

# Lucasian Primality Criterion for Specific Class of $k \cdot 2^n - 1$

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**Abstract:** Conjectured polynomial time primality test for specific class of numbers of the form  $k \cdot 2^n - 1$  is introduced .

**Keywords:** Primality test , Polynomial time , Prime numbers .

**AMS Classification:** 11A51 .

## 1 Introduction

In 1969 Hans Riesel provided polynomial time primality test for numbers of the form  $k \cdot 2^n - 1$  with  $k$  odd ,  $k < 2^n$  and  $n > 2$  , see Theorem 5 in [1] . In this note I present polynomial time primality test for numbers of the form  $k \cdot 2^n - 1$  with  $3 \mid k$  that is special case of Riesel test .

## 2 The Main Result

**Definition 2.1.** Let  $P_m(x) = 2^{-m} \cdot \left( (x - \sqrt{x^2 - 4})^m + (x + \sqrt{x^2 - 4})^m \right)$  , where  $m$  and  $x$  are nonnegative integers .

**Conjecture 2.1.** Let  $N = k \cdot 2^n - 1$  such that  $n > 2$  ,  $k > 0$  ,  $3 \mid k$  ,  $k < 2^n$  and

$$\begin{cases} k \equiv 1 \pmod{10} \text{ with } n \equiv 2, 3 \pmod{4} \\ k \equiv 3 \pmod{10} \text{ with } n \equiv 0, 3 \pmod{4} \\ k \equiv 7 \pmod{10} \text{ with } n \equiv 1, 2 \pmod{4} \\ k \equiv 9 \pmod{10} \text{ with } n \equiv 0, 1 \pmod{4} \end{cases}$$

Let  $S_i = P_2(S_{i-1})$  with  $S_0 = P_k(5778)$  , thus  
 $N$  is prime iff  $S_{n-2} \equiv 0 \pmod{N}$

## References

- [1] Riesel, Hans (1969) , "Lucasian Criteria for the Primality of  $N = h \cdot 2^n - 1$ " , *Mathematics of Computation* (AmericanMathematical Society), 23 (108): 869-875 .