# Four Prime-Generating Recurrences

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Abstract : Prime number generating recurrences are introduced . Keywords : Prime , Recurrence AMS Classification :11A41

# **1** Introduction

Let  $a_1 = 1$ , for n > 1,  $a_n = a_{n-1} + lcm(a_{n-1}, n)$  [1]. This sequence has properties related to primes. For instance  $a_{n+1}/a_n - 1$  consists of 1's or primes only.

# 2 Main result

#### Prime Number Generator I

Let  $b_n = b_{n-1} + lcm(n-1, b_{n-2})$  with  $b_1 = 2$  and  $b_2 = 2$ then  $a_n = b_{n+2}/b_n - 1$  is either 1 or prime [2].

#### Conjecture 1

1. Every term of this sequence is either prime or 1.

2. Every odd prime number is member of this sequence .

### Maxima implementation

n; ans:0; n1:2; n2:2; list:[1,1]; (for k from 3 thru n do (ans:n1+lcm(k-1,n1) , list:append(list,[ans/n1-1]) , n1:n2 , n2:ans))print(list);

### Prime Number Generator II

Let  $b_n = b_{n-1} + lcm(\lfloor \sqrt{2} \cdot n \rfloor, b_{n-1})$  with  $b_1 = 2$ then  $a_n = b_{n+1}/b_n - 1$  is either 1 or prime.

### Conjecture 2

1. Every term of this sequence is either prime of the form  $\lfloor \sqrt{2} \cdot n \rfloor$  or 1 .

2. Every prime of the form  $\lfloor \sqrt{2} \cdot n \rfloor$  is member of this sequence .

### Maxima implementation

n; ans:0; n1:2; list:[1]; (for k from 2 thru n do (ans:n1+lcm(floor(sqrt(2)\*k),n1) , list:append(list,[ans/n1-1]) , n1:ans))\$ print(list);

# Prime Number Generator III

Let  $b_n = b_{n-1} + lcm(\lfloor\sqrt{3} \cdot n\rfloor, b_{n-1})$  with  $b_1 = 3$ then  $a_n = b_{n+1}/b_n - 1$  is either 1 or prime.

# Conjecture 3

1. Every term of this sequence is either prime of the form  $\lfloor \sqrt{3} \cdot n \rfloor$  or 1 .

2. Every prime of the form  $\lfloor \sqrt{3} \cdot n \rfloor$  is member of this sequence .

# Maxima implementation

n; ans:0; n1:3; list:[1]; (for k from 2 thru n do (ans:n1+lcm(floor(sqrt(3)\*k),n1) , list:append(list,[ans/n1-1]) , n1:ans))\$ print(list);

### Prime Number Generator IV

Let  $b_n = b_{n-1} + lcm(\lfloor \sqrt{n^3} \rfloor, b_{n-1})$  with  $b_1 = 2$ then  $a_n = b_{n+1}/b_n - 1$  is either 1 or prime.

### **Conjecture 4**

1. Every term of this sequence is either prime of the form  $\lfloor \sqrt{n^3} \rfloor$  or 1. 2. Every prime of the form  $\lfloor \sqrt{n^3} \rfloor$  is member of this sequence.

#### Maxima implementation

n; ans:0; n1:2; list:[1]; (for k from 2 thru n do (ans:n1+lcm(floor( $sqrt(k^3)$ ),n1), list:append(list,[ans/n1-1]), n1:ans))\$ print(list);

# References

 OEIS Foundation Inc. (2011), The On-Line Encyclopedia of Integer Sequences, http://oeis.org/A135504.
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