Gravitation as the result of the reintegration of migrated electrons and positrons to their atomic nuclei.

Osvaldo Domann

odomann@yahoo.com

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Abstract

This paper presents the mechanism of gravitation based on an approach where the energies of electrons and positrons are stored in fundamental particles (FPs) that move radially and continuously through a focal point in space, point where classically the energies of subatomic particles are thought to be concentrated. FPs store the energy in longitudinal and transversal rotations which define corresponding angular momenta. Forces between subatomic particles are the product of the interactions of their FPs. The laws of interactions between fundamental particles are postulated in that way, that the linear momenta for all the basic laws of physics can subsequently be derived from them, linear momenta that are generated out of opposed pairs of angular momenta of fundamental particles.

The flattening of Galaxies' Rotation Curve is derived without the need of the definition of Dark Matter and the origin of Dark Energy is shown.

Finally, the quantification of the gravitation force is derived.

1 Introduction.

Our "Standard Model" describes a particle as a point-like entity with the energy concentrated on one point in space. The mechanism how forces between charged particles are generated is not explained. This limitation of our Standard Model results in the introduction of a series of artificial particles and constructions like Gluons, Bosons, Gravitons, Quarks, Higgs, particle's wave, etc., to explain the mechanism of interaction between particles.

The present approach postulates that a particle is formed by rays of Fundamental Particles (FPs) that move through a focal point in space. The relativistic energy of the particle is stored by the FPs as longitudinal and transversal rotations. Interactions between two particles are now the result of the interactions between FPs of the two particles.

The steps followed to describe mathematically the new model are:

- 1. Definition of a distribution function $d\kappa$ that assigns to each volume dV in space a differential energy dE of the total relativistic energy of the particle.
- 2. Definition of a field magnitude $d\bar{H}$ associated with the angular momenta of FPs.
- 3. Definition of interaction laws between $d\bar{H}$ fields of FPs in that way, that all forces between particles can be mathematically derived.

In what follows electrons and positrons are called "Basic Subatomic Particles" (BSPs).

The total relativistic energy of a BSP is

$$E_e = \sqrt{E_o^2 + E_p^2} = E_s + E_n \quad with \quad E_s = \frac{E_o^2}{\sqrt{E_o^2 + E_p^2}} \qquad E_n = \frac{E_p^2}{\sqrt{E_o^2 + E_p^2}}$$
 (1)

The differential energies for each differential volume are:

$$dE_e = E_e d\kappa = \nu J_e \qquad dE_s = E_s d\kappa = \nu J_s \qquad dE_n = E_n d\kappa = \nu J_n$$
 (2)

with $d\kappa$ the distribution function, ν the angular frequency and J the angular momenta.

$$d\kappa = \frac{1}{2} \frac{r_o}{r_r^2} dr \sin \varphi \, d\varphi \, \frac{d\gamma}{2\pi} \qquad dV = dr \, r \, d\varphi \, r \, \sin \varphi \, d\gamma \tag{3}$$

 $d\kappa$ is inverse proportional to the square distance to the focal point and gives the fraction of the relativistic energy for the volume dV of the FP.

FPs leaving the focal point (emitted FPs) have only longitudinal angular momenta J_e and associated to it a longitudinal emitted field $d\bar{H}_e$ defined as

$$d\bar{H}_e = H_e \ d\kappa \ \bar{s}_e = \sqrt{\nu \ J_e \ d\kappa} \ \bar{s}_e \qquad with \qquad H_e^2 = E_e \tag{4}$$

FPs moving to the focal point (regenerating FPs) have longitudinal J_s and transversal J_n angular momenta and associated to them respectively a longitudinal emitted field $d\bar{H}_s$ defined as

$$d\bar{H}_s = H_s \ d\kappa \ \bar{s} = \sqrt{\nu J_s \ d\kappa} \ \bar{s} \qquad with \qquad H_s^2 = E_s$$
 (5)

and a transversal emitted field $d\bar{H}_n$ defined as

$$d\bar{H}_n = H_n \ d\kappa \ \bar{n} = \sqrt{\nu \ J_n \ d\kappa} \ \bar{n} \qquad with \qquad H_n^2 = E_n \tag{6}$$

For the total field magnitude H_e it is $H_e^2 = H_s^2 + H_n^2$.

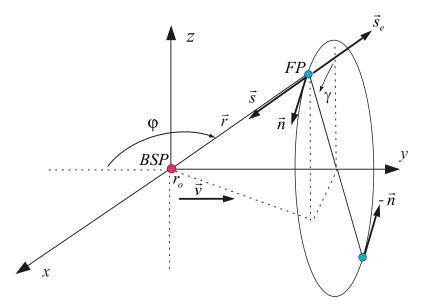


Figure 1: Unit vector \bar{s}_e for an emitted FP and unit vectors \bar{s} and \bar{n} for a regenerating FP of a BSP moving with $v \neq c$

Fig. 1 shows at the origin of the Cartesian coordinates the focus of a BSP moving with speed \bar{v} . The vector \bar{s}_e is an unit vector in the moving direction of the emitted fundamental particle (FP). The vector \bar{s} is an unit vector in the moving direction of the regenerating FP. The vector \bar{n} is an unit vector transversal to the moving direction of the regenerating FP and oriented according the right screw rule relative to the velocity \bar{v} of the BSP.

The differential linear momentum dp of a moving BSP is generated out of pairs of opposed transversal fields $d\bar{H}_n$ at the regenerating FPs of the BSP. Opposed pairs of transversal fields $d\bar{H}_n$ are generated because of the axial symmetry relative to the velocity \bar{v} of the BSP as shown in Fig. 1.

Conclusion: Basic subatomic particles (BSPs) are structured particles with longitudinal and transversal angular momenta. The sign of the angular momenta of emitted FPs define the sign of the BSP (electron or positron). The transversal field $d\bar{H}_n$ gives the mechanical linear moment and the magnetic moment.

Interaction laws between FPs of two BSPs are defined as products between their $d\bar{H}$ fields.

- Coulomb law: The close path integration of the cross product between longitudinal $d\bar{H}_s$ fields gives the Coulomb equation.
- Ampere law: The close path integration of the cross product between transversal $d\bar{H}_n$ fields gives the Lorentz, Ampere and Bragg equations.
- Induction law: The close path integration of the product between the transversal field $d\bar{H}_n$ and the absolute value of the longitudinal $d\bar{H}_s$ field of a static BSP

gives the Maxwell equations and the gravitation equations.

The fundamental equation to calculate the differential force between two BSPs is

$$dF = \frac{dp}{\Delta t} = \frac{1}{c\Delta t} dE_p = \frac{1}{c\Delta t} |d\bar{H}_1 \times d\bar{H}_2| \tag{7}$$

2 Mechanism of Gravitation.

To explain the mechanism of gravitation, the concept of reintegration of BSPs that have migrated out of their nuclei is required.

Because of $d\bar{H}_s = dH_s\bar{s}$ and $\bar{J}_s = J_s\bar{s}$ the interaction law between FPs of static BSPs (Coulomb) follows the cross product between longitudinal angular momenta $|\bar{J}_{e_1} \times \bar{J}_{s_2}| = J_{e_1} J_{s_2} \sin \beta = J_n$ of the FPs, cross product which is zero for the distance d = 0 between BSPs because of $\beta = \pi/2$.

In Fig. 2 the differential linear momentum dp_2 at BSP 2 is generated by pairs of opposed angular momentum \bar{J}_{n_2} of regenerating FPs.

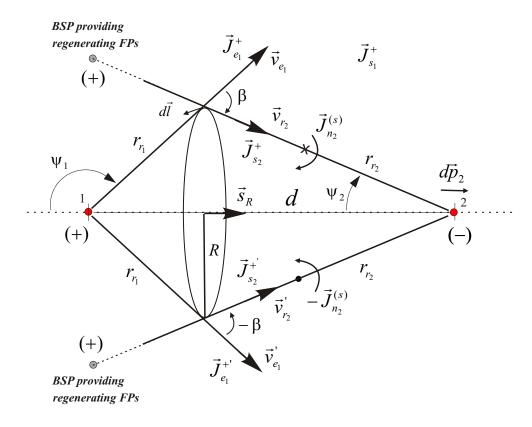


Figure 2: Generation of angular momentum J_n at regenerating fundamental particles of two static basic subatomic particles at the distance d

Fig. 3 gives the linear momentum between two BSPs as a function of the distance d. The variable r_o represents the radii of the focus of the BSPs, which are constant for non relativistic speeds.

Nucleons are composed of electrons and positrons which are concentrated in the range of $0 \le \gamma \le 0.1$ of the curve of Fig. 3 where the attractions and repulsions between them are zero.

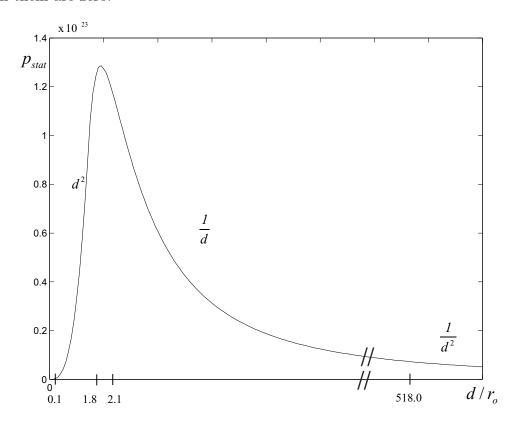


Figure 3: Linear momentum p_{stat} as function of $\gamma = d/r_o$ between two static BSPs with equal radii $r_{o_1} = r_{o_2}$

Electrons and positrons of a nucleon migrate slowly into the range of $0.1 \le \gamma \le 1.8$ polarizing the nucleon, and are subsequently reintegrated with high speed when their FPs cross with FPs of the remaining electrons and positrons of the nucleon because of $\beta < \pi/2$ (Neutron 1 at Fig. 4). Opposed linear momenta $d\bar{p}_a$ and $d\bar{p}_b$ are generated at BSPs a and b.

The movement of BSP b generates the dH_n field shown in Fig. 4, field that is passed to the static BSP p of neutron 2 according the **induction law** of sec. 1. The final result is that neutron 1 moves with the linear momentum $-d\bar{p}_a$ and neutron 2 with the opposed linear momentum $d\bar{p}_p$. The mechanism is independent of the sign of the interacting BSPs explaining the attracting force of gravitation. It is important to note that as BSPs a and b generate opposed dH_n fields that are passed to BSP p of neutron

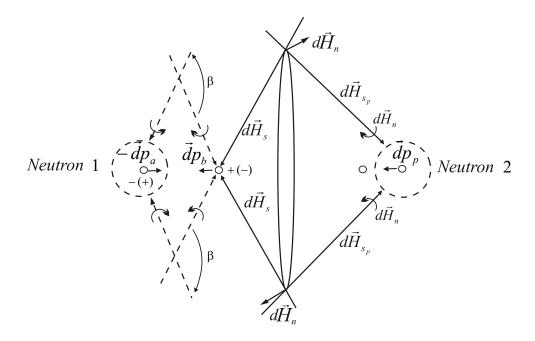


Figure 4: Transmission of momentum dp_b from neutron 1 to neutron 2

2, the field of BSP b is closer to BSP p and has a higher probability to be passed to BSP p.

3 Gravitation force.

To calculate the gravitation force induced by the reintegration of migrated BSPs, we need to know the number of migrated BSPs in the time Δt for a neutral body with mass M.

The following equation was derived in [6] for the **induced gravitation** force generated by one reintegrated electron or positron

$$F_i = \frac{dp}{\Delta t} = \frac{k c \sqrt{m} \sqrt{m_p}}{4 K d^2} \int \int_{Induction} with \qquad \int \int_{Induction} = 2.4662 \quad (8)$$

with m the mass of the reintegrating BSP, m_p the mass of the resting BSP, $k = 7.4315 \cdot 10^{-2}$. It is also

$$\Delta t = K r_o^2$$
 $r_o = 3.8590 \cdot 10^{-13} \ m$ and $K = 5.4274 \cdot 10^4 \ s/m^2$ (9)

The direction of the force F_i on BSP p of neutron 2 in Fig. 4 is independent of the sign of the BSPs and is always oriented in de direction of the reintegrating BSP b of neutron 1.

For two bodies with masses M_1 and M_2 and where the number of reintegrated BSPs in the time Δt is respectively Δ_{G_1} and Δ_{G_2} it must be

$$F_i \Delta_{G_1} \Delta_{G_2} = G \frac{M_1 M_2}{d^2} \quad with \quad G = 6.6726 \cdot 10^{-11} \frac{m^3}{kg \, s^2}$$
 (10)

As the direction of the force F_i is the same for reintegrating electrons Δ_G^- and positrons Δ_G^+ it is

$$\Delta_G = |\Delta_G^-| + |\Delta_G^+| \tag{11}$$

We get that

$$\Delta_{G_1} \Delta_{G_2} = G \frac{4 K M_1 M_2}{m k c \int \int_{Induction}}$$
(12)

or

$$\Delta_{G_1} \Delta_{G_2} = 2.8922 \cdot 10^{17} \ M_1 \ M_2 = \gamma_G^2 \ M_1 \ M_2 \tag{13}$$

The number of migrated BSPs in the time Δt for a neutral body with mass M is thus

$$\Delta_G = \gamma_G M \quad with \quad \gamma_G = 5.3779 \cdot 10^8 \ kg^{-1}$$
 (14)

Calculation example: The number of migrated BSPs that are reintegrated at the sun and the earth in the time Δt are respectively, with $M_{\odot} = 1.9891 \cdot 10^{30} \ kg$ and $M_{\dagger} = 5.9736 \cdot 10^{24} \ kg$

$$\Delta_{G_{\odot}} = 1.0697 \cdot 10^{39} \quad and \quad \Delta_{\dagger} = 3.2125 \cdot 10^{33}$$
 (15)

The power exchanged between two masses due to gravitation is

$$P_G = F_i \ c = \frac{E_p}{\Delta t} = \frac{k \ m \ c^2}{4 \ K \ d^2} \ \Delta_{G_1} \ \Delta_{G_2} \ \int \int_{Induktion}$$
 (16)

The power exchanged between the sun and the earth is, with $d_{\odot\dagger}=1.49476\cdot 10^{11}~m$

$$P_G = F_G c = G \frac{M_{\odot} M_{\uparrow}}{d_{\odot \uparrow}^2} c = 1.0646 \cdot 10^{31} J/s$$
 (17)

4 Dark matter and dark energy.

In the previous sections we have seen that the induced gravitation force is due to the reintegration of migrated BSPs in the direction of the two gravitating bodies. When a

BSP is reintegrated to a neutron, the two BSPs of different signs that interact, produce an equivalent current in the direction of the positive BSP as shown in Fig. 5.

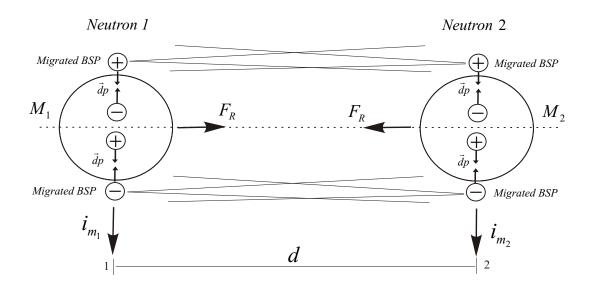


Figure 5: Resulting current due to reintegration of migrated BSPs

As the numbers of positive and negative BSPs that migrate in one direction at one neutron are equal, no average current should exists in that direction in the time Δt . It is

$$\Delta_R = \Delta_R^+ + \Delta_R^- = 0 \tag{18}$$

We now assume that because of the power exchange (16) between the two neutrons, a synchronization exists between the reintegration of BSPs of equal sign in the direction orthogonal to the axis defined by the two neutrons, resulting in parallel currents of equal sign that generate an attracting force between the neutrons. Thus the total attracting force between the two neutrons is produced first by the induced force and second by the currents of reintegrating BSPs.

$$F_T = F_G + F_R$$
 with $F_G = G \frac{M_1 M_2}{d^2}$ and $F_R = R \frac{M_1 M_2}{d}$ (19)

To obtain an equation for the force F_R we start with an equation that was deduced in [6] for the linear momentum when bending electrons through a crystal, equation that is based on the **Ampere law** of sec. 1 for the interaction of parallel currents.

$$p_b = \frac{1}{2} \left(\frac{5.8731}{64} \frac{b \, m \, k}{K \, r_o} \, \Delta'' l \right) \, \frac{1}{d} \, n = \frac{h}{2 \, d} \, n \tag{20}$$

with $b = 0.25, K = 5.4274 \cdot 10^4 \ s/m^2, r_o = 3.8590 \cdot 10^{-13} \ m$ and

$$k = 7.4315 \cdot 10^{-2}$$
 $\Delta'' l = 8.9357 \cdot 10^{-9} \ m$ $\Delta_o \ t = 8.0821 \cdot 10^{-21} \ s$ (21)

The force for one pair of BSPs is given by

$$dF_R = \frac{p_b}{\Delta_o t} = \frac{1}{2} \frac{h \nu_o}{d} = \frac{1}{2} \frac{E_o}{d} \qquad n = 1$$
 (22)

or

$$dF_R = \frac{p_b}{\Delta_o t} = \frac{K_{Dark}}{d}$$
 with $K_{Dark} = \frac{1}{2} \frac{h}{\Delta_o t} = 4.09924 \cdot 10^{-14} Nm$ (23)

The total force is

$$F_R = \frac{K_{Dark}}{d} \, \Delta_{R_1} \, \Delta_{R_2} = R \, \frac{M_1 \, M_2}{d} \tag{24}$$

We get

$$\Delta_{R_1} \ \Delta_{R_2} = \frac{R}{K_{Dark}} \ M_1 \ M_2 \tag{25}$$

or

$$\Delta_{R_1} \Delta_{R_2} = \gamma_R^2 M_1 M_2 \qquad with \qquad \gamma_R^2 = \frac{R}{K_{Dark}}$$
 (26)

The number of currents in the time Δt for a neutral body with mass M thus is

$$\Delta_R = \gamma_R M \tag{27}$$

The total attraction force gives

$$F_T = F_G + F_R = \left[\frac{G}{d^2} + \frac{R}{d} \right] M_1 M_2$$
 (28)

For sub-galactic distances the induced force F_G is predominant, while for galactic distances the force of parallel reintegrating BSPs F_R predominates, as shown in Fig. 6.

The transition distance between sub-galactic and galactic distances we get making $F_G = F_R$ resulting

$$d_{gal} = \frac{G}{R} \tag{29}$$

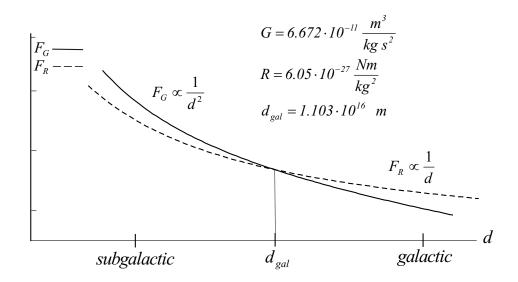


Figure 6: Gravitation forces at sub-galactic and galactic distances.

4.1 Flattening of galaxies' rotation curve.

For galactic distances the force of parallel reintegrating BSPs F_R predominates over the induced gravitation force F_G and we can write eq. (28) as

$$F_T \approx F_R = \frac{R}{d} M_1 M_2 \tag{30}$$

The equation for the centrifugal force of a body with mass M_2 is

$$F_c = M_2 \frac{v_{orb}^2}{d} \qquad with \ v_{orb} \ the \ tangential \ speed$$
 (31)

For steady state mode the centrifugal force F_c must equal the gravitation force F_T . For our case it is

$$F_c = M_2 \frac{v_{orb}^2}{d} = F_T \approx F_R = \frac{R}{d} M_1 M_2$$
 (32)

We get for the tangential speed

$$v_{orb} \approx \sqrt{R M_1}$$
 constant (33)

The tangential speed v_{orb} is constant and independent of the distance d what explains the flattening of galaxies' rotation curves.

Calculation example

With the following calculation example we will determine the value of the constant R and the transition distance d_{gal} .

For the Sun with $v_{orb}=220~km/s$ and $M_2=M_\odot=2\cdot 10^{30}~kg$ and a distance to

the core of the Milky Way of $d=25\cdot 10^{19}~m$ we get a centrifugal force of

$$F_c = M_2 \, \frac{v_{orb}^2}{d} = 3.872 \cdot 10^{20} \, N \tag{34}$$

With the mass of the core of the Milky Way of $M_1 = 4 \cdot 10^6~M_\odot$ and

$$F_c = F_T \approx F_R = R \frac{M_1 M_2}{d}$$
 we get $R = 6.05 \cdot 10^{-27} Nm/kg^2$ (35)

and with

$$F_G = F_R$$
 we get $d_{gal} = \frac{G}{R} = 1.103 \cdot 10^{16} \ m$ (36)

justifying our assumption for $F_T \approx F_R$ because the distance between the Sun and the core of the Milky Way is $d \gg d_{gal}$.

We also have that

$$\gamma_R = \sqrt{\frac{R}{K_{Dark}}} = 3.842 \cdot 10^{-7} \ kg^{-1} \tag{37}$$

If we compare with $\gamma_G = 5.3779 \cdot 10^8 \ kg^{-1}$ for the induced force we see that γ_R is very small.

Note: The flattening of galaxies' rotation curve was derived based on the assumption that the gravitation force is composed of an induced component and a component due to parallel currents of reintegrating BSPs and, that for galactic distances the induced component can be neglected.

4.2 Dark Energy:

We have assumed in sec. 4 about "Dark Matter" that because of the power exchange (16) between the two neutrons, a synchronization exists between the reintegration of BSPs of equal sign in the direction orthogonal to the axis defined by the two neutrons, resulting in parallel currents of equal sign that generate an attracting gravitation force between the neutrons.

We now assume that the synchronization of the reintegrating BSPs in the orthogonal direction of the two neutrons is between parallel currents of opposed sign, generating a repulsive gravitation force between the two neutrons. The repulsive gravitation force between matter is known as dark energy.

5 Quantification of gravitation forces.

In sec. 8.1 from [6] "Induction between an accelerated and a probe BSP expressed as closed path integration over the whole space" the elementary linear momentum p_{elem}

is derived which with

$$\Delta t(v=0) = \Delta_o t = 8.082110^{-21} \text{ s} \quad and \quad k = 7.4315 \cdot 10^{-2} < 1 \quad (38)$$

gives

$$p_{elem} = m \ c \ k = \frac{h}{c \ \Delta_o t} \ k = 2.0309 \cdot 10^{-23} \ kg \ m \ s^{-1}$$
 (39)

The elementary linear momentum p_{elem} is now used to quantize the two components of the gravitation force.

5.1 Quantification of the induced gravitation force.

From sec. 2 eq. (8) we have that the gravitation force for **one** aligned reintegrating BSPs is

$$F_i = \frac{k m c}{4 K d^2} \int \int_{Induction} with \qquad \int \int_{Induction} = 2.4662$$
 (40)

which we can write with $\Delta_o t = K r_o^2$ and $p_{elem} = k m c$ as

$$F_i = N_i \nu_o p_{elem} \quad with \quad N_i = \frac{r_o^2}{4 d^2} \int \int_{Induction}$$
 (41)

Considering that $\Delta G_1 \ \Delta G_2 = \gamma_G^2 \ M_1 \ M_2$ we can write

$$F_G = F_i \Delta G_1 \Delta G_2 = N_G \nu_o p_{elem} \quad with \quad N_G = N_i \Delta G_1 \Delta G_2 \quad (42)$$

Finally we get

$$F_G = N_G(M_1, M_2, d) \ \nu_o \ p_{elem} \qquad with \qquad N_G = 2.6555 \cdot 10^{-8} \ \frac{M_1 \ M_2}{d^2}$$
 (43)

The frequency with which elementary momenta are generated is

$$\nu_G = N_G(M_1, M_2, d) \ \nu_o = 3.2856 \cdot 10^{12} \ \frac{M_1 \ M_2}{d^2}$$
 (44)

For the earth with a mass of $M_{\oplus} = 5.974 \cdot 10^{24} \ kg$ and the sun with a mass of $M_{\odot} = 1.9889 \cdot 10^{30} \ kg$ and a distance of $d = 147.1 \cdot 10^9 \ m$ we get a frequency of $\nu_G = 1.8041 \cdot 10^{45} \ s^{-1}$ for aligned reintegrating BSPs.

5.2 Quantification of Ampere force between parallel reintegrating BSPs.

From sec. 4 eq. (22) we have for a pair of parallel reintegrating BSPs that

$$dF_R = \frac{p_b}{\Delta_o t} = \frac{1}{2} \frac{h}{\Delta_o t} \frac{1}{d} \tag{45}$$

which we can write as

$$dF_R = N \nu_o p_{elem}$$
 with $p_{elem} = k m c$ and $N = \frac{1}{2} \frac{h}{k m c d}$ (46)

where

$$k = 7.4315 \cdot 10^{-2} \tag{47}$$

For Δ_{R_1} and Δ_{R_2} BSPs we get for the total force

$$F_R = dF_R \ \Delta_{R_1} \ \Delta_{R_2} = N_R \ \nu_o \ p_{elem} \qquad with \qquad N_R = N \ \Delta_{R_1} \ \Delta_{R_2}$$
 (48)

and with $\Delta_{R_1} \Delta_{R_2} = \gamma_R^2 M_1 M_2$ we get

$$F_R = N_R(M_1, M_2, d, \Delta l) \ \nu_o \ p_{elem} \qquad with \qquad N_R = 2.4080 \cdot 10^{-24} \ \frac{M_1 \ M_2}{d}$$
 (49)

The frequency with which pairs of FPs cross in space is

$$\nu_R = N_R(M_1, M_2, d, \Delta l) \ \nu_o = 2.9792 \cdot 10^{-4} \ \frac{M_1 \ M_2}{d} \ s^{-1}$$
 (50)

For the earth with a mass of $M_{\oplus} = 5.974 \cdot 10^{24} \ kg$ and the sun with a mass of $M_{\odot} = 1.9889 \cdot 10^{30} \ kg$ and a distance of $d = 147.1 \cdot 10^9 \ m$ we get a frequency of $\nu_R = 2.4063 \cdot 10^{40} \ s^{-1}$ for parallel reintegrating BSPs. The frequency ν_G for aligned BSPs is nearly 10^6 times grater than the frequency for parallel reintegrating BSPs and so the corresponding forces.

5.3 Quantification of the total gravitation force.

The total gravitation force is given by the sum of the induced force between aligned reintegrating BSPs and the force between parallel reintegrating BSPs.

$$F_T = F_G + F_R = [N_G(M_1, M_2, d) + N_R(M_1, M_2, d, \Delta l)] p_{elem} \nu_o$$
 (51)

or

$$F_T = F_G + F_R = p_{elem} \nu_o \left[\frac{2.6555 \cdot 10^{-8}}{d^2} + \frac{2.4080 \cdot 10^{-24}}{d} \right] M_1 M_2$$
 (52)

We define the distance d_{gal} as the distance for which $F_G = F_R$ and get

$$d_{gal} = \frac{2.6555 \cdot 10^{-8}}{2.4080 \cdot 10^{-24}} = 1.103 \cdot 10^{16} \ m \tag{53}$$

6 Resume.

The work is based on particles represented as structured dynamic entities with the relativistic energy distributed over the whole space on FPs, contrary to the representation used in standard theory where particles are point-like entities with the energy concentrated on one point in space.

Fundamental parts of the mechanism of gravitation are the reintegration of migrated electrons and positrons to their nuclei, and the Induction and Ampere laws between FPs of BSPs.

The gravitation force has two components, one component due to the reintegration in the direction of the two gravitating bodies and one component due to the reintegration in the direction perpendicular to it.

For sub-galactic distances the first component, which is inverse proportional to the square distance, predominates, while for galactic distances the second component, which is inverse proportional to the distance is predominant.

The second component explains the flattening of galaxies' rotation curves without the need of additional virtual matter (dark matter).

The second component also explains the repulsive forces between galaxies without the need of additional virtual energies (dark energy).

The two components of the gravitation force are quantized with the help of the elementary linear momentum deduced for the reintegration of migrated electrons and positrons to their nuclei.

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