

Unlocking the Mystery of Interference Patterns in Electron and Photon Double-Slit Experiments and the puzzle of 'Waves without Medium'

Henok Tadesse, Electrical engineer, BSc. , Ethiopia, Debrezeit, PO Box:

Mobile phone: +251 910 751339 or +251 912 228639 email: entkidmt@yahoo.com or wchmar@gmail.com

November 16, 2014

Abstract

The formidable problem with double-slit experiments is: if electrons and photons exhibit wave properties (seen as interference patterns), then *what* is waving? What is the medium for transmission of 'electron waves'? Such a medium has been disproved experimentally, in the case of the photon, and not even conceivable for the electron. Erwin Schrodinger was on the right track with his view of the electron as a 'smeared' object, rather than as a point particle. Then how is a wave possible without a medium? How can a wave property and a particle property co-exist in a single physical entity (wave- particle duality)? Nature uses a simple and subtle trick : the average electron *mass density* at a given region of space is directly proportional to the root mean square (RMS) intensity of oscillation (velocity) of the electron (the electron wave) in that region. The instantaneous mass density of the electron at a given point is directly proportional to the instantaneous magnitude of vibrational velocity of the electron at that point. The average photon *energy density* in a given region of space is directly proportional to the root mean square of rate of change of the electric and magnetic fields in that region. The instantaneous energy density of the photon at a given point of space and time is directly proportional to the magnitude of rate of change of the electric and magnetic fields at that point. The rate of change of electric and magnetic fields in turn depends on the frequency, amplitude and phase of the wave. The electron mass and photon energy will always be concentrated at regions of high wave amplitude. This means that the electron and the photon are dragged by their respective waves. The new theory provides a hint on the mystery behind Planck's relation: $E=h.f$. Higher frequency photons have higher energy than lower frequency photons just because higher frequency photons *also* have higher amplitudes of electric and magnetic field oscillations. If we assume that ordinary waves also have the same fundamental properties as electron waves, then we may be able to explain the lack of backward propagation in Huygens' principle. We may be able to explain why the bouncing oil droplet in the Couder-Fort oil bath experiment starts to go in the direction of the wave propagation.

Introduction

The behavior of electrons and photons in double-slit experiments has been puzzling scientists for decades. There is no intuitive, logical and complete explanation of the observed interference patterns so far. The formidable problem is: if electrons and photons exhibit wave properties (seen as interference patterns), then *what* is waving? What is the medium for the photon wave? The case of the electron is even more perplexing than that of the photon. Does 'interference' of a particle give any sense at all? For the photon (light), at least scientists in the nineteenth century could conceive of a medium (the ether), even though the ether hypothesis was finally disproved by the Michelson-Morley experiment.

(The author invites the reader to read a new explanation [1, 2] of the Michelson-Morley experiment). In the case of the electron, it is not even possible to conceive of a 'medium' for 'electron waves'. Therefore, the idea of a 'medium' was somewhat conceptually feasible but disproved experimentally, in the case of the photon, but not even conceivable for the electron.

Schrodinger's wave function has succeeded in predicting and explaining the results of experiments. But what physical quantity the wave function actually represents is still unknown. According to the Copenhagen interpretation, which is the mainstream interpretation today, the wave function represents a wave of probability associated with every particle. It is the probability of finding the particle at each point of space and time. So it is probability that is waving. So many people reject this idea outright, on their first exposure. Probability is not a physical quantity. Negative probability has no physical meaning. It is counterintuitive.

Alternative interpretations exist, such as the 'wave-only' and 'pilot-wave'. These are more intuitive, but incomplete. For example, in 'wave-only' interpretations, the nature of the wave is unknown. No interpretation exists so far that solves the central puzzle: *what* is waving?

Erwin Schrodinger was on the right track with his view of the electron as a 'smeared' object, rather than as a point particle, in interpreting the wave function, and with his rejection of the Copenhagen interpretation. Yet he was still far from the ultimate mystery.

The view of a particle as having a definite size is 'correct' only if we are talking about ordinary, daily experiences. One comes to a dead end if one tries to explore the microscopic with such a view. If we continue the quest for the meaning of a particle, breaking it down into atoms, electrons, protons, neutrons, then to quarks, we ultimately reach the level of elementary particles, which can not be broken down further. This is a remarkable progress to satisfy our curiosity. However, it will still not bring an end to our curiosity. Conceptually, can we keep on breaking down the particle for ever? There should be an end: elementary particles. Then why does our intuition still keep asking what elementary particles themselves are?

The problem turns out to be our ordinary view of a particle as having a definite size, occupying a definite amount of space.

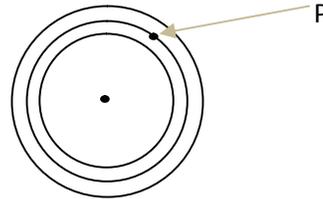
Such a view ends up in a conceptual discontinuity. Einstein was aware of this problem and was searching for a theory in which a particle is a manifestation of some continuous field. If the electron has a definite diameter, then it will not be possible to represent it mathematically, because there will be a discontinuity at its edge.

As the central mystery of Quantum Mechanics is all contained in the electron or photon double-slit experiment, as Richard Feynman said, we will explore it next.

Discussion

Ordinary waves, such as water and sound waves, are travelling disturbances of their material medium. Consider dropping a stone on a still water, creating circular waves, expanding in every direction with

center at the point where the stone was dropped. If we observe what happens at some point P, we see that the water was initially standing still before the arrival of the wave, then a disturbance occurs as the wave arrives, with water molecules oscillating vertically, and the water becomes standing still again after the wave packet has passed.



The water molecules move up and down, vertically, as the wave arrives, because water waves are transverse waves. Although the water molecules oscillate vertically, the molecules are not translating as a whole horizontally with the wave; the water is stationary, is not translating. The same applies to sound and string waves. For sound waves, the air is generally stationary, it is the wave (the disturbance) that is propagating. The air molecules oscillate about their stationary position. The air is not translating as a whole. In all cases, the material media are stationary as a whole.

Here we introduce a subtle and crucial distinction: after the waves have already passed through point P, the water is there, it doesn't disappear. In the case of a particle, however, from our daily experiences, if a particle has already passed through some point of space, we will not find that particle any more at that point.

Now we start modeling the electron step by step, so that we will be able to explain the double-slit interference pattern. At first, consider the electron as a spatially spread object, as an electron field, not as a point particle. Consider it as a sea. Its mass is distributed in space, not concentrated at a single 'point' in space, with a mass density associated with each point of space. Such a representation should be complete, i.e. it should be possible to represent it mathematically. This requires that there should be no discontinuities. Therefore, theoretically, the electron field should extend to infinity.

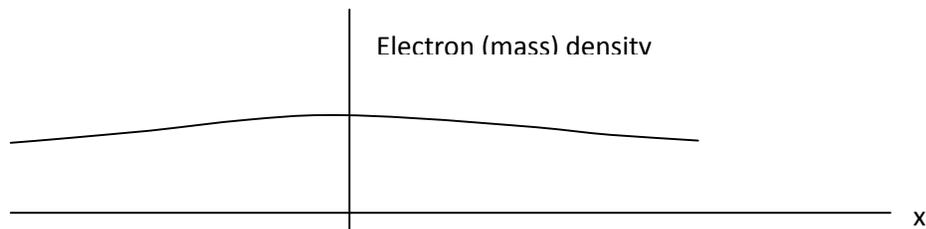


Fig.1

The integration of the mass density of the electron over all of space gives us the known mass of the electron.

The above figure is a one dimensional representation of the electron field. (Note that we are not talking about the familiar electric field of the electron. We are talking about particle field). The vertical axis

represents mass density of the electron at each point x , instead of probability density of the Copenhagen interpretation. So the electron has been represented here as some kind of fluid, rather than as a rigid classical particle with definite size or as a 'point' particle. As a fluid, just like a body of air or water, therefore, it can transmit waves. Unlike water or sound waves, however, the electron field, which is the medium for electron waves, is not stationary and is moving as a whole. (The explanation for this is that the electron mass density at a given point in space is directly proportional to the oscillation of the electron at that point. This theory will be explained shortly.)

Just as a water wave is a disturbance of water, an electron wave is a disturbance of electron field. The medium for electron waves is the electron (the electron field) itself.

For water waves, the water molecules move up and down independently, in the transverse direction to the velocity of the wave. In a similar way, in the case of electron wave, different 'parts' of the electron can move (oscillate) differently, independently. No 'part' of the electron is rigidly connected with any other 'part'. Therefore, the electron field can transmit waves in a similar way as ordinary fluids or solids. However, as a particle, all 'parts' of the electron exist as a single entity (the electron). For example, the whole electron (electron field) is emitted and absorbed as a unit. Therefore, each 'part' of the electron can have different, independent motion (oscillation, vibration), like ordinary fluids or solids. Instead of saying: different 'parts' of the electron oscillate differently, we better say: the electron can oscillate differently at different points in space. Just as parts of a sea can have different, independent vertical oscillations, the electron can have different, independent oscillations at different points of space. As water waves are transverse waves, the motion of the molecules is along the vertical direction, in the transverse direction to the velocity of the wave. For the electron wave, we assume the electron wave to be a longitudinal wave.

But an electron is not a purely wave phenomenon as depicted above. Even though we have visualized it as sea, as a field, it is still an entity (a particle). It is localized in space, it has mass and momentum.

Then how can we incorporate the particle nature of the electron in the above picture?

Consider a water wave packet (a few cycles) described previously. Once the wave packet has already passed through a point, the water becomes standing still at that point, just as it was before the arrival of the wave packet. But disappearance of the wave doesn't mean disappearance of the water itself.

The case of the electron wave packet is different. Once the electron (the electron wave packet) has passed through a point in space, the sea (the field) of electron should disappear from that point, because the electron is a particle. From our daily experiences, once a particle has passed through a point in space, it disappears from that point.

Thus, the electron wave packet will be the same thing as the electron itself.

From every day experiences, we know that once a particle has passed through a point of space, the particle will disappear from that point. The electron should not disappear from that point completely, however, as this will introduce a discontinuity. Once the electron wave packet has already passed

through a point, the magnitude of oscillation of the electron and hence the mass density of the electron at that point continuously diminishes towards zero, but should never be zero, for the sake of (conceptual) continuity.

Therefore, we can have a wave without a medium. The electron itself is the medium for the electron wave.

But how is it possible for the electron (the electron field) to disappear once the wave has passed through a point? The answer to this question solves the puzzle associated with double-slit experiments. Here is the trick used by nature:

The average mass density of the electron in a given region of space is directly proportional to the root mean square(RMS) rate of change of the electric and magnetic fields in that region. The instantaneous mass density of the electron at any given point is directly proportional to the instantaneous magnitude of velocity of the electron at that point. The velocity of the electron in turn depends on the frequency, amplitude and phase of the electron wave. Note that we are not talking about the familiar translational velocity of a particle, which is the same as the group velocity of the matter wave. We mean the velocity due to oscillation (vibration) of the electron at that point (analogous to the vertical oscillation of water molecules, for a water wave). It means that the mass density of the electron is zero at points where the amplitude of oscillation (wave) is zero. This means that there will be no electron at a point where there is no oscillation (vibration). The electron has no representation at that point. The electron can never be detected at that point. Where the amplitude of the electron wave (or oscillation) is zero, there will be no electron. This is unlike a water wave because the water exists independently of the amplitude of the oscillation (or independent of amplitude of the wave) at a point, whether there is oscillation or not.

This means that the EXISTENCE of the electron at a point in space depends on the vibration intensity of the electron at that point. This resolves the central mystery of quantum mechanics by linking EXISTENCE with intensity of vibration. The more intense the electron vibration at a point in space, the higher the mass density at that point. This will resolve the puzzle of interference in electron double slit experiments. It also resolves the puzzle of 'a wave without a medium'.

$dm/dV(x,y,z,t) \propto |v(x,y,z,t)|$, where dm/dV is the electron mass density at (x,y,z,t) and $|v(x,y,z,t)|$ is the magnitude of the velocity of the electron at (x,y,z,t)

The reader may ask: no mention has been made about the familiar translational velocity of the electron (the particle). The translational velocity of the electron is the same as the group velocity of the electron wave.

A more complete explanation of the electron wave should also include the phase velocity and the wavelength. The de Broglie wavelength is yet to be explained.

To complete our understanding of the particle nature in the wave picture of the electron depicted so far, we should look at the phenomenon of electron detection.

How is the electron and the photon detected? The following interpretation is made.

The electron is *represented* at each point in the electron field. The more the electron mass density at a given point, the more representation the electron has at that point. (The mass density here corresponds to probability density in Copenhagen interpretation).

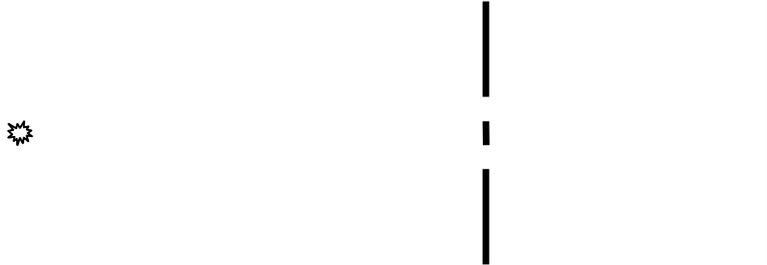


Fig.2

The electron is detected at only one point on the detector screen because the electron, as a single entity, is detected as an entity. The detector detects the electron as a unit, not part of it. At the instant of detection, the mass of the electron that is distributed in the space along the screen will *collapse* to the point of detection. This corresponds to the collapse of the probability wave function in the Copenhagen interpretation. What collapses is the electron mass density wave. The probability that the electron is detected at a certain point on the screen is proportional to the mass density of the electron at that point. The probability here, unlike the probability in the Copenhagen interpretation, is in accordance with the principles of causality and determinism.

The photon

So far we explained the electron wave. Instead of the *mass density* for the electron, *energy density* applies for the photon; otherwise the explanation of the photon wave is similar.

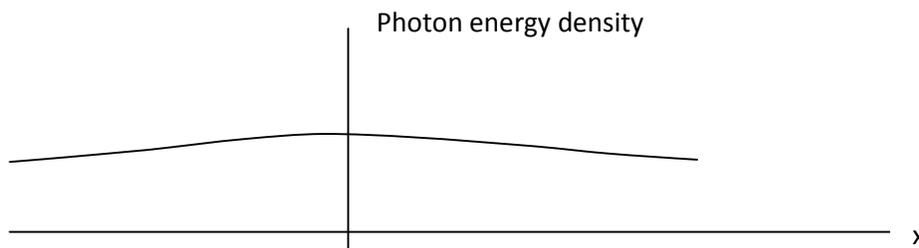


Fig.3

Just as mass is distributed continuously in space for the electron, the electric and magnetic field is distributed continuously in space for the photon. The integration of the energy density of the photon over space gives the energy of the photon.

Consider again a packet of water waves created by dropping a stone in to a lake. At a point some distance away from the point of disturbance, the water molecules are standing still, before the arrival of the wave. As the wave arrives, the water molecules start to oscillate vertically about their initial

position. Once the disturbance has passed away, the water at that point becomes still again. The disappearance of the wave (the disturbance) doesn't mean the disappearance of the water itself, in the case of water waves. This applies to all ordinary waves such as sound waves and string waves.

The case of the photon is distinct from water waves. We consider the photon as a wave of electric and magnetic fields. Assume a light source emitting photons. Consider a point in space at some distance from the light source. If we take the direct analogy of water waves, the electric and magnetic fields would be 'standing still', i.e. static, not varying, before the arrival of the wave. This means that static electric and magnetic fields would exist at that point even if the photon hadn't arrived yet. As the photon arrives, the electric and magnetic fields would oscillate at that point. Once the photon has already passed away, then the electric and magnetic fields would become static again.

The above direct analogy of a photon with a water wave is erroneous. No varying or static electric and magnetic fields should exist before the arrival of the photon and after the photon has passed through that point. How is this possible?

Nature does this with a subtle trick, in a similar way to the electron wave:

The square of electric and magnetic fields, i.e. the photon energy density, at a point in space and time is directly proportional to the magnitude of rate of change of the electric and magnetic fields at that point. The rate of change of electric and magnetic fields depends on the frequency, amplitude and phase of the wave.

$$(E)^2(x,y,z,t) \propto |d/dt(E(x,y,z,t))|, \text{ where } E \text{ is the electric field intensity at point } x,y,z,t \text{ or}$$

$$d\epsilon/dV(x,y,z,t) \propto |d/dt(E(x,y,z,t))|, \text{ where } d\epsilon/dV \text{ is the photon energy density at point } x,y,z,t$$

Therefore, once the photon wave has already passed through a point of space, there will be neither oscillating (varying) nor static electric and magnetic fields at that point, and hence the intensity of these fields will also diminish continuously towards zero.

This resolves the centuries old puzzle. Light wave does not require a medium of transmission.

Instead of the photon energy density spatial distribution assumed previously (Fig.3), the localized energy density distribution is shown below (Fig.4).

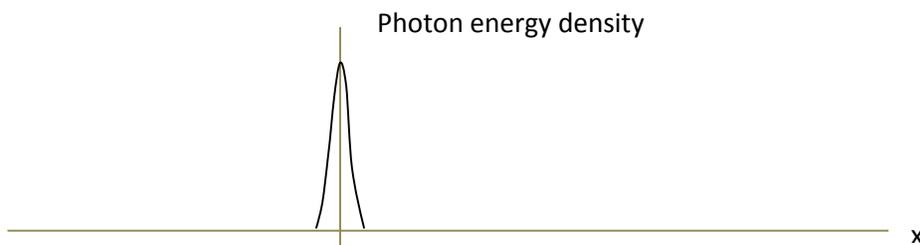


Fig.4

The lower the frequency of oscillation, the lower will be the rate of change of the electric and magnetic field intensities, and hence the lower the intensity (amplitude) of these fields, and hence the lower the energy density of the photon, as discussed so far. The higher the frequency of oscillation, the higher also the intensity of the fields, hence the higher the photon energy density. This may give a hint to the mystery underlying Planck's relation. The square of intensity of electric and magnetic fields (i.e. the photon energy density) is directly proportional to the frequency of the photon. The constant of proportionality is Planck's constant. $Energy = h \cdot f$

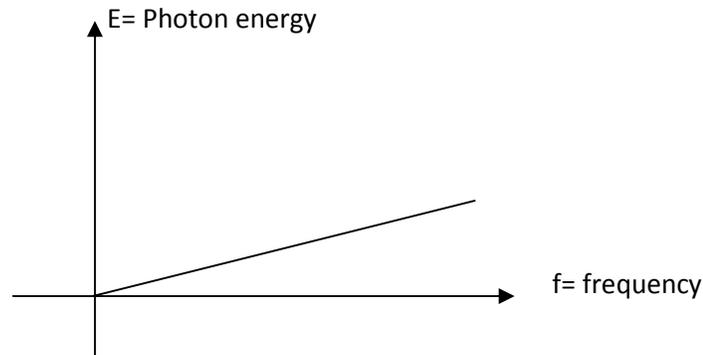


Fig.4

Electron and photon double-slit experiments



Fig.6

Now we can easily explain the observed interference pattern in the double-slit experiment. An electron source emits electrons one at a time from an electron gun. The electron wave front encounters the plate with two slits. The electron wave, as a wave, is capable of passing through both slits. The electron oscillates at every point in space, just like ordinary waves, such as sound or water waves. Assume the electron wave to be longitudinal. The two slits act as two sources and the two electron waves from the two slits interfere at all points in space and along the detector screen. At some points on the detector screen, the waves interfere constructively, hence resulting in higher intensity of longitudinal oscillation

of the electron at those points and destructively at some points, resulting in lower intensity of oscillation (vibration) at those points. As discussed already, the more the intensity of vibration at a given point on the screen, the higher will be the mass density of the electron at that point. The higher the electron mass density at a given point, the higher the probability of detection of the electron at that point. The instant the electron is detected at some point on the screen, the mass of the electron that is distributed in space collapses to that point, during the process of detection.

At points on the screen where the waves interfere completely destructively, there will be no oscillation and hence also no electron (zero mass density) at that point. Therefore, the electron will never be detected at that point because the electron has no *representation* at that point.

We can equivalently look at the phenomenon as follows:

As the electron encounters the two slits, it is scattered in different directions after passing through the slits. The electron is 'broken down' and directed in different directions. The mass of the electron directed in certain directions is larger (regions of constructive interference) than the mass directed in other directions (regions with less constructive interference, or with destructive interference). Even though the electron is broken down into 'pieces' with different masses and sizes, all the scattered masses still act as a single entity. When the electron is detected at some point on the screen, all the scattered masses collapse to that point.

Implications to the Couder-Fort Oil Bath Experiment and the lack of backward propagation in Huygens' principle

Here I attempt to propose why the bouncing oil droplets start to 'walk' in the direction of the wave propagation, based on the discussion made so far.

From classical physics, we know that a water wave makes the water molecules oscillate vertically as the wave propagates forward. The water molecules will not propagate (translate) horizontally with the wave. This applies to all ordinary waves such as string waves, sound waves, solid waves.

We already have seen in this paper that this is not the case for the electron. The electron propagates with the electron wave. The electron translates while oscillating.

But the 'walking' of the bouncing-droplet may be explained if we assume that ordinary waves also have the same fundamental properties as the electron wave. In a water wave, the molecules of water may not only undergo periodic vertical displacements, but also propagate horizontally with the wave. This effect may be so small that we can't observe it in ordinary experiences.

The oil droplet acquires a horizontal velocity component from molecules of the oil bath being displaced horizontally with the wave.

We know that Huygens' principle doesn't explain the lack of backward propagation. Why do the waves not propagate backwards?

This problem can be solved if we assume that the water molecules are also translating horizontally, while oscillating vertically. In this case there will always be a forward momentum, so that the waves always propagate only forwards. Therefore, the reason why waves do not propagate backwards is the same reason that a particle (an object with mass) does not suddenly change its direction of motion. The object continues to move in the same direction because of its momentum. The same may apply to a wave. The amount of water being displaced (dragged) horizontally with the wave may be too small to be observed in our daily experiences.

Conclusion

The two puzzles in quantum mechanics are:

How can an electron (a particle) create an interference pattern, as observed in double-slit experiments?
What is the medium for matter waves and the medium for photon waves?

This paper reveals that a single but subtle law of nature underlies *both* these puzzles: The electron mass density at a point in space and time is directly proportional to the velocity of the electron at that point and at that instant. The photon energy density at a point of space is directly proportional to the rate of change of electric and magnetic field intensities at that point.

References

1. <http://vixra.org/pdf/1406.0045v5.pdf>