

# Inverse Square-Law Possibly-Followed by Single Photons

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## Abstract:

Inverse square-law is followed by electric charges, gravity, and light. Light has shown even an unexpected property, of double-slit-interference of single photons. So it is not unreasonable to expect inverse-square-law to be followed by single photons. Assuming that the single photon is emitted either from the surface of an electron, or a globular-cluster, or a galaxy, the derivation presented here suggests that even a single photon seems to follow the inverse square-law.

## The Derivation:

The inverse square-law followed by star-light is well known. Luminosity of a star is expressed as:

$$L = \sigma AT^4, \dots\dots\dots(1)$$

Where  $A$  is the area and  $\sigma$  is the Stefan-Boltzmann constant, with a value of:  $5.670373(21) \times 10^{-8}$  Watt  $m^{-2} K^{-4}$ .

And the flux  $F$  is:

$$F = \frac{L}{4\pi r^2}, \dots\dots\dots(2)$$

where  $r$  is the distance from the observer to the light source.

We intend to consider three different cases of a single photon either emitted from the surface of an electron, or a globular-cluster, or a galaxy. Let us take energy lost by a single photon, ( $hf_0 - hf$ ) and assume that this is the energy radiated by the source. We can take the initial area  $A$  in the expression-1, of emitting surface for electron as  $4\pi r_e^2$ , for the globular-cluster  $4\pi R_{globu}^2$ , and for a galaxy  $4\pi R_{gal}^2$ . We can express a quantity comparable with luminosity of a star  $L$  as:

$$L' = (4\pi r_e^2) (hf_0 - hf) \dots\dots\dots(3)$$

And we can express a quantity comparable with the flux  $L$  in the expression-2 as:

$$F' = L' / (4\pi D^2), \text{ where } D \text{ is a very long distance away from the source.}$$

Assuming that  $F'$  is gravitational potential-energy of the photon at that distance  $D$ :

$$[ G M_{gal} ( h f / c^2 ) / D ] = [ ( 4 \pi R_{gal}^2 ) ( h f_0 - h f ) / ( 2 \pi D^2 ) ]$$

$$\text{i.e. } [ G M_{gal} ( h f / c^2 ) / D ] [ ( 4 \pi D^2 ) / ( 4 \pi R_{gal}^2 ) ] = ( h f_0 - h f )$$

$$\text{i.e. } [ G M_{gal} / ( R_{gal}^2 ) ] D ( h f / c^2 ) = ( h f_0 - h f ) \dots\dots\dots(4)$$

Now, Sivaram C. has numerically shown that:

$$[ G M_{gal} / R_{gal}^2 ] = [ G M_{globu} / R_{globu}^2 ] = [ G m_e / r_e^2 ] = a_0 \text{ of MOND} = H_0 c ,$$

Where  $H_0$  is Hubble's constant, and  $c$  is speed of light, and 'a<sub>0</sub> of MOND' stands for the critical-acceleration of Milgom's Modified Newtonian Dynamics. So we can write the expression-4 as:

$$( H_0 c ) D ( h f / c^2 ) = ( h f_0 - h f )$$

$$\text{i.e. } ( h f_0 - h f ) / ( h f ) = ( H_0 D / c ) \dots\dots\dots(5)$$

We know that the expression-5 is a well known expression for the 'cosmological red-shift'. Therefore, our initial assumption, that even a single photon may be following the inverse square-law, leads to familiar observation of the 'cosmological red-shift'. This derivation leads us to a possibility that the 'cosmological red-shift' may be due to the inverse square-law followed by single photons.

**References:**

[1] Sivaram, C. (1994) *Astrophysics and Space science* 215, 185-189

[2] Tank Hasmukh K. "Some criteria for short-listing the cosmological red-shift's explanations" <http://vixra.org/abs/1501.0193>