{\partial t^2} = 0. \quad (15)$$

$$\frac{\partial^2 \xi_z}{\partial x^2} - \frac{1}{c^2} \frac{\partial^2 \xi_z}{\partial t^2} = 0; \quad \frac{\partial^2 B_y}{\partial x^2} - \frac{1}{c^2} \frac{\partial^2 B_y}{\partial t^2} = 0. \quad (15A)$$

We know that the general solution for these equations are given by (9A) itself. In other words, despite the fact that the wave represented in (15) and (15A) are helical waves existing in the physical space, we obtain the same wave function as given in (9A) as the solution.

Let us now examine the solution obtained in depth. We observe that although (15) and (15A) together represents a circularly polarized wave travelling along a helical path with its axis along the x-axis, its form is same as what we obtained for the wave travelling along the x-axis. In fact, it is easy to see that the helical path will coincide with the linear path when we take the radius of the helical path to be zero. In that sense, the helical path solution is more general than the linear path solution. The fact that (15) and (15A) do not express the physical amplitude of the wave should not be taken as a serious defect in the solution. Note that the wave equation for the electric and the magnetic fields appear as separate wave equations. In a similar way, we may express the wave equations representing the spatial oscillations also by way of separate equations. For this, we substitute for ξ_y and ξ_z from (12) into (15) and (15A) to obtain

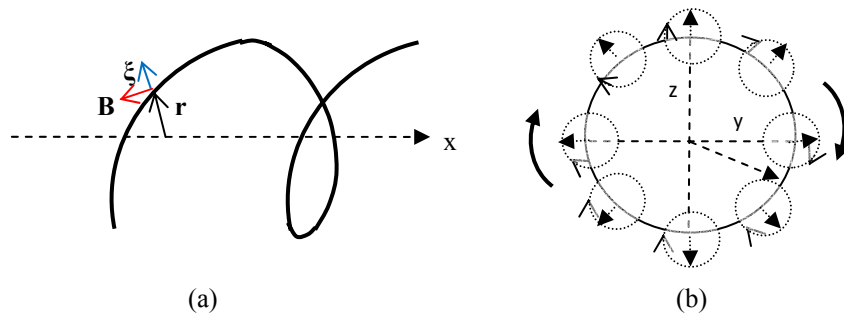
$$\frac{\partial^2 y}{\partial x^2} - \frac{1}{c^2} \frac{\partial^2 y}{\partial t^2} = 0; \quad \frac{\partial^2 z}{\partial x^2} - \frac{1}{c^2} \frac{\partial^2 z}{\partial t^2} = 0. \quad (15B)$$

We should keep in mind that all these wave equations involving ξ_y , B_y , ξ_z , B_z , y and z are coupled. Since the conventional approach treats the radius of the helical wave in the real space as zero, the amplitude of the oscillations in the physical space turns out to be zero. Therefore, the wave as defined in (15B) does not make its appearance in the conventional approach.

We saw that in the case of the conventional solutions discussed in the previous section, ξ_y and ξ_z has no variation in the y and z directions. The variations in ξ_y and ξ_z are in the x-direction and they travel as a wave front. In the case of the helical wave solution obtained now, we observe that ξ_y and ξ_z would vary in the y and z directions. In fact, they vary in proportion to the displacement from the axis. In this case, we have to examine how the wave front is formed. It is reasonable to assume that the displacement of the point along the y and z directions will set off disturbance in those directions. Therefore, we can imagine a wave front of helical waves moving parallel to each other just like in the conventional approach. The only difference is that here we have a front constituted by the helical waves while in the conventional approach the wave front is constituted by the linear waves.

The form of the EM wave in terms of the new solution will be as given in figure 2. If we take any point on the helical wave with its axis along the x-axis, then the electric field will be directed perpendicular to the x-axis in the y-z plane in the direction of the radius vector

representing the displacement from the x-axis while the magnetic vector at the same point will be orthogonal to both the x-axis and the electric vector. Note that in the conventional approach while the wave length and the frequency are related to each other, the magnitude of the electric vector (also the magnetic vector) is not connected to them in any manner. Going by the same reasoning, the radius of the helical wave should also be able to take on any value. Actually, this lack of clarity on the value of the electric and the magnetic vectors is quite surprising. There is no reason why only this aspect of the wave should remain undefined when all other



(a) shows that the field of the EM wave moves on a helical path with the electrical field always perpendicular to the direction of propagation but parallel to the radius vector while the magnetic field is orthogonal to both electric and the direction of propagation. (b) gives the transverse cross sectional view of the helical wave. Note that the electric field (magnetic field not shown) is always directed outward in line with the radius vector.

Figure. 2

aspects (frequency and the wave length) are clearly defined for the wave. In section 5, we shall show that there is justification in limiting the spatial amplitude of the EM wave and attributing a definite value for the radius of the helical wave and consequently for the magnitude of the electric vector.

3 Solutions with the Electric Vector Oriented Differently

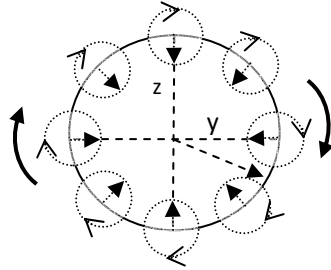
In the preceding discussion we have considered the case where the electric field is defined by (12) and (12A). This applies to the case where the radial vector and the electric field are in phase. In fact, the condition of the zero divergence of the electric field would be satisfied even if we had taken

$$\xi_y = -\alpha y \quad \text{and} \quad \xi_z = \alpha z \quad , \quad (16)$$

$$\text{where } y = R \cos [\omega t - kx] \quad \text{and} \quad z = -R \sin [\omega t - kx] \quad . \quad (16A)$$

In this case, the electric vector would be having a phase difference of π with the radius vector and hence would be directed inward when the EM wave is viewed in the direction of the propagation of the EM wave (see figure 3). Note that in this case the direction of the electric

field is the reverse of the case represented by (12) and (12A). Therefore, the field created would be in the opposite direction. This phase difference does not in any way affect the



The figure gives the view of the EM wave in the direction of the progression .Here the phase of the electric field denoted by the arrow in the epicycle differs from that of the radius vector by π .

Figure.3

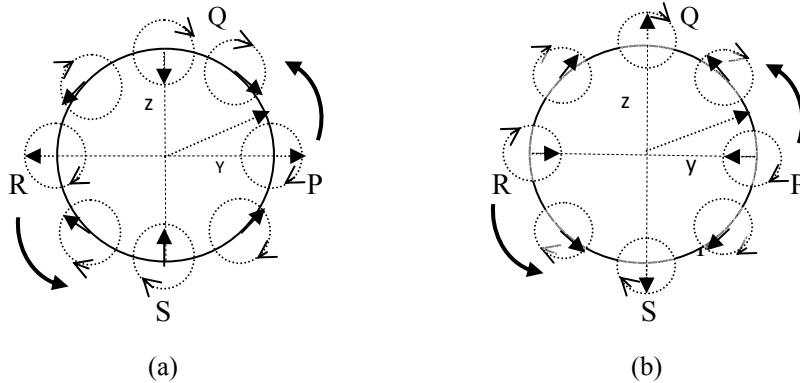
behavior of the EM wave significantly because for all practical purpose the radius of the helical wave can be treated as negligibly small and this leads us to the conventional picture of the EM wave.

Apart from these two, there are two other possibilities which we shall discuss now. The third possibility arises when we take

$$\xi_y = \alpha y \quad \text{and} \quad \xi_z = -\alpha z \quad , \quad (17)$$

$$\text{where } y = R \cos [\omega t - kx] \quad \text{and} \quad z = R \sin [\omega t - kx] \quad . \quad (17A)$$

This represents the case where the rotation of the electric field and the radial vector are in the



(a) shows the case where the rotation of the helical wave is in the anti-clockwise direction while the electric field rotates in the opposite direction. The field has positive component ξ_y at P on the y-axis and becomes $-\xi_z$ at Q, then $-\xi_y$ at R and ξ_z at S. (b) represents the case with the same direction of rotation but with the phase of of the electric vector differing from that of case (a) by π .

Figure 4

opposite directions. Here ξ_y and ξ_z are related to y and z just as in the first case. However, (17A) represents a wave which is rotating in the anti-clockwise direction (see figure 4.a). Here The electric vector does not maintain its direction with regard to the radius vector.

The fourth possibility arises when we take

$$\xi_y = -\alpha y \quad \text{and} \quad \xi_z = \alpha z , \quad (18)$$

$$\text{where } y = R \cos [\omega t - kx] \quad \text{and} \quad z = R \sin [\omega t - kx] . \quad (18A)$$

The direction of the electrical field at any point on the helical wave is given in figure 4(b). Here also the picture is similar to the third case except that there is a phase difference of π .

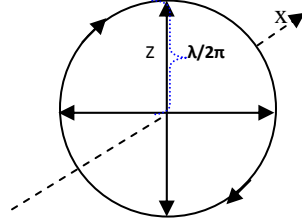
We can construct four more different combinations of the rotation of the helical wave and the electrical vector. Those would pertain to the states where the rotations of the helical wave and the electrical vector are reverse of those which are given above. Note that in the conventional description of the EM wave, these different structures would not show up since the radius of the helical wave in the physical space is taken to be zero. This would reduce the possibilities to only two helicity states which pertains to the right handed circular polarization and the left handed circular polarization. It may be possible to set up an experiment which could establish the fact that the EM wave has a helical structure in the physical space. We shall discuss about it in section 5.

4 Determining the Spatial Amplitude of the EM Wave

These new solutions of the Maxwell's equations do not alter our views regarding all the phenomena which are understood in the conventional approach. The reason why the possibility of the "new solutions" were never explored may be traced to the historical origin of the concept of the EM wave. Right from the beginning, the EM wave was thought of in terms of the linearly polarized wave and the linearly polarized state was considered as the most basic state of the wave. The circularly polarized wave was assumed to be a composite state formed by two such basic linearly polarized states with a phase difference of $\frac{1}{2}\pi$. Because of such an assumption, the solutions sought from the Maxwell's equations were for waves which are linearly polarized. And it can be easily seen from the above discussion that a linearly polarized state is not consistent with the helical structure of the wave in the physical space. It allows only such solution where the electric and the magnetic fields have no variations in the transverse directions and this is the one which is universally followed in all text books.

Let us now see if we could determine the physical amplitude of the EM wave exactly. We saw that the circularly polarized EM wave represents the locus of a point possessing electric field which undergoes two mutually orthogonal oscillations in the physical space in the transverse directions with a phase difference $\frac{1}{2}\pi$. The electric (also the magnitude of the magnetic) field at the point is directly proportional to its displacement from the x-axis, which is taken as the line of propagation of the EM wave. The path taken by such a point in the

transverse direction will be a circular one (see figure 5). The simplest case of the circular motion is obtained if we assume that it is executed at the velocity of light, c . Any other velocity would involve introduction of a new attribute to the electromagnetic wave. Since the



The figure represents transverse view of a propagating electromagnetic wave. The vertical and the horizontal lines stand for two perpendicular oscillations having phase difference of $\frac{1}{2}\pi$. Here the circular velocity is taken as c .

Figure.5

wave is also progressing with the velocity c , It is obvious that by the time the EM wave progresses the distance of one wave length, it would have executed one full circle in the transverse direction. This would mean that the circumference of the circular path is also λ . Therefore, we may conclude that the radius, R of the circle would be given by

$$R = \lambda/2\pi = 1/k \quad . \quad (19)$$

Once the value of R is fixed, then we have from (12) that

$$\xi = \alpha R = \alpha / k = (\alpha/2\pi) \lambda \quad . \quad (19A)$$

This shows that the magnitude of the electric vector is proportional to the wave length. Since the magnitude of the magnetic vector is equal to that of the electric vector in the case of the EM wave, we have

$$B = (\alpha/2\pi) \lambda \quad . \quad (19B)$$

Here it is interesting to examine the difference between the helical wave solution and the conventional solution of the Maxwell's equations. We know that the conventional solution actually represents not a single wave, but a wave front and the electric field has no gradient in the transverse directions. We should assume that the solution also represents a wave front and not a single wave. Note that when the radius of the helical wave is taken to be zero, the new solution should coincide with the conventional approach. In other words, if we introduce a scale where the radius of the helical wave is negligibly small, then, the new solutions also would lead to zero gradient of the field in the transverse direction. The only difference is that in small regions in the transverse direction, the electric field would be proportional to the

spatial displacement from the line of propagation. Viewed in this manner, the picture presented by the new solutions become quite clear and understandable.

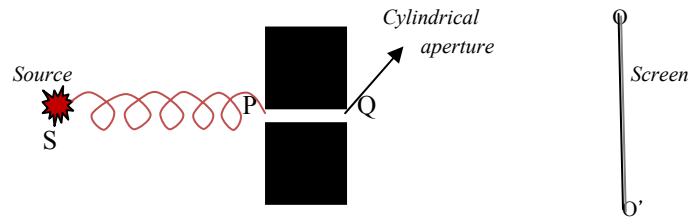
5 Discussion

It is quite surprising that the solutions of the Maxwell's equations in terms of the helical waves have been overlooked for so long. We know that photon, as it possesses unit spin, has to be treated as a circularly polarized state. In that sense, the new solutions are consistent with this treatment. But strictly speaking a photon cannot be treated as a wave as it represents the particulate aspect of light. All the same, the circular polarized state appears to be more fundamental than the linear one. But we should keep in mind that a linearly polarized state can be obtained by the superposition of two circularly polarized states of opposite helicity. Here we are forced to redefine the term helicity because now we have two types of rotations which have to be reckoned. The first one is the rotation of the electric (and also the magnetic) vector and the second one is the rotation of the spatial amplitude which gives it the helical structure. In the conventional approach also the rotation of the spatial amplitude can be introduced. But since the magnitude of the amplitude is zero, this rotation does not become apparent. Strictly speaking, the helicity could be attributed to the rotation of the spatial amplitude instead of the rotation of the electric field. In other words, the spin could be attributed to the rotation of only the spatial amplitude. The rotation of the electric vector may have to be taken as an additional attribute different from spin. In the conventional approach, both rotations coincide and therefore this issue does not arise. The rotation of the electric vector may provide us with a new quantum number. This aspect needs to be investigated further.

When we combine two EM waves having different phases for their spatial oscillations and the oscillations of the electric field, we obtain a number of possibilities which could be easily worked out. We may get a case where the wave is circularly polarized as far as the electric vector is concerned, but it could be linearly polarized for its spatial amplitude. Likewise, the EM wave could be circularly polarized for its spatial amplitude, but could be linearly polarized for its electric vector. However, it can be easily seen that whichever way we combine two circularly polarized helical waves of the same frequency, the resultant linearly polarized wave will have amplitude in the physical space. On the other hand, if we combine two waves having their frequencies close to each other, then, the amplitude could vanish almost completely in a small region due to the destructive interference and show up elsewhere resulting in the formation of beats. Therefore, it is necessary to have a source of monochromatic light to verify the correctness of the proposed helical structure of the EM wave.

The problem we face when we want to measure the helical structure of the EM wave is that this property gets camouflaged by the formation of the secondary waves formed with each point on the original wave as a source. To overcome this problem we may take the length of

the aperture to be around one wave length. Now if we observe the photons passing through a hollow cylinder of length, say equal to the wave length of the photon to be observed. The



S is a very weak monochromatic microwave source. PQ is the cylindrical adjustable aperture while OO' represents the screen which measures the intensity of the microwave falling on it. If the helical wave hypothesis is correct, the aperture could block all waves having wave length more than $2\pi r$.

Figure. 6

experimental set up is very simple (see figure.6). We have to have a source of EM wave preferably Maser (even a monochromatic source in the microwave region will do) having wavelength in the range of , say, 0.10 m. A metal sheet of 0.10 m thickness having a cylindrical aperture (PQ) with adjustable radius could be installed close to the Maser source. It is important to have the length of the aperture in the range of the wave length of the EM wave to be used to avoid formation of the secondary waves at Q. A screen should be place behind the metal sheet to capture the microwave energy passing through the aperture.

Let the cylindrical aperture be kept very large to begin with. The intensity of the energy received on the screen from the Maser source will be quite high. Now as we reduce the radius of the cylindrical aperture, the intensity received on the screen would keep on decreasing. If the helical wave hypothesis is correct, then when the radius of the aperture becomes less than $\lambda/2\pi$, there should be a sudden drop in the intensity of the energy received on the screen. In principle, there should be an absolute cut off at this aperture. But then due to interference which cannot be avoided completely, some energy may leak through the aperture. But the dip in the energy intensity received on the screen should be sharp. In the conventional approach, the aperture radius of $\lambda/2\pi$ does not have any significance and therefore the reduction in the intensity should be smooth.

Another foolproof method to check the veracity of the hypothesis is to use a source of the monochromatic radiation in the microwave range so weak that only one photon is emitted at an instant. This way the possibility of two waves interfering with each other and affecting its basic structure could be avoided. Since the light source is so weak that it emits only one photon in one instant, the helical structure of the wave would be maintained. Here some objection could be raised against the proposal on the ground that the moment we opt for the photon picture, we have to discard the wave picture, and treat the photon as a point particle. To avoid such controversies, we just propose that the wave train emitted by the source is a single one at a time so that there is no interference to destroy its basic structure. We shall make the radius of

the cylindrical aperture adjustable. Initially, the radius of the aperture may be kept at twice the wave length of the wave as in the earlier experiment. If the basic structure of the EM radiation is a helical one in space with a radius $\lambda/2\pi$, then there should be a clear cut off of the radiation passing through the aperture when its radius becomes $\lambda/2\pi$. In terms of the conventional approach, there will not be any cut off although the intensity may fall off. So the existence of a cut off at the aperture radius of $\lambda/2\pi$ will be the proof for the helical structure of the EM wave.

References:

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