

The Derivation of the Schwarzschild Solution from a Scalar Model of Spherical Quantum Waves

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It is shown that if space is modeled as an elastic medium that propagates spherical, scalar quantum-waves, then the ratio of the square of the wave velocity to c^2 reveals the same results as the familiar time dilation formula that is produced from the Schwarzschild G_{44} component. The Schwarzschild radius derived from the scalar-wave model is shown to be equal to the radius of the universe, implying that there are no gravitational singularities present within the radius of the universe.

1. Introduction

Einstein's highly coupled, non-linear field equations were based on the postulate that mass warps surrounding space. The solution to these equations for a spherically symmetric, non-rotating mass was found by Schwarzschild in 1916 and the G_{44} component describes the Schwarzschild radius and time dilation effect of the mass [1]. This result has led to the conclusion that a mass occupying a radius less than the Schwarzschild radius must be a black hole which consumes matter and from which light cannot escape gravitationally. It will be shown that the time-dilation formula from G_{44} can be reproduced with simple potential-energy equations that describe the speed at which spherical quantum waves propagate in an elastic space fabric. The resulting singularity from this scalar model shows that the radius of the singularity is the radius of the universe, a natural consequence of escape velocity as modeled by Newtonian gravitation. The time-dilation formulas that result from this Newtonian model duplicate the G_{44} solution without the complexity of a singularity and its associated problems.

2 The Spherical Wave Model

Albert Einstein first developed the concept that mass warps surrounding space. The same concept in reverse is part of the elastic space model proposed, where the compression length of space determines the rest energy of a particle. The characteristic-compression length, r , of the space fabric will be shown to be related to the rest energy of the particle through this elastic space model, where particles are in reality the interference of two wave centers of spherical standing waves due to the compression of the space fabric. This compression is part of a standing wave structure where a spherical wave coming into the particle center combines with a spherical, outgoing wave that is propagating out of the wave center to form the two solutions of a spherical wave function which we measure as a particle at the wave center [2,3].

This wave function is not to be confused with the Schrödinger wave equation, which requires the use of Planck's constant, h , in Schrödinger's equation. The discrete nature of matter can be described with standing matter waves that have

integer wave numbers and can be described completely with Newtonian physics which is more fundamental as a unit of discreteness than the use of Planck's constant as in Schrödinger's equation.

Also, Schrödinger's wave equation is believed to propagate at instantaneous speed, although this has not been proven experimentally. It has been shown that Schrödinger's wave function travels faster than c , and faster than our current technology is capable of measuring, but not necessarily instantaneously. The spherical wave equation proposed by Wolff [2] has the features of transferring information faster than the speed of light when a shear force exists in the fabric, however standing spherical waves which create particle wave-centers always travel at the speed of light in this model as will be shown. In this sense, Wolff's spherical wave function meets the experimental requirements of a wave function that describes quantum entanglement and information transfer that is faster than c but which has a more physically-intuitive basis than the probability-density function associated with Schrödinger's equation.

Schrödinger himself disagreed with the probabilistic interpretation of his equation and instead stated the following: "Let me say at the outset, that in this discourse, I am opposing not a few special statements of quantum mechanics held today (1950's), I am opposing as it were the whole of it, I am opposing its basic views that have been shaped 25 years ago, when Max Born put forward his probability interpretation, which was accepted by almost everybody" [6]. Schrödinger also stated that "What we observe as material bodies and forces are nothing but shapes and variations in the structure of space. Particles are just *schaumkommen* (appearances)." [7]

The probability-density function of Schrödinger's equation which predicts the location of particles in space can also be interpreted as the location in space of wave peaks of a standing wave which must have an integer number of full wavelengths within the given length of the standing wave motion. The larger the integer number, the greater probability of a particle in any given region of space. From this interpretation, the prediction of wave-centers of a particle becomes deterministic instead of probabilistic, based on the analysis of a fixed standing wave. Thus, the experimental predictions of Schrödinger's wave equation may be shown to be equivalent to a deterministic, standing matter wave equation as shown originally by interpretation of the Bohr radius

in the Hydrogen atom as an integer number of matter wave-lengths.

The form of the basic spherical wave equation of amplitude Φ for waves moving at speed c is:

$$\nabla^2 \Phi - \frac{1}{c^2} \frac{\partial^2 \Phi}{\partial t^2} = 0 \quad (1)$$

The two amplitude solutions of the wave equation are as follows:

$$\Phi^{IN} = \frac{A_0}{r} e^{(i\omega t + ikr)} \quad (2)$$

$$\Phi^{OUT} = \frac{A_0}{r} e^{(i\omega t - ikr)} \quad (3)$$

The combination of (2) and (3) as follows creates the electron wave-center and removes the problem of infinite amplitude at $r = 0$:

$$\Phi^{IN} - \Phi^{OUT} = \frac{A_{in}}{r} e^{(i\omega_i t + ik_i r)} - \frac{A_{out}}{r} e^{(i\omega_o t - ik_o r)} \quad (4)$$

Where ω_i and ω_o are the in-going and outgoing mass-frequencies of the electron, which are the same if there is no relative motion and k_i and k_o are their associated wave numbers. Upon inspection it is seen that (4) will produce a finite amplitude at $r = 0$, as can be seen by taking the limit as r approaches 0. This eliminates the need for renormalization of the function that is found in dealing with the electron radius and the renormalization procedures of QFT.

As the solutions (2) and (3) are scalar equations that are independent of θ and ϕ and are only dependent upon the spherical coordinate r , we may simplify the equations for the compression force produced by both incoming and outgoing waves as follows:

$$\left\| \partial \Phi^2 / \partial r \right\| = F \approx kr \quad (5)$$

where F is the force of compression given by the partial derivative of the potential with respect to r , r is the distance over which the space fabric is compressed, and k is the elastic constant of space. By integrating the force law of (5) from a chosen reference $r = 0$ to any arbitrary point r in the space fabric, and setting the result equal to the rest-energy of a particle we obtain:

$$mc^2 = \frac{1}{2} kr^2 \quad (6)$$

where m is the mass of the particle and k is the elasticity constant of space. From this relation we can derive k from known quantities as follows. If $m =$ the mass of the Universe, 1.44×10^{53} Kg, and for $r =$ radius of the Universe, 1.9×10^{26} meters we obtain:

$$k = 7.18 \times 10^{17} \text{ Newtons/meter} \quad (7)$$

For $m =$ mass of pi-meson(+), 139.6 MeV and $r =$ range of strong nuclear force which is the maximum known nuclear radii

(7×10^{-15} meters), we obtain $k = 7.18 \times 10^{17}$ Newton/meter which is the same as (7). If $m =$ mass of electron, 9.11×10^{-31} Kg and $r =$ classical electron radius of 2.82×10^{-15} meters, then $k = 2.0 \times 10^{16}$ Newton/meters which is a factor of about 10 from (7). Also, for $r =$ the Planck length, $k = 7.18 \times 10^{17}$ Newton/meter, we find that $m = 10^{-68}$ Kg, an estimate of the photon mass as first proposed by J.P. Vigiier [4]. For the case of $r = 10^{-18}$ meters, which is the approximate weak nuclear force range and using k from (7), we find $m = 2.2 \text{ eV} / c^2$ which is a predicted mass for the electron-neutrino.

Thus, it is shown from (6) and (7) that the key force ranges for gravitational, strong, weak and electromagnetic forces yield a rest-mass of a particle that has been hypothesized or is measured in mass as the particle associated with transmitting the corresponding force.

As shown from the examples in (5) and (6), we can use a scalar formula for the speed of the spherical, standing waves in a fabric of elasticity k :

$$\text{speed} = \sqrt{kr / \sigma} \quad (8)$$

Where $k = 7.18 \times 10^{17}$ Newton/meter as previously determined from (7), r is the displacement or amplitude of the wave in the space fabric, and σ is the mass-per-unit length of the space-fabric.

For a wave that has a displacement equal to the radius of the universe, the numerator under the radical in (8) becomes:

$$F = k(10^{26} \text{ meters}) = 7.18 \times 10^{43} \text{ Newton} \quad (9)$$

Now we examine σ , or the linear mass-per-unit length of the space fabric. If we take the average mass of the Universe found from critical and average density determinations as 1.44×10^{53} Kg, and the distance that the force in (9) acts over as the radius of the Universe = 1.9×10^{26} meters, we find σ as:

$$\sigma = \frac{1.44 \times 10^{53} \text{ Kg}}{10^{26} \text{ meters}} = 1.44 \times 10^{27} \text{ Kg/meter} \quad (10)$$

$$\text{speed} = \sqrt{\frac{kR_u}{M_u / R_u}} = \sqrt{\frac{k}{M_u}} R_u = 2.28 \times 10^8 \text{ m/s} \quad (11)$$

Substituting the value for σ from (10) and the value of kR_u from (9), we find the speed of the spherical standing waves from (9) to be:

$$\text{MISSING EQ?} \quad (12)$$

Which is seen to be very nearly c . Also note that the radical in (11), $\sqrt{k / M_u} = 2.28 \times 10^{-18}$ seconds⁻¹, which is Hubble's constant, H_o . Then the familiar Hubble relation, $\text{speed} = Hr$ is revealed from (11). The speed in (11) is that of the spherical waves either going into or coming out of the center coordinates

of a particle, as the solution to the spherical wave equation yields a positive and negative solution.

3. Time Dilation Effects

From (8) and (9) we know that the upper limit for v is c and this corresponds to a tensile force equivalent to the mass of the universe and hence the speed of the incoming waves to each particle in the universe. Therefore, particles with masses smaller than M_u will exhibit a force that is less than (9) with correspondingly lower speeds for the particle's outgoing wave. If we take a given example mass of 10^6 Kg and calculate from (6) what the displacement r is (knowing k from above) we find $r = 500.6$ meters. This is the compression length in the space fabric that corresponds to this mass and because the force is less than in (9), we expect the speed of the scalar quantum waves to be less than c , which will amount to time-dilation effects at distance r from the particle of this mass.

When we substitute $r = 500.6$ meters into (8) we find $v = 0.73$ cm/sec, which is the speed of the out-going quantum wave solution from the mass at 500.6 meters from the center of the mass. There is also the pull on the example mass (10^6 Kg) from the remaining mass in the Universe (kR_u) which is similar to Mach's principle [5], and results in a velocity c of the in-going quantum waves at the particle, based on the two solutions of the wave equation.

The time dilation effects result from the ratio of the speed of outgoing to incoming quantum waves at the particle center. When we take the ratio of the out-wave speed to the in-wave speed of c we find $v/c = 2.43 \times 10^{-12}$ and

$$v^2 / c^2 = 5.90 \times 10^{-24} \tag{12}$$

From the Schwarzschild solution, the time dilation at a distance r from the center of the gravitational source M is

$$T = T_0 / \sqrt{1 - 2GM / rc^2} \tag{13}$$

For the example of the mass of 10^6 Kg and $r = 500.6$ meters, it is found that the denominator of (13) is the same as one-half of (12):

$$\frac{1}{2} v^2 / c^2 = 2.96 \times 10^{-24} = 2GM / rc^2 \tag{14}$$

where v^2 / c^2 is substituted from (12). If we apply the Lorentz transformation to (12) and the results of (14) we arrive at the formula:

$$T = T_0 / \sqrt{1 - \frac{1}{2} v^2 / c^2} \tag{15}$$

which is essentially the Lorentz transformation relating the speed of in and out waves which is equivalent to (13).

From (12) and (14), the time dilation formula of (15) is derived that is numerically equivalent to the Schwarzschild solution of (13), regardless of the mass that is chosen for the example. This is derived from the simple scalar equations of (6) and (8).

There is a difference when solving for the singularity in (15). By setting the denominator of (15) equal to 0 and substituting (8) for v we find the relation:

$$kr / \sigma c^2 = 2 \tag{16}$$

Where σ is found from (10). Then r is found from (16) to be

$$r = R_u = 1.9 \times 10^{26} \text{ meters} \tag{17}$$

indicating that the only black hole that exists is the Universe itself.

4. Conclusions

The Schwarzschild solution for time dilation is duplicated in the proposed model of spherical matter waves. Starting from a model of a spherical wave equation, the scalar formulas for force and speed are used to describe the nature of spherical waves in space, showing the speed of the waves to be c and this in turn defines the rest energy of the particle produced at the wave center of the spherical waves as mc^2 . It is shown that the particles associated with transmitting the four forces of nature can be described by an equivalence between the energy of compression in the space fabric and the rest-energy of the particle.

It is also shown that the Lorentz transformation of the outgoing spherical quantum wave to the in-going spherical quantum wave produces the same time-dilation effects as the Schwarzschild G_{44} solution from an arbitrary mass M . The similarity to a Schwarzschild radius that results from the spherical wave model is a radius that is equal to the radius of the universe, implying there are no gravitational singularities present in the universe.

References

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