

IRREDUCIBLE REPRESENTATIONS OF SMALL ABSTRACT GROUPS COMPUTED WITH GAP

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ABSTRACT. This is a table of all irreducible matrix representations of all 181 groups up to order 40, generated with the GAP software.

1. CONSTRUCTION

The GAP function `IrreducibleRepresentationsDixon` generates irreducible representations of finite abstract groups [4, 3, 7, 1]. The skeleton of the GAP source code looks as follows:

```
#!/usr/bin/env gap

LoadPackage("SONATA") ;;
LoadPackage("ctbllib") ;;

irrforgroup := function(g)
  local els,e,gid,fna,ir,irr,id ;

  Print("-----\n") ;
  els := Elements(g) ;;
  gid := IdGroup(g) ;;
  Print(gid,"\n") ;

  # print elements by generators
  id := 1 ;;
  for e in els do
    if id > 1 then
      Print(id,"=",els[id],". ") ;
    fi;
    id := id+1 ;
  od;
  Print("\n") ;

  Print(StructureDescription(g),"\n") ;

  ir := IrrDixonSchneider(g) ;;
  Print(ir) ;
  Display(CharacterTable(g)) ;

  Irr(g) ;;
  irr := IrreducibleRepresentationsDixon(g) ;;
  Print(irr,"\n") ;
```

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```

end;;

# need to start at n=2 because n=1 hangs up the IrreducibleRepresentations(g) part
for n in [2..36] do
  alls := AllSmallGroups(n) ;
  for g in alls do
    irrforgroup(g) ;
  od ;
od;

```

2. RESULTS

2.1. Notations. We denote the k -th group of order o by $G_o^{(k)}$ enumerating the groups as within GAP. This aligns the following contents with my representations of the cycle graphs [6].

g_j are the group elements, where g_1 is the unit element. The generators are the elements g_2 (and g_3 etc. if more generators are needed). The irreducible representations are only provided for the generators here because the others are obtained by multiplying their representations. The degrees of the representations divide the group order [5].

The representations are denoted by R_r where r runs from 1 up to the number of classes in $G_o^{(k)}$. The trivial representations R_1 , where $R_1(g_j) = 1$ or the equivalent higher order unit matrix, are not listed explicitly.

$e_n \equiv e^{2\pi i/n}$ are complex numbers which equal the principal values of roots of unity:

$$(1) \quad e_n = e^{2\pi i/n}; \quad c_{p/q} \equiv \cos(p\pi/q); \quad s_{p/q} \equiv \sin(p\pi/q).$$

$e_4 = i$ is the imaginary unit. \Re and \Im are the real and imaginary parts of their arguments. The symbols

$$\lambda \equiv \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}, \quad \phi \equiv \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}, \quad \epsilon \equiv \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}, \quad \kappa \equiv \begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix},$$

are used for some frequently used 2×2 matrices [2]. $\varphi = (1 + \sqrt{5})/2$ is the golden ratio. Other constants α_o are defined in the text if the matrices would not fit in the lines otherwise; their (first) sub-indices are the order of the group.

2.2. Order 2. $G_2^{(1)}$

$$R_2(g_2) = -1.$$

2.3. Order 3. $G_3^{(1)}$

$$R_2(g_2) = e_3.$$

$$R_3(g_2) = e_3^*.$$

2.4. Order 4. $G_4^{(1)}$

$$R_2(g_2) = -1. \quad R_2(g_3) = 1.$$

$$R_3(g_2) = i. \quad R_3(g_3) = -1.$$

$$R_4(g_2) = -i. \quad R_4(g_3) = -1.$$

$G_4^{(2)}$

$$\begin{aligned} R_2(g_2) &= -1. & R_2(g_3) &= 1. \\ R_3(g_2) &= 1. & R_3(g_3) &= -1. \\ R_4(g_2) &= -1. & R_4(g_3) &= -1. \end{aligned}$$

 2.5. **Order 5.** $G_5^{(1)}$

$$R_j(g_2) = e_5^{j-1}, \quad j = 1 \dots 5.$$

 2.6. **Order 6.** $G_6^{(1)}$

$$\begin{aligned} R_2(g_2) &= -1. & R_2(g_3) &= 1. \\ R_3(g_2) &= \begin{pmatrix} -1 & -1 \\ 0 & 1 \end{pmatrix}. & R_3(g_3) &= \begin{pmatrix} 0 & 1 \\ -1 & -1 \end{pmatrix}. \end{aligned}$$

 $G_6^{(2)}$

$$\begin{aligned} R_2(g_2) &= -1. & R_2(g_3) &= 1. \\ R_3(g_2) &= -1. & R_3(g_3) &= e_3^2. \\ R_4(g_2) &= -1. & R_4(g_3) &= e_3. \\ R_5(g_2) &= 1. & R_5(g_3) &= e_3^2. \\ R_6(g_2) &= 1. & R_6(g_3) &= e_3. \end{aligned}$$

 2.7. **Order 7.** $G_7^{(1)}$

$$R_j(g_2) = e_7^{j-1}, \quad j = 1 \dots, 7.$$

 2.8. **Order 8.** $G_8^{(1)}$

$$\begin{aligned} R_2(g_2) &= -1. & R_2(g_3) &= 1. & R_2(g_4) &= 1. \\ R_3(g_2) &= -i. & R_3(g_3) &= -1. & R_3(g_4) &= 1. \\ R_4(g_2) &= i. & R_4(g_3) &= -1. & R_4(g_4) &= 1. \\ R_5(g_2) &= -e_8. & R_5(g_3) &= i. & R_5(g_4) &= -1. \\ R_6(g_2) &= -e_8^3. & R_6(g_3) &= -i. & R_6(g_4) &= -1. \\ R_7(g_2) &= e_8^3. & R_7(g_3) &= -i. & R_7(g_4) &= -1. \\ R_8(g_2) &= e_8. & R_8(g_3) &= i. & R_8(g_4) &= -1. \end{aligned}$$

 $G_8^{(2)}$

$$\begin{aligned} R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= 1. \\ R_3(g_2) &= -1. & R_3(g_3) &= 1. & R_3(g_4) &= 1. \\ R_4(g_2) &= 1. & R_4(g_3) &= -1. & R_4(g_4) &= 1. \\ R_5(g_2) &= -i. & R_5(g_3) &= -1. & R_5(g_4) &= -1. \\ R_6(g_2) &= i. & R_6(g_3) &= -1. & R_6(g_4) &= -1. \\ R_7(g_2) &= -i. & R_7(g_3) &= 1. & R_7(g_4) &= -1. \\ R_8(g_2) &= i. & R_8(g_3) &= 1. & R_8(g_4) &= -1. \end{aligned}$$

$G_8^{(3)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= 1. \\
R_3(g_2) &= -1. & R_3(g_3) &= 1. & R_3(g_4) &= 1. \\
R_4(g_2) &= 1. & R_4(g_3) &= -1. & R_4(g_4) &= 1. \\
R_5(g_2) &= \lambda. & R_5(g_3) &= \phi. & R_5(g_4) &= -\epsilon.
\end{aligned}$$

 $G_8^{(4)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= 1. \\
R_3(g_2) &= -1. & R_3(g_3) &= 1. & R_3(g_4) &= 1. \\
R_4(g_2) &= 1. & R_4(g_3) &= -1. & R_4(g_4) &= 1. \\
R_5(g_2) &= i\lambda. & R_5(g_3) &= \kappa. & R_5(g_4) &= -\epsilon.
\end{aligned}$$

 $G_8^{(5)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= -1. \\
R_3(g_2) &= -1. & R_3(g_3) &= -1. & R_3(g_4) &= 1. \\
R_4(g_2) &= -1. & R_4(g_3) &= 1. & R_4(g_4) &= -1. \\
R_5(g_2) &= -1. & R_5(g_3) &= 1. & R_5(g_4) &= 1. \\
R_6(g_2) &= 1. & R_6(g_3) &= -1. & R_6(g_4) &= -1. \\
R_7(g_2) &= 1. & R_7(g_3) &= -1. & R_7(g_4) &= 1. \\
R_8(g_2) &= 1. & R_8(g_3) &= 1. & R_8(g_4) &= -1.
\end{aligned}$$

2.9. Order 9. $G_9^{(1)}$

$$\begin{aligned}
R_2(g_2) &= e_3. & R_2(g_3) &= 1. \\
R_3(g_2) &= e_3^2. & R_3(g_3) &= 1. \\
R_4(g_2) &= -e_9^4 - e_9^7. & R_4(g_3) &= e_3. \\
R_5(g_2) &= e_9^4. & R_5(g_3) &= e_3. \\
R_6(g_2) &= e_9^7. & R_6(g_3) &= e_3. \\
R_7(g_2) &= e_9^2. & R_7(g_3) &= e_3^2. \\
R_8(g_2) &= e_9^5. & R_8(g_3) &= e_3^2. \\
R_9(g_2) &= -e_9^2 - e_9^5. & R_9(g_3) &= e_3^2.
\end{aligned}$$

 $G_9^{(2)}$

$$\begin{aligned}
R_2(g_2) &= e_3. & R_2(g_3) &= 1. \\
R_3(g_2) &= e_3^2. & R_3(g_3) &= 1. \\
R_4(g_2) &= 1. & R_4(g_3) &= e_3. \\
R_5(g_2) &= e_3. & R_5(g_3) &= e_3. \\
R_6(g_2) &= e_3^2. & R_6(g_3) &= e_3. \\
R_7(g_2) &= 1. & R_7(g_3) &= e_3^2. \\
R_8(g_2) &= e_3. & R_8(g_3) &= e_3^2. \\
R_9(g_2) &= e_3^2. & R_9(g_3) &= e_3^2.
\end{aligned}$$

2.10. **Order 10.** $G_{10}^{(1)}$

$$\begin{aligned}
 R_2(g_2) &= -1. & R_2(g_3) &= 1. \\
 R_3(g_2) &= \begin{pmatrix} \varphi & -1 \\ -\varphi & -\varphi \end{pmatrix}. & R_3(g_3) &= \begin{pmatrix} 0 & 1 \\ -1 & \varphi \end{pmatrix}. \\
 R_4(g_2) &= \phi. & R_4(g_3) &= \begin{pmatrix} -\varphi & -\varphi \\ \varphi & -1 \end{pmatrix}.
 \end{aligned}$$

 $G_{10}^{(2)}$

$$\begin{aligned}
 R_2(g_2) &= -1. & R_2(g_3) &= 1. \\
 R_3(g_2) &= -1. & R_3(g_3) &= e_5^4. \\
 R_4(g_2) &= -1. & R_4(g_3) &= e_5^3. \\
 R_5(g_2) &= -1. & R_5(g_3) &= e_5^2. \\
 R_6(g_2) &= -1. & R_6(g_3) &= e_5. \\
 R_7(g_2) &= 1. & R_7(g_3) &= e_5^4. \\
 R_8(g_2) &= 1. & R_8(g_3) &= e_5^3. \\
 R_9(g_2) &= 1. & R_9(g_3) &= e_5^2. \\
 R_{10}(g_2) &= 1. & R_{10}(g_3) &= e_5.
 \end{aligned}$$

 2.11. **Order 11.** $G_{11}^{(1)}$

$$R_j(g_2) = e_{11}^{j-1}, \quad j = 1, \dots, 11.$$

 2.12. **Order 12.** $G_{12}^{(1)}$

$$\begin{aligned}
 R_2(g_2) &= -1. & R_2(g_3) &= 1. & R_2(g_4) &= 1. \\
 R_3(g_2) &= -i. & R_3(g_3) &= -1. & R_3(g_4) &= 1. \\
 R_4(g_2) &= i. & R_4(g_3) &= -1. & R_4(g_4) &= 1. \\
 R_5(g_2) &= \begin{pmatrix} -i & 1 \\ 0 & i \end{pmatrix}. & R_5(g_3) &= -\epsilon. & R_5(g_4) &= \begin{pmatrix} 0 & i \\ i & -1 \end{pmatrix}. \\
 R_6(g_2) &= \begin{pmatrix} 1 & 0 \\ -1 & -1 \end{pmatrix}. & R_6(g_3) &= \epsilon. & R_6(g_4) &= \begin{pmatrix} 0 & 1 \\ -1 & -1 \end{pmatrix}.
 \end{aligned}$$

 $G_{12}^{(2)}$

$$\begin{aligned}
 R_2(g_2) &= -1. & R_2(g_3) &= 1. & R_2(g_4) &= 1. \\
 R_3(g_2) &= -1. & R_3(g_3) &= e_3^2. & R_3(g_4) &= 1. \\
 R_4(g_2) &= -1. & R_4(g_3) &= e_3. & R_4(g_4) &= 1. \\
 R_5(g_2) &= 1. & R_5(g_3) &= e_3^2. & R_5(g_4) &= 1. \\
 R_6(g_2) &= 1. & R_6(g_3) &= e_3. & R_6(g_4) &= 1. \\
 R_7(g_2) &= -i. & R_7(g_3) &= 1. & R_7(g_4) &= -1. \\
 R_8(g_2) &= i. & R_8(g_3) &= 1. & R_8(g_4) &= -1. \\
 R_9(g_2) &= -i. & R_9(g_3) &= e_3^2. & R_9(g_4) &= -1. \\
 R_{10}(g_2) &= -i. & R_{10}(g_3) &= e_3. & R_{10}(g_4) &= -1. \\
 R_{11}(g_2) &= i. & R_{11}(g_3) &= e_3^2. & R_{11}(g_4) &= -1. \\
 R_{12}(g_2) &= i. & R_{12}(g_3) &= e_3. & R_{12}(g_4) &= -1.
 \end{aligned}$$

 $G_{12}^{(3)}$

$$R_2(g_2) = e_3^2. \quad R_2(g_3) = 1. \quad R_2(g_4) = 1.$$

$$R_3(g_2) = e_3. \quad R_3(g_3) = 1. \quad R_3(g_4) = 1.$$

$$R_4(g_2) = \begin{pmatrix} 1 & 0 & 0 \\ -1 & -1 & -1 \\ 0 & 1 & 0 \end{pmatrix}. \quad R_4(g_3) = \begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ -1 & -1 & -1 \end{pmatrix}. \quad R_4(g_4) = \begin{pmatrix} -1 & -1 & -1 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix}.$$

 $G_{12}^{(4)}$

$$R_2(g_2) = -1. \quad R_2(g_3) = -1. \quad R_2(g_4) = 1.$$

$$R_3(g_2) = -1. \quad R_3(g_3) = 1. \quad R_3(g_4) = 1.$$

$$R_4(g_2) = 1. \quad R_4(g_3) = -1. \quad R_4(g_4) = 1.$$

$$R_5(g_2) = \phi. \quad R_5(g_3) = -\epsilon. \quad R_5(g_4) = \begin{pmatrix} 0 & 1 \\ -1 & -1 \end{pmatrix}.$$

$$R_6(g_2) = \begin{pmatrix} -1 & -1 \\ 0 & 1 \end{pmatrix}. \quad R_6(g_3) = \epsilon. \quad R_6(g_4) = \begin{pmatrix} 0 & 1 \\ -1 & -1 \end{pmatrix}.$$

 $G_{12}^{(5)}$

$$R_2(g_2) = -1. \quad R_2(g_3) = -1. \quad R_2(g_4) = 1.$$

$$R_3(g_2) = -1. \quad R_3(g_3) = 1. \quad R_3(g_4) = 1.$$

$$R_4(g_2) = 1. \quad R_4(g_3) = -1. \quad R_4(g_4) = 1.$$

$$R_5(g_2) = -1. \quad R_5(g_3) = -1. \quad R_5(g_4) = e_3^2.$$

$$R_6(g_2) = -1. \quad R_6(g_3) = -1. \quad R_6(g_4) = e_3.$$

$$R_7(g_2) = -1. \quad R_7(g_3) = 1. \quad R_7(g_4) = e_3^2.$$

$$R_8(g_2) = -1. \quad R_8(g_3) = 1. \quad R_8(g_4) = e_3.$$

$$R_9(g_2) = 1. \quad R_9(g_3) = -1. \quad R_9(g_4) = e_3^2.$$

$$R_{10}(g_2) = 1. \quad R_{10}(g_3) = -1. \quad R_{10}(g_4) = e_3.$$

$$R_{11}(g_2) = 1. \quad R_{11}(g_3) = 1. \quad R_{11}(g_4) = e_3^2.$$

$$R_{12}(g_2) = 1. \quad R_{12}(g_3) = 1. \quad R_{12}(g_4) = e_3.$$

2.13. **Order 13.** $G_{13}^{(1)}$

$$R_j(g_2) = e_{13}^{j-1}, \quad j = 1, \dots, 13.$$

2.14. Order 14. $G_{14}^{(1)}$

$$R_2(g_2) = -1. \quad R_2(g_3) = 1.$$

$$R_3(g_2) = \begin{pmatrix} 2(c_{1/7} - c_{2/7}) & -2c_{2/7} \\ 2(c_{2/7} - c_{1/7}) & 2(c_{2/7} - c_{1/7}) \end{pmatrix}. \quad R_3(g_3) = \begin{pmatrix} 0 & 1 \\ -1 & 2c_{2/7} \end{pmatrix}.$$

$$R_4(g_2) = \begin{pmatrix} -2(c_{1/7} + c_{3/7}) & -2(c_{1/7} + c_{3/7}) \\ 2c_{1/7} & 2(c_{1/7} + c_{3/7}) \end{pmatrix}. \\ R_4(g_3) = \begin{pmatrix} -2(c_{1/7} + c_{3/7}) & -2(c_{1/7} + c_{3/7}) \\ 2(c_{1/7} + c_{3/7}) & 2c_{1/7} \end{pmatrix}.$$

$$R_5(g_2) = \begin{pmatrix} -2\Re e_{14}^3 & -1 \\ 1 - 2\Re e_{14} & 2\Re e_{14}^3 \end{pmatrix}. \quad R_5(g_3) = \begin{pmatrix} 1 - 2\Re e_{14} & 2\Re e_{14}^3 \\ -2\Re e_{14} & -1 \end{pmatrix}.$$

 $G_{14}^{(2)}$

$$R_2(g_2) = -1. \quad R_2(g_3) = 1.$$

$$R_3(g_2) = -1. \quad R_3(g_3) = e_7^6.$$

$$R_4(g_2) = -1. \quad R_4(g_3) = e_7^5.$$

$$R_5(g_2) = -1. \quad R_5(g_3) = e_7^4.$$

$$R_6(g_2) = -1. \quad R_6(g_3) = e_7^3.$$

$$R_7(g_2) = -1. \quad R_7(g_3) = e_7^2.$$

$$R_8(g_2) = -1. \quad R_8(g_3) = e_7.$$

$$R_9(g_2) = 1. \quad R_9(g_3) = e_7^6.$$

$$R_{10}(g_2) = 1. \quad R_{10}(g_3) = e_7^5.$$

$$R_{11}(g_2) = 1. \quad R_{11}(g_3) = e_7^4.$$

$$R_{12}(g_2) = 1. \quad R_{12}(g_3) = e_7^3.$$

$$R_{13}(g_2) = 1. \quad R_{13}(g_3) = e_7^2.$$

$$R_{14}(g_2) = 1. \quad R_{14}(g_3) = e_7.$$

2.15. **Order 15.** $G_{15}^{(1)}$

$$\begin{aligned}
R_2(g_2) &= 1. & R_2(g_3) &= e_5^4. \\
R_3(g_2) &= 1. & R_3(g_3) &= e_5^3. \\
R_4(g_2) &= 1. & R_4(g_3) &= e_5^2. \\
R_5(g_2) &= 1. & R_5(g_3) &= e_5. \\
R_6(g_2) &= e_3^2. & R_6(g_3) &= 1. \\
R_7(g_2) &= e_3. & R_7(g_3) &= 1. \\
R_8(g_2) &= e_3^2. & R_8(g_3) &= e_5^4. \\
R_9(g_2) &= e_3^2. & R_9(g_3) &= e_5^3. \\
R_{10}(g_2) &= e_3^2. & R_{10}(g_3) &= e_5^2. \\
R_{11}(g_2) &= e_3^2. & R_{11}(g_3) &= e_5. \\
R_{12}(g_2) &= e_3. & R_{12}(g_3) &= e_5^4. \\
R_{13}(g_2) &= e_3. & R_{13}(g_3) &= e_5^3. \\
R_{14}(g_2) &= e_3. & R_{14}(g_3) &= e_5^2. \\
R_{15}(g_2) &= e_3. & R_{15}(g_3) &= e_5.
\end{aligned}$$

2.16. **Order 16.** $G_{16}^{(1)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= 1. & R_2(g_4) &= 1. & R_2(g_5) &= 1. \\
R_3(g_2) &= -i. & R_3(g_3) &= -1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. \\
R_4(g_2) &= i. & R_4(g_3) &= -1. & R_4(g_4) &= 1. & R_4(g_5) &= 1. \\
R_5(g_2) &= -e_8. & R_5(g_3) &= i. & R_5(g_4) &= -1. & R_5(g_5) &= 1. \\
R_6(g_2) &= -e_8^3. & R_6(g_3) &= -i. & R_6(g_4) &= -1. & R_6(g_5) &= 1. \\
R_7(g_2) &= e_8^3. & R_7(g_3) &= -i. & R_7(g_4) &= -1. & R_7(g_5) &= 1. \\
R_8(g_2) &= e_8. & R_8(g_3) &= i. & R_8(g_4) &= -1. & R_8(g_5) &= 1. \\
R_9(g_2) &= -e_{16}. & R_9(g_3) &= e_8. & R_9(g_4) &= i. & R_9(g_5) &= -1. \\
R_{10}(g_2) &= -e_{16}^3. & R_{10}(g_3) &= e_8^3. & R_{10}(g_4) &= -i. & R_{10}(g_5) &= -1. \\
R_{11}(g_2) &= -e_{16}^5. & R_{11}(g_3) &= -e_8. & R_{11}(g_4) &= i. & R_{11}(g_5) &= -1. \\
R_{12}(g_2) &= -e_{16}^7. & R_{12}(g_3) &= -e_8^3. & R_{12}(g_4) &= -i. & R_{12}(g_5) &= -1. \\
R_{13}(g_2) &= e_{16}^7. & R_{13}(g_3) &= -e_8^3. & R_{13}(g_4) &= -i. & R_{13}(g_5) &= -1. \\
R_{14}(g_2) &= e_{16}^5. & R_{14}(g_3) &= -e_8. & R_{14}(g_4) &= i. & R_{14}(g_5) &= -1. \\
R_{15}(g_2) &= e_{16}^3. & R_{15}(g_3) &= e_8^3. & R_{15}(g_4) &= -i. & R_{15}(g_5) &= -1. \\
R_{16}(g_2) &= e_{16}. & R_{16}(g_3) &= e_8. & R_{16}(g_4) &= i. & R_{16}(g_5) &= -1.
\end{aligned}$$

$G_{16}^{(2)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= 1. & R_2(g_5) &= 1. \\
R_3(g_2) &= -1. & R_3(g_3) &= 1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. \\
R_4(g_2) &= 1. & R_4(g_3) &= -1. & R_4(g_4) &= 1. & R_4(g_5) &= 1. \\
R_5(g_2) &= -1. & R_5(g_3) &= -i. & R_5(g_4) &= 1. & R_5(g_5) &= -1. \\
R_6(g_2) &= -1. & R_6(g_3) &= i. & R_6(g_4) &= 1. & R_6(g_5) &= -1. \\
R_7(g_2) &= 1. & R_7(g_3) &= -i. & R_7(g_4) &= 1. & R_7(g_5) &= -1. \\
R_8(g_2) &= 1. & R_8(g_3) &= i. & R_8(g_4) &= 1. & R_8(g_5) &= -1. \\
R_9(g_2) &= -i. & R_9(g_3) &= -1. & R_9(g_4) &= -1. & R_9(g_5) &= 1. \\
R_{10}(g_2) &= i. & R_{10}(g_3) &= -1. & R_{10}(g_4) &= -1. & R_{10}(g_5) &= 1. \\
R_{11}(g_2) &= -i. & R_{11}(g_3) &= 1. & R_{11}(g_4) &= -1. & R_{11}(g_5) &= 1. \\
R_{12}(g_2) &= i. & R_{12}(g_3) &= 1. & R_{12}(g_4) &= -1. & R_{12}(g_5) &= 1. \\
R_{13}(g_2) &= -i. & R_{13}(g_3) &= -i. & R_{13}(g_4) &= -1. & R_{13}(g_5) &= -1. \\
R_{14}(g_2) &= i. & R_{14}(g_3) &= i. & R_{14}(g_4) &= -1. & R_{14}(g_5) &= -1. \\
R_{15}(g_2) &= -i. & R_{15}(g_3) &= i. & R_{15}(g_4) &= -1. & R_{15}(g_5) &= -1. \\
R_{16}(g_2) &= i. & R_{16}(g_3) &= -i. & R_{16}(g_4) &= -1. & R_{16}(g_5) &= -1.
\end{aligned}$$

 $G_{16}^{(3)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= 1. & R_2(g_5) &= 1. \\
R_3(g_2) &= -1. & R_3(g_3) &= 1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. \\
R_4(g_2) &= 1. & R_4(g_3) &= -1. & R_4(g_4) &= 1. & R_4(g_5) &= 1. \\
R_5(g_2) &= -i. & R_5(g_3) &= -1. & R_5(g_4) &= 1. & R_5(g_5) &= -1. \\
R_6(g_2) &= i. & R_6(g_3) &= -1. & R_6(g_4) &= 1. & R_6(g_5) &= -1. \\
R_7(g_2) &= -i. & R_7(g_3) &= 1. & R_7(g_4) &= 1. & R_7(g_5) &= -1. \\
R_8(g_2) &= i. & R_8(g_3) &= 1. & R_8(g_4) &= 1. & R_8(g_5) &= -1. \\
R_9(g_2) &= -\lambda. & R_9(g_3) &= -\phi. & R_9(g_4) &= -\epsilon. & R_9(g_5) &= \epsilon. \\
R_{10}(g_2) &= i\lambda. & R_{10}(g_3) &= \phi. & R_{10}(g_4) &= -\epsilon. & R_{10}(g_5) &= -\epsilon.
\end{aligned}$$

 $G_{16}^{(4)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= 1. & R_2(g_5) &= 1. \\
R_3(g_2) &= -1. & R_3(g_3) &= 1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. \\
R_4(g_2) &= 1. & R_4(g_3) &= -1. & R_4(g_4) &= 1. & R_4(g_5) &= 1. \\
R_5(g_2) &= -i. & R_5(g_3) &= -1. & R_5(g_4) &= 1. & R_5(g_5) &= -1. \\
R_6(g_2) &= i. & R_6(g_3) &= -1. & R_6(g_4) &= 1. & R_6(g_5) &= -1. \\
R_7(g_2) &= -i. & R_7(g_3) &= 1. & R_7(g_4) &= 1. & R_7(g_5) &= -1. \\
R_8(g_2) &= i. & R_8(g_3) &= 1. & R_8(g_4) &= 1. & R_8(g_5) &= -1. \\
R_9(g_2) &= \lambda. & R_9(g_3) &= -\kappa. & R_9(g_4) &= -\epsilon. & R_9(g_5) &= \epsilon. \\
R_{10}(g_2) &= i\lambda. & R_{10}(g_3) &= \kappa. & R_{10}(g_4) &= -\epsilon. & R_{10}(g_5) &= -\epsilon.
\end{aligned}$$

$G_{16}^{(5)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= 1. & R_2(g_5) &= 1. \\
R_3(g_2) &= -1. & R_3(g_3) &= 1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. \\
R_4(g_2) &= 1. & R_4(g_3) &= -1. & R_4(g_4) &= 1. & R_4(g_5) &= 1. \\
R_5(g_2) &= -i. & R_5(g_3) &= -1. & R_5(g_4) &= -1. & R_5(g_5) &= 1. \\
R_6(g_2) &= i. & R_6(g_3) &= -1. & R_6(g_4) &= -1. & R_6(g_5) &= 1. \\
R_7(g_2) &= -i. & R_7(g_3) &= 1. & R_7(g_4) &= -1. & R_7(g_5) &= 1. \\
R_8(g_2) &= i. & R_8(g_3) &= 1. & R_8(g_4) &= -1. & R_8(g_5) &= 1. \\
R_9(g_2) &= -e_8. & R_9(g_3) &= -1. & R_9(g_4) &= i. & R_9(g_5) &= -1. \\
R_{10}(g_2) &= -e_8^3. & R_{10}(g_3) &= -1. & R_{10}(g_4) &= -i. & R_{10}(g_5) &= -1. \\
R_{11}(g_2) &= e_8^3. & R_{11}(g_3) &= -1. & R_{11}(g_4) &= -i. & R_{11}(g_5) &= -1. \\
R_{12}(g_2) &= e_8. & R_{12}(g_3) &= -1. & R_{12}(g_4) &= i. & R_{12}(g_5) &= -1. \\
R_{13}(g_2) &= -e_8. & R_{13}(g_3) &= 1. & R_{13}(g_4) &= i. & R_{13}(g_5) &= -1. \\
R_{14}(g_2) &= -e_8^3. & R_{14}(g_3) &= 1. & R_{14}(g_4) &= -i. & R_{14}(g_5) &= -1. \\
R_{15}(g_2) &= e_8^3. & R_{15}(g_3) &= 1. & R_{15}(g_4) &= -i. & R_{15}(g_5) &= -1. \\
R_{16}(g_2) &= e_8. & R_{16}(g_3) &= 1. & R_{16}(g_4) &= i. & R_{16}(g_5) &= -1.
\end{aligned}$$

 $G_{16}^{(6)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= 1. & R_2(g_5) &= 1. \\
R_3(g_2) &= -1. & R_3(g_3) &= 1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. \\
R_4(g_2) &= 1. & R_4(g_3) &= -1. & R_4(g_4) &= 1. & R_4(g_5) &= 1. \\
R_5(g_2) &= -i. & R_5(g_3) &= -1. & R_5(g_4) &= -1. & R_5(g_5) &= 1. \\
R_6(g_2) &= i. & R_6(g_3) &= -1. & R_6(g_4) &= -1. & R_6(g_5) &= 1. \\
R_7(g_2) &= -i. & R_7(g_3) &= 1. & R_7(g_4) &= -1. & R_7(g_5) &= 1. \\
R_8(g_2) &= i. & R_8(g_3) &= 1. & R_8(g_4) &= -1. & R_8(g_5) &= 1. \\
R_9(g_2) &= \begin{pmatrix} e_8^3 & 0 \\ 0 & -e_8^3 \end{pmatrix}. & R_9(g_3) &= \begin{pmatrix} 0 & -e_8^3 \\ e_8 & 0 \end{pmatrix}. & R_9(g_4) &= -i\epsilon. & R_9(g_5) &= -\epsilon. \\
R_{10}(g_2) &= \begin{pmatrix} -e_8 & 0 \\ 0 & e_8 \end{pmatrix}. & R_{10}(g_3) &= -i\kappa. & R_{10}(g_4) &= i\epsilon. & R_{10}(g_5) &= -\epsilon.
\end{aligned}$$

 $G_{16}^{(7)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= 1. & R_2(g_5) &= 1. \\
R_3(g_2) &= -1. & R_3(g_3) &= 1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. \\
R_4(g_2) &= 1. & R_4(g_3) &= -1. & R_4(g_4) &= 1. & R_4(g_5) &= 1. \\
R_5(g_2) &= \lambda. & R_5(g_3) &= \phi. & R_5(g_4) &= -\epsilon. & R_5(g_5) &= \epsilon. \\
R_6(g_2) &= \begin{pmatrix} -1 & 0 \\ -\sqrt{2}i & 1 \end{pmatrix}. & R_6(g_3) &= \begin{pmatrix} \sqrt{2} & -1 \\ 1 & -\sqrt{2}i \end{pmatrix}. \\
R_6(g_4) &= \begin{pmatrix} -1 & \sqrt{2} \\ -\sqrt{2}i & 1 \end{pmatrix}. & R_6(g_5) &= -\epsilon. \\
R_7(g_2) &= -\phi. & R_7(g_3) &= \begin{pmatrix} 1/\sqrt{2} & -1/\sqrt{2} \\ -1/\sqrt{2} & -1/\sqrt{2} \end{pmatrix}. & R_7(g_4) &= -\kappa. & R_7(g_5) &= -\epsilon.
\end{aligned}$$

$G_{16}^{(8)}$

$$R_2(g_2) = -1. \quad R_2(g_3) = -1. \quad R_2(g_4) = 1. \quad R_2(g_5) = 1.$$

$$R_3(g_2) = -1. \quad R_3(g_3) = 1. \quad R_3(g_4) = 1. \quad R_3(g_5) = 1.$$

$$R_4(g_2) = 1. \quad R_4(g_3) = -1. \quad R_4(g_4) = 1. \quad R_4(g_5) = 1.$$

$$R_5(g_2) = -\lambda. \quad R_5(g_3) = -\phi. \quad R_5(g_4) = -\epsilon. \quad R_5(g_5) = \epsilon.$$

$$R_6(g_2) = \begin{pmatrix} -i & \sqrt{2}i \\ 0 & i \end{pmatrix}. \quad R_6(g_3) = -\phi. \quad R_6(g_4) = \begin{pmatrix} -1 & \sqrt{2} \\ -\sqrt{2}i & 1 \end{pmatrix}. \quad R_6(g_5) = -\epsilon.$$

$$R_7(g_2) = \begin{pmatrix} -i & 0 \\ \sqrt{2} & i \end{pmatrix}. \quad R_7(g_3) = i\kappa. \quad R_7(g_4) = \begin{pmatrix} 1 & \sqrt{2}i \\ \sqrt{2}i & -1 \end{pmatrix}. \quad R_7(g_5) = -\epsilon.$$

 $G_{16}^{(9)}$

$$R_2(g_2) = -1. \quad R_2(g_3) = -1. \quad R_2(g_4) = 1. \quad R_2(g_5) = 1.$$

$$R_3(g_2) = -1. \quad R_3(g_3) = 1. \quad R_3(g_4) = 1. \quad R_3(g_5) = 1.$$

$$R_4(g_2) = 1. \quad R_4(g_3) = -1. \quad R_4(g_4) = 1. \quad R_4(g_5) = 1.$$

$$R_5(g_2) = -\lambda. \quad R_5(g_3) = -\phi. \quad R_5(g_4) = -\epsilon. \quad R_5(g_5) = \epsilon.$$

$$R_6(g_2) = \begin{pmatrix} i & -\sqrt{2}i \\ 0 & -i \end{pmatrix}. \quad R_6(g_3) = \begin{pmatrix} \sqrt{2}i & -1 \\ -1 & -\sqrt{2}i \end{pmatrix}. \quad R_6(g_4) = \begin{pmatrix} 1 & \sqrt{2}i \\ \sqrt{2}i & -1 \end{pmatrix}. \quad R_6(g_5) = -\epsilon.$$

$$R_7(g_2) = -i\phi. \quad R_7(g_3) = \begin{pmatrix} -1/\sqrt{2} & i/\sqrt{2} \\ i/\sqrt{2} & i/\sqrt{2} \end{pmatrix}. \quad R_7(g_4) = -\kappa. \quad R_7(g_5) = -\epsilon.$$

 $G_{16}^{(10)}$

$$R_2(g_2) = -1. \quad R_2(g_3) = -1. \quad R_2(g_4) = -1. \quad R_2(g_5) = 1.$$

$$R_3(g_2) = -1. \quad R_3(g_3) = -1. \quad R_3(g_4) = 1. \quad R_3(g_5) = 1.$$

$$R_4(g_2) = -1. \quad R_4(g_3) = 1. \quad R_4(g_4) = -1. \quad R_4(g_5) = 1.$$

$$R_5(g_2) = -1. \quad R_5(g_3) = 1. \quad R_5(g_4) = 1. \quad R_5(g_5) = 1.$$

$$R_6(g_2) = 1. \quad R_6(g_3) = -1. \quad R_6(g_4) = -1. \quad R_6(g_5) = 1.$$

$$R_7(g_2) = 1. \quad R_7(g_3) = -1. \quad R_7(g_4) = 1. \quad R_7(g_5) = 1.$$

$$R_8(g_2) = 1. \quad R_8(g_3) = 1. \quad R_8(g_4) = -1. \quad R_8(g_5) = 1.$$

$$R_9(g_2) = -i. \quad R_9(g_3) = -1. \quad R_9(g_4) = -1. \quad R_9(g_5) = -1.$$

$$R_{10}(g_2) = i. \quad R_{10}(g_3) = -1. \quad R_{10}(g_4) = -1. \quad R_{10}(g_5) = -1.$$

$$R_{11}(g_2) = -i. \quad R_{11}(g_3) = -1. \quad R_{11}(g_4) = 1. \quad R_{11}(g_5) = -1.$$

$$R_{12}(g_2) = i. \quad R_{12}(g_3) = -1. \quad R_{12}(g_4) = 1. \quad R_{12}(g_5) = -1.$$

$$R_{13}(g_2) = -i. \quad R_{13}(g_3) = 1. \quad R_{13}(g_4) = -1. \quad R_{13}(g_5) = -1.$$

$$R_{14}(g_2) = i. \quad R_{14}(g_3) = 1. \quad R_{14}(g_4) = -1. \quad R_{14}(g_5) = -1.$$

$$R_{15}(g_2) = -i. \quad R_{15}(g_3) = 1. \quad R_{15}(g_4) = 1. \quad R_{15}(g_5) = -1.$$

$$R_{16}(g_2) = i. \quad R_{16}(g_3) = 1. \quad R_{16}(g_4) = 1. \quad R_{16}(g_5) = -1.$$

$G_{16}^{(11)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= -1. & R_2(g_5) &= 1. \\
R_3(g_2) &= -1. & R_3(g_3) &= -1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. \\
R_4(g_2) &= -1. & R_4(g_3) &= 1. & R_4(g_4) &= -1. & R_4(g_5) &= 1. \\
R_5(g_2) &= -1. & R_5(g_3) &= 1. & R_5(g_4) &= 1. & R_5(g_5) &= 1. \\
R_6(g_2) &= 1. & R_6(g_3) &= -1. & R_6(g_4) &= -1. & R_6(g_5) &= 1. \\
R_7(g_2) &= 1. & R_7(g_3) &= -1. & R_7(g_4) &= 1. & R_7(g_5) &= 1. \\
R_8(g_2) &= 1. & R_8(g_3) &= 1. & R_8(g_4) &= -1. & R_8(g_5) &= 1. \\
R_9(g_2) &= -\lambda. & R_9(g_3) &= -\phi. & R_9(g_4) &= \epsilon. & R_9(g_5) &= -\epsilon. \\
R_{10}(g_2) &= \lambda. & R_{10}(g_3) &= -\phi. & R_{10}(g_4) &= -\epsilon. & R_{10}(g_5) &= -\epsilon.
\end{aligned}$$

 $G_{16}^{(12)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= -1. & R_2(g_5) &= 1. \\
R_3(g_2) &= -1. & R_3(g_3) &= -1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. \\
R_4(g_2) &= -1. & R_4(g_3) &= 1. & R_4(g_4) &= -1. & R_4(g_5) &= 1. \\
R_5(g_2) &= -1. & R_5(g_3) &= 1. & R_5(g_4) &= 1. & R_5(g_5) &= 1. \\
R_6(g_2) &= 1. & R_6(g_3) &= -1. & R_6(g_4) &= -1. & R_6(g_5) &= 1. \\
R_7(g_2) &= 1. & R_7(g_3) &= -1. & R_7(g_4) &= 1. & R_7(g_5) &= 1. \\
R_8(g_2) &= 1. & R_8(g_3) &= 1. & R_8(g_4) &= -1. & R_8(g_5) &= 1. \\
R_9(g_2) &= -i\lambda. & R_9(g_3) &= -i\phi. & R_9(g_4) &= \epsilon. & R_9(g_5) &= -\epsilon. \\
R_{10}(g_2) &= -i\lambda. & R_{10}(g_3) &= -i\phi. & R_{10}(g_4) &= -\epsilon. & R_{10}(g_5) &= -\epsilon.
\end{aligned}$$

 $G_{16}^{(13)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= -1. & R_2(g_5) &= 1. \\
R_3(g_2) &= -1. & R_3(g_3) &= -1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. \\
R_4(g_2) &= -1. & R_4(g_3) &= 1. & R_4(g_4) &= -1. & R_4(g_5) &= 1. \\
R_5(g_2) &= -1. & R_5(g_3) &= 1. & R_5(g_4) &= 1. & R_5(g_5) &= 1. \\
R_6(g_2) &= 1. & R_6(g_3) &= -1. & R_6(g_4) &= -1. & R_6(g_5) &= 1. \\
R_7(g_2) &= 1. & R_7(g_3) &= -1. & R_7(g_4) &= 1. & R_7(g_5) &= 1. \\
R_8(g_2) &= 1. & R_8(g_3) &= 1. & R_8(g_4) &= -1. & R_8(g_5) &= 1. \\
R_9(g_2) &= -\lambda. & R_9(g_3) &= -\phi. & R_9(g_4) &= -i\epsilon. & R_9(g_5) &= -\epsilon. \\
R_{10}(g_2) &= -\lambda. & R_{10}(g_3) &= -\phi. & R_{10}(g_4) &= i\epsilon. & R_{10}(g_5) &= -\epsilon.
\end{aligned}$$

$G_{16}^{(14)}$

$$\begin{aligned}
 R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= -1. & R_2(g_5) &= -1. \\
 R_3(g_2) &= -1. & R_3(g_3) &= -1. & R_3(g_4) &= -1. & R_3(g_5) &= 1. \\
 R_4(g_2) &= -1. & R_4(g_3) &= -1. & R_4(g_4) &= 1. & R_4(g_5) &= -1. \\
 R_5(g_2) &= -1. & R_5(g_3) &= -1. & R_5(g_4) &= 1. & R_5(g_5) &= 1. \\
 R_6(g_2) &= -1. & R_6(g_3) &= 1. & R_6(g_4) &= -1. & R_6(g_5) &= -1. \\
 R_7(g_2) &= -1. & R_7(g_3) &= 1. & R_7(g_4) &= -1. & R_7(g_5) &= 1. \\
 R_8(g_2) &= -1. & R_8(g_3) &= 1. & R_8(g_4) &= 1. & R_8(g_5) &= -1. \\
 R_9(g_2) &= -1. & R_9(g_3) &= 1. & R_9(g_4) &= 1. & R_9(g_5) &= 1. \\
 R_{10}(g_2) &= 1. & R_{10}(g_3) &= -1. & R_{10}(g_4) &= -1. & R_{10}(g_5) &= -1. \\
 R_{11}(g_2) &= 1. & R_{11}(g_3) &= -1. & R_{11}(g_4) &= -1. & R_{11}(g_5) &= 1. \\
 R_{12}(g_2) &= 1. & R_{12}(g_3) &= -1. & R_{12}(g_4) &= 1. & R_{12}(g_5) &= -1. \\
 R_{13}(g_2) &= 1. & R_{13}(g_3) &= -1. & R_{13}(g_4) &= 1. & R_{13}(g_5) &= 1. \\
 R_{14}(g_2) &= 1. & R_{14}(g_3) &= 1. & R_{14}(g_4) &= -1. & R_{14}(g_5) &= -1. \\
 R_{15}(g_2) &= 1. & R_{15}(g_3) &= 1. & R_{15}(g_4) &= -1. & R_{15}(g_5) &= 1. \\
 R_{16}(g_2) &= 1. & R_{16}(g_3) &= 1. & R_{16}(g_4) &= 1. & R_{16}(g_5) &= -1.
 \end{aligned}$$

 2.17. **Order 17.** $G_{17}^{(1)}$

$$R_j(g_2) = e_{17}^{j-1}, \quad j = 1, \dots, 17.$$

 2.18. **Order 18.** $G_{18}^{(1)}$

$$\begin{aligned}
 R_2(g_2) &= -1. & R_2(g_3) &= 1. & R_2(g_4) &= 1. \\
 R_3(g_2) &= \begin{pmatrix} 1 & 0 \\ -1 & -1 \end{pmatrix}. & R_3(g_3) &= \begin{pmatrix} -1 & -1 \\ 1 & 0 \end{pmatrix}. & R_3(g_4) &= \epsilon. \\
 R_4(g_2) &= \begin{pmatrix} 1/(2c_{18}) & -1 + 2\Re e_9 - 2\Re e_{18}^2 \\ -1/(2c_{18}) & -1/(2c_{18}) \end{pmatrix}. \\
 R_4(g_3) &= \begin{pmatrix} 1 - 2\Re e_9 + 2\Re e_{18}^2 & \Re e_{18}^7 \\ -\Re e_{18}^7 & -1 \end{pmatrix}. \\
 R_4(g_4) &= \begin{pmatrix} \Re e_{18}^7 & 1 - 2\Re e_9 + 2\Re e_{18}^2 \\ -1 + 2\Re e_9 - 2\Re e_{18}^2 & 1/(2c_{18}) \end{pmatrix}. \\
 R_5(g_2) &= \begin{pmatrix} -2(\Re e_9^2 + \Re e_{18})/3 & (-2e_9^2 - e_9^4 - e_9^5 - 2e_9^7)/3 \\ (-e_9^2 - 2e_9^4 - 2e_9^5 - e_9^7)/3 & (e_9^2 - e_9^4 - e_9^5 + e_9^7)/3 \end{pmatrix}. \\
 R_5(g_3) &= \begin{pmatrix} -2(\Re e_9^2 + \Re e_{18})/3 & (-2e_9^2 - e_9^4 - e_9^5 - 2e_9^7)/3 \\ (2e_9^2 + e_9^4 + e_9^5 + 2e_9^7)/3 & (e_9^2 + 2e_9^4 + 2e_9^5 + e_9^7)/3 \end{pmatrix}. \\
 R_5(g_4) &= \begin{pmatrix} 0 & 1 \\ -1 & -1 \end{pmatrix}.
 \end{aligned}$$

$$\begin{aligned}
R_6(g_2) &= \begin{pmatrix} e_9^2 + e_9^7 & -1 \\ -e_9^3 + e_9^4 + e_9^5 - e_9^6 & -e_9^2 - e_9^7 \end{pmatrix}. \\
R_6(g_3) &= \begin{pmatrix} e_9^3 - e_9^4 - e_9^5 + e_9^6 & e_9^2 + e_9^3 + e_9^6 + e_9^7 \\ -e_9^2 - e_9^3 - e_9^6 - e_9^7 & -e_9^2 - e_9^3 - e_9^6 - e_9^7 \end{pmatrix}. \\
R_6(g_4) &= \begin{pmatrix} -e_9^2 - e_9^7 & -e_9^3 + e_9^4 + e_9^5 - e_9^6 \\ e_9^3 - e_9^4 - e_9^5 + e_9^6 & e_9^2 + e_9^3 + e_9^6 + e_9^7 \end{pmatrix}.
\end{aligned}$$

 $G_{18}^{(2)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= 1. & R_2(g_4) &= 1. \\
R_3(g_2) &= -1. & R_3(g_3) &= e_3^2. & R_3(g_4) &= 1. \\
R_4(g_2) &= -1. & R_4(g_3) &= e_3. & R_4(g_4) &= 1. \\
R_5(g_2) &= -1. & R_5(g_3) &= -e_9^2 - e_9^5. & R_5(g_4) &= e_3^2. \\
R_6(g_2) &= -1. & R_6(g_3) &= -e_9^4 - e_9^7. & R_6(g_4) &= e_3. \\
R_7(g_2) &= -1. & R_7(g_3) &= e_9^7. & R_7(g_4) &= e_3. \\
R_8(g_2) &= -1. & R_8(g_3) &= e_9^5. & R_8(g_4) &= e_3^2. \\
R_9(g_2) &= -1. & R_9(g_3) &= e_9^4. & R_9(g_4) &= e_3. \\
R_{10}(g_2) &= -1. & R_{10}(g_3) &= e_9^2. & R_{10}(g_4) &= e_3^2. \\
R_{11}(g_2) &= 1. & R_{11}(g_3) &= e_3^2. & R_{11}(g_4) &= 1. \\
R_{12}(g_2) &= 1. & R_{12}(g_3) &= e_3. & R_{12}(g_4) &= 1. \\
R_{13}(g_2) &= 1. & R_{13}(g_3) &= -e_9^2 - e_9^5. & R_{13}(g_4) &= e_3^2. \\
R_{14}(g_2) &= 1. & R_{14}(g_3) &= -e_9^4 - e_9^7. & R_{14}(g_4) &= e_3. \\
R_{15}(g_2) &= 1. & R_{15}(g_3) &= e_9^7. & R_{15}(g_4) &= e_3. \\
R_{16}(g_2) &= 1. & R_{16}(g_3) &= e_9^5. & R_{16}(g_4) &= e_3^2. \\
R_{17}(g_2) &= 1. & R_{17}(g_3) &= e_9^4. & R_{17}(g_4) &= e_3. \\
R_{18}(g_2) &= 1. & R_{18}(g_3) &= e_9^2. & R_{18}(g_4) &= e_3^2.
\end{aligned}$$

 $G_{18}^{(3)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= 1. & R_2(g_4) &= 1. \\
R_3(g_2) &= -1. & R_3(g_3) &= e_3^2. & R_3(g_4) &= 1. \\
R_4(g_2) &= -1. & R_4(g_3) &= e_3. & R_4(g_4) &= 1. \\
R_5(g_2) &= 1. & R_5(g_3) &= e_3^2. & R_5(g_4) &= 1. \\
R_6(g_2) &= 1. & R_6(g_3) &= e_3. & R_6(g_4) &= 1. \\
R_7(g_2) &= \begin{pmatrix} 1 & 0 \\ -1 & -1 \end{pmatrix}. & R_7(g_3) &= \epsilon. & R_7(g_4) &= \begin{pmatrix} 0 & 1 \\ -1 & -1 \end{pmatrix}. \\
R_8(g_2) &= \begin{pmatrix} 0 & e_3^2 \\ e_3 & 0 \end{pmatrix}. & R_8(g_3) &= \begin{pmatrix} e_3 & 0 \\ 0 & e_3 \end{pmatrix}. & R_8(g_4) &= \begin{pmatrix} -1 & -e_3^2 \\ e_3 & 0 \end{pmatrix}. \\
R_9(g_2) &= \begin{pmatrix} 1 & 0 \\ -e_3 & -1 \end{pmatrix}. & R_9(g_3) &= \begin{pmatrix} e_3^2 & 0 \\ 0 & e_3^2 \end{pmatrix}. & R_9(g_4) &= \begin{pmatrix} 0 & e_3^2 \\ -e_3 & -1 \end{pmatrix}.
\end{aligned}$$

$G_{18}^{(4)}$

$$\begin{aligned}
 R_2(g_2) &= -1. & R_2(g_3) &= 1. & R_2(g_4) &= 1. \\
 R_3(g_2) &= \begin{pmatrix} 1 & 0 \\ -1 & -1 \end{pmatrix}. & R_3(g_3) &= \epsilon. & R_3(g_4) &= \begin{pmatrix} 0 & 1 \\ -1 & -1 \end{pmatrix}. \\
 R_4(g_2) &= \begin{pmatrix} -1 & -1 \\ 0 & 1 \end{pmatrix}. & R_4(g_3) &= \begin{pmatrix} -1 & -1 \\ 1 & 0 \end{pmatrix}. & R_4(g_4) &= \epsilon. \\
 R_5(g_2) &= \phi. & R_5(g_3) &= \begin{pmatrix} 0 & 1 \\ -1 & -1 \end{pmatrix}. & R_5(g_4) &= \begin{pmatrix} 0 & 1 \\ -1 & -1 \end{pmatrix}. \\
 R_6(g_2) &= \begin{pmatrix} -1 & -1 \\ 0 & 1 \end{pmatrix}. & R_6(g_3) &= \begin{pmatrix} 0 & 1 \\ -1 & -1 \end{pmatrix}. & R_6(g_4) &= \begin{pmatrix} -1 & -1 \\ 1 & 0 \end{pmatrix}.
 \end{aligned}$$

 $G_{18}^{(5)}$

$$\begin{aligned}
 R_2(g_2) &= -1. & R_2(g_3) &= 1. & R_2(g_4) &= 1. \\
 R_3(g_2) &= -1. & R_3(g_3) &= 1. & R_3(g_4) &= e_3^2. \\
 R_4(g_2) &= -1. & R_4(g_3) &= 1. & R_4(g_4) &= e_3. \\
 R_5(g_2) &= -1. & R_5(g_3) &= e_3^2. & R_5(g_4) &= 1. \\
 R_6(g_2) &= -1. & R_6(g_3) &= e_3. & R_6(g_4) &= 1. \\
 R_7(g_2) &= -1. & R_7(g_3) &= e_3^2. & R_7(g_4) &= e_3^2. \\
 R_8(g_2) &= -1. & R_8(g_3) &= e_3. & R_8(g_4) &= e_3. \\
 R_9(g_2) &= -1. & R_9(g_3) &= e_3^2. & R_9(g_4) &= e_3. \\
 R_{10}(g_2) &= -1. & R_{10}(g_3) &= e_3. & R_{10}(g_4) &= e_3^2. \\
 R_{11}(g_2) &= 1. & R_{11}(g_3) &= 1. & R_{11}(g_4) &= e_3^2. \\
 R_{12}(g_2) &= 1. & R_{12}(g_3) &= 1. & R_{12}(g_4) &= e_3. \\
 R_{13}(g_2) &= 1. & R_{13}(g_3) &= e_3^2. & R_{13}(g_4) &= 1. \\
 R_{14}(g_2) &= 1. & R_{14}(g_3) &= e_3. & R_{14}(g_4) &= 1. \\
 R_{15}(g_2) &= 1. & R_{15}(g_3) &= e_3^2. & R_{15}(g_4) &= e_3^2. \\
 R_{16}(g_2) &= 1. & R_{16}(g_3) &= e_3. & R_{16}(g_4) &= e_3. \\
 R_{17}(g_2) &= 1. & R_{17}(g_3) &= e_3^2. & R_{17}(g_4) &= e_3. \\
 R_{18}(g_2) &= 1. & R_{18}(g_3) &= e_3. & R_{18}(g_4) &= e_3^2.
 \end{aligned}$$

 2.19. **Order 19.** $G_{19}^{(1)}$

$$R_j(g_2) = e_{19}^{j-1}, \quad j = 1, \dots, 19.$$

2.20. Order 20. $G_{20}^{(1)}$

$$R_2(g_2) = -1. \quad R_2(g_3) = 1. \quad R_2(g_4) = 1.$$

$$R_3(g_2) = -i. \quad R_3(g_3) = -1. \quad R_3(g_4) = 1.$$

$$R_4(g_2) = i. \quad R_4(g_3) = -1. \quad R_4(g_4) = 1.$$

$$R_5(g_2) = i\phi. \quad R_5(g_3) = -\epsilon. \quad R_5(g_4) = \begin{pmatrix} -2\Re e_5 & -2\Re e_5 \\ 2\Re e_5 & -1 \end{pmatrix}.$$

$$R_6(g_2) = \begin{pmatrix} i & 0 \\ -\varphi & -i \end{pmatrix}. \quad R_6(g_3) = -\epsilon. \quad R_6(g_4) = \begin{pmatrix} -1 & -e_{20}^{13} - e_{20}^{17} \\ -e_{20}^{13} - e_{20}^{17} & -\varphi \end{pmatrix}.$$

$$R_7(g_2) = \begin{pmatrix} 2\Re e_5 & -1 \\ -2\Re e_5 & -2\Re e_5 \end{pmatrix}. \quad R_7(g_3) = \epsilon. \quad R_7(g_4) = \begin{pmatrix} -2\Re e_5 & -2\Re e_5 \\ 2\Re e_5 & -1 \end{pmatrix}.$$

$$R_8(g_2) = \begin{pmatrix} 1 & 0 \\ \varphi & -1 \end{pmatrix}. \quad R_8(g_3) = \epsilon. \quad R_8(g_4) = \begin{pmatrix} -\varphi & -\varphi \\ \varphi & -1 \end{pmatrix}.$$

 $G_{20}^{(2)}$

$$R_2(g_2) = -1. \quad R_2(g_3) = 1. \quad R_2(g_4) = 1.$$

$$R_3(g_2) = -1. \quad R_3(g_3) = e_5^4. \quad R_3(g_4) = 1.$$

$$R_4(g_2) = -1. \quad R_4(g_3) = e_5^3. \quad R_4(g_4) = 1.$$

$$R_5(g_2) = -1. \quad R_5(g_3) = e_5^2. \quad R_5(g_4) = 1.$$

$$R_6(g_2) = -1. \quad R_6(g_3) = e_5. \quad R_6(g_4) = 1.$$

$$R_7(g_2) = 1. \quad R_7(g_3) = e_5^4. \quad R_7(g_4) = 1.$$

$$R_8(g_2) = 1. \quad R_8(g_3) = e_5^3. \quad R_8(g_4) = 1.$$

$$R_9(g_2) = 1. \quad R_9(g_3) = e_5^2. \quad R_9(g_4) = 1.$$

$$R_{10}(g_2) = 1. \quad R_{10}(g_3) = e_5. \quad R_{10}(g_4) = 1.$$

$$R_{11}(g_2) = -i. \quad R_{11}(g_3) = 1. \quad R_{11}(g_4) = -1.$$

$$R_{12}(g_2) = i. \quad R_{12}(g_3) = 1. \quad R_{12}(g_4) = -1.$$

$$R_{13}(g_2) = -i. \quad R_{13}(g_3) = e_5^4. \quad R_{13}(g_4) = -1.$$

$$R_{14}(g_2) = -i. \quad R_{14}(g_3) = e_5^3. \quad R_{14}(g_4) = -1.$$

$$R_{15}(g_2) = -i. \quad R_{15}(g_3) = e_5^2. \quad R_{15}(g_4) = -1.$$

$$R_{16}(g_2) = -i. \quad R_{16}(g_3) = e_5. \quad R_{16}(g_4) = -1.$$

$$R_{17}(g_2) = i. \quad R_{17}(g_3) = e_5^4. \quad R_{17}(g_4) = -1.$$

$$R_{18}(g_2) = i. \quad R_{18}(g_3) = e_5^3. \quad R_{18}(g_4) = -1.$$

$$R_{19}(g_2) = i. \quad R_{19}(g_3) = e_5^2. \quad R_{19}(g_4) = -1.$$

$$R_{20}(g_2) = i. \quad R_{20}(g_3) = e_5. \quad R_{20}(g_4) = -1.$$

$G_{20}^{(3)}$

$$\begin{aligned} R_2(g_2) &= -1. & R_2(g_3) &= 1. & R_2(g_4) &= 1. \\ R_3(g_2) &= -i. & R_3(g_3) &= -1. & R_3(g_4) &= 1. \\ R_4(g_2) &= i. & R_4(g_3) &= -1. & R_4(g_4) &= 1. \end{aligned}$$

$$R_5(g_2) = \begin{pmatrix} 0 & 0 & 0 & 1 \\ 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ -1 & -1 & -1 & -1 \end{pmatrix}.$$

$$R_5(g_3) = \begin{pmatrix} -1 & -1 & -1 & -1 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{pmatrix}.$$

$$R_5(g_4) = \begin{pmatrix} 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 \\ -1 & -1 & -1 & -1 \\ 0 & 0 & 1 & 0 \end{pmatrix}.$$

 $G_{20}^{(4)}$

$$\begin{aligned} R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= 1. \\ R_3(g_2) &= -1. & R_3(g_3) &= 1. & R_3(g_4) &= 1. \\ R_4(g_2) &= 1. & R_4(g_3) &= -1. & R_4(g_4) &= 1. \end{aligned}$$

$$R_5(g_2) = \begin{pmatrix} -2\Re e_5 & -2\Re e_5 \\ -1 & 2\Re e_5 \end{pmatrix}. \quad R_5(g_3) = -\epsilon. \quad R_5(g_4) = \begin{pmatrix} -1 & 2\Re e_5 \\ -2\Re e_5 & -2\Re e_5 \end{pmatrix}.$$

$$R_6(g_2) = \begin{pmatrix} \varphi & -1 \\ -\varphi & -\varphi \end{pmatrix}. \quad R_6(g_3) = -\epsilon. \quad R_6(g_4) = \begin{pmatrix} -\varphi & -\varphi \\ \varphi & -1 \end{pmatrix}.$$

$$R_7(g_2) = \phi. \quad R_7(g_3) = \epsilon. \quad R_7(g_4) = \begin{pmatrix} \varphi & -1 \\ 1 & 0 \end{pmatrix}.$$

$$R_8(g_2) = \phi. \quad R_8(g_3) = \epsilon. \quad R_8(g_4) = \begin{pmatrix} -\varphi & -\varphi \\ \varphi & -1 \end{pmatrix}.$$

 $G_{20}^{(5)}$

$$\begin{aligned} R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= 1. \\ R_3(g_2) &= -1. & R_3(g_3) &= 1. & R_3(g_4) &= 1. \\ R_4(g_2) &= 1. & R_4(g_3) &= -1. & R_4(g_4) &= 1. \end{aligned}$$

$$R_5(g_2) = -1. \quad R_5(g_3) = -1. \quad R_5(g_4) = e_5^4.$$

$$R_6(g_2) = -1. \quad R_6(g_3) = -1. \quad R_6(g_4) = e_5^3.$$

$$R_7(g_2) = -1. \quad R_7(g_3) = -1. \quad R_7(g_4) = e_5^2.$$

$$R_8(g_2) = -1. \quad R_8(g_3) = -1. \quad R_8(g_4) = e_5.$$

$$R_9(g_2) = -1. \quad R_9(g_3) = 1. \quad R_9(g_4) = e_5^4.$$

$$R_{10}(g_2) = -1. \quad R_{10}(g_3) = 1. \quad R_{10}(g_4) = e_5^3.$$

$$R_{11}(g_2) = -1. \quad R_{11}(g_3) = 1. \quad R_{11}(g_4) = e_5^2.$$

$$R_{12}(g_2) = -1. \quad R_{12}(g_3) = 1. \quad R_{12}(g_4) = e_5.$$

$$\begin{aligned}
R_{13}(g_2) &= 1. & R_{13}(g_3) &= -1. & R_{13}(g_4) &= e_5^4. \\
R_{14}(g_2) &= 1. & R_{14}(g_3) &= -1. & R_{14}(g_4) &= e_5^3. \\
R_{15}(g_2) &= 1. & R_{15}(g_3) &= -1. & R_{15}(g_4) &= e_5^2. \\
R_{16}(g_2) &= 1. & R_{16}(g_3) &= -1. & R_{16}(g_4) &= e_5. \\
R_{17}(g_2) &= 1. & R_{17}(g_3) &= 1. & R_{17}(g_4) &= e_5^4. \\
R_{18}(g_2) &= 1. & R_{18}(g_3) &= 1. & R_{18}(g_4) &= e_5^3. \\
R_{19}(g_2) &= 1. & R_{19}(g_3) &= 1. & R_{19}(g_4) &= e_5^2. \\
R_{20}(g_2) &= 1. & R_{20}(g_3) &= 1. & R_{20}(g_4) &= e_5.
\end{aligned}$$

2.21. **Order 21.** $G_{21}^{(1)}$

$$R_2(g_2) = e_3^2. \quad R_2(g_3) = 1.$$

$$R_3(g_2) = e_3. \quad R_3(g_3) = 1.$$

$$R_4(g_2) = \begin{pmatrix} (e_7^3 + e_7^5 + e_7^6)/2 & e_7 + e_7^2 + e_7^4 + (e_7^3 + e_7^5 + e_7^6)/2 & -(e_7^3 + e_7^5 + e_7^6)/2 \\ e_7 + e_7^2 + e_7^4 + (e_7^3 + e_7^5 + e_7^6)/2 & -(e_7^3 + e_7^5 + e_7^6)/2 & (e_7^3 + e_7^5 + e_7^6)/2 \\ 1 & 0 & 0 \end{pmatrix}.$$

$$R_4(g_3) = \begin{pmatrix} 0 & 0 & 1 \\ e_7 + e_7^2 + e_7^4 + (e_7^3 + e_7^5 + e_7^6)/2 & -(e_7^3 + e_7^5 + e_7^6)/2 & (e_7^3 + e_7^5 + e_7^6)/2 \\ -(e_7^3 + e_7^5 + e_7^6)/2 & (e_7^3 + e_7^5 + e_7^6)/2 & e_7 + e_7^2 + e_7^4 + (e_7^3 + e_7^5 + e_7^6)/2 \end{pmatrix}.$$

$$R_5(g_2) = \begin{pmatrix} 0 & 1 & 0 \\ e_7^3 + e_7^5 + e_7^6 & 1 & -e_7 - e_7^2 - e_7^4 \\ e_7 + e_7^2 + e_7^4 & -1 & -1 \end{pmatrix}.$$

$$R_5(g_3) = \begin{pmatrix} 1 & e_7 + e_7^2 + e_7^4 & -e_7^3 - e_7^5 - e_7^6 \\ -1 & e_7^3 + e_7^5 + e_7^6 & -1 \\ e_7 + e_7^2 + e_7^4 & -1 & -1 \end{pmatrix}.$$

$G_{21}^{(2)}$

$$R_2(g_2) = 1. \quad R_2(g_3) = e_7^6.$$

$$R_3(g_2) = 1. \quad R_3(g_3) = e_7^5.$$

$$R_4(g_2) = 1. \quad R_4(g_3) = e_7^4.$$

$$R_5(g_2) = 1. \quad R_5(g_3) = e_7^3.$$

$$R_6(g_2) = 1. \quad R_6(g_3) = e_7^2.$$

$$R_7(g_2) = 1. \quad R_7(g_3) = e_7.$$

$$R_8(g_2) = e_3^2. \quad R_8(g_3) = 1.$$

$$R_9(g_2) = e_3. \quad R_9(g_3) = 1.$$

$$R_{10}(g_2) = e_3^2. \quad R_{10}(g_3) = e_7^6.$$

$$R_{11}(g_2) = e_3^2. \quad R_{11}(g_3) = e_7^5.$$

$$R_{12}(g_2) = e_3^2. \quad R_{12}(g_3) = e_7^4.$$

$$R_{13}(g_2) = e_3^2. \quad R_{13}(g_3) = e_7^3.$$

$$R_{14}(g_2) = e_3^2. \quad R_{14}(g_3) = e_7^2.$$

$$R_{15}(g_2) = e_3^2. \quad R_{15}(g_3) = e_7.$$

$$R_{16}(g_2) = e_3. \quad R_{16}(g_3) = e_7^6.$$

$$R_{17}(g_2) = e_3. \quad R_{17}(g_3) = e_7^5.$$

$$R_{18}(g_2) = e_3. \quad R_{18}(g_3) = e_7^4.$$

$$R_{19}(g_2) = e_3. \quad R_{19}(g_3) = e_7^3.$$

$$R_{20}(g_2) = e_3. \quad R_{20}(g_3) = e_7^2.$$

$$R_{21}(g_2) = e_3. \quad R_{21}(g_3) = e_7.$$

2.22. Order 22. $G_{22}^{(1)}$

$$R_2(g_2) = -1. \quad R_2(g_3) = 1.$$

$$R_3(g_2) = \begin{pmatrix} e_{11}^3 + e_{11}^8 & -1 \\ \alpha_{22,1} & -e_{11}^3 - e_{11}^8 \end{pmatrix}. \quad R_3(g_3) = \begin{pmatrix} -e_{11}^2 - e_{11}^3 - e_{11}^8 - e_{11}^9 & \alpha_{22,2} \\ -\alpha_{22,2} & -\alpha_{22,2} \end{pmatrix}.$$

Constants:

$$\alpha_{22,1} \equiv -e_{11} - e_{11}^2 - e_{11}^3 - e_{11}^4 - e_{11}^7 - e_{11}^8 - e_{11}^9 - e_{11}^{10};$$

$$\alpha_{22,2} \equiv -e_{11}^2 - e_{11}^3 - e_{11}^4 - e_{11}^7 - e_{11}^8 - e_{11}^9.$$

$$R_4(g_2) = \begin{pmatrix} e_{11}^3 + e_{11}^4 + e_{11}^5 + e_{11}^6 + e_{11}^7 + e_{11}^8 & e_{11}^3 + e_{11}^4 + e_{11}^5 + e_{11}^6 + e_{11}^7 + e_{11}^8 \\ -e_{11}^4 - e_{11}^5 - e_{11}^6 - e_{11}^7 & -e_{11}^3 - e_{11}^4 - e_{11}^5 - e_{11}^6 - e_{11}^7 - e_{11}^8 \end{pmatrix}.$$

$$R_4(g_3) = \begin{pmatrix} 0 & 1 \\ -1 & e_{11}^5 + e_{11}^6 \end{pmatrix}.$$

$$R_5(g_2) = \begin{pmatrix} \alpha_{22,2} & -e_{11}^2 - e_{11}^3 - e_{11}^8 - e_{11}^9 \\ -\alpha_{22,2} & -\alpha_{22,2} \end{pmatrix}.$$

$$R_5(g_3) = \begin{pmatrix} -e_{11}^3 - e_{11}^8 & \alpha_{11,1} \\ -\alpha_{11,1} & e_{11}^2 + e_{11}^3 + e_{11}^8 + e_{11}^9 \end{pmatrix}.$$

$$R_6(g_2) = \begin{pmatrix} & e_{11}^2 + e_{11}^9 & -1 \\ -e_{11} - e_{11}^2 - e_{11}^3 - e_{11}^5 - e_{11}^6 - e_{11}^8 - e_{11}^9 - e_{11}^{10} & -e_{11}^2 - e_{11}^9 & \end{pmatrix}.$$

$$R_6(g_3) = \begin{pmatrix} -e_{11} - e_{11}^2 - e_{11}^5 - e_{11}^6 - e_{11}^9 - e_{11}^{10} & -e_{11}^2 - e_{11}^5 - e_{11}^6 - e_{11}^9 \\ e_{11}^2 + e_{11}^5 + e_{11}^6 + e_{11}^9 & e_{11} + e_{11}^2 + e_{11}^3 + e_{11}^5 + e_{11}^6 + e_{11}^8 + e_{11}^9 + e_{11}^{10} \end{pmatrix}.$$

$$R_7(g_2) = \begin{pmatrix} 1 & 0 \\ e_{11} + e_{11}^{10} & -1 \end{pmatrix}. \quad R_7(g_3) = \begin{pmatrix} e_{11} + e_{11}^{10} & -1 \\ 1 & 0 \end{pmatrix}.$$

$G_{22}^{(2)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= 1. \\
R_3(g_2) &= -1. & R_3(g_3) &= e_{11}^{10}. \\
R_4(g_2) &= -1. & R_4(g_3) &= e_{11}^9. \\
R_5(g_2) &= -1. & R_5(g_3) &= e_{11}^8. \\
R_6(g_2) &= -1. & R_6(g_3) &= e_{11}^7. \\
R_7(g_2) &= -1. & R_7(g_3) &= e_{11}^6. \\
R_8(g_2) &= -1. & R_8(g_3) &= e_{11}^5. \\
R_9(g_2) &= -1. & R_9(g_3) &= e_{11}^4. \\
R_{10}(g_2) &= -1. & R_{10}(g_3) &= e_{11}^3. \\
R_{11}(g_2) &= -1. & R_{11}(g_3) &= e_{11}^2. \\
R_{12}(g_2) &= -1. & R_{12}(g_3) &= e_{11}. \\
R_{13}(g_2) &= 1. & R_{13}(g_3) &= e_{11}^{10}. \\
R_{14}(g_2) &= 1. & R_{14}(g_3) &= e_{11}^9. \\
R_{15}(g_2) &= 1. & R_{15}(g_3) &= e_{11}^8. \\
R_{16}(g_2) &= 1. & R_{16}(g_3) &= e_{11}^7. \\
R_{17}(g_2) &= 1. & R_{17}(g_3) &= e_{11}^6. \\
R_{18}(g_2) &= 1. & R_{18}(g_3) &= e_{11}^5. \\
R_{19}(g_2) &= 1. & R_{19}(g_3) &= e_{11}^4. \\
R_{20}(g_2) &= 1. & R_{20}(g_3) &= e_{11}^3. \\
R_{21}(g_2) &= 1. & R_{21}(g_3) &= e_{11}^2. \\
R_{22}(g_2) &= 1. & R_{22}(g_3) &= e_{11}.
\end{aligned}$$

2.23. Order 23. $G_{23}^{(1)}$

$$R_j(g_2) = e_{23}^{j-1}, \quad j = 1, \dots, 23.$$

2.24. Order 24. $G_{24}^{(1)}$

$$\begin{aligned}
 R_2(g_2) &= -1. & R_2(g_3) &= 1. & R_2(g_4) &= 1. & R_2(g_5) &= 1. \\
 R_3(g_2) &= -i. & R_3(g_3) &= -1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. \\
 R_4(g_2) &= i. & R_4(g_3) &= -1. & R_4(g_4) &= 1. & R_4(g_5) &= 1. \\
 R_5(g_2) &= -e_8. & R_5(g_3) &= i. & R_5(g_4) &= -1. & R_5(g_5) &= 1. \\
 R_6(g_2) &= -e_8^3. & R_6(g_3) &= -i. & R_6(g_4) &= -1. & R_6(g_5) &= 1. \\
 R_7(g_2) &= e_8^3. & R_7(g_3) &= -i. & R_7(g_4) &= -1. & R_7(g_5) &= 1. \\
 R_8(g_2) &= e_8. & R_8(g_3) &= i. & R_8(g_4) &= -1. & R_8(g_5) &= 1. \\
 R_9(g_2) &= \kappa. & R_9(g_3) &= -\epsilon. & R_9(g_4) &= \epsilon. & R_9(g_5) &= \begin{pmatrix} -1 & i \\ i & 0 \end{pmatrix}. \\
 R_{10}(g_2) &= \phi. & R_{10}(g_3) &= \epsilon. & R_{10}(g_4) &= \epsilon. & R_{10}(g_5) &= \begin{pmatrix} -1 & -1 \\ 1 & 0 \end{pmatrix}. \\
 R_{11}(g_2) &= \begin{pmatrix} e_8^3 & 0 \\ -i & -e_8^3 \end{pmatrix}. & R_{11}(g_3) &= -i\epsilon. & R_{11}(g_4) &= -\epsilon. & R_{11}(g_5) &= \begin{pmatrix} -1 & -e_8 \\ -e_8^3 & 0 \end{pmatrix}. \\
 R_{12}(g_2) &= \begin{pmatrix} e_8 & 0 \\ e_8^3 & -e_8 \end{pmatrix}. & R_{12}(g_3) &= i\epsilon. & R_{12}(g_4) &= -\epsilon. & R_{12}(g_5) &= \begin{pmatrix} 0 & i \\ i & -1 \end{pmatrix}.
 \end{aligned}$$

 $G_{24}^{(2)}$

$$\begin{aligned}
 R_2(g_2) &= -1. & R_2(g_3) &= 1. & R_2(g_4) &= 1. & R_2(g_5) &= 1. \\
 R_3(g_2) &= -1. & R_3(g_3) &= e_3^2. & R_3(g_4) &= 1. & R_3(g_5) &= 1. \\
 R_4(g_2) &= -1. & R_4(g_3) &= e_3. & R_4(g_4) &= 1. & R_4(g_5) &= 1. \\
 R_5(g_2) &= 1. & R_5(g_3) &= e_3^2. & R_5(g_4) &= 1. & R_5(g_5) &= 1. \\
 R_6(g_2) &= 1. & R_6(g_3) &= e_3. & R_6(g_4) &= 1. & R_6(g_5) &= 1. \\
 R_7(g_2) &= -i. & R_7(g_3) &= 1. & R_7(g_4) &= -1. & R_7(g_5) &= 1. \\
 R_8(g_2) &= i. & R_8(g_3) &= 1. & R_8(g_4) &= -1. & R_8(g_5) &= 1. \\
 R_9(g_2) &= -i. & R_9(g_3) &= e_3^2. & R_9(g_4) &= -1. & R_9(g_5) &= 1. \\
 R_{10}(g_2) &= -i. & R_{10}(g_3) &= e_3. & R_{10}(g_4) &= -1. & R_{10}(g_5) &= 1. \\
 R_{11}(g_2) &= i. & R_{11}(g_3) &= e_3^2. & R_{11}(g_4) &= -1. & R_{11}(g_5) &= 1. \\
 R_{12}(g_2) &= i. & R_{12}(g_3) &= e_3. & R_{12}(g_4) &= -1. & R_{12}(g_5) &= 1. \\
 R_{13}(g_2) &= -e_8. & R_{13}(g_3) &= 1. & R_{13}(g_4) &= i. & R_{13}(g_5) &= -1. \\
 R_{14}(g_2) &= -e_8^3. & R_{14}(g_3) &= 1. & R_{14}(g_4) &= -i. & R_{14}(g_5) &= -1. \\
 R_{15}(g_2) &= e_8^3. & R_{15}(g_3) &= 1. & R_{15}(g_4) &= -i. & R_{15}(g_5) &= -1. \\
 R_{16}(g_2) &= e_8. & R_{16}(g_3) &= 1. & R_{16}(g_4) &= i. & R_{16}(g_5) &= -1. \\
 R_{17}(g_2) &= -e_8. & R_{17}(g_3) &= e_3^2. & R_{17}(g_4) &= i. & R_{17}(g_5) &= -1. \\
 R_{18}(g_2) &= -e_8. & R_{18}(g_3) &= e_3. & R_{18}(g_4) &= i. & R_{18}(g_5) &= -1. \\
 R_{19}(g_2) &= -e_8^3. & R_{19}(g_3) &= e_3^2. & R_{19}(g_4) &= -i. & R_{19}(g_5) &= -1. \\
 R_{20}(g_2) &= -e_8^3. & R_{20}(g_3) &= e_3. & R_{20}(g_4) &= -i. & R_{20}(g_5) &= -1. \\
 R_{21}(g_2) &= e_8^3. & R_{21}(g_3) &= e_3^2. & R_{21}(g_4) &= -i. & R_{21}(g_5) &= -1. \\
 R_{22}(g_2) &= e_8^3. & R_{22}(g_3) &= e_3. & R_{22}(g_4) &= -i. & R_{22}(g_5) &= -1. \\
 R_{23}(g_2) &= e_8. & R_{23}(g_3) &= e_3^2. & R_{23}(g_4) &= i. & R_{23}(g_5) &= -1. \\
 R_{24}(g_2) &= e_8. & R_{24}(g_3) &= e_3. & R_{24}(g_4) &= i. & R_{24}(g_5) &= -1.
 \end{aligned}$$

$$\begin{aligned}
& G_{24}^{(3)} \\
& R_2(g_2) = e_3^2. \quad R_2(g_3) = 1. \quad R_2(g_4) = 1. \quad R_2(g_5) = 1. \\
& R_3(g_2) = e_3. \quad R_3(g_3) = 1. \quad R_3(g_4) = 1. \quad R_3(g_5) = 1. \\
& R_4(g_2) = \begin{pmatrix} e_3^2 & -e_3 \\ 0 & e_3 \end{pmatrix}. \quad R_4(g_3) = \begin{pmatrix} -e_3 & 1 \\ e_3 & e_3 \end{pmatrix}. \quad R_4(g_4) = \begin{pmatrix} 0 & -e_3 \\ e_3^2 & 0 \end{pmatrix}. \quad R_4(g_5) = -\epsilon. \\
& R_5(g_2) = \begin{pmatrix} 0 & -1 \\ e_3^2 & -e_3 \end{pmatrix}. \quad R_5(g_3) = \begin{pmatrix} -e_3 & -e_3^2 \\ -e_3^2 & e_3 \end{pmatrix}. \quad R_5(g_4) = \begin{pmatrix} -e_3^2 & e_3 \\ e_3 & e_3^2 \end{pmatrix}. \quad R_5(g_5) = -\epsilon. \\
& R_6(g_2) = \begin{pmatrix} 0 & 1 \\ -e_3 & -e_3^2 \end{pmatrix}. \quad R_6(g_3) = \begin{pmatrix} -e_3^2 & e_3 \\ e_3 & e_3^2 \end{pmatrix}. \quad R_6(g_4) = \begin{pmatrix} -e_3 & -e_3^2 \\ -e_3^2 & e_3 \end{pmatrix}. \quad R_6(g_5) = -\epsilon. \\
& R_7(g_2) = \begin{pmatrix} -1 & -1 & -1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{pmatrix}. \quad R_7(g_3) = \begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ -1 & -1 & -1 \end{pmatrix}. \\
& R_7(g_4) = \begin{pmatrix} 0 & 0 & 1 \\ -1 & -1 & -1 \\ 1 & 0 & 0 \end{pmatrix}. \quad R_7(g_5) = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}.
\end{aligned}$$

$$\begin{aligned}
& G_{24}^{(4)} \\
& R_2(g_2) = -1. \quad R_2(g_3) = -1. \quad R_2(g_4) = 1. \quad R_2(g_5) = 1. \\
& R_3(g_2) = -1. \quad R_3(g_3) = 1. \quad R_3(g_4) = 1. \quad R_3(g_5) = 1. \\
& R_4(g_2) = 1. \quad R_4(g_3) = -1. \quad R_4(g_4) = 1. \quad R_4(g_5) = 1. \\
& R_5(g_2) = -i\lambda. \quad R_5(g_3) = -i\phi. \quad R_5(g_4) = -\epsilon. \quad R_5(g_5) = \epsilon. \\
& R_6(g_2) = \begin{pmatrix} 1 & 0 \\ -1 & -1 \end{pmatrix}. \quad R_6(g_3) = -\epsilon. \quad R_6(g_4) = \epsilon. \quad R_6(g_5) = \begin{pmatrix} 0 & 1 \\ -1 & -1 \end{pmatrix}. \\
& R_7(g_2) = \begin{pmatrix} 1 & 0 \\ -1 & -1 \end{pmatrix}. \quad R_7(g_3) = \epsilon. \quad R_7(g_4) = \epsilon. \quad R_7(g_5) = \begin{pmatrix} -1 & -1 \\ 1 & 0 \end{pmatrix}. \\
& R_8(g_2) = \begin{pmatrix} 2i & \alpha_{24} \\ \alpha_{24} & -2i \end{pmatrix}. \quad R_8(g_3) = \begin{pmatrix} \alpha_{24} & -2i \\ -2i & -\alpha_{24} \end{pmatrix}. \quad R_8(g_4) = -\epsilon. \quad R_8(g_5) = \begin{pmatrix} -2 & \sqrt{3}i \\ \sqrt{3}i & 1 \end{pmatrix}.
\end{aligned}$$

Constants:

$$\alpha_{24} \equiv -e_{12}^7 + e_{12}^{11}.$$

$$R_9(g_2) = -i\lambda. \quad R_9(g_3) = i\phi. \quad R_9(g_4) = -\epsilon. \quad R_9(g_5) = \begin{pmatrix} -1/2 & \sqrt{3}i/2 \\ \sqrt{3}i/2 & -1/2 \end{pmatrix}.$$

$$\begin{aligned}
& G_{24}^{(5)} \\
& R_2(g_2) = -1. \quad R_2(g_3) = -1. \quad R_2(g_4) = 1. \quad R_2(g_5) = 1. \\
& R_3(g_2) = -1. \quad R_3(g_3) = 1. \quad R_3(g_4) = 1. \quad R_3(g_5) = 1. \\
& R_4(g_2) = 1. \quad R_4(g_3) = -1. \quad R_4(g_4) = 1. \quad R_4(g_5) = 1. \\
& R_5(g_2) = -1. \quad R_5(g_3) = -i. \quad R_5(g_4) = -1. \quad R_5(g_5) = 1. \\
& R_6(g_2) = -1. \quad R_6(g_3) = i. \quad R_6(g_4) = -1. \quad R_6(g_5) = 1. \\
& R_7(g_2) = 1. \quad R_7(g_3) = -i. \quad R_7(g_4) = -1. \quad R_7(g_5) = 1. \\
& R_8(g_2) = 1. \quad R_8(g_3) = i. \quad R_8(g_4) = -1. \quad R_8(g_5) = 1. \\
& R_9(g_2) = \begin{pmatrix} 1 & 0 \\ -1 & -1 \end{pmatrix}. \quad R_9(g_3) = -\epsilon. \quad R_9(g_4) = \epsilon. \quad R_9(g_5) = \begin{pmatrix} -1 & -1 \\ 1 & 0 \end{pmatrix}.
\end{aligned}$$

$$R_{10}(g_2) = \begin{pmatrix} 1 & 0 \\ -1 & -1 \end{pmatrix}. \quad R_{10}(g_3) = \epsilon. \quad R_{10}(g_4) = \epsilon. \quad R_{10}(g_5) = \begin{pmatrix} 0 & 1 \\ -1 & -1 \end{pmatrix}.$$

$$R_{11}(g_2) = \begin{pmatrix} 1 & 0 \\ 1 & -1 \end{pmatrix}. \quad R_{11}(g_3) = -i\epsilon. \quad R_{11}(g_4) = -\epsilon. \quad R_{11}(g_5) = \begin{pmatrix} 0 & -1 \\ 1 & -1 \end{pmatrix}.$$

$$R_{12}(g_2) = \phi. \quad R_{12}(g_3) = i\epsilon. \quad R_{12}(g_4) = -\epsilon. \quad R_{12}(g_5) = \begin{pmatrix} 0 & 1 \\ -1 & -1 \end{pmatrix}.$$

 $G_{24}^{(6)}$

$$R_2(g_2) = -1. \quad R_2(g_3) = -1. \quad R_2(g_4) = 1. \quad R_2(g_5) = 1.$$

$$R_3(g_2) = -1. \quad R_3(g_3) = 1. \quad R_3(g_4) = 1. \quad R_3(g_5) = 1.$$

$$R_4(g_2) = 1. \quad R_4(g_3) = -1. \quad R_4(g_4) = 1. \quad R_4(g_5) = 1.$$

$$R_5(g_2) = \lambda. \quad R_5(g_3) = \kappa. \quad R_5(g_4) = -\epsilon. \quad R_5(g_5) = \epsilon.$$

$$R_6(g_2) = \phi. \quad R_6(g_3) = -\epsilon. \quad R_6(g_4) = \epsilon. \quad R_6(g_5) = \begin{pmatrix} 0 & 1 \\ -1 & -1 \end{pmatrix}.$$

$$R_7(g_2) = \begin{pmatrix} -1 & -1 \\ 0 & 1 \end{pmatrix}. \quad R_7(g_3) = \epsilon. \quad R_7(g_4) = \epsilon. \quad R_7(g_5) = \begin{pmatrix} -1 & -1 \\ 1 & 0 \end{pmatrix}.$$

$$R_8(g_2) = \begin{pmatrix} 1 & 0 \\ -1 & -1 \end{pmatrix}. \quad R_8(g_3) = \begin{pmatrix} \alpha_{24}/3 & 2\alpha_{24}/3 \\ -2\alpha_{24}/3 & -\alpha_{24}/3 \end{pmatrix}. \quad R_8(g_4) = -\epsilon. \quad R_8(g_5) = \begin{pmatrix} -1 & -1 \\ 1 & 0 \end{pmatrix}.$$

$$R_9(g_2) = \begin{pmatrix} -1 & -1 \\ 0 & 1 \end{pmatrix}. \quad R_9(g_3) = \begin{pmatrix} \alpha_{24}/3 & 2\alpha_{24}/3 \\ -2\alpha_{24}/3 & -\alpha_{24}/3 \end{pmatrix}. \quad R_9(g_4) = -\epsilon. \quad R_9(g_5) = \begin{pmatrix} 0 & 1 \\ -1 & -1 \end{pmatrix}.$$

 $G_{24}^{(7)}$

$$R_2(g_2) = -1. \quad R_2(g_3) = -1. \quad R_2(g_4) = 1. \quad R_2(g_5) = 1.$$

$$R_3(g_2) = -1. \quad R_3(g_3) = 1. \quad R_3(g_4) = 1. \quad R_3(g_5) = 1.$$

$$R_4(g_2) = 1. \quad R_4(g_3) = -1. \quad R_4(g_4) = 1. \quad R_4(g_5) = 1.$$

$$R_5(g_2) = -i. \quad R_5(g_3) = -1. \quad R_5(g_4) = -1. \quad R_5(g_5) = 1.$$

$$R_6(g_2) = i. \quad R_6(g_3) = -1. \quad R_6(g_4) = -1. \quad R_6(g_5) = 1.$$

$$R_7(g_2) = -i. \quad R_7(g_3) = 1. \quad R_7(g_4) = -1. \quad R_7(g_5) = 1.$$

$$R_8(g_2) = i. \quad R_8(g_3) = 1. \quad R_8(g_4) = -1. \quad R_8(g_5) = 1.$$

$$R_9(g_2) = \begin{pmatrix} -i & -1 \\ 0 & i \end{pmatrix}. \quad R_9(g_3) = -\epsilon. \quad R_9(g_4) = -\epsilon. \quad R_9(g_5) = \begin{pmatrix} -1 & i \\ i & 0 \end{pmatrix}.$$

$$R_{10}(g_2) = \begin{pmatrix} 1 & 0 \\ -1 & -1 \end{pmatrix}. \quad R_{10}(g_3) = -\epsilon. \quad R_{10}(g_4) = \epsilon. \quad R_{10}(g_5) = \begin{pmatrix} 0 & 1 \\ -1 & -1 \end{pmatrix}.$$

$$R_{11}(g_2) = i\phi. \quad R_{11}(g_3) = \epsilon. \quad R_{11}(g_4) = -\epsilon. \quad R_{11}(g_5) = \begin{pmatrix} -1 & -1 \\ 1 & 0 \end{pmatrix}.$$

$$R_{12}(g_2) = \begin{pmatrix} -1 & -1 \\ 0 & 1 \end{pmatrix}. \quad R_{12}(g_3) = \epsilon. \quad R_{12}(g_4) = \epsilon. \quad R_{12}(g_5) = \begin{pmatrix} -1 & -1 \\ 1 & 0 \end{pmatrix}.$$

$$\begin{aligned}
& G_{24}^{(8)} \\
& R_2(g_2) = -1. \quad R_2(g_3) = -1. \quad R_2(g_4) = 1. \quad R_2(g_5) = 1. \\
& R_3(g_2) = -1. \quad R_3(g_3) = 1. \quad R_3(g_4) = 1. \quad R_3(g_5) = 1. \\
& R_4(g_2) = 1. \quad R_4(g_3) = -1. \quad R_4(g_4) = 1. \quad R_4(g_5) = 1. \\
& R_5(g_2) = \begin{pmatrix} 1 & 0 \\ 1 & -1 \end{pmatrix}. \quad R_5(g_3) = -\epsilon. \quad R_5(g_4) = \epsilon. \quad R_5(g_5) = \begin{pmatrix} -1 & 1 \\ -1 & 0 \end{pmatrix}. \\
& R_6(g_2) = \begin{pmatrix} 1 & 0 \\ -1 & -1 \end{pmatrix}. \quad R_6(g_3) = \epsilon. \quad R_6(g_4) = \epsilon. \quad R_6(g_5) = \begin{pmatrix} 0 & 1 \\ -1 & -1 \end{pmatrix}. \\
& R_7(g_2) = \lambda. \quad R_7(g_3) = -\phi. \quad R_7(g_4) = -\epsilon. \quad R_7(g_5) = \epsilon. \\
& R_8(g_2) = \begin{pmatrix} 1/2 & -\sqrt{3}i/2 \\ \sqrt{3}i/2 & -1/2 \end{pmatrix}. \quad R_8(g_3) = -\phi. \quad R_8(g_4) = -\epsilon. \quad R_8(g_5) = \begin{pmatrix} -1/2 & \sqrt{3}i/2 \\ \sqrt{3}i/2 & -1/2 \end{pmatrix}. \\
& R_9(g_2) = \begin{pmatrix} 1 & -1 \\ 0 & -1 \end{pmatrix}. \quad R_9(g_3) = \begin{pmatrix} -i/\sqrt{3} & 2i/\sqrt{3} \\ -2i/\sqrt{3} & i/\sqrt{3} \end{pmatrix}. \quad R_9(g_4) = -\epsilon. \quad R_9(g_5) = \begin{pmatrix} 0 & -1 \\ 1 & -1 \end{pmatrix}.
\end{aligned}$$

$$\begin{aligned}
& G_{24}^{(9)} \\
& R_2(g_2) = -1. \quad R_2(g_3) = -1. \quad R_2(g_4) = 1. \quad R_2(g_5) = 1. \\
& R_3(g_2) = -1. \quad R_3(g_3) = 1. \quad R_3(g_4) = 1. \quad R_3(g_5) = 1. \\
& R_4(g_2) = 1. \quad R_4(g_3) = -1. \quad R_4(g_4) = 1. \quad R_4(g_5) = 1. \\
& R_5(g_2) = -1. \quad R_5(g_3) = -1. \quad R_5(g_4) = e_3^2. \quad R_5(g_5) = 1. \\
& R_6(g_2) = -1. \quad R_6(g_3) = -1. \quad R_6(g_4) = e_3. \quad R_6(g_5) = 1. \\
& R_7(g_2) = -1. \quad R_7(g_3) = 1. \quad R_7(g_4) = e_3^2. \quad R_7(g_5) = 1. \\
& R_8(g_2) = -1. \quad R_8(g_3) = 1. \quad R_8(g_4) = e_3. \quad R_8(g_5) = 1. \\
& R_9(g_2) = 1. \quad R_9(g_3) = -1. \quad R_9(g_4) = e_3^2. \quad R_9(g_5) = 1. \\
& R_{10}(g_2) = 1. \quad R_{10}(g_3) = -1. \quad R_{10}(g_4) = e_3. \quad R_{10}(g_5) = 1. \\
& R_{11}(g_2) = 1. \quad R_{11}(g_3) = 1. \quad R_{11}(g_4) = e_3^2. \quad R_{11}(g_5) = 1. \\
& R_{12}(g_2) = 1. \quad R_{12}(g_3) = 1. \quad R_{12}(g_4) = e_3. \quad R_{12}(g_5) = 1. \\
& R_{13}(g_2) = -i. \quad R_{13}(g_3) = -1. \quad R_{13}(g_4) = 1. \quad R_{13}(g_5) = -1. \\
& R_{14}(g_2) = i. \quad R_{14}(g_3) = -1. \quad R_{14}(g_4) = 1. \quad R_{14}(g_5) = -1. \\
& R_{15}(g_2) = -i. \quad R_{15}(g_3) = -1. \quad R_{15}(g_4) = e_3^2. \quad R_{15}(g_5) = -1. \\
& R_{16}(g_2) = -i. \quad R_{16}(g_3) = -1. \quad R_{16}(g_4) = e_3. \quad R_{16}(g_5) = -1. \\
& R_{17}(g_2) = i. \quad R_{17}(g_3) = -1. \quad R_{17}(g_4) = e_3^2. \quad R_{17}(g_5) = -1. \\
& R_{18}(g_2) = i. \quad R_{18}(g_3) = -1. \quad R_{18}(g_4) = e_3. \quad R_{18}(g_5) = -1. \\
& R_{19}(g_2) = -i. \quad R_{19}(g_3) = 1. \quad R_{19}(g_4) = 1. \quad R_{19}(g_5) = -1. \\
& R_{20}(g_2) = i. \quad R_{20}(g_3) = 1. \quad R_{20}(g_4) = 1. \quad R_{20}(g_5) = -1. \\
& R_{21}(g_2) = -i. \quad R_{21}(g_3) = 1. \quad R_{21}(g_4) = e_3^2. \quad R_{21}(g_5) = -1. \\
& R_{22}(g_2) = -i. \quad R_{22}(g_3) = 1. \quad R_{22}(g_4) = e_3. \quad R_{22}(g_5) = -1. \\
& R_{23}(g_2) = i. \quad R_{23}(g_3) = 1. \quad R_{23}(g_4) = e_3^2. \quad R_{23}(g_5) = -1. \\
& R_{24}(g_2) = i. \quad R_{24}(g_3) = 1. \quad R_{24}(g_4) = e_3. \quad R_{24}(g_5) = -1.
\end{aligned}$$

$G_{24}^{(10)}$

$$R_2(g_2) = -1. \quad R_2(g_3) = -1. \quad R_2(g_4) = 1. \quad R_2(g_5) = 1.$$

$$R_3(g_2) = -1. \quad R_3(g_3) = 1. \quad R_3(g_4) = 1. \quad R_3(g_5) = 1.$$

$$R_4(g_2) = 1. \quad R_4(g_3) = -1. \quad R_4(g_4) = 1. \quad R_4(g_5) = 1.$$

$$R_5(g_2) = -1. \quad R_5(g_3) = -1. \quad R_5(g_4) = e_3^2. \quad R_5(g_5) = 1.$$

$$R_6(g_2) = -1. \quad R_6(g_3) = -1. \quad R_6(g_4) = e_3. \quad R_6(g_5) = 1.$$

$$R_7(g_2) = -1. \quad R_7(g_3) = 1. \quad R_7(g_4) = e_3^2. \quad R_7(g_5) = 1.$$

$$R_8(g_2) = -1. \quad R_8(g_3) = 1. \quad R_8(g_4) = e_3. \quad R_8(g_5) = 1.$$

$$R_9(g_2) = 1. \quad R_9(g_3) = -1. \quad R_9(g_4) = e_3^2. \quad R_9(g_5) = 1.$$

$$R_{10}(g_2) = 1. \quad R_{10}(g_3) = -1. \quad R_{10}(g_4) = e_3. \quad R_{10}(g_5) = 1.$$

$$R_{11}(g_2) = 1. \quad R_{11}(g_3) = 1. \quad R_{11}(g_4) = e_3^2. \quad R_{11}(g_5) = 1.$$

$$R_{12}(g_2) = 1. \quad R_{12}(g_3) = 1. \quad R_{12}(g_4) = e_3. \quad R_{12}(g_5) = 1.$$

$$R_{13}(g_2) = -\lambda. \quad R_{13}(g_3) = \phi. \quad R_{13}(g_4) = \epsilon. \quad R_{13}(g_5) = -\epsilon.$$

$$R_{14}(g_2) = \lambda. \quad R_{14}(g_3) = -\phi. \quad R_{14}(g_4) = \begin{pmatrix} e_3^2 & 0 \\ 0 & e_3^2 \end{pmatrix}. \quad R_{14}(g_5) = -\epsilon.$$

$$R_{15}(g_2) = \lambda. \quad R_{15}(g_3) = \begin{pmatrix} 0 & -e_3 \\ -e_3^2 & 0 \end{pmatrix}. \quad R_{15}(g_4) = \begin{pmatrix} e_3 & 0 \\ 0 & e_3 \end{pmatrix}. \quad R_{15}(g_5) = -\epsilon.$$

 $G_{24}^{(11)}$

$$R_2(g_2) = -1. \quad R_2(g_3) = -1. \quad R_2(g_4) = 1. \quad R_2(g_5) = 1.$$

$$R_3(g_2) = -1. \quad R_3(g_3) = 1. \quad R_3(g_4) = 1. \quad R_3(g_5) = 1.$$

$$R_4(g_2) = 1. \quad R_4(g_3) = -1. \quad R_4(g_4) = 1. \quad R_4(g_5) = 1.$$

$$R_5(g_2) = -1. \quad R_5(g_3) = -1. \quad R_5(g_4) = e_3^2. \quad R_5(g_5) = 1.$$

$$R_6(g_2) = -1. \quad R_6(g_3) = -1. \quad R_6(g_4) = e_3. \quad R_6(g_5) = 1.$$

$$R_7(g_2) = -1. \quad R_7(g_3) = 1. \quad R_7(g_4) = e_3^2. \quad R_7(g_5) = 1.$$

$$R_8(g_2) = -1. \quad R_8(g_3) = 1. \quad R_8(g_4) = e_3. \quad R_8(g_5) = 1.$$

$$R_9(g_2) = 1. \quad R_9(g_3) = -1. \quad R_9(g_4) = e_3^2. \quad R_9(g_5) = 1.$$

$$R_{10}(g_2) = 1. \quad R_{10}(g_3) = -1. \quad R_{10}(g_4) = e_3. \quad R_{10}(g_5) = 1.$$

$$R_{11}(g_2) = 1. \quad R_{11}(g_3) = 1. \quad R_{11}(g_4) = e_3^2. \quad R_{11}(g_5) = 1.$$

$$R_{12}(g_2) = 1. \quad R_{12}(g_3) = 1. \quad R_{12}(g_4) = e_3. \quad R_{12}(g_5) = 1.$$

$$R_{13}(g_2) = i\lambda. \quad R_{13}(g_3) = i\phi. \quad R_{13}(g_4) = \epsilon. \quad R_{13}(g_5) = -\epsilon.$$

$$R_{14}(g_2) = -i\lambda. \quad R_{14}(g_3) = \begin{pmatrix} 0 & e_{12}^7 \\ e_{12}^{11} & 0 \end{pmatrix}. \quad R_{14}(g_4) = \begin{pmatrix} e_3^2 & 0 \\ 0 & e_3^2 \end{pmatrix}. \quad R_{14}(g_5) = -\epsilon.$$

$$R_{15}(g_2) = i\lambda. \quad R_{15}(g_3) = \begin{pmatrix} 0 & e_{12}^{11} \\ e_{12}^7 & 0 \end{pmatrix}. \quad R_{15}(g_4) = \begin{pmatrix} e_3 & 0 \\ 0 & e_3 \end{pmatrix}. \quad R_{15}(g_5) = -\epsilon.$$

$$\begin{aligned}
& G_{24}^{(12)} \\
& R_2(g_2) = -1. \quad R_2(g_3) = 1. \quad R_2(g_4) = 1. \quad R_2(g_5) = 1. \\
R_3(g_2) &= \begin{pmatrix} 1 & 0 \\ -1 & -1 \end{pmatrix}. \quad R_3(g_3) = \begin{pmatrix} -1 & -1 \\ 1 & 0 \end{pmatrix}. \quad R_3(g_4) = \epsilon. \quad R_3(g_5) = \epsilon. \\
R_4(g_2) &= \begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 1 & 1 & -1 \end{pmatrix}. \quad R_4(g_3) = \begin{pmatrix} 0 & -1 & 0 \\ 0 & 1 & -1 \\ 1 & 1 & -1 \end{pmatrix}. \\
R_4(g_4) &= \begin{pmatrix} -1 & 0 & 0 \\ 1 & 1 & -1 \\ 0 & 0 & -1 \end{pmatrix}. \quad R_4(g_5) = \begin{pmatrix} 0 & 0 & 1 \\ 0 & -1 & 0 \\ 1 & 0 & 0 \end{pmatrix}. \\
R_5(g_2) &= \begin{pmatrix} -1 & 0 & 0 \\ -1 & 1 & 0 \\ 1 & 0 & 1 \end{pmatrix}. \quad R_5(g_3) = \begin{pmatrix} -1 & 0 & -1 \\ -1 & 1 & 0 \\ 1 & 0 & 0 \end{pmatrix}. \\
R_5(g_4) &= \begin{pmatrix} 0 & -1 & -1 \\ 0 & -1 & 0 \\ -1 & 1 & 0 \end{pmatrix}. \quad R_5(g_5) = \begin{pmatrix} 0 & 1 & 1 \\ 1 & 0 & 1 \\ 0 & 0 & -1 \end{pmatrix}.
\end{aligned}$$

$$\begin{aligned}
& G_{24}^{(13)} \\
& R_2(g_2) = -1. \quad R_2(g_3) = 1. \quad R_2(g_4) = 1. \quad R_2(g_5) = 1. \\
R_3(g_2) &= -1. \quad R_3(g_3) = e_3^2. \quad R_3(g_4) = 1. \quad R_3(g_5) = 1. \\
R_4(g_2) &= -1. \quad R_4(g_3) = e_3. \quad R_4(g_4) = 1. \quad R_4(g_5) = 1. \\
R_5(g_2) &= 1. \quad R_5(g_3) = e_3^2. \quad R_5(g_4) = 1. \quad R_5(g_5) = 1. \\
R_6(g_2) &= 1. \quad R_6(g_3) = e_3. \quad R_6(g_4) = 1. \quad R_6(g_5) = 1. \\
R_7(g_2) &= \begin{pmatrix} -1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & -1 \end{pmatrix}. \quad R_7(g_3) = \begin{pmatrix} 0 & 0 & 1 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \end{pmatrix}. \\
R_7(g_4) &= \begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ -1 & -1 & -1 \end{pmatrix}. \quad R_7(g_5) = \begin{pmatrix} 0 & 0 & 1 \\ -1 & -1 & -1 \\ 1 & 0 & 0 \end{pmatrix}. \\
R_8(g_2) &= \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}. \quad R_8(g_3) = \begin{pmatrix} 1 & 0 & 0 \\ -1 & -1 & -1 \\ 0 & 1 & 0 \end{pmatrix}. \\
R_8(g_4) &= \begin{pmatrix} 0 & 0 & 1 \\ -1 & -1 & -1 \\ 1 & 0 & 0 \end{pmatrix}. \quad R_8(g_5) = \begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ -1 & -1 & -1 \end{pmatrix}.
\end{aligned}$$

$$\begin{aligned}
& G_{24}^{(14)} \\
& R_2(g_2) = -1. \quad R_2(g_3) = -1. \quad R_2(g_4) = -1. \quad R_2(g_5) = 1. \\
R_3(g_2) &= -1. \quad R_3(g_3) = -1. \quad R_3(g_4) = 1. \quad R_3(g_5) = 1. \\
R_4(g_2) &= -1. \quad R_4(g_3) = 1. \quad R_4(g_4) = -1. \quad R_4(g_5) = 1. \\
R_5(g_2) &= -1. \quad R_5(g_3) = 1. \quad R_5(g_4) = 1. \quad R_5(g_5) = 1.
\end{aligned}$$

$$\begin{aligned}
 R_6(g_2) &= 1. & R_6(g_3) &= -1. & R_6(g_4) &= -1. & R_6(g_5) &= 1. \\
 R_7(g_2) &= 1. & R_7(g_3) &= -1. & R_7(g_4) &= 1. & R_7(g_5) &= 1. \\
 R_8(g_2) &= 1. & R_8(g_3) &= 1. & R_8(g_4) &= -1. & R_8(g_5) &= 1. \\
 R_9(g_2) &= \begin{pmatrix} -1 & -1 \\ 0 & 1 \end{pmatrix}. & R_9(g_3) &= -\epsilon. & R_9(g_4) &= -\epsilon. & R_9(g_5) &= \begin{pmatrix} 0 & 1 \\ -1 & -1 \end{pmatrix}. \\
 R_{10}(g_2) &= \begin{pmatrix} -1 & 1 \\ 0 & 1 \end{pmatrix}. & R_{10}(g_3) &= -\epsilon. & R_{10}(g_4) &= \epsilon. & R_{10}(g_5) &= \begin{pmatrix} -1 & 1 \\ -1 & 0 \end{pmatrix}. \\
 R_{11}(g_2) &= \begin{pmatrix} -1 & 1 \\ 0 & 1 \end{pmatrix}. & R_{11}(g_3) &= \epsilon. & R_{11}(g_4) &= -\epsilon. & R_{11}(g_5) &= \begin{pmatrix} -1 & 1 \\ -1 & 0 \end{pmatrix}. \\
 R_{12}(g_2) &= \begin{pmatrix} 1 & 0 \\ -1 & -1 \end{pmatrix}. & R_{12}(g_3) &= \epsilon. & R_{12}(g_4) &= \epsilon. & R_{12}(g_5) &= \begin{pmatrix} 0 & 1 \\ -1 & -1 \end{pmatrix}.
 \end{aligned}$$

 $G_{24}^{(15)}$

$$\begin{aligned}
 R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= -1. & R_2(g_5) &= 1. \\
 R_3(g_2) &= -1. & R_3(g_3) &= -1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. \\
 R_4(g_2) &= -1. & R_4(g_3) &= 1. & R_4(g_4) &= -1. & R_4(g_5) &= 1. \\
 R_5(g_2) &= -1. & R_5(g_3) &= 1. & R_5(g_4) &= 1. & R_5(g_5) &= 1. \\
 R_6(g_2) &= 1. & R_6(g_3) &= -1. & R_6(g_4) &= -1. & R_6(g_5) &= 1. \\
 R_7(g_2) &= 1. & R_7(g_3) &= -1. & R_7(g_4) &= 1. & R_7(g_5) &= 1. \\
 R_8(g_2) &= 1. & R_8(g_3) &= 1. & R_8(g_4) &= -1. & R_8(g_5) &= 1. \\
 R_9(g_2) &= -1. & R_9(g_3) &= -1. & R_9(g_4) &= -1. & R_9(g_5) &= e_3^2. \\
 R_{10}(g_2) &= -1. & R_{10}(g_3) &= -1. & R_{10}(g_4) &= -1. & R_{10}(g_5) &= e_3. \\
 R_{11}(g_2) &= -1. & R_{11}(g_3) &= -1. & R_{11}(g_4) &= 1. & R_{11}(g_5) &= e_3^2. \\
 R_{12}(g_2) &= -1. & R_{12}(g_3) &= -1. & R_{12}(g_4) &= 1. & R_{12}(g_5) &= e_3. \\
 R_{13}(g_2) &= -1. & R_{13}(g_3) &= 1. & R_{13}(g_4) &= -1. & R_{13}(g_5) &= e_3^2. \\
 R_{14}(g_2) &= -1. & R_{14}(g_3) &= 1. & R_{14}(g_4) &= -1. & R_{14}(g_5) &= e_3. \\
 R_{15}(g_2) &= -1. & R_{15}(g_3) &= 1. & R_{15}(g_4) &= 1. & R_{15}(g_5) &= e_3^2. \\
 R_{16}(g_2) &= -1. & R_{16}(g_3) &= 1. & R_{16}(g_4) &= 1. & R_{16}(g_5) &= e_3. \\
 R_{17}(g_2) &= 1. & R_{17}(g_3) &= -1. & R_{17}(g_4) &= -1. & R_{17}(g_5) &= e_3^2. \\
 R_{18}(g_2) &= 1. & R_{18}(g_3) &= -1. & R_{18}(g_4) &= -1. & R_{18}(g_5) &= e_3. \\
 R_{19}(g_2) &= 1. & R_{19}(g_3) &= -1. & R_{19}(g_4) &= 1. & R_{19}(g_5) &= e_3^2. \\
 R_{20}(g_2) &= 1. & R_{20}(g_3) &= -1. & R_{20}(g_4) &= 1. & R_{20}(g_5) &= e_3. \\
 R_{21}(g_2) &= 1. & R_{21}(g_3) &= 1. & R_{21}(g_4) &= -1. & R_{21}(g_5) &= e_3^2. \\
 R_{22}(g_2) &= 1. & R_{22}(g_3) &= 1. & R_{22}(g_4) &= -1. & R_{22}(g_5) &= e_3. \\
 R_{23}(g_2) &= 1. & R_{23}(g_3) &= 1. & R_{23}(g_4) &= 1. & R_{23}(g_5) &= e_3^2. \\
 R_{24}(g_2) &= 1. & R_{24}(g_3) &= 1. & R_{24}(g_4) &= 1. & R_{24}(g_5) &= e_3.
 \end{aligned}$$

2.25. Order 25. $G_{25}^{(1)}$

$$\begin{aligned}
R_2(g_2) &= e_5. & R_2(g_3) &= 1. \\
R_3(g_2) &= e_5^2. & R_3(g_3) &= 1. \\
R_4(g_2) &= e_5^3. & R_4(g_3) &= 1. \\
R_5(g_2) &= e_5^4. & R_5(g_3) &= 1. \\
R_6(g_2) &= -e_{25}^6 - e_{25}^{11} - e_{25}^{16} - e_{25}^{21}. & R_6(g_3) &= e_5. \\
R_7(g_2) &= e_{25}^6. & R_7(g_3) &= e_5. \\
R_8(g_2) &= e_{25}^{11}. & R_8(g_3) &= e_5. \\
R_9(g_2) &= e_{25}^{16}. & R_9(g_3) &= e_5. \\
R_{10}(g_2) &= e_{25}^{21}. & R_{10}(g_3) &= e_5. \\
R_{11}(g_2) &= -e_{25}^7 - e_{25}^{12} - e_{25}^{17} - e_{25}^{22}. & R_{11}(g_3) &= e_5^2. \\
R_{12}(g_2) &= e_{25}^7. & R_{12}(g_3) &= e_5^2. \\
R_{13}(g_2) &= e_{25}^{12}. & R_{13}(g_3) &= e_5^2. \\
R_{14}(g_2) &= e_{25}^{17}. & R_{14}(g_3) &= e_5^2. \\
R_{15}(g_2) &= e_{25}^{22}. & R_{15}(g_3) &= e_5^2. \\
R_{16}(g_2) &= e_{25}^3. & R_{16}(g_3) &= e_5^3. \\
R_{17}(g_2) &= e_{25}^8. & R_{17}(g_3) &= e_5^3. \\
R_{18}(g_2) &= e_{25}^{13}. & R_{18}(g_3) &= e_5^3. \\
R_{19}(g_2) &= e_{25}^{18}. & R_{19}(g_3) &= e_5^3. \\
R_{20}(g_2) &= -e_{25}^3 - e_{25}^8 - e_{25}^{13} - e_{25}^{18}. & R_{20}(g_3) &= e_5^3. \\
R_{21}(g_2) &= e_{25}^4. & R_{21}(g_3) &= e_5^4. \\
R_{22}(g_2) &= e_{25}^9. & R_{22}(g_3) &= e_5^4. \\
R_{23}(g_2) &= e_{25}^{14}. & R_{23}(g_3) &= e_5^4. \\
R_{24}(g_2) &= e_{25}^{19}. & R_{24}(g_3) &= e_5^4. \\
R_{25}(g_2) &= -e_{25}^4 - e_{25}^9 - e_{25}^{14} - e_{25}^{19}. & R_{25}(g_3) &= e_5^4.
\end{aligned}$$

 $G_{25}^{(2)}$

$$\begin{aligned}
R_2(g_2) &= e_5. & R_2(g_3) &= 1. \\
R_3(g_2) &= e_5^2. & R_3(g_3) &= 1. \\
R_4(g_2) &= e_5^3. & R_4(g_3) &= 1. \\
R_5(g_2) &= e_5^4. & R_5(g_3) &= 1. \\
R_6(g_2) &= 1. & R_6(g_3) &= e_5. \\
R_7(g_2) &= e_5. & R_7(g_3) &= e_5. \\
R_8(g_2) &= e_5^2. & R_8(g_3) &= e_5. \\
R_9(g_2) &= e_5^3. & R_9(g_3) &= e_5. \\
R_{10}(g_2) &= e_5^4. & R_{10}(g_3) &= e_5. \\
R_{11}(g_2) &= 1. & R_{11}(g_3) &= e_5^2. \\
R_{12}(g_2) &= e_5. & R_{12}(g_3) &= e_5^2. \\
R_{13}(g_2) &= e_5^2. & R_{13}(g_3) &= e_5^2. \\
R_{14}(g_2) &= e_5^3. & R_{14}(g_3) &= e_5^2. \\
R_{15}(g_2) &= e_5^4. & R_{15}(g_3) &= e_5^2.
\end{aligned}$$

$$\begin{aligned}
R_{16}(g_2) &= 1. & R_{16}(g_3) &= e_5^3. \\
R_{17}(g_2) &= e_5. & R_{17}(g_3) &= e_5^3. \\
R_{18}(g_2) &= e_5^2. & R_{18}(g_3) &= e_5^3. \\
R_{19}(g_2) &= e_5^3. & R_{19}(g_3) &= e_5^3. \\
R_{20}(g_2) &= e_5^4. & R_{20}(g_3) &= e_5^3. \\
R_{21}(g_2) &= 1. & R_{21}(g_3) &= e_5^4. \\
R_{22}(g_2) &= e_5. & R_{22}(g_3) &= e_5^4. \\
R_{23}(g_2) &= e_5^2. & R_{23}(g_3) &= e_5^4. \\
R_{24}(g_2) &= e_5^3. & R_{24}(g_3) &= e_5^4. \\
R_{25}(g_2) &= e_5^4. & R_{25}(g_3) &= e_5^4.
\end{aligned}$$

2.26. **Order 26.** $G_{26}^{(1)}$

$$R_2(g_2) = -1. \quad R_2(g_3) = 1.$$

$$R_3(g_2) = \begin{pmatrix} e_{13} + e_{13}^{12} & -1 \\ \alpha_{26,1} & -e_{13} - e_{13}^{12} \end{pmatrix}. \quad R_3(g_3) = \begin{pmatrix} e_{13} + e_{13}^3 + e_{13}^{10} + e_{13}^{12} & \alpha_{26,1} \\ \alpha_{26,1} & -e_{13} - e_{13}^{12} \end{pmatrix}.$$

Constants:

$$\alpha_{26,1} \equiv -e_{13} - e_{13}^3 - e_{13}^4 - e_{13}^5 - e_{13}^6 - e_{13}^7 - e_{13}^8 - e_{13}^9 - e_{13}^{10} - e_{13}^{12}.$$

$$R_4(g_2) = \begin{pmatrix} -1 & e_{13}^5 + e_{13}^8 \\ 0 & 1 \end{pmatrix}.$$

$$R_4(g_3) = \begin{pmatrix} e_{13} + e_{13}^2 + e_{13}^4 + e_{13}^5 + e_{13}^8 + e_{13}^9 + e_{13}^{11} + e_{13}^{12} & e_{13} + e_{13}^2 + e_{13}^5 + e_{13}^8 + e_{13}^{11} + e_{13}^{12} \\ -e_{13} - e_{13}^2 - e_{13}^5 - e_{13}^8 - e_{13}^{11} - e_{13}^{12} & -e_{13} - e_{13}^2 - e_{13}^5 - e_{13}^8 - e_{13}^{11} - e_{13}^{12} \end{pmatrix}.$$

$$R_5(g_2) = \begin{pmatrix} \alpha_{26,2} & e_{13}^5 + e_{13}^6 + e_{13}^7 + e_{13}^8 \\ -e_{13}^6 - e_{13}^7 & -\alpha_{26,2} \end{pmatrix}. \quad R_5(g_3) = \begin{pmatrix} e_{13}^6 + e_{13}^7 & -1 \\ 1 & 0 \end{pmatrix}.$$

Constants:

$$\alpha_{26,2} \equiv e_{13}^2 + e_{13}^3 + e_{13}^4 + e_{13}^5 + e_{13}^6 + e_{13}^7 + e_{13}^8 + e_{13}^9 + e_{13}^{10} + e_{13}^{11}.$$

$$R_6(g_2) = \begin{pmatrix} \alpha_{26,3} & e_{13}^2 + e_{13}^6 + e_{13}^7 + e_{13}^{11} \\ -e_{13}^2 - e_{13}^{11} & -\alpha_{26,3} \end{pmatrix}.$$

$$R_6(g_3) = \begin{pmatrix} e_{13} + e_{13}^2 + e_{13}^3 + e_{13}^6 + e_{13}^7 + e_{13}^{10} + e_{13}^{11} + e_{13}^{12} & e_{13}^2 + e_{13}^3 + e_{13}^6 + e_{13}^7 + e_{13}^{10} + e_{13}^{11} \\ -e_{13}^2 - e_{13}^3 - e_{13}^6 - e_{13}^7 - e_{13}^{10} - e_{13}^{11} & -e_{13}^2 - e_{13}^3 - e_{13}^6 - e_{13}^7 - e_{13}^{10} - e_{13}^{11} \end{pmatrix}.$$

Constants:

$$\alpha_{26,3} \equiv e_{13} + e_{13}^2 + e_{13}^3 + e_{13}^5 + e_{13}^6 + e_{13}^7 + e_{13}^8 + e_{13}^{10} + e_{13}^{11} + e_{13}^{12}.$$

$$R_7(g_2) = \begin{pmatrix} \alpha_{26,4} & e_{13} + e_{13}^3 + e_{13}^5 + e_{13}^8 + e_{13}^{10} + e_{13}^{12} \\ -e_{13} - e_{13}^3 - e_{13}^{10} - e_{13}^{12} & -\alpha_{26,4} \end{pmatrix}.$$

$$R_7(g_3) = \begin{pmatrix} e_{13} + e_{13}^3 + e_{13}^5 + e_{13}^8 + e_{13}^{10} + e_{13}^{12} & \alpha_{26,4} \\ -\alpha_{26,4} & -e_{13} - e_{13}^3 - e_{13}^{10} - e_{13}^{12} \end{pmatrix}.$$

Constants:

$$\alpha_{26,4} \equiv e_{13} + e_{13}^3 + e_{13}^5 + e_{13}^6 + e_{13}^7 + e_{13}^8 + e_{13}^{10} + e_{13}^{12}.$$

$$R_8(g_2) = \begin{pmatrix} -e_{13} - e_{13}^4 - e_{13}^6 - e_{13}^7 - e_{13}^9 - e_{13}^{12} & -e_{13} - e_{13}^4 - e_{13}^6 - e_{13}^7 - e_{13}^9 - e_{13}^{12} \\ e_{13} + e_{13}^2 + e_{13}^4 + e_{13}^6 + e_{13}^7 + e_{13}^9 + e_{13}^{11} + e_{13}^{12} & e_{13} + e_{13}^4 + e_{13}^6 + e_{13}^7 + e_{13}^9 + e_{13}^{12} \end{pmatrix}.$$

$$R_8(g_3) = \begin{pmatrix} e_{13} + e_{13}^2 + e_{13}^4 + e_{13}^6 + e_{13}^7 + e_{13}^9 + e_{13}^{11} + e_{13}^{12} & e_{13} + e_{13}^4 + e_{13}^6 + e_{13}^7 + e_{13}^9 + e_{13}^{12} \\ -e_{13} - e_{13}^4 - e_{13}^6 - e_{13}^7 - e_{13}^9 - e_{13}^{12} & -e_{13} - e_{13}^4 - e_{13}^6 - e_{13}^7 - e_{13}^9 - e_{13}^{12} \end{pmatrix}.$$

$G_{26}^{(2)}$

$$R_2(g_2) = -1. \quad R_2(g_3) = 1.$$

$$R_3(g_2) = -1. \quad R_3(g_3) = e_{13}^{12}.$$

$$R_4(g_2) = -1. \quad R_4(g_3) = e_{13}^{11}.$$

$$R_5(g_2) = -1. \quad R_5(g_3) = e_{13}^{10}.$$

$$R_6(g_2) = -1. \quad R_6(g_3) = e_{13}^9.$$

$$R_7(g_2) = -1. \quad R_7(g_3) = e_{13}^8.$$

$$R_8(g_2) = -1. \quad R_8(g_3) = e_{13}^7.$$

$$R_9(g_2) = -1. \quad R_9(g_3) = e_{13}^6.$$

$$R_{10}(g_2) = -1. \quad R_{10}(g_3) = e_{13}^5.$$

$$R_{11}(g_2) = -1. \quad R_{11}(g_3) = e_{13}^4.$$

$$R_{12}(g_2) = -1. \quad R_{12}(g_3) = e_{13}^3.$$

$$R_{13}(g_2) = -1. \quad R_{13}(g_3) = e_{13}^2.$$

$$R_{14}(g_2) = -1. \quad R_{14}(g_3) = e_{13}.$$

$$R_{15}(g_2) = 1. \quad R_{15}(g_3) = e_{13}^{12}.$$

$$R_{16}(g_2) = 1. \quad R_{16}(g_3) = e_{13}^{11}.$$

$$R_{17}(g_2) = 1. \quad R_{17}(g_3) = e_{13}^{10}.$$

$$R_{18}(g_2) = 1. \quad R_{18}(g_3) = e_{13}^9.$$

$$R_{19}(g_2) = 1. \quad R_{19}(g_3) = e_{13}^8.$$

$$R_{20}(g_2) = 1. \quad R_{20}(g_3) = e_{13}^7.$$

$$R_{21}(g_2) = 1. \quad R_{21}(g_3) = e_{13}^6.$$

$$R_{22}(g_2) = 1. \quad R_{22}(g_3) = e_{13}^5.$$

$$R_{23}(g_2) = 1. \quad R_{23}(g_3) = e_{13}^4.$$

$$R_{24}(g_2) = 1. \quad R_{24}(g_3) = e_{13}^3.$$

$$R_{25}(g_2) = 1. \quad R_{25}(g_3) = e_{13}^2.$$

$$R_{26}(g_2) = 1. \quad R_{26}(g_3) = e_{13}.$$

2.27. Order 27. $G_{27}^{(1)}$

$$\begin{aligned}
R_2(g_2) &= e_3^2. & R_2(g_3) &= 1. & R_2(g_4) &= 1. \\
R_3(g_2) &= e_3. & R_3(g_3) &= 1. & R_3(g_4) &= 1. \\
R_4(g_2) &= -e_9^2 - e_9^5. & R_4(g_3) &= e_3^2. & R_4(g_4) &= 1. \\
R_5(g_2) &= -e_9^4 - e_9^7. & R_5(g_3) &= e_3. & R_5(g_4) &= 1. \\
R_6(g_2) &= e_9^7. & R_6(g_3) &= e_3. & R_6(g_4) &= 1. \\
R_7(g_2) &= e_9^5. & R_7(g_3) &= e_3^2. & R_7(g_4) &= 1. \\
R_8(g_2) &= e_9^4. & R_8(g_3) &= e_3. & R_8(g_4) &= 1. \\
R_9(g_2) &= e_9^2. & R_9(g_3) &= e_3^2. & R_9(g_4) &= 1. \\
R_{10}(g_2) &= -e_{27}^5 - e_{27}^{14}. & R_{10}(g_3) &= e_9^5. & R_{10}(g_4) &= e_3^2. \\
R_{11}(g_2) &= -e_{27}^7 - e_{27}^{16}. & R_{11}(g_3) &= e_9^7. & R_{11}(g_4) &= e_3. \\
R_{12}(g_2) &= -e_{27}^8 - e_{27}^{17}. & R_{12}(g_3) &= -e_9^2 - e_9^5. & R_{12}(g_4) &= e_3^2. \\
R_{13}(g_2) &= -e_{27}^{10} - e_{27}^{19}. & R_{13}(g_3) &= -e_9^4 - e_9^7. & R_{13}(g_4) &= e_3. \\
R_{14}(g_2) &= -e_{27}^{11} - e_{27}^{20}. & R_{14}(g_3) &= e_9^2. & R_{14}(g_4) &= e_3^2. \\
R_{15}(g_2) &= -e_{27}^{13} - e_{27}^{22}. & R_{15}(g_3) &= e_9^4. & R_{15}(g_4) &= e_3. \\
R_{16}(g_2) &= e_{27}^{22}. & R_{16}(g_3) &= e_9^4. & R_{16}(g_4) &= e_3. \\
R_{17}(g_2) &= e_{27}^{20}. & R_{17}(g_3) &= e_9^2. & R_{17}(g_4) &= e_3^2. \\
R_{18}(g_2) &= e_{27}^{19}. & R_{18}(g_3) &= -e_9^4 - e_9^7. & R_{18}(g_4) &= e_3. \\
R_{19}(g_2) &= e_{27}^{17}. & R_{19}(g_3) &= -e_9^2 - e_9^5. & R_{19}(g_4) &= e_3^2. \\
R_{20}(g_2) &= e_{27}^{16}. & R_{20}(g_3) &= e_9^7. & R_{20}(g_4) &= e_3. \\
R_{21}(g_2) &= e_{27}^{14}. & R_{21}(g_3) &= e_9^5. & R_{21}(g_4) &= e_3^2. \\
R_{22}(g_2) &= e_{27}^{13}. & R_{22}(g_3) &= e_9^4. & R_{22}(g_4) &= e_3. \\
R_{23}(g_2) &= e_{27}^{11}. & R_{23}(g_3) &= e_9^2. & R_{23}(g_4) &= e_3^2. \\
R_{24}(g_2) &= e_{27}^{10}. & R_{24}(g_3) &= -e_9^4 - e_9^7. & R_{24}(g_4) &= e_3. \\
R_{25}(g_2) &= e_{27}^8. & R_{25}(g_3) &= -e_9^2 - e_9^5. & R_{25}(g_4) &= e_3^2. \\
R_{26}(g_2) &= e_{27}^7. & R_{26}(g_3) &= e_9^7. & R_{26}(g_4) &= e_3. \\
R_{27}(g_2) &= e_{27}^5. & R_{27}(g_3) &= e_9^5. & R_{27}(g_4) &= e_3^2.
\end{aligned}$$

 $G_{27}^{(2)}$

$$\begin{aligned}
R_2(g_2) &= 1. & R_2(g_3) &= e_3^2. & R_2(g_4) &= 1. \\
R_3(g_2) &= 1. & R_3(g_3) &= e_3. & R_3(g_4) &= 1. \\
R_4(g_2) &= e_3^2. & R_4(g_3) &= 1. & R_4(g_4) &= 1. \\
R_5(g_2) &= e_3. & R_5(g_3) &= 1. & R_5(g_4) &= 1. \\
R_6(g_2) &= e_3^2. & R_6(g_3) &= e_3^2. & R_6(g_4) &= 1. \\
R_7(g_2) &= e_3. & R_7(g_3) &= e_3. & R_7(g_4) &= 1. \\
R_8(g_2) &= e_3^2. & R_8(g_3) &= e_3. & R_8(g_4) &= 1. \\
R_9(g_2) &= e_3. & R_9(g_3) &= e_3^2. & R_9(g_4) &= 1. \\
R_{10}(g_2) &= -e_9^2 - e_9^5. & R_{10}(g_3) &= 1. & R_{10}(g_4) &= e_3^2. \\
R_{11}(g_2) &= -e_9^4 - e_9^7. & R_{11}(g_3) &= 1. & R_{11}(g_4) &= e_3. \\
R_{12}(g_2) &= e_9^7. & R_{12}(g_3) &= 1. & R_{12}(g_4) &= e_3. \\
R_{13}(g_2) &= e_9^5. & R_{13}(g_3) &= 1. & R_{13}(g_4) &= e_3^2.
\end{aligned}$$

$$\begin{aligned}
R_{14}(g_2) &= e_9^4. & R_{14}(g_3) &= 1. & R_{14}(g_4) &= e_3. \\
R_{15}(g_2) &= e_9^2. & R_{15}(g_3) &= 1. & R_{15}(g_4) &= e_3^2. \\
R_{16}(g_2) &= -e_9^2 - e_9^5. & R_{16}(g_3) &= e_3^2. & R_{16}(g_4) &= e_3^2. \\
R_{17}(g_2) &= -e_9^4 - e_9^7. & R_{17}(g_3) &= e_3. & R_{17}(g_4) &= e_3. \\
R_{18}(g_2) &= e_9^7. & R_{18}(g_3) &= e_3. & R_{18}(g_4) &= e_3. \\
R_{19}(g_2) &= e_9^5. & R_{19}(g_3) &= e_3^2. & R_{19}(g_4) &= e_3^2. \\
R_{20}(g_2) &= e_9^4. & R_{20}(g_3) &= e_3. & R_{20}(g_4) &= e_3. \\
R_{21}(g_2) &= e_9^2. & R_{21}(g_3) &= e_3^2. & R_{21}(g_4) &= e_3^2. \\
R_{22}(g_2) &= -e_9^2 - e_9^5. & R_{22}(g_3) &= e_3. & R_{22}(g_4) &= e_3^2. \\
R_{23}(g_2) &= -e_9^4 - e_9^7. & R_{23}(g_3) &= e_3^2. & R_{23}(g_4) &= e_3. \\
R_{24}(g_2) &= e_9^7. & R_{24}(g_3) &= e_3^2. & R_{24}(g_4) &= e_3. \\
R_{25}(g_2) &= e_9^5. & R_{25}(g_3) &= e_3. & R_{25}(g_4) &= e_3^2. \\
R_{26}(g_2) &= e_9^4. & R_{26}(g_3) &= e_3^2. & R_{26}(g_4) &= e_3. \\
R_{27}(g_2) &= e_9^2. & R_{27}(g_3) &= e_3. & R_{27}(g_4) &= e_3^2.
\end{aligned}$$

 $G_{27}^{(3)}$

$$\begin{aligned}
R_2(g_2) &= 1. & R_2(g_3) &= e_3^2. & R_2(g_4) &= 1. \\
R_3(g_2) &= 1. & R_3(g_3) &= e_3. & R_3(g_4) &= 1. \\
R_4(g_2) &= e_3^2. & R_4(g_3) &= 1. & R_4(g_4) &= 1. \\
R_5(g_2) &= e_3. & R_5(g_3) &= 1. & R_5(g_4) &= 1. \\
R_6(g_2) &= e_3^2. & R_6(g_3) &= e_3^2. & R_6(g_4) &= 1. \\
R_7(g_2) &= e_3. & R_7(g_3) &= e_3. & R_7(g_4) &= 1. \\
R_8(g_2) &= e_3^2. & R_8(g_3) &= e_3. & R_8(g_4) &= 1. \\
R_9(g_2) &= e_3. & R_9(g_3) &= e_3^2. & R_9(g_4) &= 1. \\
R_{10}(g_2) &= \begin{pmatrix} 1 & 0 & 0 \\ 0 & e_3 & 0 \\ 0 & 0 & e_3^2 \end{pmatrix}. & R_{10}(g_3) &= \begin{pmatrix} 0 & 0 & e_3 \\ e_3^2 & 0 & 0 \\ 0 & 1 & 0 \end{pmatrix}. & R_{10}(g_4) &= \begin{pmatrix} e_3^2 & 0 & 0 \\ 0 & e_3^2 & 0 \\ 0 & 0 & e_3^2 \end{pmatrix}. \\
R_{11}(g_2) &= \begin{pmatrix} 1 & 0 & 0 \\ 0 & e_3 & 0 \\ 0 & 0 & e_3^2 \end{pmatrix}. & R_{11}(g_3) &= \begin{pmatrix} 0 & e_3^2 & 0 \\ 0 & 0 & 1 \\ e_3 & 0 & 0 \end{pmatrix}. & R_{11}(g_4) &= \begin{pmatrix} e_3 & 0 & 0 \\ 0 & e_3 & 0 \\ 0 & 0 & e_3 \end{pmatrix}.
\end{aligned}$$

 $G_{27}^{(4)}$

$$\begin{aligned}
R_2(g_2) &= 1. & R_2(g_3) &= e_3^2. & R_2(g_4) &= 1. \\
R_3(g_2) &= 1. & R_3(g_3) &= e_3. & R_3(g_4) &= 1. \\
R_4(g_2) &= e_3^2. & R_4(g_3) &= 1. & R_4(g_4) &= 1. \\
R_5(g_2) &= e_3. & R_5(g_3) &= 1. & R_5(g_4) &= 1. \\
R_6(g_2) &= e_3^2. & R_6(g_3) &= e_3^2. & R_6(g_4) &= 1. \\
R_7(g_2) &= e_3. & R_7(g_3) &= e_3. & R_7(g_4) &= 1. \\
R_8(g_2) &= e_3^2. & R_8(g_3) &= e_3. & R_8(g_4) &= 1. \\
R_9(g_2) &= e_3. & R_9(g_3) &= e_3^2. & R_9(g_4) &= 1. \\
R_{10}(g_2) &= \begin{pmatrix} -e_9^2 - e_9^5 & 0 & 0 \\ 0 & e_9^5 & 0 \\ 0 & 0 & e_9^2 \end{pmatrix}. & R_{10}(g_3) &= \begin{pmatrix} 0 & -e_9^4 - e_9^7 & 0 \\ 0 & 0 & e_3^2 \\ e_9^2 & 0 & 0 \end{pmatrix}. & R_{10}(g_4) &= \begin{pmatrix} e_3^2 & 0 & 0 \\ 0 & e_3^2 & 0 \\ 0 & 0 & e_3^2 \end{pmatrix}.
\end{aligned}$$

$$R_{11}(g_2) = \begin{pmatrix} -e_9^4 - e_9^7 & 0 & 0 \\ 0 & e_9^7 & 0 \\ 0 & 0 & e_9^4 \end{pmatrix}, \quad R_{11}(g_3) = \begin{pmatrix} 0 & 0 & -e_9^2 - e_9^5 \\ e_9^5 & 0 & 0 \\ 0 & e_9^5 & 0 \end{pmatrix}, \quad R_{11}(g_4) = \begin{pmatrix} e_3 & 0 & 0 \\ 0 & e_3 & 0 \\ 0 & 0 & e_3 \end{pmatrix}.$$

 $G_{27}^{(5)}$

$$\begin{aligned} R_2(g_2) &= 1. & R_2(g_3) &= 1. & R_2(g_4) &= e_3^2. \\ R_3(g_2) &= 1. & R_3(g_3) &= 1. & R_3(g_4) &= e_3. \\ R_4(g_2) &= 1. & R_4(g_3) &= e_3^2. & R_4(g_4) &= 1. \\ R_5(g_2) &= 1. & R_5(g_3) &= e_3. & R_5(g_4) &= 1. \\ R_6(g_2) &= 1. & R_6(g_3) &= e_3^2. & R_6(g_4) &= e_3^2. \\ R_7(g_2) &= 1. & R_7(g_3) &= e_3. & R_7(g_4) &= e_3. \\ R_8(g_2) &= 1. & R_8(g_3) &= e_3^2. & R_8(g_4) &= e_3. \\ R_9(g_2) &= 1. & R_9(g_3) &= e_3. & R_9(g_4) &= e_3^2. \\ R_{10}(g_2) &= e_3^2. & R_{10}(g_3) &= 1. & R_{10}(g_4) &= 1. \\ R_{11}(g_2) &= e_3. & R_{11}(g_3) &= 1. & R_{11}(g_4) &= 1. \\ R_{12}(g_2) &= e_3^2. & R_{12}(g_3) &= 1. & R_{12}(g_4) &= e_3^2. \\ R_{13}(g_2) &= e_3. & R_{13}(g_3) &= 1. & R_{13}(g_4) &= e_3. \\ R_{14}(g_2) &= e_3^2. & R_{14}(g_3) &= 1. & R_{14}(g_4) &= e_3. \\ R_{15}(g_2) &= e_3. & R_{15}(g_3) &= 1. & R_{15}(g_4) &= e_3^2. \\ R_{16}(g_2) &= e_3^2. & R_{16}(g_3) &= e_3^2. & R_{16}(g_4) &= 1. \\ R_{17}(g_2) &= e_3. & R_{17}(g_3) &= e_3. & R_{17}(g_4) &= 1. \\ R_{18}(g_2) &= e_3^2. & R_{18}(g_3) &= e_3^2. & R_{18}(g_4) &= e_3^2. \\ R_{19}(g_2) &= e_3. & R_{19}(g_3) &= e_3. & R_{19}(g_4) &= e_3. \\ R_{20}(g_2) &= e_3^2. & R_{20}(g_3) &= e_3^2. & R_{20}(g_4) &= e_3. \\ R_{21}(g_2) &= e_3. & R_{21}(g_3) &= e_3. & R_{21}(g_4) &= e_3^2. \\ R_{22}(g_2) &= e_3^2. & R_{22}(g_3) &= e_3. & R_{22}(g_4) &= 1. \\ R_{23}(g_2) &= e_3. & R_{23}(g_3) &= e_3^2. & R_{23}(g_4) &= 1. \\ R_{24}(g_2) &= e_3^2. & R_{24}(g_3) &= e_3. & R_{24}(g_4) &= e_3^2. \\ R_{25}(g_2) &= e_3. & R_{25}(g_3) &= e_3^2. & R_{25}(g_4) &= e_3. \\ R_{26}(g_2) &= e_3^2. & R_{26}(g_3) &= e_3. & R_{26}(g_4) &= e_3. \\ R_{27}(g_2) &= e_3. & R_{27}(g_3) &= e_3^2. & R_{27}(g_4) &= e_3^2. \end{aligned}$$

2.28. **Order 28.** $G_{28}^{(1)}$

$$R_2(g_2) = -1. \quad R_2(g_3) = 1. \quad R_2(g_4) = 1.$$

$$R_3(g_2) = -i. \quad R_3(g_3) = -1. \quad R_3(g_4) = 1.$$

$$R_4(g_2) = i. \quad R_4(g_3) = -1. \quad R_4(g_4) = 1.$$

$$R_5(g_2) = -i\phi. \quad R_5(g_3) = -\epsilon. \quad R_5(g_4) = \begin{pmatrix} -2c_{1/7} & 1 \\ -1 & 0 \end{pmatrix}.$$

$$R_6(g_2) = \begin{pmatrix} -e_{28}^{19} - e_{28}^{23} & e_{28}^{15} + e_{28}^{19} + e_{28}^{23} + e_{28}^{27} \\ i & e_{28}^{19} + e_{28}^{23} \end{pmatrix}.$$

$$R_6(g_3) = -\epsilon.$$

$$R_6(g_4) = \begin{pmatrix} -2(c_{1/7} + c_{3/7}) & 2(c_{1/7} + c_{3/7}) \\ -2(c_{1/7} + c_{3/7}) & 2c_{1/7} \end{pmatrix}.$$

$$R_7(g_2) = \begin{pmatrix} -i & 2c_{2/7} \\ 0 & i \end{pmatrix}. \quad R_7(g_3) = -\epsilon. \quad R_7(g_4) = \begin{pmatrix} 0 & -i \\ -i & 2c_{2/7} \end{pmatrix}.$$

$$R_8(g_2) = \begin{pmatrix} 1 & 0 \\ -2c_{1/7} & -1 \end{pmatrix}. \quad R_8(g_3) = \epsilon. \quad R_8(g_4) = \begin{pmatrix} 0 & 1 \\ -1 & -2c_{1/7} \end{pmatrix}.$$

$$R_9(g_2) = \phi. \quad R_9(g_3) = \epsilon. \quad R_9(g_4) = \begin{pmatrix} -2(c_{1/7} + c_{3/7}) & -2(c_{1/7} + c_{3/7}) \\ 2(c_{1/7} + c_{3/7}) & 2c_{1/7} \end{pmatrix}.$$

$$R_{10}(g_2) = \begin{pmatrix} 2\Re e_{14}^3 & 1 - 2\Re e_{14} \\ -1 & -2\Re e_{14}^3 \end{pmatrix}. \quad R_{10}(g_3) = \epsilon. \quad R_{10}(g_4) = \begin{pmatrix} 2\Re e_{14} - 1 & 2\Re e_{14} - 1 \\ 1 - 2\Re e_{14} & 2\Re e_{14}^3 \end{pmatrix}.$$

 $G_{28}^{(2)}$

$$R_2(g_2) = -1. \quad R_2(g_3) = 1. \quad R_2(g_4) = 1.$$

$$R_3(g_2) = -1. \quad R_3(g_3) = e_7^6. \quad R_3(g_4) = 1.$$

$$R_4(g_2) = -1. \quad R_4(g_3) = e_7^5. \quad R_4(g_4) = 1.$$

$$R_5(g_2) = -1. \quad R_5(g_3) = e_7^4. \quad R_5(g_4) = 1.$$

$$R_6(g_2) = -1. \quad R_6(g_3) = e_7^3. \quad R_6(g_4) = 1.$$

$$R_7(g_2) = -1. \quad R_7(g_3) = e_7^2. \quad R_7(g_4) = 1.$$

$$R_8(g_2) = -1. \quad R_8(g_3) = e_7. \quad R_8(g_4) = 1.$$

$$R_9(g_2) = 1. \quad R_9(g_3) = e_7^6. \quad R_9(g_4) = 1.$$

$$R_{10}(g_2) = 1. \quad R_{10}(g_3) = e_7^5. \quad R_{10}(g_4) = 1.$$

$$R_{11}(g_2) = 1. \quad R_{11}(g_3) = e_7^4. \quad R_{11}(g_4) = 1.$$

$$R_{12}(g_2) = 1. \quad R_{12}(g_3) = e_7^3. \quad R_{12}(g_4) = 1.$$

$$R_{13}(g_2) = 1. \quad R_{13}(g_3) = e_7^2. \quad R_{13}(g_4) = 1.$$

$$R_{14}(g_2) = 1. \quad R_{14}(g_3) = e_7. \quad R_{14}(g_4) = 1.$$

$$R_{15}(g_2) = -i. \quad R_{15}(g_3) = 1. \quad R_{15}(g_4) = -1.$$

$$R_{16}(g_2) = i. \quad R_{16}(g_3) = 1. \quad R_{16}(g_4) = -1.$$

$$R_{17}(g_2) = -i. \quad R_{17}(g_3) = e_7^6. \quad R_{17}(g_4) = -1.$$

$$R_{18}(g_2) = -i. \quad R_{18}(g_3) = e_7^5. \quad R_{18}(g_4) = -1.$$

$$R_{19}(g_2) = -i. \quad R_{19}(g_3) = e_7^4. \quad R_{19}(g_4) = -1.$$

$$R_{20}(g_2) = -i. \quad R_{20}(g_3) = e_7^3. \quad R_{20}(g_4) = -1.$$

$$\begin{aligned}
 R_{21}(g_2) &= -i. & R_{21}(g_3) &= e_7^2. & R_{21}(g_4) &= -1. \\
 R_{22}(g_2) &= -i. & R_{22}(g_3) &= e_7. & R_{22}(g_4) &= -1. \\
 R_{23}(g_2) &= i. & R_{23}(g_3) &= e_7^6. & R_{23}(g_4) &= -1. \\
 R_{24}(g_2) &= i. & R_{24}(g_3) &= e_7^5. & R_{24}(g_4) &= -1. \\
 R_{25}(g_2) &= i. & R_{25}(g_3) &= e_7^4. & R_{25}(g_4) &= -1. \\
 R_{26}(g_2) &= i. & R_{26}(g_3) &= e_7^3. & R_{26}(g_4) &= -1. \\
 R_{27}(g_2) &= i. & R_{27}(g_3) &= e_7^2. & R_{27}(g_4) &= -1. \\
 R_{28}(g_2) &= i. & R_{28}(g_3) &= e_7. & R_{28}(g_4) &= -1.
 \end{aligned}$$

 $G_{28}^{(3)}$

$$\begin{aligned}
 R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= 1. \\
 R_3(g_2) &= -1. & R_3(g_3) &= 1. & R_3(g_4) &= 1. \\
 R_4(g_2) &= 1. & R_4(g_3) &= -1. & R_4(g_4) &= 1. \\
 R_5(g_2) &= \begin{pmatrix} -2(c_{1/7} + c_{3/7}) & -2(c_{1/7} + c_{3/7}) \\ 2c_{1/7} & 2(c_{1/7} + c_{3/7}) \end{pmatrix}. & R_5(g_3) &= -\epsilon. & R_5(g_4) &= \begin{pmatrix} -2c_{1/7} & -1 \\ 1 & 0 \end{pmatrix}. \\
 R_6(g_2) &= \begin{pmatrix} -2c_{2/7} & 2(c_{1/7} - c_{2/7}) \\ -1 & 2c_{2/7} \end{pmatrix}. & R_6(g_3) &= -\epsilon. & R_6(g_4) &= \begin{pmatrix} -1 & 2c_{2/7} \\ -2c_{2/7} & 2(c_{1/7} - c_{2/7}) \end{pmatrix}. \\
 R_7(g_2) &= \begin{pmatrix} 2c_{2/7} & -1 \\ 2(c_{1/7} - c_{2/7}) & -2c_{2/7} \end{pmatrix}. & R_7(g_3) &= -\epsilon. & R_7(g_4) &= \begin{pmatrix} 0 & 1 \\ -1 & 2c_{2/7} \end{pmatrix}. \\
 R_8(g_2) &= \phi. & R_8(g_3) &= \epsilon. & R_8(g_4) &= \begin{pmatrix} 2(c_{2/7} - c_{1/7}) & 2(c_{2/7} - c_{1/7}) \\ 2(c_{1/7} - c_{2/7}) & -2c_{2/7} \end{pmatrix}. \\
 R_9(g_2) &= \begin{pmatrix} -2c_{2/7} & 2(c_{1/7} - c_{2/7}) \\ -1 & 2c_{2/7} \end{pmatrix}. & R_9(g_3) &= \epsilon. & R_9(g_4) &= \begin{pmatrix} 2(c_{1/7} - c_{2/7}) & -2c_{2/7} \\ 2c_{2/7} & -1 \end{pmatrix}. \\
 R_{10}(g_2) &= \begin{pmatrix} -1 & -2\Re e_{14}^3 \\ 0 & 1 \end{pmatrix}. & R_{10}(g_3) &= \epsilon. & R_{10}(g_4) &= \begin{pmatrix} 2\Re e_{14} - 1 & 2\Re e_{14} - 1 \\ 1 - 2\Re e_{14} & 2\Re e_{14}^3 \end{pmatrix}.
 \end{aligned}$$

 $G_{28}^{(4)}$

$$\begin{aligned}
 R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= 1. \\
 R_3(g_2) &= -1. & R_3(g_3) &= 1. & R_3(g_4) &= 1. \\
 R_4(g_2) &= 1. & R_4(g_3) &= -1. & R_4(g_4) &= 1. \\
 R_5(g_2) &= -1. & R_5(g_3) &= -1. & R_5(g_4) &= e_7^6. \\
 R_6(g_2) &= -1. & R_6(g_3) &= -1. & R_6(g_4) &= e_7^5. \\
 R_7(g_2) &= -1. & R_7(g_3) &= -1. & R_7(g_4) &= e_7^4. \\
 R_8(g_2) &= -1. & R_8(g_3) &= -1. & R_8(g_4) &= e_7^3. \\
 R_9(g_2) &= -1. & R_9(g_3) &= -1. & R_9(g_4) &= e_7^2. \\
 R_{10}(g_2) &= -1. & R_{10}(g_3) &= -1. & R_{10}(g_4) &= e_7. \\
 R_{11}(g_2) &= -1. & R_{11}(g_3) &= 1. & R_{11}(g_4) &= e_7^6. \\
 R_{12}(g_2) &= -1. & R_{12}(g_3) &= 1. & R_{12}(g_4) &= e_7^5. \\
 R_{13}(g_2) &= -1. & R_{13}(g_3) &= 1. & R_{13}(g_4) &= e_7^4. \\
 R_{14}(g_2) &= -1. & R_{14}(g_3) &= 1. & R_{14}(g_4) &= e_7^3. \\
 R_{15}(g_2) &= -1. & R_{15}(g_3) &= 1. & R_{15}(g_4) &= e_7^2. \\
 R_{16}(g_2) &= -1. & R_{16}(g_3) &= 1. & R_{16}(g_4) &= e_7.
 \end{aligned}$$

$$\begin{aligned}
R_{17}(g_2) &= 1. & R_{17}(g_3) &= -1. & R_{17}(g_4) &= e_7^6. \\
R_{18}(g_2) &= 1. & R_{18}(g_3) &= -1. & R_{18}(g_4) &= e_7^5. \\
R_{19}(g_2) &= 1. & R_{19}(g_3) &= -1. & R_{19}(g_4) &= e_7^4. \\
R_{20}(g_2) &= 1. & R_{20}(g_3) &= -1. & R_{20}(g_4) &= e_7^3. \\
R_{21}(g_2) &= 1. & R_{21}(g_3) &= -1. & R_{21}(g_4) &= e_7^2. \\
R_{22}(g_2) &= 1. & R_{22}(g_3) &= -1. & R_{22}(g_4) &= e_7. \\
R_{23}(g_2) &= 1. & R_{23}(g_3) &= 1. & R_{23}(g_4) &= e_7^6. \\
R_{24}(g_2) &= 1. & R_{24}(g_3) &= 1. & R_{24}(g_4) &= e_7^5. \\
R_{25}(g_2) &= 1. & R_{25}(g_3) &= 1. & R_{25}(g_4) &= e_7^4. \\
R_{26}(g_2) &= 1. & R_{26}(g_3) &= 1. & R_{26}(g_4) &= e_7^3. \\
R_{27}(g_2) &= 1. & R_{27}(g_3) &= 1. & R_{27}(g_4) &= e_7^2. \\
R_{28}(g_2) &= 1. & R_{28}(g_3) &= 1. & R_{28}(g_4) &= e_7.
\end{aligned}$$

2.29. **Order 29.** $G_{29}^{(1)}$

$$R_j(g_2) = e_{29}^{j-1}, \quad j = 1, \dots, 29.$$

2.30. **Order 30.** $G_{30}^{(1)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= 1. & R_2(g_4) &= 1. \\
R_3(g_2) &= -1. & R_3(g_3) &= e_5^4. & R_3(g_4) &= 1. \\
R_4(g_2) &= -1. & R_4(g_3) &= e_5^3. & R_4(g_4) &= 1. \\
R_5(g_2) &= -1. & R_5(g_3) &= e_5^2. & R_5(g_4) &= 1. \\
R_6(g_2) &= -1. & R_6(g_3) &= e_5. & R_6(g_4) &= 1. \\
R_7(g_2) &= 1. & R_7(g_3) &= e_5^4. & R_7(g_4) &= 1. \\
R_8(g_2) &= 1. & R_8(g_3) &= e_5^3. & R_8(g_4) &= 1. \\
R_9(g_2) &= 1. & R_9(g_3) &= e_5^2. & R_9(g_4) &= 1. \\
R_{10}(g_2) &= 1. & R_{10}(g_3) &= e_5. & R_{10}(g_4) &= 1.
\end{aligned}$$

$$R_{11}(g_2) = \phi. \quad R_{11}(g_3) = \epsilon. \quad R_{11}(g_4) = \begin{pmatrix} -1 & -1 \\ 1 & 0 \end{pmatrix}.$$

$$R_{12}(g_2) = \begin{pmatrix} -1 & -e_5 \\ 0 & 1 \end{pmatrix}. \quad R_{12}(g_3) = \begin{pmatrix} e_5^2 & 0 \\ 0 & e_5^2 \end{pmatrix}. \quad R_{12}(g_4) = \begin{pmatrix} -1 & -e_5 \\ e_5^4 & 0 \end{pmatrix}.$$

$$R_{13}(g_2) = \begin{pmatrix} -1 & -1 \\ 0 & 1 \end{pmatrix}. \quad R_{13}(g_3) = \begin{pmatrix} e_5 & 0 \\ 0 & e_5 \end{pmatrix}. \quad R_{13}(g_4) = \begin{pmatrix} 0 & 1 \\ -1 & -1 \end{pmatrix}.$$

$$R_{14}(g_2) = \begin{pmatrix} 0 & e_5^2 \\ e_5^3 & 0 \end{pmatrix}. \quad R_{14}(g_3) = \begin{pmatrix} e_5^4 & 0 \\ 0 & e_5^4 \end{pmatrix}. \quad R_{14}(g_4) = \begin{pmatrix} -1 & -e_5^2 \\ e_5^3 & 0 \end{pmatrix}.$$

$$R_{15}(g_2) = \begin{pmatrix} 1 & 0 \\ -1 & -1 \end{pmatrix}. \quad R_{15}(g_3) = \begin{pmatrix} e_5^3 & 0 \\ 0 & e_5^3 \end{pmatrix}. \quad R_{15}(g_4) = \begin{pmatrix} -1 & -1 \\ 1 & 0 \end{pmatrix}.$$

$G_{30}^{(2)}$

$$R_2(g_2) = -1. \quad R_2(g_3) = 1. \quad R_2(g_4) = 1.$$

$$R_3(g_2) = -1. \quad R_3(g_3) = e_3^2. \quad R_3(g_4) = 1.$$

$$R_4(g_2) = -1. \quad R_4(g_3) = e_3. \quad R_4(g_4) = 1.$$

$$R_5(g_2) = 1. \quad R_5(g_3) = e_3^2. \quad R_5(g_4) = 1.$$

$$R_6(g_2) = 1. \quad R_6(g_3) = e_3. \quad R_6(g_4) = 1.$$

$$R_7(g_2) = \begin{pmatrix} -2\Re e_5 & -2\Re e_5 \\ -1 & 2\Re e_5 \end{pmatrix}. \quad R_7(g_3) = \epsilon. \quad R_7(g_4) = \begin{pmatrix} 0 & 1 \\ -1 & 2\Re e_5 \end{pmatrix}.$$

$$R_8(g_2) = \begin{pmatrix} 2\Re e_5 & -1 \\ -2\Re e_5 & -2\Re e_5 \end{pmatrix}. \quad R_8(g_3) = \epsilon. \quad R_8(g_4) = \begin{pmatrix} -1 & 2\Re e_5 \\ -2\Re e_5 & -2\Re e_5 \end{pmatrix}.$$

$$R_9(g_2) = \begin{pmatrix} -\varphi & -\varphi \\ -1 & \varphi \end{pmatrix}. \quad R_9(g_3) = \begin{pmatrix} e_3^2 & 0 \\ 0 & e_3^2 \end{pmatrix}. \quad R_9(g_4) = \begin{pmatrix} -\varphi & -\varphi \\ \varphi & -1 \end{pmatrix}.$$

$$R_{10}(g_2) = \begin{pmatrix} 2\Re e_5 & -e_3 \\ -e_{15}^7 - e_{15}^{13} & -2\Re e_5 \end{pmatrix}. \quad R_{10}(g_3) = \begin{pmatrix} e_3 & 0 \\ 0 & e_3 \end{pmatrix}. \quad R_{10}(g_4) = \begin{pmatrix} 0 & e_3 \\ -e_3^2 & 2\Re e_5 \end{pmatrix}.$$

$$R_{11}(g_2) = \begin{pmatrix} 0 & e_3^2 \\ e_3 & 0 \end{pmatrix}. \quad R_{11}(g_3) = \begin{pmatrix} e_3^2 & 0 \\ 0 & e_3^2 \end{pmatrix}. \quad R_{11}(g_4) = \begin{pmatrix} \varphi & -e_3^2 \\ e_3 & 0 \end{pmatrix}.$$

$$R_{12}(g_2) = \begin{pmatrix} 1 & 0 \\ e_{15}^{11} + e_{15}^{14} & -1 \end{pmatrix}. \quad R_{12}(g_3) = \begin{pmatrix} e_3 & 0 \\ 0 & e_3 \end{pmatrix}. \quad R_{12}(g_4) = \begin{pmatrix} 0 & e_3^2 \\ -e_3 & \varphi \end{pmatrix}.$$

 $G_{30}^{(3)}$

$$R_2(g_2) = -1. \quad R_2(g_3) = 1. \quad R_2(g_4) = 1.$$

$$R_3(g_2) = \begin{pmatrix} 1 & 0 \\ -1 & -1 \end{pmatrix}. \quad R_3(g_3) = \begin{pmatrix} -1 & -1 \\ 1 & 0 \end{pmatrix}. \quad R_3(g_4) = \epsilon.$$

$$R_4(g_2) = \begin{pmatrix} \varphi & -1 \\ -\varphi & -\varphi \end{pmatrix}. \quad R_4(g_3) = \epsilon. \quad R_4(g_4) = \begin{pmatrix} 0 & 1 \\ -1 & \varphi \end{pmatrix}.$$

$$R_5(g_2) = \begin{pmatrix} 1 & 0 \\ 2\Re e_5 & -1 \end{pmatrix}. \quad R_5(g_3) = \epsilon. \quad R_5(g_4) = \begin{pmatrix} 0 & 1 \\ -1 & 2\Re e_5 \end{pmatrix}.$$

$$R_6(g_2) = \begin{pmatrix} \alpha_{30,1} & \alpha_{30,2} \\ \alpha_{30,3} & -\alpha_{30,1} \end{pmatrix}. \quad R_6(g_3) = \begin{pmatrix} \alpha_{30,1} & \alpha_{30,2} \\ -\alpha_{30,2} & \alpha_{30,4} \end{pmatrix}. \quad R_6(g_4) = \begin{pmatrix} -e_{15}^7 - e_{15}^8 & -\alpha_{30,3} \\ \alpha_{30,3} & -\alpha_{30,1} \end{pmatrix}.$$

Constants:

$$\alpha_{30,1} \equiv e_{15} + e_{15}^4 - e_{15}^7 - e_{15}^8 + e_{15}^{11} + e_{15}^{14};$$

$$\alpha_{30,2} \equiv 2e_{15} + 2e_{15}^2 + e_{15}^4 + e_{15}^7 + e_{15}^8 + e_{15}^{11} + 2e_{15}^{13} + 2e_{15}^{14};$$

$$\alpha_{30,3} \equiv -2e_{15} - e_{15}^2 - e_{15}^4 - e_{15}^7 - e_{15}^8 - e_{15}^{11} - e_{15}^{13} - 2e_{15}^{14};$$

$$\alpha_{30,4} \equiv -2e_{15} - e_{15}^2 - 2e_{15}^4 - 2e_{15}^{11} - e_{15}^{13} - 2e_{15}^{14}.$$

$$R_7(g_2) = \begin{pmatrix} e_{15}^7 + e_{15}^8 & -1 \\ -\alpha_{30,3} & -e_{15}^7 - e_{15}^8 \end{pmatrix}. \quad R_7(g_3) = \begin{pmatrix} \alpha_{30,4} & -\alpha_{30,2} \\ \alpha_{30,2} & \alpha_{30,1} \end{pmatrix}. \quad R_7(g_4) = \begin{pmatrix} -e_{15}^7 - e_{15}^8 & -\alpha_{30,3} \\ \alpha_{30,3} & -\alpha_{30,1} \end{pmatrix}.$$

$$R_8(g_2) = \begin{pmatrix} \alpha_{30,5} & \alpha_{30,6} \\ \alpha_{30,7} & -\alpha_{30,5} \end{pmatrix}. \quad R_8(g_3) = \begin{pmatrix} \alpha_{30,8} & -\alpha_{30,6} \\ \alpha_{30,6} & \alpha_{30,5} \end{pmatrix}. \quad R_8(g_4) = \begin{pmatrix} -\alpha_{30,8} & \alpha_{30,9} \\ -\alpha_{30,9} & -e_{15}^4 - e_{15}^{11} \end{pmatrix}.$$

Constants:

$$\alpha_{30,5} \equiv -e_{15} - 2e_{15}^2 - 2e_{15}^7 - 2e_{15}^8 - 2e_{15}^{13} - e_{15}^{14};$$

$$\alpha_{30,6} \equiv -2e_{15} - e_{15}^2 - e_{15}^4 - 2e_{15}^7 - 2e_{15}^8 - e_{15}^{11} - e_{15}^{13} - 2e_{15}^{14};$$

$$\alpha_{30,7} \equiv e_{15} + e_{15}^2 + 2e_{15}^7 + 2e_{15}^8 + e_{15}^{13} + e_{15}^{14};$$

$$\alpha_{30,8} \equiv e_{15}^2 - e_{15}^4 + e_{15}^7 + e_{15}^8 - e_{15}^{11} + e_{15}^{13};$$

$$\alpha_{30,9} \equiv -e_{15} - e_{15}^2 - e_{15}^4 - 2e_{15}^7 - 2e_{15}^8 - e_{15}^{11} - e_{15}^{13} - e_{15}^{14}.$$

$$R_9(g_2) = \begin{pmatrix} \alpha_{30,10}/3 & \alpha_{30,11}/3 \\ \alpha_{30,12}/3 & -\alpha_{30,10}/3 \end{pmatrix}. \quad R_9(g_3) = \begin{pmatrix} 0 & 1 \\ -1 & -1 \end{pmatrix}. \quad R_9(g_4) = \begin{pmatrix} \alpha_{30,11}/3 & \alpha_{30,10}/3 \\ -\alpha_{30,10}/3 & \alpha_{30,12}/3 \end{pmatrix}.$$

Constants:

$$\begin{aligned} \alpha_{30,10} &\equiv -e_{15}^2 + e_{15}^7 + e_{15}^8 - e_{15}^{13}; \\ \alpha_{30,11} &\equiv -2e_{15}^2 - e_{15}^7 - e_{15}^8 - 2e_{15}^{13}; \\ \alpha_{30,12} &\equiv -e_{15}^2 - 2e_{15}^7 - 2e_{15}^8 - e_{15}^{13}. \end{aligned}$$

$G_{30}^{(4)}$

$$\begin{aligned} R_2(g_2) &= -1. & R_2(g_3) &= 1. & R_2(g_4) &= 1. \\ R_3(g_2) &= -1. & R_3(g_3) &= 1. & R_3(g_4) &= e_5^4. \\ R_4(g_2) &= -1. & R_4(g_3) &= 1. & R_4(g_4) &= e_5^3. \\ R_5(g_2) &= -1. & R_5(g_3) &= 1. & R_5(g_4) &= e_5^2. \\ R_6(g_2) &= -1. & R_6(g_3) &= 1. & R_6(g_4) &= e_5. \\ R_7(g_2) &= -1. & R_7(g_3) &= e_3^2. & R_7(g_4) &= 1. \\ R_8(g_2) &= -1. & R_8(g_3) &= e_3. & R_8(g_4) &= 1. \\ R_9(g_2) &= -1. & R_9(g_3) &= e_3^2. & R_9(g_4) &= e_5^4. \\ R_{10}(g_2) &= -1. & R_{10}(g_3) &= e_3^2. & R_{10}(g_4) &= e_5^3. \\ R_{11}(g_2) &= -1. & R_{11}(g_3) &= e_3^2. & R_{11}(g_4) &= e_5^2. \\ R_{12}(g_2) &= -1. & R_{12}(g_3) &= e_3^2. & R_{12}(g_4) &= e_5. \\ R_{13}(g_2) &= -1. & R_{13}(g_3) &= e_3. & R_{13}(g_4) &= e_5^4. \\ R_{14}(g_2) &= -1. & R_{14}(g_3) &= e_3. & R_{14}(g_4) &= e_5^3. \\ R_{15}(g_2) &= -1. & R_{15}(g_3) &= e_3. & R_{15}(g_4) &= e_5^2. \\ R_{16}(g_2) &= -1. & R_{16}(g_3) &= e_3. & R_{16}(g_4) &= e_5. \\ R_{17}(g_2) &= 1. & R_{17}(g_3) &= 1. & R_{17}(g_4) &= e_5^4. \\ R_{18}(g_2) &= 1. & R_{18}(g_3) &= 1. & R_{18}(g_4) &= e_5^3. \\ R_{19}(g_2) &= 1. & R_{19}(g_3) &= 1. & R_{19}(g_4) &= e_5^2. \\ R_{20}(g_2) &= 1. & R_{20}(g_3) &= 1. & R_{20}(g_4) &= e_5. \\ R_{21}(g_2) &= 1. & R_{21}(g_3) &= e_3^2. & R_{21}(g_4) &= 1. \\ R_{22}(g_2) &= 1. & R_{22}(g_3) &= e_3. & R_{22}(g_4) &= 1. \\ R_{23}(g_2) &= 1. & R_{23}(g_3) &= e_3^2. & R_{23}(g_4) &= e_5^4. \\ R_{24}(g_2) &= 1. & R_{24}(g_3) &= e_3^2. & R_{24}(g_4) &= e_5^3. \\ R_{25}(g_2) &= 1. & R_{25}(g_3) &= e_3^2. & R_{25}(g_4) &= e_5^2. \\ R_{26}(g_2) &= 1. & R_{26}(g_3) &= e_3^2. & R_{26}(g_4) &= e_5. \\ R_{27}(g_2) &= 1. & R_{27}(g_3) &= e_3. & R_{27}(g_4) &= e_5^4. \\ R_{28}(g_2) &= 1. & R_{28}(g_3) &= e_3. & R_{28}(g_4) &= e_5^3. \\ R_{29}(g_2) &= 1. & R_{29}(g_3) &= e_3. & R_{29}(g_4) &= e_5^2. \\ R_{30}(g_2) &= 1. & R_{30}(g_3) &= e_3. & R_{30}(g_4) &= e_5. \end{aligned}$$

2.31. **Order 31.** $G_{31}^{(1)}$

$$R_j(g_2) = e_{31}^{j-1}, \quad j = 1, \dots, 31.$$

2.32. **Order 32.** $G_{32}^{(1)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= 1. & R_2(g_4) &= 1. & R_2(g_5) &= 1. & R_2(g_6) &= 1. \\
R_3(g_2) &= -i. & R_3(g_3) &= -1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. & R_3(g_6) &= 1. \\
R_4(g_2) &= i. & R_4(g_3) &= -1. & R_4(g_4) &= 1. & R_4(g_5) &= 1. & R_4(g_6) &= 1. \\
R_5(g_2) &= -e_8. & R_5(g_3) &= i. & R_5(g_4) &= -1. & R_5(g_5) &= 1. & R_5(g_6) &= 1. \\
R_6(g_2) &= -e_8^3. & R_6(g_3) &= -i. & R_6(g_4) &= -1. & R_6(g_5) &= 1. & R_6(g_6) &= 1. \\
R_7(g_2) &= e_8^3. & R_7(g_3) &= -i. & R_7(g_4) &= -1. & R_7(g_5) &= 1. & R_7(g_6) &= 1. \\
R_8(g_2) &= e_8. & R_8(g_3) &= i. & R_8(g_4) &= -1. & R_8(g_5) &= 1. & R_8(g_6) &= 1. \\
R_9(g_2) &= -e_{16}. & R_9(g_3) &= e_8. & R_9(g_4) &= i. & R_9(g_5) &= -1. & R_9(g_6) &= 1. \\
R_{10}(g_2) &= -e_{16}^3. & R_{10}(g_3) &= e_8^3. & R_{10}(g_4) &= -i. & R_{10}(g_5) &= -1. & R_{10}(g_6) &= 1. \\
R_{11}(g_2) &= -e_{16}^5. & R_{11}(g_3) &= -e_8. & R_{11}(g_4) &= i. & R_{11}(g_5) &= -1. & R_{11}(g_6) &= 1. \\
R_{12}(g_2) &= -e_{16}^7. & R_{12}(g_3) &= -e_8^3. & R_{12}(g_4) &= -i. & R_{12}(g_5) &= -1. & R_{12}(g_6) &= 1. \\
R_{13}(g_2) &= e_{16}^7. & R_{13}(g_3) &= -e_8^3. & R_{13}(g_4) &= -i. & R_{13}(g_5) &= -1. & R_{13}(g_6) &= 1. \\
R_{14}(g_2) &= e_{16}^5. & R_{14}(g_3) &= -e_8. & R_{14}(g_4) &= i. & R_{14}(g_5) &= -1. & R_{14}(g_6) &= 1. \\
R_{15}(g_2) &= e_{16}^3. & R_{15}(g_3) &= e_8^3. & R_{15}(g_4) &= -i. & R_{15}(g_5) &= -1. & R_{15}(g_6) &= 1. \\
R_{16}(g_2) &= e_{16}. & R_{16}(g_3) &= e_8. & R_{16}(g_4) &= i. & R_{16}(g_5) &= -1. & R_{16}(g_6) &= 1. \\
R_{17}(g_2) &= -e_{32}. & R_{17}(g_3) &= e_{16}. & R_{17}(g_4) &= e_8. & R_{17}(g_5) &= i. & R_{17}(g_6) &= -1. \\
R_{18}(g_2) &= -e_{32}^3. & R_{18}(g_3) &= e_{16}^3. & R_{18}(g_4) &= e_8^3. & R_{18}(g_5) &= -i. & R_{18}(g_6) &= -1. \\
R_{19}(g_2) &= -e_{32}^5. & R_{19}(g_3) &= e_{16}^5. & R_{19}(g_4) &= -e_8. & R_{19}(g_5) &= i. & R_{19}(g_6) &= -1. \\
R_{20}(g_2) &= -e_{32}^7. & R_{20}(g_3) &= e_{16}^7. & R_{20}(g_4) &= -e_8^3. & R_{20}(g_5) &= -i. & R_{20}(g_6) &= -1. \\
R_{21}(g_2) &= -e_{32}^9. & R_{21}(g_3) &= -e_{16}. & R_{21}(g_4) &= e_8. & R_{21}(g_5) &= i. & R_{21}(g_6) &= -1. \\
R_{22}(g_2) &= -e_{32}^{11}. & R_{22}(g_3) &= -e_{16}^3. & R_{22}(g_4) &= e_8^3. & R_{22}(g_5) &= -i. & R_{22}(g_6) &= -1. \\
R_{23}(g_2) &= -e_{32}^{13}. & R_{23}(g_3) &= -e_{16}^5. & R_{23}(g_4) &= -e_8. & R_{23}(g_5) &= i. & R_{23}(g_6) &= -1. \\
R_{24}(g_2) &= -e_{32}^{15}. & R_{24}(g_3) &= -e_{16}^7. & R_{24}(g_4) &= -e_8^3. & R_{24}(g_5) &= -i. & R_{24}(g_6) &= -1. \\
R_{25}(g_2) &= e_{32}^{15}. & R_{25}(g_3) &= -e_{16}^7. & R_{25}(g_4) &= -e_8^3. & R_{25}(g_5) &= -i. & R_{25}(g_6) &= -1. \\
R_{26}(g_2) &= e_{32}^{13}. & R_{26}(g_3) &= -e_{16}^5. & R_{26}(g_4) &= -e_8. & R_{26}(g_5) &= i. & R_{26}(g_6) &= -1. \\
R_{27}(g_2) &= e_{32}^{11}. & R_{27}(g_3) &= -e_{16}^3. & R_{27}(g_4) &= e_8^3. & R_{27}(g_5) &= -i. & R_{27}(g_6) &= -1. \\
R_{28}(g_2) &= e_{32}^9. & R_{28}(g_3) &= -e_{16}. & R_{28}(g_4) &= e_8. & R_{28}(g_5) &= i. & R_{28}(g_6) &= -1. \\
R_{29}(g_2) &= e_{32}^7. & R_{29}(g_3) &= e_{16}^7. & R_{29}(g_4) &= -e_8^3. & R_{29}(g_5) &= -i. & R_{29}(g_6) &= -1. \\
R_{30}(g_2) &= e_{32}^5. & R_{30}(g_3) &= e_{16}^5. & R_{30}(g_4) &= -e_8. & R_{30}(g_5) &= i. & R_{30}(g_6) &= -1. \\
R_{31}(g_2) &= e_{32}^3. & R_{31}(g_3) &= e_{16}^3. & R_{31}(g_4) &= e_8^3. & R_{31}(g_5) &= -i. & R_{31}(g_6) &= -1. \\
R_{32}(g_2) &= e_{32}. & R_{32}(g_3) &= e_{16}. & R_{32}(g_4) &= e_8. & R_{32}(g_5) &= i. & R_{32}(g_6) &= -1.
\end{aligned}$$

$G_{32}^{(2)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= 1. & R_2(g_5) &= 1. & R_2(g_6) &= 1. \\
R_3(g_2) &= -1. & R_3(g_3) &= 1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. & R_3(g_6) &= 1. \\
R_4(g_2) &= 1. & R_4(g_3) &= -1. & R_4(g_4) &= 1. & R_4(g_5) &= 1. & R_4(g_6) &= 1. \\
R_5(g_2) &= -1. & R_5(g_3) &= -i. & R_5(g_4) &= 1. & R_5(g_5) &= 1. & R_5(g_6) &= -1. \\
R_6(g_2) &= -1. & R_6(g_3) &= i. & R_6(g_4) &= 1. & R_6(g_5) &= 1. & R_6(g_6) &= -1. \\
R_7(g_2) &= 1. & R_7(g_3) &= -i. & R_7(g_4) &= 1. & R_7(g_5) &= 1. & R_7(g_6) &= -1. \\
R_8(g_2) &= 1. & R_8(g_3) &= i. & R_8(g_4) &= 1. & R_8(g_5) &= 1. & R_8(g_6) &= -1. \\
R_9(g_2) &= -i. & R_9(g_3) &= -1. & R_9(g_4) &= 1. & R_9(g_5) &= -1. & R_9(g_6) &= 1. \\
R_{10}(g_2) &= i. & R_{10}(g_3) &= -1. & R_{10}(g_4) &= 1. & R_{10}(g_5) &= -1. & R_{10}(g_6) &= 1. \\
R_{11}(g_2) &= -i. & R_{11}(g_3) &= 1. & R_{11}(g_4) &= 1. & R_{11}(g_5) &= -1. & R_{11}(g_6) &= 1. \\
R_{12}(g_2) &= i. & R_{12}(g_3) &= 1. & R_{12}(g_4) &= 1. & R_{12}(g_5) &= -1. & R_{12}(g_6) &= 1. \\
R_{13}(g_2) &= -i. & R_{13}(g_3) &= -i. & R_{13}(g_4) &= 1. & R_{13}(g_5) &= -1. & R_{13}(g_6) &= -1. \\
R_{14}(g_2) &= i. & R_{14}(g_3) &= i. & R_{14}(g_4) &= 1. & R_{14}(g_5) &= -1. & R_{14}(g_6) &= -1. \\
R_{15}(g_2) &= -i. & R_{15}(g_3) &= i. & R_{15}(g_4) &= 1. & R_{15}(g_5) &= -1. & R_{15}(g_6) &= -1. \\
R_{16}(g_2) &= i. & R_{16}(g_3) &= -i. & R_{16}(g_4) &= 1. & R_{16}(g_5) &= -1. & R_{16}(g_6) &= -1. \\
R_{17}(g_2) &= -i\lambda. & R_{17}(g_3) &= -i\phi. & R_{17}(g_4) &= -\epsilon. & R_{17}(g_5) &= -\epsilon. & R_{17}(g_6) &= -\epsilon. \\
R_{18}(g_2) &= i\lambda. & R_{18}(g_3) &= i\kappa. & R_{18}(g_4) &= -\epsilon. & R_{18}(g_5) &= -\epsilon. & R_{18}(g_6) &= \epsilon. \\
R_{19}(g_2) &= -\lambda. & R_{19}(g_3) &= \kappa. & R_{19}(g_4) &= -\epsilon. & R_{19}(g_5) &= \epsilon. & R_{19}(g_6) &= -\epsilon. \\
R_{20}(g_2) &= \lambda. & R_{20}(g_3) &= \phi. & R_{20}(g_4) &= -\epsilon. & R_{20}(g_5) &= \epsilon. & R_{20}(g_6) &= \epsilon.
\end{aligned}$$

 $G_{32}^{(3)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= 1. & R_2(g_5) &= 1. & R_2(g_6) &= 1. \\
R_3(g_2) &= -1. & R_3(g_3) &= 1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. & R_3(g_6) &= 1. \\
R_4(g_2) &= 1. & R_4(g_3) &= -1. & R_4(g_4) &= 1. & R_4(g_5) &= 1. & R_4(g_6) &= 1. \\
R_5(g_2) &= -1. & R_5(g_3) &= -i. & R_5(g_4) &= 1. & R_5(g_5) &= -1. & R_5(g_6) &= 1. \\
R_6(g_2) &= -1. & R_6(g_3) &= i. & R_6(g_4) &= 1. & R_6(g_5) &= -1. & R_6(g_6) &= 1. \\
R_7(g_2) &= 1. & R_7(g_3) &= -i. & R_7(g_4) &= 1. & R_7(g_5) &= -1. & R_7(g_6) &= 1. \\
R_8(g_2) &= 1. & R_8(g_3) &= i. & R_8(g_4) &= 1. & R_8(g_5) &= -1. & R_8(g_6) &= 1. \\
R_9(g_2) &= -i. & R_9(g_3) &= -1. & R_9(g_4) &= -1. & R_9(g_5) &= 1. & R_9(g_6) &= 1. \\
R_{10}(g_2) &= i. & R_{10}(g_3) &= -1. & R_{10}(g_4) &= -1. & R_{10}(g_5) &= 1. & R_{10}(g_6) &= 1. \\
R_{11}(g_2) &= -i. & R_{11}(g_3) &= 1. & R_{11}(g_4) &= -1. & R_{11}(g_5) &= 1. & R_{11}(g_6) &= 1. \\
R_{12}(g_2) &= i. & R_{12}(g_3) &= 1. & R_{12}(g_4) &= -1. & R_{12}(g_5) &= 1. & R_{12}(g_6) &= 1. \\
R_{13}(g_2) &= -i. & R_{13}(g_3) &= -i. & R_{13}(g_4) &= -1. & R_{13}(g_5) &= -1. & R_{13}(g_6) &= 1. \\
R_{14}(g_2) &= i. & R_{14}(g_3) &= i. & R_{14}(g_4) &= -1. & R_{14}(g_5) &= -1. & R_{14}(g_6) &= 1. \\
R_{15}(g_2) &= -i. & R_{15}(g_3) &= i. & R_{15}(g_4) &= -1. & R_{15}(g_5) &= -1. & R_{15}(g_6) &= 1. \\
R_{16}(g_2) &= i. & R_{16}(g_3) &= -i. & R_{16}(g_4) &= -1. & R_{16}(g_5) &= -1. & R_{16}(g_6) &= 1. \\
R_{17}(g_2) &= -e_8. & R_{17}(g_3) &= -1. & R_{17}(g_4) &= i. & R_{17}(g_5) &= 1. & R_{17}(g_6) &= -1. \\
R_{18}(g_2) &= -e_8^3. & R_{18}(g_3) &= -1. & R_{18}(g_4) &= -i. & R_{18}(g_5) &= 1. & R_{18}(g_6) &= -1. \\
R_{19}(g_2) &= e_8^3. & R_{19}(g_3) &= -1. & R_{19}(g_4) &= -i. & R_{19}(g_5) &= 1. & R_{19}(g_6) &= -1. \\
R_{20}(g_2) &= e_8. & R_{20}(g_3) &= -1. & R_{20}(g_4) &= i. & R_{20}(g_5) &= 1. & R_{20}(g_6) &= -1.
\end{aligned}$$

$$\begin{aligned}
 R_{21}(g_2) &= -e_8. & R_{21}(g_3) &= 1. & R_{21}(g_4) &= i. & R_{21}(g_5) &= 1. & R_{21}(g_6) &= -1. \\
 R_{22}(g_2) &= -e_8^3. & R_{22}(g_3) &= 1. & R_{22}(g_4) &= -i. & R_{22}(g_5) &= 1. & R_{22}(g_6) &= -1. \\
 R_{23}(g_2) &= e_8^3. & R_{23}(g_3) &= 1. & R_{23}(g_4) &= -i. & R_{23}(g_5) &= 1. & R_{23}(g_6) &= -1. \\
 R_{24}(g_2) &= e_8. & R_{24}(g_3) &= 1. & R_{24}(g_4) &= i. & R_{24}(g_5) &= 1. & R_{24}(g_6) &= -1. \\
 R_{25}(g_2) &= -e_8. & R_{25}(g_3) &= -i. & R_{25}(g_4) &= i. & R_{25}(g_5) &= -1. & R_{25}(g_6) &= -1. \\
 R_{26}(g_2) &= -e_8^3. & R_{26}(g_3) &= i. & R_{26}(g_4) &= -i. & R_{26}(g_5) &= -1. & R_{26}(g_6) &= -1. \\
 R_{27}(g_2) &= e_8^3. & R_{27}(g_3) &= i. & R_{27}(g_4) &= -i. & R_{27}(g_5) &= -1. & R_{27}(g_6) &= -1. \\
 R_{28}(g_2) &= e_8. & R_{28}(g_3) &= -i. & R_{28}(g_4) &= i. & R_{28}(g_5) &= -1. & R_{28}(g_6) &= -1. \\
 R_{29}(g_2) &= -e_8. & R_{29}(g_3) &= i. & R_{29}(g_4) &= i. & R_{29}(g_5) &= -1. & R_{29}(g_6) &= -1. \\
 R_{30}(g_2) &= -e_8^3. & R_{30}(g_3) &= -i. & R_{30}(g_4) &= -i. & R_{30}(g_5) &= -1. & R_{30}(g_6) &= -1. \\
 R_{31}(g_2) &= e_8^3. & R_{31}(g_3) &= -i. & R_{31}(g_4) &= -i. & R_{31}(g_5) &= -1. & R_{31}(g_6) &= -1. \\
 R_{32}(g_2) &= e_8. & R_{32}(g_3) &= i. & R_{32}(g_4) &= i. & R_{32}(g_5) &= -1. & R_{32}(g_6) &= -1.
 \end{aligned}$$

 $G_{32}^{(4)}$

$$\begin{aligned}
 R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= 1. & R_2(g_5) &= 1. & R_2(g_6) &= 1. \\
 R_3(g_2) &= -1. & R_3(g_3) &= 1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. & R_3(g_6) &= 1. \\
 R_4(g_2) &= 1. & R_4(g_3) &= -1. & R_4(g_4) &= 1. & R_4(g_5) &= 1. & R_4(g_6) &= 1. \\
 R_5(g_2) &= -1. & R_5(g_3) &= -i. & R_5(g_4) &= 1. & R_5(g_5) &= -1. & R_5(g_6) &= 1. \\
 R_6(g_2) &= -1. & R_6(g_3) &= i. & R_6(g_4) &= 1. & R_6(g_5) &= -1. & R_6(g_6) &= 1. \\
 R_7(g_2) &= 1. & R_7(g_3) &= -i. & R_7(g_4) &= 1. & R_7(g_5) &= -1. & R_7(g_6) &= 1. \\
 R_8(g_2) &= 1. & R_8(g_3) &= i. & R_8(g_4) &= 1. & R_8(g_5) &= -1. & R_8(g_6) &= 1. \\
 R_9(g_2) &= -i. & R_9(g_3) &= -1. & R_9(g_4) &= -1. & R_9(g_5) &= 1. & R_9(g_6) &= 1. \\
 R_{10}(g_2) &= i. & R_{10}(g_3) &= -1. & R_{10}(g_4) &= -1. & R_{10}(g_5) &= 1. & R_{10}(g_6) &= 1. \\
 R_{11}(g_2) &= -i. & R_{11}(g_3) &= 1. & R_{11}(g_4) &= -1. & R_{11}(g_5) &= 1. & R_{11}(g_6) &= 1. \\
 R_{12}(g_2) &= i. & R_{12}(g_3) &= 1. & R_{12}(g_4) &= -1. & R_{12}(g_5) &= 1. & R_{12}(g_6) &= 1. \\
 R_{13}(g_2) &= -i. & R_{13}(g_3) &= -i. & R_{13}(g_4) &= -1. & R_{13}(g_5) &= -1. & R_{13}(g_6) &= 1. \\
 R_{14}(g_2) &= i. & R_{14}(g_3) &= i. & R_{14}(g_4) &= -1. & R_{14}(g_5) &= -1. & R_{14}(g_6) &= 1. \\
 R_{15}(g_2) &= -i. & R_{15}(g_3) &= i. & R_{15}(g_4) &= -1. & R_{15}(g_5) &= -1. & R_{15}(g_6) &= 1. \\
 R_{16}(g_2) &= i. & R_{16}(g_3) &= -i. & R_{16}(g_4) &= -1. & R_{16}(g_5) &= -1. & R_{16}(g_6) &= 1. \\
 R_{17}(g_2) &= \begin{pmatrix} -e_8^3 & 0 \\ 0 & e_8^3 \end{pmatrix}. & R_{17}(g_3) &= \begin{pmatrix} 0 & -e_8^3 \\ -e_8 & 0 \end{pmatrix}. & R_{17}(g_4) &= -i\epsilon. & R_{17}(g_5) &= -\epsilon. & R_{17}(g_6) &= -\epsilon. \\
 R_{18}(g_2) &= \begin{pmatrix} -e_8 & 0 \\ 0 & e_8 \end{pmatrix}. & R_{18}(g_3) &= \begin{pmatrix} 0 & e_8 \\ e_8^3 & 0 \end{pmatrix}. & R_{18}(g_4) &= i\epsilon. & R_{18}(g_5) &= -\epsilon. & R_{18}(g_6) &= -\epsilon. \\
 R_{19}(g_2) &= \begin{pmatrix} e_8^3 & 0 \\ 0 & -e_8^3 \end{pmatrix}. & R_{19}(g_3) &= i\kappa. & R_{19}(g_4) &= -i\epsilon. & R_{19}(g_5) &= \epsilon. & R_{19}(g_6) &= -\epsilon. \\
 R_{20}(g_2) &= \begin{pmatrix} -e_8 & 0 \\ 0 & e_8 \end{pmatrix}. & R_{20}(g_3) &= \phi. & R_{20}(g_4) &= i\epsilon. & R_{20}(g_5) &= \epsilon. & R_{20}(g_6) &= -\epsilon.
 \end{aligned}$$

$G_{32}^{(5)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= 1. & R_2(g_5) &= 1. & R_2(g_6) &= 1. \\
R_3(g_2) &= -1. & R_3(g_3) &= 1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. & R_3(g_6) &= 1. \\
R_4(g_2) &= 1. & R_4(g_3) &= -1. & R_4(g_4) &= 1. & R_4(g_5) &= 1. & R_4(g_6) &= 1. \\
R_5(g_2) &= -i. & R_5(g_3) &= -1. & R_5(g_4) &= 1. & R_5(g_5) &= -1. & R_5(g_6) &= 1. \\
R_6(g_2) &= i. & R_6(g_3) &= -1. & R_6(g_4) &= 1. & R_6(g_5) &= -1. & R_6(g_6) &= 1. \\
R_7(g_2) &= -i. & R_7(g_3) &= 1. & R_7(g_4) &= 1. & R_7(g_5) &= -1. & R_7(g_6) &= 1. \\
R_8(g_2) &= i. & R_8(g_3) &= 1. & R_8(g_4) &= 1. & R_8(g_5) &= -1. & R_8(g_6) &= 1. \\
R_9(g_2) &= -e_8. & R_9(g_3) &= -1. & R_9(g_4) &= 1. & R_9(g_5) &= i. & R_9(g_6) &= -1. \\
R_{10}(g_2) &= -e_8^3. & R_{10}(g_3) &= -1. & R_{10}(g_4) &= 1. & R_{10}(g_5) &= -i. & R_{10}(g_6) &= -1. \\
R_{11}(g_2) &= e_8^3. & R_{11}(g_3) &= -1. & R_{11}(g_4) &= 1. & R_{11}(g_5) &= -i. & R_{11}(g_6) &= -1. \\
R_{12}(g_2) &= e_8. & R_{12}(g_3) &= -1. & R_{12}(g_4) &= 1. & R_{12}(g_5) &= i. & R_{12}(g_6) &= -1. \\
R_{13}(g_2) &= -e_8. & R_{13}(g_3) &= 1. & R_{13}(g_4) &= 1. & R_{13}(g_5) &= i. & R_{13}(g_6) &= -1. \\
R_{14}(g_2) &= -e_8^3. & R_{14}(g_3) &= 1. & R_{14}(g_4) &= 1. & R_{14}(g_5) &= -i. & R_{14}(g_6) &= -1. \\
R_{15}(g_2) &= e_8^3. & R_{15}(g_3) &= 1. & R_{15}(g_4) &= 1. & R_{15}(g_5) &= -i. & R_{15}(g_6) &= -1. \\
R_{16}(g_2) &= e_8. & R_{16}(g_3) &= 1. & R_{16}(g_4) &= 1. & R_{16}(g_5) &= i. & R_{16}(g_6) &= -1. \\
R_{17}(g_2) &= -i\lambda. & R_{17}(g_3) &= \phi. & R_{17}(g_4) &= -\epsilon. & R_{17}(g_5) &= -\epsilon. & R_{17}(g_6) &= \epsilon. \\
R_{18}(g_2) &= \lambda. & R_{18}(g_3) &= \phi. & R_{18}(g_4) &= -\epsilon. & R_{18}(g_5) &= \epsilon. & R_{18}(g_6) &= \epsilon. \\
R_{19}(g_2) &= \begin{pmatrix} -e_8^3 & 0 \\ 0 & e_8^3 \end{pmatrix}. & R_{19}(g_3) &= \begin{pmatrix} 0 & e_8^3 \\ -e_8 & 0 \end{pmatrix}. & R_{19}(g_4) &= -\epsilon. & R_{19}(g_5) &= -i\epsilon. & R_{19}(g_6) &= -\epsilon. \\
R_{20}(g_2) &= \begin{pmatrix} e_8 & 0 \\ 0 & -e_8 \end{pmatrix}. & R_{20}(g_3) &= \begin{pmatrix} 0 & e_8 \\ -e_8^3 & 0 \end{pmatrix}. & R_{20}(g_4) &= -\epsilon. & R_{20}(g_5) &= i\epsilon. & R_{20}(g_6) &= -\epsilon.
\end{aligned}$$

 $G_{32}^{(6)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= 1. & R_2(g_5) &= 1. & R_2(g_6) &= 1. \\
R_3(g_2) &= -1. & R_3(g_3) &= 1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. & R_3(g_6) &= 1. \\
R_4(g_2) &= 1. & R_4(g_3) &= -1. & R_4(g_4) &= 1. & R_4(g_5) &= 1. & R_4(g_6) &= 1. \\
R_5(g_2) &= -i. & R_5(g_3) &= -1. & R_5(g_4) &= 1. & R_5(g_5) &= -1. & R_5(g_6) &= 1. \\
R_6(g_2) &= i. & R_6(g_3) &= -1. & R_6(g_4) &= 1. & R_6(g_5) &= -1. & R_6(g_6) &= 1. \\
R_7(g_2) &= -i. & R_7(g_3) &= 1. & R_7(g_4) &= 1. & R_7(g_5) &= -1. & R_7(g_6) &= 1. \\
R_8(g_2) &= i. & R_8(g_3) &= 1. & R_8(g_4) &= 1. & R_8(g_5) &= -1. & R_8(g_6) &= 1. \\
R_9(g_2) &= i\lambda. & R_9(g_3) &= \phi. & R_9(g_4) &= -\epsilon. & R_9(g_5) &= -\epsilon. & R_9(g_6) &= \epsilon. \\
R_{10}(g_2) &= -\lambda. & R_{10}(g_3) &= -\phi. & R_{10}(g_4) &= -\epsilon. & R_{10}(g_5) &= \epsilon. & R_{10}(g_6) &= \epsilon.
\end{aligned}$$

$$\begin{aligned}
 R_{11}(g_2) &= \begin{pmatrix} 0 & 0 & -1 & 0 \\ 0 & -1 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}, & R_{11}(g_3) &= \begin{pmatrix} 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 \end{pmatrix}. \\
 R_{11}(g_4) &= \begin{pmatrix} 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & -1 \\ -1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \end{pmatrix}, & R_{11}(g_5) &= \begin{pmatrix} -1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}. \\
 & & R_{11}(g_6) &= \begin{pmatrix} -1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & -1 \end{pmatrix}.
 \end{aligned}$$

 $G_{32}^{(7)}$

$$\begin{aligned}
 R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= 1. & R_2(g_5) &= 1. & R_2(g_6) &= 1. \\
 R_3(g_2) &= -1. & R_3(g_3) &= 1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. & R_3(g_6) &= 1. \\
 R_4(g_2) &= 1. & R_4(g_3) &= -1. & R_4(g_4) &= 1. & R_4(g_5) &= 1. & R_4(g_6) &= 1. \\
 R_5(g_2) &= -i. & R_5(g_3) &= -1. & R_5(g_4) &= 1. & R_5(g_5) &= -1. & R_5(g_6) &= 1. \\
 R_6(g_2) &= i. & R_6(g_3) &= -1. & R_6(g_4) &= 1. & R_6(g_5) &= -1. & R_6(g_6) &= 1. \\
 R_7(g_2) &= -i. & R_7(g_3) &= 1. & R_7(g_4) &= 1. & R_7(g_5) &= -1. & R_7(g_6) &= 1. \\
 R_8(g_2) &= i. & R_8(g_3) &= 1. & R_8(g_4) &= 1. & R_8(g_5) &= -1. & R_8(g_6) &= 1. \\
 R_9(g_2) &= -i\lambda. & R_9(g_3) &= \phi. & R_9(g_4) &= -\epsilon. & R_9(g_5) &= -\epsilon. & R_9(g_6) &= \epsilon. \\
 R_{10}(g_2) &= -\lambda. & R_{10}(g_3) &= \phi. & R_{10}(g_4) &= -\epsilon. & R_{10}(g_5) &= \epsilon. & R_{10}(g_6) &= \epsilon.
 \end{aligned}$$

$$\begin{aligned}
 R_{11}(g_2) &= \begin{pmatrix} -e_8 & 0 & 0 & 0 \\ 0 & 0 & -i & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & e_8 \end{pmatrix}, & R_{11}(g_3) &= \begin{pmatrix} 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & e_8 \\ -1 & 0 & 0 & 0 \\ 0 & -e_8^3 & 0 & 0 \end{pmatrix}. \\
 R_{11}(g_4) &= \begin{pmatrix} 0 & 0 & 0 & 1 \\ 0 & 0 & -e_8 & 0 \\ 0 & e_8^3 & 0 & 0 \\ 1 & 0 & 0 & 0 \end{pmatrix}, & R_{11}(g_5) &= \begin{pmatrix} i & 0 & 0 & 0 \\ 0 & -i & 0 & 0 \\ 0 & 0 & -i & 0 \\ 0 & 0 & 0 & i \end{pmatrix}. \\
 & & R_{11}(g_6) &= \begin{pmatrix} -1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & -1 \end{pmatrix}.
 \end{aligned}$$

 $G_{32}^{(8)}$

$$\begin{aligned}
 R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= 1. & R_2(g_5) &= 1. & R_2(g_6) &= 1. \\
 R_3(g_2) &= -1. & R_3(g_3) &= 1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. & R_3(g_6) &= 1. \\
 R_4(g_2) &= 1. & R_4(g_3) &= -1. & R_4(g_4) &= 1. & R_4(g_5) &= 1. & R_4(g_6) &= 1. \\
 R_5(g_2) &= -i. & R_5(g_3) &= -1. & R_5(g_4) &= 1. & R_5(g_5) &= -1. & R_5(g_6) &= 1. \\
 R_6(g_2) &= i. & R_6(g_3) &= -1. & R_6(g_4) &= 1. & R_6(g_5) &= -1. & R_6(g_6) &= 1. \\
 R_7(g_2) &= -i. & R_7(g_3) &= 1. & R_7(g_4) &= 1. & R_7(g_5) &= -1. & R_7(g_6) &= 1.
 \end{aligned}$$

$$\begin{aligned}
R_8(g_2) &= i. & R_8(g_3) &= 1. & R_8(g_4) &= 1. & R_8(g_5) &= -1. & R_8(g_6) &= 1. \\
R_9(g_2) &= -i\lambda. & R_9(g_3) &= \phi. & R_9(g_4) &= -\epsilon. & R_9(g_5) &= -\epsilon. & R_9(g_6) &= \epsilon. \\
R_{10}(g_2) &= -\lambda. & R_{10}(g_3) &= \phi. & R_{10}(g_4) &= -\epsilon. & R_{10}(g_5) &= \epsilon. & R_{10}(g_6) &= \epsilon.
\end{aligned}$$

$$\begin{aligned}
R_{11}(g_2) &= \begin{pmatrix} e_8 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & -i & 0 & 0 \\ 0 & 0 & 0 & -e_8 \end{pmatrix}. & R_{11}(g_3) &= \begin{pmatrix} 0 & -i & 0 & 0 \\ -i & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & -1 & 0 \end{pmatrix}. \\
R_{11}(g_4) &= \begin{pmatrix} 0 & 0 & 0 & e_8 \\ 0 & 0 & -e_8^3 & 0 \\ 0 & e_8 & 0 & 0 \\ -e_8^3 & 0 & 0 & 0 \end{pmatrix}. & R_{11}(g_5) &= \begin{pmatrix} i & 0 & 0 & 0 \\ 0 & -i & 0 & 0 \\ 0 & 0 & -i & 0 \\ 0 & 0 & 0 & i \end{pmatrix}. \\
& & R_{11}(g_6) &= \begin{pmatrix} -1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & -1 \end{pmatrix}.
\end{aligned}$$

 $G_{32}^{(9)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= 1. & R_2(g_5) &= 1. & R_2(g_6) &= 1. \\
R_3(g_2) &= -1. & R_3(g_3) &= 1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. & R_3(g_6) &= 1. \\
R_4(g_2) &= 1. & R_4(g_3) &= -1. & R_4(g_4) &= 1. & R_4(g_5) &= 1. & R_4(g_6) &= 1. \\
R_5(g_2) &= -i. & R_5(g_3) &= -1. & R_5(g_4) &= 1. & R_5(g_5) &= -1. & R_5(g_6) &= 1. \\
R_6(g_2) &= i. & R_6(g_3) &= -1. & R_6(g_4) &= 1. & R_6(g_5) &= -1. & R_6(g_6) &= 1. \\
R_7(g_2) &= -i. & R_7(g_3) &= 1. & R_7(g_4) &= 1. & R_7(g_5) &= -1. & R_7(g_6) &= 1. \\
R_8(g_2) &= i. & R_8(g_3) &= 1. & R_8(g_4) &= 1. & R_8(g_5) &= -1. & R_8(g_6) &= 1. \\
R_9(g_2) &= i\lambda. & R_9(g_3) &= \phi. & R_9(g_4) &= -\epsilon. & R_9(g_5) &= -\epsilon. & R_9(g_6) &= \epsilon. \\
R_{10}(g_2) &= \lambda. & R_{10}(g_3) &= \phi. & R_{10}(g_4) &= -\epsilon. & R_{10}(g_5) &= \epsilon. & R_{10}(g_6) &= \epsilon. \\
R_{11}(g_2) &= \begin{pmatrix} -i & 0 \\ \sqrt{2} & i \end{pmatrix}. & R_{11}(g_3) &= -i\kappa. & R_{11}(g_4) &= \begin{pmatrix} 1 & \sqrt{2}i \\ \sqrt{2}i & -1 \end{pmatrix}. & R_{11}(g_5) &= -\epsilon. & R_{11}(g_6) &= -\epsilon. \\
R_{12}(g_2) &= -i\phi. & R_{12}(g_3) &= \begin{pmatrix} -1/\sqrt{2} & -1/\sqrt{2} \\ -1/\sqrt{2} & 1/\sqrt{2} \end{pmatrix}. & R_{12}(g_4) &= \kappa. & R_{12}(g_5) &= -\epsilon. & R_{12}(g_6) &= -\epsilon. \\
R_{13}(g_2) &= \begin{pmatrix} -1 & \sqrt{2} \\ 0 & 1 \end{pmatrix}. & R_{13}(g_3) &= -\phi. & R_{13}(g_4) &= \begin{pmatrix} -1 & \sqrt{2} \\ -\sqrt{2}i & 1 \end{pmatrix}. & R_{13}(g_5) &= \epsilon. & R_{13}(g_6) &= -\epsilon. \\
R_{14}(g_2) &= -\lambda. & R_{14}(g_3) &= \begin{pmatrix} -1/\sqrt{2} & -1/\sqrt{2} \\ -1/\sqrt{2} & 1/\sqrt{2} \end{pmatrix}. & R_{14}(g_4) &= -\kappa. & R_{14}(g_5) &= \epsilon. & R_{14}(g_6) &= -\epsilon.
\end{aligned}$$

$G_{32}^{(10)}$

$$\begin{aligned}
 R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= 1. & R_2(g_5) &= 1. & R_2(g_6) &= 1. \\
 R_3(g_2) &= -1. & R_3(g_3) &= 1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. & R_3(g_6) &= 1. \\
 R_4(g_2) &= 1. & R_4(g_3) &= -1. & R_4(g_4) &= 1. & R_4(g_5) &= 1. & R_4(g_6) &= 1. \\
 R_5(g_2) &= -i. & R_5(g_3) &= -1. & R_5(g_4) &= 1. & R_5(g_5) &= -1. & R_5(g_6) &= 1. \\
 R_6(g_2) &= i. & R_6(g_3) &= -1. & R_6(g_4) &= 1. & R_6(g_5) &= -1. & R_6(g_6) &= 1. \\
 R_7(g_2) &= -i. & R_7(g_3) &= 1. & R_7(g_4) &= 1. & R_7(g_5) &= -1. & R_7(g_6) &= 1. \\
 R_8(g_2) &= i. & R_8(g_3) &= 1. & R_8(g_4) &= 1. & R_8(g_5) &= -1. & R_8(g_6) &= 1. \\
 R_9(g_2) &= i\lambda. & R_9(g_3) &= i\kappa. & R_9(g_4) &= -\epsilon. & R_9(g_5) &= -\epsilon. & R_9(g_6) &= \epsilon. \\
 R_{10}(g_2) &= -\lambda. & R_{10}(g_3) &= \phi. & R_{10}(g_4) &= -\epsilon. & R_{10}(g_5) &= \epsilon. & R_{10}(g_6) &= \epsilon. \\
 R_{11}(g_2) &= -\kappa. & R_{11}(g_3) &= \begin{pmatrix} -1/\sqrt{2} & -1/\sqrt{2} \\ 1/\sqrt{2} & i/\sqrt{2} \end{pmatrix}. & R_{11}(g_4) &= -i\phi. & R_{11}(g_5) &= -\epsilon. & R_{11}(g_6) &= -\epsilon. \\
 R_{12}(g_2) &= \begin{pmatrix} i & -\sqrt{2}i \\ 0 & -i \end{pmatrix}. & R_{12}(g_3) &= \begin{pmatrix} -\sqrt{2}i & i \\ -i & \sqrt{2}i \end{pmatrix}. & R_{12}(g_4) &= \begin{pmatrix} 1 & -\sqrt{2}i \\ \sqrt{2} & -1 \end{pmatrix}. \\
 & & & & R_{12}(g_5) &= -\epsilon. & R_{12}(g_6) &= -\epsilon. \\
 R_{13}(g_2) &= \begin{pmatrix} -1 & \sqrt{2}i \\ 0 & 1 \end{pmatrix}. & R_{13}(g_3) &= \begin{pmatrix} \sqrt{2}i & 1 \\ 1 & -\sqrt{2}i \end{pmatrix}. & R_{13}(g_4) &= \begin{pmatrix} 1 & -\sqrt{2}i \\ -\sqrt{2}i & -1 \end{pmatrix}. \\
 & & & & R_{13}(g_5) &= \epsilon. & R_{13}(g_6) &= -\epsilon. \\
 R_{14}(g_2) &= \begin{pmatrix} 1 & -\sqrt{2}i \\ 0 & -1 \end{pmatrix}. & R_{14}(g_3) &= \begin{pmatrix} \sqrt{2}i & 1 \\ 1 & -\sqrt{2}i \end{pmatrix}. & R_{14}(g_4) &= \begin{pmatrix} 1 & -\sqrt{2}i \\ -\sqrt{2}i & -1 \end{pmatrix}. \\
 & & & & R_{14}(g_5) &= \epsilon. & R_{14}(g_6) &= -\epsilon.
 \end{aligned}$$

 $G_{32}^{(11)}$

$$\begin{aligned}
 R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= 1. & R_2(g_5) &= 1. & R_2(g_6) &= 1. \\
 R_3(g_2) &= -1. & R_3(g_3) &= 1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. & R_3(g_6) &= 1. \\
 R_4(g_2) &= 1. & R_4(g_3) &= -1. & R_4(g_4) &= 1. & R_4(g_5) &= 1. & R_4(g_6) &= 1. \\
 R_5(g_2) &= -i. & R_5(g_3) &= -1. & R_5(g_4) &= 1. & R_5(g_5) &= -1. & R_5(g_6) &= 1. \\
 R_6(g_2) &= i. & R_6(g_3) &= -1. & R_6(g_4) &= 1. & R_6(g_5) &= -1. & R_6(g_6) &= 1. \\
 R_7(g_2) &= -i. & R_7(g_3) &= 1. & R_7(g_4) &= 1. & R_7(g_5) &= -1. & R_7(g_6) &= 1. \\
 R_8(g_2) &= i. & R_8(g_3) &= 1. & R_8(g_4) &= 1. & R_8(g_5) &= -1. & R_8(g_6) &= 1. \\
 R_9(g_2) &= -i\lambda. & R_9(g_3) &= -i\kappa. & R_9(g_4) &= -\epsilon. & R_9(g_5) &= -\epsilon. & R_9(g_6) &= \epsilon. \\
 R_{10}(g_2) &= -\lambda. & R_{10}(g_3) &= \phi. & R_{10}(g_4) &= -\epsilon. & R_{10}(g_5) &= \epsilon. & R_{10}(g_6) &= \epsilon. \\
 R_{11}(g_2) &= \begin{pmatrix} -e_8^3 & 0 \\ 0 & e_8^3 \end{pmatrix}. & R_{11}(g_3) &= \begin{pmatrix} -1/\sqrt{2} & (1+i)/2 \\ (1-i)/2 & 1/\sqrt{2} \end{pmatrix}. & R_{11}(g_4) &= \begin{pmatrix} 0 & e_8 \\ e_8^3 & 0 \end{pmatrix}. \\
 & & & & R_{11}(g_5) &= -i\epsilon. & R_{11}(g_6) &= -\epsilon.
 \end{aligned}$$

$$R_{12}(g_2) = \begin{pmatrix} e_8 & 0 \\ -1+i & -e_8 \end{pmatrix}. \quad R_{12}(g_3) = \begin{pmatrix} -\sqrt{2}i & -i \\ -i & \sqrt{2} \end{pmatrix}. \quad R_{12}(g_4) = \begin{pmatrix} -1 & -\sqrt{2}i \\ -\sqrt{2}i & 1 \end{pmatrix}. \\ R_{12}(g_5) = i\epsilon. \quad R_{12}(g_6) = -\epsilon.$$

$$R_{13}(g_2) = \begin{pmatrix} e_8^3 & -\sqrt{2}i \\ 0 & -e_8^3 \end{pmatrix}. \quad R_{13}(g_3) = \begin{pmatrix} -\sqrt{2}i & -e_8^3 \\ -e_8 & \sqrt{2} \end{pmatrix}. \quad R_{13}(g_4) = \begin{pmatrix} 1 & -1+i \\ 1+i & -1 \end{pmatrix}. \\ R_{13}(g_5) = -i\epsilon. \quad R_{13}(g_6) = -\epsilon.$$

$$R_{14}(g_2) = \begin{pmatrix} e_8 & 0 \\ 0 & -e_8 \end{pmatrix}. \quad R_{14}(g_3) = \begin{pmatrix} 1/\sqrt{2} & (1-i)/2 \\ (1+i)/2 & -1/\sqrt{2} \end{pmatrix}. \quad R_{14}(g_4) = \begin{pmatrix} 0 & e_8^3 \\ e_8 & 0 \end{pmatrix}. \\ R_{14}(g_5) = i\epsilon. \quad R_{14}(g_6) = -\epsilon.$$

 $G_{32}^{(12)}$

$$R_2(g_2) = -1. \quad R_2(g_3) = -1. \quad R_2(g_4) = 1. \quad R_2(g_5) = 1. \quad R_2(g_6) = 1. \\ R_3(g_2) = -1. \quad R_3(g_3) = 1. \quad R_3(g_4) = 1. \quad R_3(g_5) = 1. \quad R_3(g_6) = 1. \\ R_4(g_2) = 1. \quad R_4(g_3) = -1. \quad R_4(g_4) = 1. \quad R_4(g_5) = 1. \quad R_4(g_6) = 1. \\ R_5(g_2) = -i. \quad R_5(g_3) = -1. \quad R_5(g_4) = 1. \quad R_5(g_5) = -1. \quad R_5(g_6) = 1. \\ R_6(g_2) = i. \quad R_6(g_3) = -1. \quad R_6(g_4) = 1. \quad R_6(g_5) = -1. \quad R_6(g_6) = 1. \\ R_7(g_2) = -i. \quad R_7(g_3) = 1. \quad R_7(g_4) = 1. \quad R_7(g_5) = -1. \quad R_7(g_6) = 1. \\ R_8(g_2) = i. \quad R_8(g_3) = 1. \quad R_8(g_4) = 1. \quad R_8(g_5) = -1. \quad R_8(g_6) = 1. \\ R_9(g_2) = -e_8. \quad R_9(g_3) = -1. \quad R_9(g_4) = 1. \quad R_9(g_5) = i. \quad R_9(g_6) = -1. \\ R_{10}(g_2) = -e_8^3. \quad R_{10}(g_3) = -1. \quad R_{10}(g_4) = 1. \quad R_{10}(g_5) = -i. \quad R_{10}(g_6) = -1. \\ R_{11}(g_2) = e_8^3. \quad R_{11}(g_3) = -1. \quad R_{11}(g_4) = 1. \quad R_{11}(g_5) = -i. \quad R_{11}(g_6) = -1. \\ R_{12}(g_2) = e_8. \quad R_{12}(g_3) = -1. \quad R_{12}(g_4) = 1. \quad R_{12}(g_5) = i. \quad R_{12}(g_6) = -1. \\ R_{13}(g_2) = -e_8. \quad R_{13}(g_3) = 1. \quad R_{13}(g_4) = 1. \quad R_{13}(g_5) = i. \quad R_{13}(g_6) = -1. \\ R_{14}(g_2) = -e_8^3. \quad R_{14}(g_3) = 1. \quad R_{14}(g_4) = 1. \quad R_{14}(g_5) = -i. \quad R_{14}(g_6) = -1. \\ R_{15}(g_2) = e_8^3. \quad R_{15}(g_3) = 1. \quad R_{15}(g_4) = 1. \quad R_{15}(g_5) = -i. \quad R_{15}(g_6) = -1. \\ R_{16}(g_2) = e_8. \quad R_{16}(g_3) = 1. \quad R_{16}(g_4) = 1. \quad R_{16}(g_5) = i. \quad R_{16}(g_6) = -1. \\ R_{17}(g_2) = -i\lambda. \quad R_{17}(g_3) = -\kappa. \quad R_{17}(g_4) = -\epsilon. \quad R_{17}(g_5) = -\epsilon. \quad R_{17}(g_6) = \epsilon. \\ R_{18}(g_2) = -\lambda. \quad R_{18}(g_3) = \kappa. \quad R_{18}(g_4) = -\epsilon. \quad R_{18}(g_5) = \epsilon. \quad R_{18}(g_6) = \epsilon. \\ R_{19}(g_2) = \begin{pmatrix} e_8^3 & 0 \\ 0 & -e_8^3 \end{pmatrix}. \quad R_{19}(g_3) = \begin{pmatrix} 0 & e_8^3 \\ e_8 & 0 \end{pmatrix}. \quad R_{19}(g_4) = -\epsilon. \quad R_{19}(g_5) = -i\epsilon. \quad R_{19}(g_6) = -\epsilon. \\ R_{20}(g_2) = \begin{pmatrix} -e_8 & 0 \\ 0 & e_8 \end{pmatrix}. \quad R_{20}(g_3) = \begin{pmatrix} 0 & -e_8 \\ -e_8^3 & 0 \end{pmatrix}. \quad R_{20}(g_4) = -\epsilon. \quad R_{20}(g_5) = i\epsilon. \quad R_{20}(g_6) = -\epsilon.$$

$G_{32}^{(13)}$

$$R_2(g_2) = -1. \quad R_2(g_3) = -1. \quad R_2(g_4) = 1. \quad R_2(g_5) = 1. \quad R_2(g_6) = 1.$$

$$R_3(g_2) = -1. \quad R_3(g_3) = 1. \quad R_3(g_4) = 1. \quad R_3(g_5) = 1. \quad R_3(g_6) = 1.$$

$$R_4(g_2) = 1. \quad R_4(g_3) = -1. \quad R_4(g_4) = 1. \quad R_4(g_5) = 1. \quad R_4(g_6) = 1.$$

$$R_5(g_2) = -i. \quad R_5(g_3) = -1. \quad R_5(g_4) = 1. \quad R_5(g_5) = -1. \quad R_5(g_6) = 1.$$

$$R_6(g_2) = i. \quad R_6(g_3) = -1. \quad R_6(g_4) = 1. \quad R_6(g_5) = -1. \quad R_6(g_6) = 1.$$

$$R_7(g_2) = -i. \quad R_7(g_3) = 1. \quad R_7(g_4) = 1. \quad R_7(g_5) = -1. \quad R_7(g_6) = 1.$$

$$R_8(g_2) = i. \quad R_8(g_3) = 1. \quad R_8(g_4) = 1. \quad R_8(g_5) = -1. \quad R_8(g_6) = 1.$$

$$R_9(g_2) = i\lambda. \quad R_9(g_3) = -i\phi. \quad R_9(g_4) = -\epsilon. \quad R_9(g_5) = -\epsilon. \quad R_9(g_6) = \epsilon.$$

$$R_{10}(g_2) = \lambda. \quad R_{10}(g_3) = \kappa. \quad R_{10}(g_4) = -\epsilon. \quad R_{10}(g_5) = \epsilon. \quad R_{10}(g_6) = \epsilon.$$

$$R_{11}(g_2) = \begin{pmatrix} i & \sqrt{2} \\ 0 & -i \end{pmatrix}. \quad R_{11}(g_3) = \begin{pmatrix} 0 & 1 \\ 1 & -\sqrt{2}i \end{pmatrix}. \quad R_{11}(g_4) = \begin{pmatrix} 1 & -\sqrt{2}i \\ -\sqrt{2}i & -1 \end{pmatrix}. \\ R_{11}(g_5) = -\epsilon. \quad R_{11}(g_6) = -\epsilon.$$

$$R_{12}(g_2) = i\lambda. \quad R_{12}(g_3) = \begin{pmatrix} i/\sqrt{2} & i/\sqrt{2} \\ -1/\sqrt{2} & i/\sqrt{2} \end{pmatrix}. \quad R_{12}(g_4) = -\kappa. \quad R_{12}(g_5) = -\epsilon. \quad R_{12}(g_6) = -\epsilon.$$

$$R_{13}(g_2) = -\phi. \quad R_{13}(g_3) = \begin{pmatrix} -1/\sqrt{2} & i/\sqrt{2} \\ -1/\sqrt{2} & -1/\sqrt{2} \end{pmatrix}. \quad R_{13}(g_4) = \kappa. \quad R_{13}(g_5) = \epsilon. \quad R_{13}(g_6) = -\epsilon.$$

$$R_{14}(g_2) = \begin{pmatrix} 1 & \sqrt{2}i \\ 0 & -1 \end{pmatrix}. \quad R_{14}(g_3) = \begin{pmatrix} 0 & 1 \\ 1 & \sqrt{2}i \end{pmatrix}. \quad R_{14}(g_4) = \begin{pmatrix} 1 & \sqrt{2}i \\ \sqrt{2}i & -1 \end{pmatrix}. \\ R_{14}(g_5) = \epsilon. \quad R_{14}(g_6) = -\epsilon.$$

 $G_{32}^{(14)}$

$$R_2(g_2) = -1. \quad R_2(g_3) = -1. \quad R_2(g_4) = 1. \quad R_2(g_5) = 1. \quad R_2(g_6) = 1.$$

$$R_3(g_2) = -1. \quad R_3(g_3) = 1. \quad R_3(g_4) = 1. \quad R_3(g_5) = 1. \quad R_3(g_6) = 1.$$

$$R_4(g_2) = 1. \quad R_4(g_3) = -1. \quad R_4(g_4) = 1. \quad R_4(g_5) = 1. \quad R_4(g_6) = 1.$$

$$R_5(g_2) = -i. \quad R_5(g_3) = -1. \quad R_5(g_4) = 1. \quad R_5(g_5) = -1. \quad R_5(g_6) = 1.$$

$$R_6(g_2) = i. \quad R_6(g_3) = -1. \quad R_6(g_4) = 1. \quad R_6(g_5) = -1. \quad R_6(g_6) = 1.$$

$$R_7(g_2) = -i. \quad R_7(g_3) = 1. \quad R_7(g_4) = 1. \quad R_7(g_5) = -1. \quad R_7(g_6) = 1.$$

$$R_8(g_2) = i. \quad R_8(g_3) = 1. \quad R_8(g_4) = 1. \quad R_8(g_5) = -1. \quad R_8(g_6) = 1.$$

$$R_9(g_2) = -i\lambda. \quad R_9(g_3) = \kappa. \quad R_9(g_4) = -\epsilon. \quad R_9(g_5) = -\epsilon. \quad R_9(g_6) = \epsilon.$$

$$R_{10}(g_2) = -\lambda. \quad R_{10}(g_3) = -\kappa. \quad R_{10}(g_4) = -\epsilon. \quad R_{10}(g_5) = \epsilon. \quad R_{10}(g_6) = \epsilon.$$

$$R_{11}(g_2) = \begin{pmatrix} -i & -\sqrt{2}i \\ 0 & i \end{pmatrix}. \quad R_{11}(g_3) = \begin{pmatrix} 0 & 1 \\ -1 & -\sqrt{2}i \end{pmatrix}. \quad R_{11}(g_4) = \begin{pmatrix} 1 & \sqrt{2} \\ -\sqrt{2}i & -1 \end{pmatrix}. \\ R_{11}(g_5) = -\epsilon. \quad R_{11}(g_6) = -\epsilon.$$

$$R_{12}(g_2) = -i\phi. \quad R_{12}(g_3) = \begin{pmatrix} 1/\sqrt{2} & 1/\sqrt{2} \\ -1/\sqrt{2} & 1/\sqrt{2} \end{pmatrix}. \quad R_{12}(g_4) = -\kappa. \quad R_{12}(g_5) = -\epsilon. \quad R_{12}(g_6) = -\epsilon.$$

$$R_{13}(g_2) = \begin{pmatrix} 1 & 0 \\ \sqrt{2} & -1 \end{pmatrix}. \quad R_{13}(g_3) = \begin{pmatrix} -\sqrt{2}i & 1 \\ -1 & 0 \end{pmatrix}. \quad R_{13}(g_4) = \begin{pmatrix} -1 & \sqrt{2} \\ -\sqrt{2}i & 1 \end{pmatrix}.$$

$$R_{13}(g_5) = \epsilon. \quad R_{13}(g_6) = -\epsilon.$$

$$R_{14}(g_2) = \lambda. \quad R_{14}(g_3) = \begin{pmatrix} 1/\sqrt{2} & -1/\sqrt{2} \\ 1/\sqrt{2} & 1/\sqrt{2} \end{pmatrix}. \quad R_{14}(g_4) = \kappa. \quad R_{14}(g_5) = \epsilon. \quad R_{14}(g_6) = -\epsilon.$$

 $G_{32}^{(15)}$

$$R_2(g_2) = -1. \quad R_2(g_3) = -1. \quad R_2(g_4) = 1. \quad R_2(g_5) = 1. \quad R_2(g_6) = 1.$$

$$R_3(g_2) = -1. \quad R_3(g_3) = 1. \quad R_3(g_4) = 1. \quad R_3(g_5) = 1. \quad R_3(g_6) = 1.$$

$$R_4(g_2) = 1. \quad R_4(g_3) = -1. \quad R_4(g_4) = 1. \quad R_4(g_5) = 1. \quad R_4(g_6) = 1.$$

$$R_5(g_2) = -i. \quad R_5(g_3) = -1. \quad R_5(g_4) = 1. \quad R_5(g_5) = -1. \quad R_5(g_6) = 1.$$

$$R_6(g_2) = i. \quad R_6(g_3) = -1. \quad R_6(g_4) = 1. \quad R_6(g_5) = -1. \quad R_6(g_6) = 1.$$

$$R_7(g_2) = -i. \quad R_7(g_3) = 1. \quad R_7(g_4) = 1. \quad R_7(g_5) = -1. \quad R_7(g_6) = 1.$$

$$R_8(g_2) = i. \quad R_8(g_3) = 1. \quad R_8(g_4) = 1. \quad R_8(g_5) = -1. \quad R_8(g_6) = 1.$$

$$R_9(g_2) = i\lambda. \quad R_9(g_3) = i\phi. \quad R_9(g_4) = -\epsilon. \quad R_9(g_5) = -\epsilon. \quad R_9(g_6) = \epsilon.$$

$$R_{10}(g_2) = \lambda. \quad R_{10}(g_3) = \kappa. \quad R_{10}(g_4) = -\epsilon. \quad R_{10}(g_5) = \epsilon. \quad R_{10}(g_6) = \epsilon.$$

$$R_{11}(g_2) = \begin{pmatrix} 0 & -1 \\ i & 0 \end{pmatrix}. \quad R_{11}(g_3) = \begin{pmatrix} -1/\sqrt{2} & (1-i)/2 \\ (1+i)/2 & -1/\sqrt{2} \end{pmatrix}. \quad R_{11}(g_4) = \begin{pmatrix} 0 & -e_8 \\ -e_8^3 & 0 \end{pmatrix}.$$

$$R_{11}(g_5) = -i\epsilon. \quad R_{11}(g_6) = -\epsilon.$$

$$R_{12}(g_2) = \begin{pmatrix} e_8 & -1-i \\ 0 & -e_8 \end{pmatrix}. \quad R_{12}(g_3) = \begin{pmatrix} 0 & -i \\ i & -\sqrt{2}i \end{pmatrix}. \quad R_{12}(g_4) = \begin{pmatrix} 1 & -\sqrt{2}i \\ \sqrt{2} & -1 \end{pmatrix}.$$

$$R_{12}(g_5) = i\epsilon. \quad R_{12}(g_6) = -\epsilon.$$

$$R_{13}(g_2) = \begin{pmatrix} -e_8^3 & \sqrt{2}i \\ 0 & e_8^3 \end{pmatrix}. \quad R_{13}(g_3) = \begin{pmatrix} 0 & e_8 \\ -e_8^3 & \sqrt{2}i \end{pmatrix}. \quad R_{13}(g_4) = \begin{pmatrix} 1 & -1+i \\ 1+i & -1 \end{pmatrix}.$$

$$R_{13}(g_5) = -i\epsilon. \quad R_{13}(g_6) = -\epsilon.$$

$$R_{14}(g_2) = \begin{pmatrix} e_8 & 0 \\ 0 & -e_8 \end{pmatrix}. \quad R_{14}(g_3) = \begin{pmatrix} i/\sqrt{2} & (1+i)/2 \\ (1-i)/2 & i/\sqrt{2} \end{pmatrix}. \quad R_{14}(g_4) = \begin{pmatrix} 0 & e_8^3 \\ e_8 & 0 \end{pmatrix}.$$

$$R_{14}(g_5) = i\epsilon. \quad R_{14}(g_6) = -\epsilon.$$

 $G_{32}^{(16)}$

$$R_2(g_2) = -1. \quad R_2(g_3) = -1. \quad R_2(g_4) = 1. \quad R_2(g_5) = 1. \quad R_2(g_6) = 1.$$

$$R_3(g_2) = -1. \quad R_3(g_3) = 1. \quad R_3(g_4) = 1. \quad R_3(g_5) = 1. \quad R_3(g_6) = 1.$$

$$R_4(g_2) = 1. \quad R_4(g_3) = -1. \quad R_4(g_4) = 1. \quad R_4(g_5) = 1. \quad R_4(g_6) = 1.$$

$$R_5(g_2) = -i. \quad R_5(g_3) = -1. \quad R_5(g_4) = -1. \quad R_5(g_5) = 1. \quad R_5(g_6) = 1.$$

$$R_6(g_2) = i. \quad R_6(g_3) = -1. \quad R_6(g_4) = -1. \quad R_6(g_5) = 1. \quad R_6(g_6) = 1.$$

$$R_7(g_2) = -i. \quad R_7(g_3) = 1. \quad R_7(g_4) = -1. \quad R_7(g_5) = 1. \quad R_7(g_6) = 1.$$

$$R_8(g_2) = i. \quad R_8(g_3) = 1. \quad R_8(g_4) = -1. \quad R_8(g_5) = 1. \quad R_8(g_6) = 1.$$

$$R_9(g_2) = -e_8. \quad R_9(g_3) = -1. \quad R_9(g_4) = i. \quad R_9(g_5) = -1. \quad R_9(g_6) = 1.$$

$$\begin{aligned}
 R_{10}(g_2) &= -e_8^3. & R_{10}(g_3) &= -1. & R_{10}(g_4) &= -i. & R_{10}(g_5) &= -1. & R_{10}(g_6) &= 1. \\
 R_{11}(g_2) &= e_8^3. & R_{11}(g_3) &= -1. & R_{11}(g_4) &= -i. & R_{11}(g_5) &= -1. & R_{11}(g_6) &= 1. \\
 R_{12}(g_2) &= e_8. & R_{12}(g_3) &= -1. & R_{12}(g_4) &= i. & R_{12}(g_5) &= -1. & R_{12}(g_6) &= 1. \\
 R_{13}(g_2) &= -e_8. & R_{13}(g_3) &= 1. & R_{13}(g_4) &= i. & R_{13}(g_5) &= -1. & R_{13}(g_6) &= 1. \\
 R_{14}(g_2) &= -e_8^3. & R_{14}(g_3) &= 1. & R_{14}(g_4) &= -i. & R_{14}(g_5) &= -1. & R_{14}(g_6) &= 1. \\
 R_{15}(g_2) &= e_8^3. & R_{15}(g_3) &= 1. & R_{15}(g_4) &= -i. & R_{15}(g_5) &= -1. & R_{15}(g_6) &= 1. \\
 R_{16}(g_2) &= e_8. & R_{16}(g_3) &= 1. & R_{16}(g_4) &= i. & R_{16}(g_5) &= -1. & R_{16}(g_6) &= 1. \\
 R_{17}(g_2) &= -e_{16}. & R_{17}(g_3) &= -1. & R_{17}(g_4) &= e_8. & R_{17}(g_5) &= i. & R_{17}(g_6) &= -1. \\
 R_{18}(g_2) &= -e_{16}^3. & R_{18}(g_3) &= -1. & R_{18}(g_4) &= e_8^3. & R_{18}(g_5) &= -i. & R_{18}(g_6) &= -1. \\
 R_{19}(g_2) &= -e_{16}^5. & R_{19}(g_3) &= -1. & R_{19}(g_4) &= -e_8. & R_{19}(g_5) &= i. & R_{19}(g_6) &= -1. \\
 R_{20}(g_2) &= -e_{16}^7. & R_{20}(g_3) &= -1. & R_{20}(g_4) &= -e_8^3. & R_{20}(g_5) &= -i. & R_{20}(g_6) &= -1. \\
 R_{21}(g_2) &= e_{16}^7. & R_{21}(g_3) &= -1. & R_{21}(g_4) &= -e_8^3. & R_{21}(g_5) &= -i. & R_{21}(g_6) &= -1. \\
 R_{22}(g_2) &= e_{16}^5. & R_{22}(g_3) &= -1. & R_{22}(g_4) &= -e_8. & R_{22}(g_5) &= i. & R_{22}(g_6) &= -1. \\
 R_{23}(g_2) &= e_{16}^3. & R_{23}(g_3) &= -1. & R_{23}(g_4) &= e_8^3. & R_{23}(g_5) &= -i. & R_{23}(g_6) &= -1. \\
 R_{24}(g_2) &= e_{16}. & R_{24}(g_3) &= -1. & R_{24}(g_4) &= e_8. & R_{24}(g_5) &= i. & R_{24}(g_6) &= -1. \\
 R_{25}(g_2) &= -e_{16}. & R_{25}(g_3) &= 1. & R_{25}(g_4) &= e_8. & R_{25}(g_5) &= i. & R_{25}(g_6) &= -1. \\
 R_{26}(g_2) &= -e_{16}^3. & R_{26}(g_3) &= 1. & R_{26}(g_4) &= e_8^3. & R_{26}(g_5) &= -i. & R_{26}(g_6) &= -1. \\
 R_{27}(g_2) &= -e_{16}^5. & R_{27}(g_3) &= 1. & R_{27}(g_4) &= -e_8. & R_{27}(g_5) &= i. & R_{27}(g_6) &= -1. \\
 R_{28}(g_2) &= -e_{16}^7. & R_{28}(g_3) &= 1. & R_{28}(g_4) &= -e_8^3. & R_{28}(g_5) &= -i. & R_{28}(g_6) &= -1. \\
 R_{29}(g_2) &= e_{16}^7. & R_{29}(g_3) &= 1. & R_{29}(g_4) &= -e_8^3. & R_{29}(g_5) &= -i. & R_{29}(g_6) &= -1. \\
 R_{30}(g_2) &= e_{16}^5. & R_{30}(g_3) &= 1. & R_{30}(g_4) &= -e_8. & R_{30}(g_5) &= i. & R_{30}(g_6) &= -1. \\
 R_{31}(g_2) &= e_{16}^3. & R_{31}(g_3) &= 1. & R_{31}(g_4) &= e_8^3. & R_{31}(g_5) &= -i. & R_{31}(g_6) &= -1. \\
 R_{32}(g_2) &= e_{16}. & R_{32}(g_3) &= 1. & R_{32}(g_4) &= e_8. & R_{32}(g_5) &= i. & R_{32}(g_6) &= -1.
 \end{aligned}$$

 $G_{32}^{(17)}$

$$\begin{aligned}
 R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= 1. & R_2(g_5) &= 1. & R_2(g_6) &= 1. \\
 R_3(g_2) &= -1. & R_3(g_3) &= 1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. & R_3(g_6) &= 1. \\
 R_4(g_2) &= 1. & R_4(g_3) &= -1. & R_4(g_4) &= 1. & R_4(g_5) &= 1. & R_4(g_6) &= 1. \\
 R_5(g_2) &= -i. & R_5(g_3) &= -1. & R_5(g_4) &= -1. & R_5(g_5) &= 1. & R_5(g_6) &= 1. \\
 R_6(g_2) &= i. & R_6(g_3) &= -1. & R_6(g_4) &= -1. & R_6(g_5) &= 1. & R_6(g_6) &= 1. \\
 R_7(g_2) &= -i. & R_7(g_3) &= 1. & R_7(g_4) &= -1. & R_7(g_5) &= 1. & R_7(g_6) &= 1. \\
 R_8(g_2) &= i. & R_8(g_3) &= 1. & R_8(g_4) &= -1. & R_8(g_5) &= 1. & R_8(g_6) &= 1. \\
 R_9(g_2) &= -e_8. & R_9(g_3) &= -1. & R_9(g_4) &= i. & R_9(g_5) &= -1. & R_9(g_6) &= 1. \\
 R_{10}(g_2) &= -e_8^3. & R_{10}(g_3) &= -1. & R_{10}(g_4) &= -i. & R_{10}(g_5) &= -1. & R_{10}(g_6) &= 1. \\
 R_{11}(g_2) &= e_8^3. & R_{11}(g_3) &= -1. & R_{11}(g_4) &= -i. & R_{11}(g_5) &= -1. & R_{11}(g_6) &= 1. \\
 R_{12}(g_2) &= e_8. & R_{12}(g_3) &= -1. & R_{12}(g_4) &= i. & R_{12}(g_5) &= -1. & R_{12}(g_6) &= 1. \\
 R_{13}(g_2) &= -e_8. & R_{13}(g_3) &= 1. & R_{13}(g_4) &= i. & R_{13}(g_5) &= -1. & R_{13}(g_6) &= 1. \\
 R_{14}(g_2) &= -e_8^3. & R_{14}(g_3) &= 1. & R_{14}(g_4) &= -i. & R_{14}(g_5) &= -1. & R_{14}(g_6) &= 1. \\
 R_{15}(g_2) &= e_8^3. & R_{15}(g_3) &= 1. & R_{15}(g_4) &= -i. & R_{15}(g_5) &= -1. & R_{15}(g_6) &= 1. \\
 R_{16}(g_2) &= e_8. & R_{16}(g_3) &= 1. & R_{16}(g_4) &= i. & R_{16}(g_5) &= -1. & R_{16}(g_6) &= 1.
 \end{aligned}$$

$$R_{17}(g_2) = \begin{pmatrix} e_{16}^5 & 0 \\ 0 & -e_{16}^5 \end{pmatrix}. \quad R_{17}(g_3) = \begin{pmatrix} 0 & -e_8^3 \\ e_8 & 0 \end{pmatrix}. \quad R_{17}(g_4) = \begin{pmatrix} -e_8 & 0 \\ 0 & -e_8 \end{pmatrix}. \\ R_{17}(g_5) = i\epsilon. \quad R_{17}(g_6) = -\epsilon.$$

$$R_{18}(g_2) = \begin{pmatrix} e_{16}^7 & 0 \\ 0 & -e_{16}^7 \end{pmatrix}. \quad R_{18}(g_3) = \begin{pmatrix} 0 & e_{16}^3 \\ -e_{16}^5 & 0 \end{pmatrix}. \quad R_{18}(g_4) = \begin{pmatrix} -e_8^3 & 0 \\ 0 & -e_8^3 \end{pmatrix}. \\ R_{18}(g_5) = -i\epsilon. \quad R_{18}(g_6) = -\epsilon.$$

$$R_{19}(g_2) = \begin{pmatrix} -e_{16}^3 & 0 \\ 0 & e_{16}^3 \end{pmatrix}. \quad R_{19}(g_3) = \begin{pmatrix} 0 & -e_8^3 \\ e_8 & 0 \end{pmatrix}. \quad R_{19}(g_4) = \begin{pmatrix} e_8^3 & 0 \\ 0 & e_8^3 \end{pmatrix}. \\ R_{19}(g_5) = -i\epsilon. \quad R_{19}(g_6) = -\epsilon.$$

$$R_{20}(g_2) = \begin{pmatrix} e_{16} & 0 \\ 0 & -e_{16} \end{pmatrix}. \quad R_{20}(g_3) = \begin{pmatrix} 0 & -e_{16}^7 \\ e_{16} & 0 \end{pmatrix}. \quad R_{20}(g_4) = \begin{pmatrix} e_8 & 0 \\ 0 & e_8 \end{pmatrix}. \\ R_{20}(g_5) = i\epsilon. \quad R_{20}(g_6) = -\epsilon.$$

 $G_{32}^{(18)}$

$$R_2(g_2) = -1. \quad R_2(g_3) = -1. \quad R_2(g_4) = 1. \quad R_2(g_5) = 1. \quad R_2(g_6) = 1.$$

$$R_3(g_2) = -1. \quad R_3(g_3) = 1. \quad R_3(g_4) = 1. \quad R_3(g_5) = 1. \quad R_3(g_6) = 1.$$

$$R_4(g_2) = 1. \quad R_4(g_3) = -1. \quad R_4(g_4) = 1. \quad R_4(g_5) = 1. \quad R_4(g_6) = 1.$$

$$R_5(g_2) = -\lambda. \quad R_5(g_3) = -\phi. \quad R_5(g_4) = -\epsilon. \quad R_5(g_5) = \epsilon. \quad R_5(g_6) = \epsilon.$$

$$R_6(g_2) = -\phi. \quad R_6(g_3) = \begin{pmatrix} -1/\sqrt{2} & 1/\sqrt{2} \\ 1/\sqrt{2} & 1/\sqrt{2} \end{pmatrix}. \quad R_6(g_4) = -\kappa. \quad R_6(g_5) = -\epsilon. \quad R_6(g_6) = \epsilon.$$

$$R_7(g_2) = \phi. \quad R_7(g_3) = \begin{pmatrix} -1/\sqrt{2} & 1/\sqrt{2} \\ 1/\sqrt{2} & 1/\sqrt{2} \end{pmatrix}. \quad R_7(g_4) = -\kappa. \quad R_7(g_5) = -\epsilon. \quad R_7(g_6) = \epsilon.$$

$$R_8(g_2) = \begin{pmatrix} 1 & -\sqrt{2}i \\ 0 & -1 \end{pmatrix}. \quad R_8(g_3) = \begin{pmatrix} -(\sqrt{2}+2)c_{3/8} & (e_{16} - e_{16}^3 + e_{16}^5 - e_{16}^7)/2 \\ -(\sqrt{2}+2)c_{3/8} & (e_{16} + e_{16}^3 - e_{16}^5 - e_{16}^7)/2 \end{pmatrix}.$$

$$R_8(g_4) = \begin{pmatrix} 0 & -1 \\ 1 & -\sqrt{2}i \end{pmatrix}. \quad R_8(g_5) = \begin{pmatrix} 1 & -\sqrt{2}i \\ \sqrt{2} & -1 \end{pmatrix}. \quad R_8(g_6) = -\epsilon.$$

$$R_9(g_2) = -\lambda. \quad R_9(g_3) = \begin{pmatrix} (-e_{16}^3 + e_{16}^5)/2 & (e_{16} - e_{16}^7)/2 \\ (e_{16} - e_{16}^7)/2 & (e_{16}^3 - e_{16}^5)/2 \end{pmatrix}.$$

$$R_9(g_4) = \begin{pmatrix} -1/\sqrt{2} & 1/\sqrt{2} \\ -1/\sqrt{2} & -1/\sqrt{2} \end{pmatrix}. \quad R_9(g_5) = \kappa. \quad R_9(g_6) = -\epsilon.$$

$$R_{10}(g_2) = \begin{pmatrix} 1 - \sqrt{2}i & -e_{16}^3 + e_{16}^5 \\ -e_{16} + e_{16}^3 - e_{16}^5 + e_{16}^7 & -1 + \sqrt{2} \end{pmatrix}. \quad R_{10}(g_3) = \phi.$$

$$R_{10}(g_4) = \begin{pmatrix} 1 & -e_{16}^3 + e_{16}^5 \\ e_{16}^3 - e_{16}^5 & -1 + \sqrt{2} \end{pmatrix}. \quad R_{10}(g_5) = \begin{pmatrix} 1 - \sqrt{2}i & e_{16} - e_{16}^3 + e_{16}^5 - e_{16}^7 \\ -e_{16} + e_{16}^3 - e_{16}^5 + e_{16}^7 & -1 + \sqrt{2} \end{pmatrix}. \\ R_{10}(g_6) = -\epsilon.$$

$$\begin{aligned}
 R_{11}(g_2) &= \begin{pmatrix} 1 & -e_{16}^3 + e_{16}^5 \\ 0 & -1 \end{pmatrix}. & R_{11}(g_3) &= \begin{pmatrix} e_{16}^3 - e_{16}^5 & -1 \\ 1 - \sqrt{2}i & -e_{16}^3 + e_{16}^5 \end{pmatrix}. \\
 R_{11}(g_4) &= \begin{pmatrix} -1 + \sqrt{2} & e_{16}^3 - e_{16}^5 \\ -e_{16}^3 + e_{16}^5 & 1 \end{pmatrix}. & R_{11}(g_5) &= \begin{pmatrix} -1 + \sqrt{2} & -e_{16} + e_{16}^3 - e_{16}^5 + e_{16}^7 \\ e_{16} - e_{16}^3 + e_{16}^5 - e_{16}^7 & 1 - \sqrt{2}i \end{pmatrix}. \\
 & & R_{11}(g_6) &= -\epsilon.
 \end{aligned}$$

 $G_{32}^{(19)}$

$$R_2(g_2) = -1. \quad R_2(g_3) = -1. \quad R_2(g_4) = 1. \quad R_2(g_5) = 1. \quad R_2(g_6) = 1.$$

$$R_3(g_2) = -1. \quad R_3(g_3) = 1. \quad R_3(g_4) = 1. \quad R_3(g_5) = 1. \quad R_3(g_6) = 1.$$

$$R_4(g_2) = 1. \quad R_4(g_3) = -1. \quad R_4(g_4) = 1. \quad R_4(g_5) = 1. \quad R_4(g_6) = 1.$$

$$R_5(g_2) = \lambda. \quad R_5(g_3) = -\phi. \quad R_5(g_4) = -\epsilon. \quad R_5(g_5) = \epsilon. \quad R_5(g_6) = \epsilon.$$

$$R_6(g_2) = \begin{pmatrix} -1 & 0 \\ \sqrt{2} & 1 \end{pmatrix}. \quad R_6(g_3) = -\phi. \quad R_6(g_4) = \begin{pmatrix} 1 & \sqrt{2} \\ -\sqrt{2}i & -1 \end{pmatrix}. \quad R_6(g_5) = -\epsilon. \quad R_6(g_6) = \epsilon.$$

$$\begin{aligned}
 R_7(g_2) &= \begin{pmatrix} -1 & \sqrt{2} \\ 0 & 1 \end{pmatrix}. & R_7(g_3) &= \begin{pmatrix} -\sqrt{2}i & 1 \\ -1 & \sqrt{2} \end{pmatrix}. & R_7(g_4) &= \begin{pmatrix} 1 & -\sqrt{2}i \\ \sqrt{2} & -1 \end{pmatrix}. \\
 & & R_7(g_5) &= -\epsilon. & R_7(g_6) &= \epsilon.
 \end{aligned}$$

$$\begin{aligned}
 R_8(g_2) &= \begin{pmatrix} i & 0 \\ e_{16} - e_{16}^7 & -i \end{pmatrix}. & R_8(g_3) &= \begin{pmatrix} -e_{16} - e_{16}^3 + e_{16}^5 + e_{16}^7 & e_8 + e_8^2 + e_8^3 \\ e_8 + e_8^2 + e_8^3 & e_{16} + e_{16}^3 - e_{16}^5 - e_{16}^7 \end{pmatrix}. \\
 R_8(g_4) &= \begin{pmatrix} -1 - \sqrt{2}i & e_{16}^3 + e_{16}^5 \\ e_{16}^3 + e_{16}^5 & 1 \end{pmatrix}. & R_8(g_5) &= \begin{pmatrix} -1 - \sqrt{2}i & e_{16} + e_{16}^3 + e_{16}^5 + e_{16}^7 \\ e_{16} + e_{16}^3 + e_{16}^5 + e_{16}^7 & 1 + \sqrt{2} \end{pmatrix}. \\
 & & R_8(g_6) &= -\epsilon.
 \end{aligned}$$

$$\begin{aligned}
 R_9(g_2) &= -i\phi. & R_9(g_3) &= \begin{pmatrix} (-e_{16} + e_{16}^7)/2 & (-e_{16}^3 + e_{16}^5)/2 \\ (-e_{16}^3 + e_{16}^5)/2 & (e_{16} - e_{16}^7)/2 \end{pmatrix}. \\
 R_9(g_4) &= \begin{pmatrix} -1/\sqrt{2} & 1/\sqrt{2} \\ -1/\sqrt{2} & -1/\sqrt{2} \end{pmatrix}. & R_9(g_5) &= \kappa. & R_9(g_6) &= -\epsilon.
 \end{aligned}$$

$$R_{10}(g_2) = \begin{pmatrix} i & -e_{16}^3 - e_{16}^5 \\ 0 & -i \end{pmatrix}. \quad R_{10}(g_3) = \phi.$$

$$\begin{aligned}
 R_{10}(g_4) &= \begin{pmatrix} -1 & e_{16} - e_{16}^7 \\ -e_{16} + e_{16}^7 & 1 + \sqrt{2} \end{pmatrix}. & R_{10}(g_5) &= \begin{pmatrix} 1 + \sqrt{2} & -e_{16} - e_{16}^3 + e_{16}^5 + e_{16}^7 \\ e_{16} + e_{16}^3 - e_{16}^5 - e_{16}^7 & -1 - \sqrt{2}i \end{pmatrix}. \\
 & & R_{10}(g_6) &= -\epsilon.
 \end{aligned}$$

$$\begin{aligned}
R_{11}(g_2) &= \begin{pmatrix} -e_8 - e_8^2 - e_8^3 & e_{16} + e_{16}^3 + e_{16}^5 + e_{16}^7 \\ -e_{16}^3 - e_{16}^5 & e_8 + e_8^2 + e_8^3 \end{pmatrix}. \\
R_{11}(g_3) &= \begin{pmatrix} -e_{16} - e_{16}^3 + e_{16}^5 + e_{16}^7 & 1 + \sqrt{2} \\ -1 - \sqrt{2}i & e_{16} + e_{16}^3 - e_{16}^5 - e_{16}^7 \end{pmatrix}. \\
R_{11}(g_4) &= \begin{pmatrix} 1 + \sqrt{2} & -e_{16} + e_{16}^7 \\ e_{16} - e_{16}^7 & -1 \end{pmatrix}. \\
R_{11}(g_5) &= \begin{pmatrix} -1 - \sqrt{2}i & e_{16} + e_{16}^3 - e_{16}^5 - e_{16}^7 \\ -e_{16} - e_{16}^3 + e_{16}^5 + e_{16}^7 & 1 + \sqrt{2} \end{pmatrix}. \\
R_{11}(g_6) &= -\epsilon.
\end{aligned}$$

 $G_{32}^{(20)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= 1. & R_2(g_5) &= 1. & R_2(g_6) &= 1. \\
R_3(g_2) &= -1. & R_3(g_3) &= 1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. & R_3(g_6) &= 1. \\
R_4(g_2) &= 1. & R_4(g_3) &= -1. & R_4(g_4) &= 1. & R_4(g_5) &= 1. & R_4(g_6) &= 1. \\
R_5(g_2) &= -\lambda. & R_5(g_3) &= \phi. & R_5(g_4) &= -\epsilon. & R_5(g_5) &= \epsilon. & R_5(g_6) &= \epsilon.
\end{aligned}$$

$$\begin{aligned}
R_6(g_2) &= \begin{pmatrix} -1 & -\sqrt{2}i \\ 0 & 1 \end{pmatrix}. & R_6(g_3) &= \begin{pmatrix} \sqrt{2} & 1 \\ -1 & -\sqrt{2}i \end{pmatrix}. & R_6(g_4) &= \begin{pmatrix} 1 & \sqrt{2} \\ -\sqrt{2}i & -1 \end{pmatrix}. \\
R_6(g_5) &= -\epsilon. & R_6(g_6) &= \epsilon.
\end{aligned}$$

$$R_7(g_2) = \begin{pmatrix} -1 & 0 \\ \sqrt{2} & 1 \end{pmatrix}. \quad R_7(g_3) = \phi. \quad R_7(g_4) = \begin{pmatrix} 1 & \sqrt{2} \\ -\sqrt{2}i & -1 \end{pmatrix}. \quad R_7(g_5) = -\epsilon. \quad R_7(g_6) = \epsilon.$$

$$\begin{aligned}
R_8(g_2) &= \begin{pmatrix} i & 0 \\ -\sqrt{2}i & -i \end{pmatrix}. & R_8(g_3) &= \begin{pmatrix} (e_{16} - e_{16}^3 - e_{16}^5 + e_{16}^7)/2 & (-e_{16} - e_{16}^3 - e_{16}^5 - e_{16}^7)/2 \\ (e_{16} - e_{16}^3 - e_{16}^5 + e_{16}^7)/2 & (-e_{16} + e_{16}^3 + e_{16}^5 - e_{16}^7)/2 \end{pmatrix}. \\
R_8(g_4) &= \begin{pmatrix} 0 & 1 \\ -1 & -\sqrt{2}i \end{pmatrix}. & R_8(g_5) &= \begin{pmatrix} 1 & \sqrt{2} \\ -\sqrt{2}i & -1 \end{pmatrix}. & R_8(g_6) &= -\epsilon.
\end{aligned}$$

$$\begin{aligned}
R_9(g_2) &= \begin{pmatrix} -i & 0 \\ -\sqrt{2}i & i \end{pmatrix}. & R_9(g_3) &= \begin{pmatrix} (e_{16} + e_{16}^3 + e_{16}^5 + e_{16}^7)/2 & (-e_{16} - e_{16}^3 - e_{16}^5 - e_{16}^7)/2 \\ (-e_{16} + e_{16}^3 + e_{16}^5 - e_{16}^7)/2 & (-e_{16} - e_{16}^3 - e_{16}^5 - e_{16}^7)/2 \end{pmatrix}. \\
R_9(g_4) &= \begin{pmatrix} -\sqrt{2}i & 1 \\ -1 & 0 \end{pmatrix}. & R_9(g_5) &= \begin{pmatrix} -1 & \sqrt{2} \\ -\sqrt{2}i & 1 \end{pmatrix}. & R_9(g_6) &= -\epsilon.
\end{aligned}$$

$$\begin{aligned}
R_{10}(g_2) &= -i\lambda. & R_{10}(g_3) &= \begin{pmatrix} (-e_{16}^3 - e_{16}^5)/2 & (-e_{16}^3 + e_{16}^5)/2 \\ (e_{16}^3 - e_{16}^5)/2 & (e_{16}^3 + e_{16}^5)/2 \end{pmatrix}. \\
R_{10}(g_4) &= \begin{pmatrix} 1/\sqrt{2} & i/\sqrt{2} \\ i/\sqrt{2} & 1/\sqrt{2} \end{pmatrix}. & R_{10}(g_5) &= -i\phi. & R_{10}(g_6) &= -\epsilon.
\end{aligned}$$

$$\begin{aligned}
 R_{11}(g_2) &= \begin{pmatrix} -e_8 - e_8^2 - e_8^3 & e_{16} + e_{16}^3 + e_{16}^5 + e_{16}^7 \\ -e_{16}^3 - e_{16}^5 & e_8 + e_8^2 + e_8^3 \end{pmatrix}. \\
 R_{11}(g_3) &= \begin{pmatrix} e_{16}^3 + e_{16}^5 & -e_8 - e_8^2 - e_8^3 \\ i & -e_{16}^3 - e_{16}^5 \end{pmatrix}. \\
 R_{11}(g_4) &= \begin{pmatrix} -1 & e_{16} - e_{16}^7 \\ -e_{16} + e_{16}^7 & 1 + \sqrt{2} \end{pmatrix}. \\
 R_{11}(g_5) &= \begin{pmatrix} 1 + \sqrt{2} & -e_{16} - e_{16}^3 + e_{16}^5 + e_{16}^7 \\ e_{16} + e_{16}^3 - e_{16}^5 - e_{16}^7 & -1 - \sqrt{2}i \end{pmatrix}. \\
 R_{11}(g_6) &= -\epsilon.
 \end{aligned}$$

 $G_{32}^{(21)}$

$$\begin{aligned}
 R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= -1. & R_2(g_5) &= 1. & R_2(g_6) &= 1. \\
 R_3(g_2) &= -1. & R_3(g_3) &= -1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. & R_3(g_6) &= 1. \\
 R_4(g_2) &= -1. & R_4(g_3) &= 1. & R_4(g_4) &= -1. & R_4(g_5) &= 1. & R_4(g_6) &= 1. \\
 R_5(g_2) &= -1. & R_5(g_3) &= 1. & R_5(g_4) &= 1. & R_5(g_5) &= 1. & R_5(g_6) &= 1. \\
 R_6(g_2) &= 1. & R_6(g_3) &= -1. & R_6(g_4) &= -1. & R_6(g_5) &= 1. & R_6(g_6) &= 1. \\
 R_7(g_2) &= 1. & R_7(g_3) &= -1. & R_7(g_4) &= 1. & R_7(g_5) &= 1. & R_7(g_6) &= 1. \\
 R_8(g_2) &= 1. & R_8(g_3) &= 1. & R_8(g_4) &= -1. & R_8(g_5) &= 1. & R_8(g_6) &= 1. \\
 R_9(g_2) &= -1. & R_9(g_3) &= -i. & R_9(g_4) &= -1. & R_9(g_5) &= 1. & R_9(g_6) &= -1. \\
 R_{10}(g_2) &= -1. & R_{10}(g_3) &= i. & R_{10}(g_4) &= -1. & R_{10}(g_5) &= 1. & R_{10}(g_6) &= -1. \\
 R_{11}(g_2) &= -1. & R_{11}(g_3) &= -i. & R_{11}(g_4) &= 1. & R_{11}(g_5) &= 1. & R_{11}(g_6) &= -1. \\
 R_{12}(g_2) &= -1. & R_{12}(g_3) &= i. & R_{12}(g_4) &= 1. & R_{12}(g_5) &= 1. & R_{12}(g_6) &= -1. \\
 R_{13}(g_2) &= 1. & R_{13}(g_3) &= -i. & R_{13}(g_4) &= -1. & R_{13}(g_5) &= 1. & R_{13}(g_6) &= -1. \\
 R_{14}(g_2) &= 1. & R_{14}(g_3) &= i. & R_{14}(g_4) &= -1. & R_{14}(g_5) &= 1. & R_{14}(g_6) &= -1. \\
 R_{15}(g_2) &= 1. & R_{15}(g_3) &= -i. & R_{15}(g_4) &= 1. & R_{15}(g_5) &= 1. & R_{15}(g_6) &= -1. \\
 R_{16}(g_2) &= 1. & R_{16}(g_3) &= i. & R_{16}(g_4) &= 1. & R_{16}(g_5) &= 1. & R_{16}(g_6) &= -1. \\
 R_{17}(g_2) &= -i. & R_{17}(g_3) &= -1. & R_{17}(g_4) &= -1. & R_{17}(g_5) &= -1. & R_{17}(g_6) &= 1. \\
 R_{18}(g_2) &= i. & R_{18}(g_3) &= -1. & R_{18}(g_4) &= -1. & R_{18}(g_5) &= -1. & R_{18}(g_6) &= 1. \\
 R_{19}(g_2) &= -i. & R_{19}(g_3) &= -1. & R_{19}(g_4) &= 1. & R_{19}(g_5) &= -1. & R_{19}(g_6) &= 1. \\
 R_{20}(g_2) &= i. & R_{20}(g_3) &= -1. & R_{20}(g_4) &= 1. & R_{20}(g_5) &= -1. & R_{20}(g_6) &= 1. \\
 R_{21}(g_2) &= -i. & R_{21}(g_3) &= 1. & R_{21}(g_4) &= -1. & R_{21}(g_5) &= -1. & R_{21}(g_6) &= 1. \\
 R_{22}(g_2) &= i. & R_{22}(g_3) &= 1. & R_{22}(g_4) &= -1. & R_{22}(g_5) &= -1. & R_{22}(g_6) &= 1. \\
 R_{23}(g_2) &= -i. & R_{23}(g_3) &= 1. & R_{23}(g_4) &= 1. & R_{23}(g_5) &= -1. & R_{23}(g_6) &= 1. \\
 R_{24}(g_2) &= i. & R_{24}(g_3) &= 1. & R_{24}(g_4) &= 1. & R_{24}(g_5) &= -1. & R_{24}(g_6) &= 1. \\
 R_{25}(g_2) &= -i. & R_{25}(g_3) &= -i. & R_{25}(g_4) &= -1. & R_{25}(g_5) &= -1. & R_{25}(g_6) &= -1. \\
 R_{26}(g_2) &= i. & R_{26}(g_3) &= i. & R_{26}(g_4) &= -1. & R_{26}(g_5) &= -1. & R_{26}(g_6) &= -1. \\
 R_{27}(g_2) &= -i. & R_{27}(g_3) &= -i. & R_{27}(g_4) &= 1. & R_{27}(g_5) &= -1. & R_{27}(g_6) &= -1. \\
 R_{28}(g_2) &= i. & R_{28}(g_3) &= i. & R_{28}(g_4) &= 1. & R_{28}(g_5) &= -1. & R_{28}(g_6) &= -1. \\
 R_{29}(g_2) &= -i. & R_{29}(g_3) &= i. & R_{29}(g_4) &= -1. & R_{29}(g_5) &= -1. & R_{29}(g_6) &= -1. \\
 R_{30}(g_2) &= i. & R_{30}(g_3) &= -i. & R_{30}(g_4) &= -1. & R_{30}(g_5) &= -1. & R_{30}(g_6) &= -1.
 \end{aligned}$$

$$\begin{aligned}
R_{18}(g_2) &= \lambda. & R_{18}(g_3) &= -\kappa. & R_{18}(g_4) &= -\epsilon. & R_{18}(g_5) &= -\epsilon. & R_{18}(g_6) &= \epsilon. \\
R_{19}(g_2) &= i\lambda. & R_{19}(g_3) &= i\phi. & R_{19}(g_4) &= \epsilon. & R_{19}(g_5) &= -\epsilon. & R_{19}(g_6) &= -\epsilon. \\
R_{20}(g_2) &= -\lambda. & R_{20}(g_3) &= \kappa. & R_{20}(g_4) &= \epsilon. & R_{20}(g_5) &= -\epsilon. & R_{20}(g_6) &= \epsilon.
\end{aligned}$$

 $G_{32}^{(24)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= -1. & R_2(g_5) &= 1. & R_2(g_6) &= 1. \\
R_3(g_2) &= -1. & R_3(g_3) &= -1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. & R_3(g_6) &= 1. \\
R_4(g_2) &= -1. & R_4(g_3) &= 1. & R_4(g_4) &= -1. & R_4(g_5) &= 1. & R_4(g_6) &= 1. \\
R_5(g_2) &= -1. & R_5(g_3) &= 1. & R_5(g_4) &= 1. & R_5(g_5) &= 1. & R_5(g_6) &= 1. \\
R_6(g_2) &= 1. & R_6(g_3) &= -1. & R_6(g_4) &= -1. & R_6(g_5) &= 1. & R_6(g_6) &= 1. \\
R_7(g_2) &= 1. & R_7(g_3) &= -1. & R_7(g_4) &= 1. & R_7(g_5) &= 1. & R_7(g_6) &= 1. \\
R_8(g_2) &= 1. & R_8(g_3) &= 1. & R_8(g_4) &= -1. & R_8(g_5) &= 1. & R_8(g_6) &= 1. \\
R_9(g_2) &= -i. & R_9(g_3) &= -1. & R_9(g_4) &= -1. & R_9(g_5) &= 1. & R_9(g_6) &= -1. \\
R_{10}(g_2) &= i. & R_{10}(g_3) &= -1. & R_{10}(g_4) &= -1. & R_{10}(g_5) &= 1. & R_{10}(g_6) &= -1. \\
R_{11}(g_2) &= -i. & R_{11}(g_3) &= -1. & R_{11}(g_4) &= 1. & R_{11}(g_5) &= 1. & R_{11}(g_6) &= -1. \\
R_{12}(g_2) &= i. & R_{12}(g_3) &= -1. & R_{12}(g_4) &= 1. & R_{12}(g_5) &= 1. & R_{12}(g_6) &= -1. \\
R_{13}(g_2) &= -i. & R_{13}(g_3) &= 1. & R_{13}(g_4) &= -1. & R_{13}(g_5) &= 1. & R_{13}(g_6) &= -1. \\
R_{14}(g_2) &= i. & R_{14}(g_3) &= 1. & R_{14}(g_4) &= -1. & R_{14}(g_5) &= 1. & R_{14}(g_6) &= -1. \\
R_{15}(g_2) &= -i. & R_{15}(g_3) &= 1. & R_{15}(g_4) &= 1. & R_{15}(g_5) &= 1. & R_{15}(g_6) &= -1. \\
R_{16}(g_2) &= i. & R_{16}(g_3) &= 1. & R_{16}(g_4) &= 1. & R_{16}(g_5) &= 1. & R_{16}(g_6) &= -1. \\
R_{17}(g_2) &= i\lambda. & R_{17}(g_3) &= -i\kappa. & R_{17}(g_4) &= -i\epsilon. & R_{17}(g_5) &= -\epsilon. & R_{17}(g_6) &= -\epsilon. \\
R_{18}(g_2) &= -i\lambda. & R_{18}(g_3) &= \phi. & R_{18}(g_4) &= i\epsilon. & R_{18}(g_5) &= -\epsilon. & R_{18}(g_6) &= -\epsilon. \\
R_{19}(g_2) &= -\lambda. & R_{19}(g_3) &= -\phi. & R_{19}(g_4) &= -i\epsilon. & R_{19}(g_5) &= -\epsilon. & R_{19}(g_6) &= \epsilon. \\
R_{20}(g_2) &= \lambda. & R_{20}(g_3) &= i\kappa. & R_{20}(g_4) &= i\epsilon. & R_{20}(g_5) &= -\epsilon. & R_{20}(g_6) &= \epsilon.
\end{aligned}$$

 $G_{32}^{(25)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= -1. & R_2(g_5) &= 1. & R_2(g_6) &= 1. \\
R_3(g_2) &= -1. & R_3(g_3) &= -1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. & R_3(g_6) &= 1. \\
R_4(g_2) &= -1. & R_4(g_3) &= 1. & R_4(g_4) &= -1. & R_4(g_5) &= 1. & R_4(g_6) &= 1. \\
R_5(g_2) &= -1. & R_5(g_3) &= 1. & R_5(g_4) &= 1. & R_5(g_5) &= 1. & R_5(g_6) &= 1. \\
R_6(g_2) &= 1. & R_6(g_3) &= -1. & R_6(g_4) &= -1. & R_6(g_5) &= 1. & R_6(g_6) &= 1. \\
R_7(g_2) &= 1. & R_7(g_3) &= -1. & R_7(g_4) &= 1. & R_7(g_5) &= 1. & R_7(g_6) &= 1. \\
R_8(g_2) &= 1. & R_8(g_3) &= 1. & R_8(g_4) &= -1. & R_8(g_5) &= 1. & R_8(g_6) &= 1. \\
R_9(g_2) &= -i. & R_9(g_3) &= -1. & R_9(g_4) &= -i. & R_9(g_5) &= 1. & R_9(g_6) &= -1. \\
R_{10}(g_2) &= i. & R_{10}(g_3) &= -1. & R_{10}(g_4) &= i. & R_{10}(g_5) &= 1. & R_{10}(g_6) &= -1. \\
R_{11}(g_2) &= -i. & R_{11}(g_3) &= -1. & R_{11}(g_4) &= i. & R_{11}(g_5) &= 1. & R_{11}(g_6) &= -1. \\
R_{12}(g_2) &= i. & R_{12}(g_3) &= -1. & R_{12}(g_4) &= -i. & R_{12}(g_5) &= 1. & R_{12}(g_6) &= -1. \\
R_{13}(g_2) &= -i. & R_{13}(g_3) &= 1. & R_{13}(g_4) &= -i. & R_{13}(g_5) &= 1. & R_{13}(g_6) &= -1. \\
R_{14}(g_2) &= i. & R_{14}(g_3) &= 1. & R_{14}(g_4) &= i. & R_{14}(g_5) &= 1. & R_{14}(g_6) &= -1. \\
R_{15}(g_2) &= -i. & R_{15}(g_3) &= 1. & R_{15}(g_4) &= i. & R_{15}(g_5) &= 1. & R_{15}(g_6) &= -1. \\
R_{16}(g_2) &= i. & R_{16}(g_3) &= 1. & R_{16}(g_4) &= -i. & R_{16}(g_5) &= 1. & R_{16}(g_6) &= -1.
\end{aligned}$$

$$\begin{aligned}
R_{17}(g_2) &= -\lambda. & R_{17}(g_3) &= -\phi. & R_{17}(g_4) &= -\epsilon. & R_{17}(g_5) &= -\epsilon. & R_{17}(g_6) &= \epsilon. \\
R_{18}(g_2) &= -\lambda. & R_{18}(g_3) &= -\phi. & R_{18}(g_4) &= \epsilon. & R_{18}(g_5) &= -\epsilon. & R_{18}(g_6) &= \epsilon. \\
R_{19}(g_2) &= -i\lambda. & R_{19}(g_3) &= \phi. & R_{19}(g_4) &= -i\epsilon. & R_{19}(g_5) &= -\epsilon. & R_{19}(g_6) &= -\epsilon. \\
R_{20}(g_2) &= -i\lambda. & R_{20}(g_3) &= \phi. & R_{20}(g_4) &= i\epsilon. & R_{20}(g_5) &= -\epsilon. & R_{20}(g_6) &= -\epsilon.
\end{aligned}$$

 $G_{32}^{(26)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= -1. & R_2(g_5) &= 1. & R_2(g_6) &= 1. \\
R_3(g_2) &= -1. & R_3(g_3) &= -1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. & R_3(g_6) &= 1. \\
R_4(g_2) &= -1. & R_4(g_3) &= 1. & R_4(g_4) &= -1. & R_4(g_5) &= 1. & R_4(g_6) &= 1. \\
R_5(g_2) &= -1. & R_5(g_3) &= 1. & R_5(g_4) &= 1. & R_5(g_5) &= 1. & R_5(g_6) &= 1. \\
R_6(g_2) &= 1. & R_6(g_3) &= -1. & R_6(g_4) &= -1. & R_6(g_5) &= 1. & R_6(g_6) &= 1. \\
R_7(g_2) &= 1. & R_7(g_3) &= -1. & R_7(g_4) &= 1. & R_7(g_5) &= 1. & R_7(g_6) &= 1. \\
R_8(g_2) &= 1. & R_8(g_3) &= 1. & R_8(g_4) &= -1. & R_8(g_5) &= 1. & R_8(g_6) &= 1. \\
R_9(g_2) &= -i. & R_9(g_3) &= -1. & R_9(g_4) &= -i. & R_9(g_5) &= 1. & R_9(g_6) &= -1. \\
R_{10}(g_2) &= i. & R_{10}(g_3) &= -1. & R_{10}(g_4) &= i. & R_{10}(g_5) &= 1. & R_{10}(g_6) &= -1. \\
R_{11}(g_2) &= -i. & R_{11}(g_3) &= -1. & R_{11}(g_4) &= i. & R_{11}(g_5) &= 1. & R_{11}(g_6) &= -1. \\
R_{12}(g_2) &= i. & R_{12}(g_3) &= -1. & R_{12}(g_4) &= -i. & R_{12}(g_5) &= 1. & R_{12}(g_6) &= -1. \\
R_{13}(g_2) &= -i. & R_{13}(g_3) &= 1. & R_{13}(g_4) &= -i. & R_{13}(g_5) &= 1. & R_{13}(g_6) &= -1. \\
R_{14}(g_2) &= i. & R_{14}(g_3) &= 1. & R_{14}(g_4) &= i. & R_{14}(g_5) &= 1. & R_{14}(g_6) &= -1. \\
R_{15}(g_2) &= -i. & R_{15}(g_3) &= 1. & R_{15}(g_4) &= i. & R_{15}(g_5) &= 1. & R_{15}(g_6) &= -1. \\
R_{16}(g_2) &= i. & R_{16}(g_3) &= 1. & R_{16}(g_4) &= -i. & R_{16}(g_5) &= 1. & R_{16}(g_6) &= -1. \\
R_{17}(g_2) &= -i\lambda. & R_{17}(g_3) &= -i\phi. & R_{17}(g_4) &= -\epsilon. & R_{17}(g_5) &= -\epsilon. & R_{17}(g_6) &= -\epsilon. \\
R_{18}(g_2) &= i\lambda. & R_{18}(g_3) &= i\phi. & R_{18}(g_4) &= \epsilon. & R_{18}(g_5) &= -\epsilon. & R_{18}(g_6) &= -\epsilon. \\
R_{19}(g_2) &= -\lambda. & R_{19}(g_3) &= -i\phi. & R_{19}(g_4) &= -i\epsilon. & R_{19}(g_5) &= -\epsilon. & R_{19}(g_6) &= \epsilon. \\
R_{20}(g_2) &= -\lambda. & R_{20}(g_3) &= -\kappa. & R_{20}(g_4) &= i\epsilon. & R_{20}(g_5) &= -\epsilon. & R_{20}(g_6) &= \epsilon.
\end{aligned}$$

 $G_{32}^{(27)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= -1. & R_2(g_5) &= 1. & R_2(g_6) &= 1. \\
R_3(g_2) &= -1. & R_3(g_3) &= -1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. & R_3(g_6) &= 1. \\
R_4(g_2) &= -1. & R_4(g_3) &= 1. & R_4(g_4) &= -1. & R_4(g_5) &= 1. & R_4(g_6) &= 1. \\
R_5(g_2) &= -1. & R_5(g_3) &= 1. & R_5(g_4) &= 1. & R_5(g_5) &= 1. & R_5(g_6) &= 1. \\
R_6(g_2) &= 1. & R_6(g_3) &= -1. & R_6(g_4) &= -1. & R_6(g_5) &= 1. & R_6(g_6) &= 1. \\
R_7(g_2) &= 1. & R_7(g_3) &= -1. & R_7(g_4) &= 1. & R_7(g_5) &= 1. & R_7(g_6) &= 1. \\
R_8(g_2) &= 1. & R_8(g_3) &= 1. & R_8(g_4) &= -1. & R_8(g_5) &= 1. & R_8(g_6) &= 1. \\
R_9(g_2) &= -\lambda. & R_9(g_3) &= \epsilon. & R_9(g_4) &= -\phi. & R_9(g_5) &= \epsilon. & R_9(g_6) &= -\epsilon. \\
R_{10}(g_2) &= -\lambda. & R_{10}(g_3) &= -\epsilon. & R_{10}(g_4) &= -\phi. & R_{10}(g_5) &= \epsilon. & R_{10}(g_6) &= -\epsilon. \\
R_{11}(g_2) &= -\lambda. & R_{11}(g_3) &= -\phi. & R_{11}(g_4) &= -\epsilon. & R_{11}(g_5) &= -\epsilon. & R_{11}(g_6) &= \epsilon. \\
R_{12}(g_2) &= \lambda. & R_{12}(g_3) &= \phi. & R_{12}(g_4) &= -\phi. & R_{12}(g_5) &= -\epsilon. & R_{12}(g_6) &= -\epsilon. \\
R_{13}(g_2) &= \lambda. & R_{13}(g_3) &= \phi. & R_{13}(g_4) &= \phi. & R_{13}(g_5) &= -\epsilon. & R_{13}(g_6) &= -\epsilon. \\
R_{14}(g_2) &= -\lambda. & R_{14}(g_3) &= \phi. & R_{14}(g_4) &= \epsilon. & R_{14}(g_5) &= -\epsilon. & R_{14}(g_6) &= \epsilon.
\end{aligned}$$

$G_{32}^{(28)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= -1. & R_2(g_5) &= 1. & R_2(g_6) &= 1. \\
R_3(g_2) &= -1. & R_3(g_3) &= -1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. & R_3(g_6) &= 1. \\
R_4(g_2) &= -1. & R_4(g_3) &= 1. & R_4(g_4) &= -1. & R_4(g_5) &= 1. & R_4(g_6) &= 1. \\
R_5(g_2) &= -1. & R_5(g_3) &= 1. & R_5(g_4) &= 1. & R_5(g_5) &= 1. & R_5(g_6) &= 1. \\
R_6(g_2) &= 1. & R_6(g_3) &= -1. & R_6(g_4) &= -1. & R_6(g_5) &= 1. & R_6(g_6) &= 1. \\
R_7(g_2) &= 1. & R_7(g_3) &= -1. & R_7(g_4) &= 1. & R_7(g_5) &= 1. & R_7(g_6) &= 1. \\
R_8(g_2) &= 1. & R_8(g_3) &= 1. & R_8(g_4) &= -1. & R_8(g_5) &= 1. & R_8(g_6) &= 1. \\
R_9(g_2) &= \lambda. & R_9(g_3) &= \kappa. & R_9(g_4) &= -\epsilon. & R_9(g_5) &= -\epsilon. & R_9(g_6) &= \epsilon. \\
R_{10}(g_2) &= -\lambda. & R_{10}(g_3) &= -\kappa. & R_{10}(g_4) &= \epsilon. & R_{10}(g_5) &= -\epsilon. & R_{10}(g_6) &= \epsilon. \\
R_{11}(g_2) &= -\lambda. & R_{11}(g_3) &= -\epsilon. & R_{11}(g_4) &= \phi. & R_{11}(g_5) &= \epsilon. & R_{11}(g_6) &= -\epsilon. \\
R_{12}(g_2) &= -\lambda. & R_{12}(g_3) &= \epsilon. & R_{12}(g_4) &= -\phi. & R_{12}(g_5) &= \epsilon. & R_{12}(g_6) &= -\epsilon. \\
R_{13}(g_2) &= \lambda. & R_{13}(g_3) &= -\kappa. & R_{13}(g_4) &= -i\kappa. & R_{13}(g_5) &= -\epsilon. & R_{13}(g_6) &= -\epsilon. \\
R_{14}(g_2) &= -\lambda. & R_{14}(g_3) &= -i\phi. & R_{14}(g_4) &= -\phi. & R_{14}(g_5) &= -\epsilon. & R_{14}(g_6) &= -\epsilon.
\end{aligned}$$

 $G_{32}^{(29)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= -1. & R_2(g_5) &= 1. & R_2(g_6) &= 1. \\
R_3(g_2) &= -1. & R_3(g_3) &= -1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. & R_3(g_6) &= 1. \\
R_4(g_2) &= -1. & R_4(g_3) &= 1. & R_4(g_4) &= -1. & R_4(g_5) &= 1. & R_4(g_6) &= 1. \\
R_5(g_2) &= -1. & R_5(g_3) &= 1. & R_5(g_4) &= 1. & R_5(g_5) &= 1. & R_5(g_6) &= 1. \\
R_6(g_2) &= 1. & R_6(g_3) &= -1. & R_6(g_4) &= -1. & R_6(g_5) &= 1. & R_6(g_6) &= 1. \\
R_7(g_2) &= 1. & R_7(g_3) &= -1. & R_7(g_4) &= 1. & R_7(g_5) &= 1. & R_7(g_6) &= 1. \\
R_8(g_2) &= 1. & R_8(g_3) &= 1. & R_8(g_4) &= -1. & R_8(g_5) &= 1. & R_8(g_6) &= 1. \\
R_9(g_2) &= i\lambda. & R_9(g_3) &= \kappa. & R_9(g_4) &= -\epsilon. & R_9(g_5) &= -\epsilon. & R_9(g_6) &= \epsilon. \\
R_{10}(g_2) &= i\lambda. & R_{10}(g_3) &= \kappa. & R_{10}(g_4) &= \epsilon. & R_{10}(g_5) &= -\epsilon. & R_{10}(g_6) &= \epsilon. \\
R_{11}(g_2) &= -\lambda. & R_{11}(g_3) &= -\epsilon. & R_{11}(g_4) &= \phi. & R_{11}(g_5) &= \epsilon. & R_{11}(g_6) &= -\epsilon. \\
R_{12}(g_2) &= -\lambda. & R_{12}(g_3) &= \epsilon. & R_{12}(g_4) &= -\phi. & R_{12}(g_5) &= \epsilon. & R_{12}(g_6) &= -\epsilon. \\
R_{13}(g_2) &= i\lambda. & R_{13}(g_3) &= \kappa. & R_{13}(g_4) &= i\kappa. & R_{13}(g_5) &= -\epsilon. & R_{13}(g_6) &= -\epsilon. \\
R_{14}(g_2) &= i\lambda. & R_{14}(g_3) &= -i\phi. & R_{14}(g_4) &= -\phi. & R_{14}(g_5) &= -\epsilon. & R_{14}(g_6) &= -\epsilon.
\end{aligned}$$

$G_{32}^{(30)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= -1. & R_2(g_5) &= 1. & R_2(g_6) &= 1. \\
R_3(g_2) &= -1. & R_3(g_3) &= -1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. & R_3(g_6) &= 1. \\
R_4(g_2) &= -1. & R_4(g_3) &= 1. & R_4(g_4) &= -1. & R_4(g_5) &= 1. & R_4(g_6) &= 1. \\
R_5(g_2) &= -1. & R_5(g_3) &= 1. & R_5(g_4) &= 1. & R_5(g_5) &= 1. & R_5(g_6) &= 1. \\
R_6(g_2) &= 1. & R_6(g_3) &= -1. & R_6(g_4) &= -1. & R_6(g_5) &= 1. & R_6(g_6) &= 1. \\
R_7(g_2) &= 1. & R_7(g_3) &= -1. & R_7(g_4) &= 1. & R_7(g_5) &= 1. & R_7(g_6) &= 1. \\
R_8(g_2) &= 1. & R_8(g_3) &= 1. & R_8(g_4) &= -1. & R_8(g_5) &= 1. & R_8(g_6) &= 1. \\
R_9(g_2) &= \lambda. & R_9(g_3) &= \epsilon. & R_9(g_4) &= \phi. & R_9(g_5) &= \epsilon. & R_9(g_6) &= -\epsilon. \\
R_{10}(g_2) &= -\lambda. & R_{10}(g_3) &= -\epsilon. & R_{10}(g_4) &= -\phi. & R_{10}(g_5) &= \epsilon. & R_{10}(g_6) &= -\epsilon. \\
R_{11}(g_2) &= \lambda. & R_{11}(g_3) &= i\kappa. & R_{11}(g_4) &= \kappa. & R_{11}(g_5) &= -\epsilon. & R_{11}(g_6) &= -\epsilon. \\
R_{12}(g_2) &= -\lambda. & R_{12}(g_3) &= \phi. & R_{12}(g_4) &= i\phi. & R_{12}(g_5) &= -\epsilon. & R_{12}(g_6) &= -\epsilon. \\
R_{13}(g_2) &= -\lambda. & R_{13}(g_3) &= i\kappa. & R_{13}(g_4) &= -i\epsilon. & R_{13}(g_5) &= -\epsilon. & R_{13}(g_6) &= \epsilon. \\
R_{14}(g_2) &= \lambda. & R_{14}(g_3) &= i\kappa. & R_{14}(g_4) &= i\epsilon. & R_{14}(g_5) &= -\epsilon. & R_{14}(g_6) &= \epsilon.
\end{aligned}$$

 $G_{32}^{(31)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= -1. & R_2(g_5) &= 1. & R_2(g_6) &= 1. \\
R_3(g_2) &= -1. & R_3(g_3) &= -1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. & R_3(g_6) &= 1. \\
R_4(g_2) &= -1. & R_4(g_3) &= 1. & R_4(g_4) &= -1. & R_4(g_5) &= 1. & R_4(g_6) &= 1. \\
R_5(g_2) &= -1. & R_5(g_3) &= 1. & R_5(g_4) &= 1. & R_5(g_5) &= 1. & R_5(g_6) &= 1. \\
R_6(g_2) &= 1. & R_6(g_3) &= -1. & R_6(g_4) &= -1. & R_6(g_5) &= 1. & R_6(g_6) &= 1. \\
R_7(g_2) &= 1. & R_7(g_3) &= -1. & R_7(g_4) &= 1. & R_7(g_5) &= 1. & R_7(g_6) &= 1. \\
R_8(g_2) &= 1. & R_8(g_3) &= 1. & R_8(g_4) &= -1. & R_8(g_5) &= 1. & R_8(g_6) &= 1. \\
R_9(g_2) &= \lambda. & R_9(g_3) &= \kappa. & R_9(g_4) &= \kappa. & R_9(g_5) &= -\epsilon. & R_9(g_6) &= -\epsilon. \\
R_{10}(g_2) &= \lambda. & R_{10}(g_3) &= \kappa. & R_{10}(g_4) &= -\kappa. & R_{10}(g_5) &= -\epsilon. & R_{10}(g_6) &= -\epsilon. \\
R_{11}(g_2) &= \lambda. & R_{11}(g_3) &= -i\epsilon. & R_{11}(g_4) &= \phi. & R_{11}(g_5) &= \epsilon. & R_{11}(g_6) &= -\epsilon. \\
R_{12}(g_2) &= -\lambda. & R_{12}(g_3) &= i\epsilon. & R_{12}(g_4) &= -i\kappa. & R_{12}(g_5) &= \epsilon. & R_{12}(g_6) &= -\epsilon. \\
R_{13}(g_2) &= -\lambda. & R_{13}(g_3) &= i\kappa. & R_{13}(g_4) &= -i\epsilon. & R_{13}(g_5) &= -\epsilon. & R_{13}(g_6) &= \epsilon. \\
R_{14}(g_2) &= -\lambda. & R_{14}(g_3) &= -i\kappa. & R_{14}(g_4) &= i\epsilon. & R_{14}(g_5) &= -\epsilon. & R_{14}(g_6) &= \epsilon.
\end{aligned}$$

$G_{32}^{(32)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= -1. & R_2(g_5) &= 1. & R_2(g_6) &= 1. \\
R_3(g_2) &= -1. & R_3(g_3) &= -1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. & R_3(g_6) &= 1. \\
R_4(g_2) &= -1. & R_4(g_3) &= 1. & R_4(g_4) &= -1. & R_4(g_5) &= 1. & R_4(g_6) &= 1. \\
R_5(g_2) &= -1. & R_5(g_3) &= 1. & R_5(g_4) &= 1. & R_5(g_5) &= 1. & R_5(g_6) &= 1. \\
R_6(g_2) &= 1. & R_6(g_3) &= -1. & R_6(g_4) &= -1. & R_6(g_5) &= 1. & R_6(g_6) &= 1. \\
R_7(g_2) &= 1. & R_7(g_3) &= -1. & R_7(g_4) &= 1. & R_7(g_5) &= 1. & R_7(g_6) &= 1. \\
R_8(g_2) &= 1. & R_8(g_3) &= 1. & R_8(g_4) &= -1. & R_8(g_5) &= 1. & R_8(g_6) &= 1. \\
R_9(g_2) &= i\lambda. & R_9(g_3) &= -\kappa. & R_9(g_4) &= -\kappa. & R_9(g_5) &= -\epsilon. & R_9(g_6) &= -\epsilon. \\
R_{10}(g_2) &= i\lambda. & R_{10}(g_3) &= -i\phi. & R_{10}(g_4) &= i\phi. & R_{10}(g_5) &= -\epsilon. & R_{10}(g_6) &= -\epsilon. \\
R_{11}(g_2) &= \lambda. & R_{11}(g_3) &= -i\epsilon. & R_{11}(g_4) &= -i\kappa. & R_{11}(g_5) &= \epsilon. & R_{11}(g_6) &= -\epsilon. \\
R_{12}(g_2) &= -\lambda. & R_{12}(g_3) &= i\epsilon. & R_{12}(g_4) &= i\kappa. & R_{12}(g_5) &= \epsilon. & R_{12}(g_6) &= -\epsilon. \\
R_{13}(g_2) &= -i\lambda. & R_{13}(g_3) &= -\phi. & R_{13}(g_4) &= -i\epsilon. & R_{13}(g_5) &= -\epsilon. & R_{13}(g_6) &= \epsilon. \\
R_{14}(g_2) &= -i\lambda. & R_{14}(g_3) &= i\kappa. & R_{14}(g_4) &= i\epsilon. & R_{14}(g_5) &= -\epsilon. & R_{14}(g_6) &= \epsilon.
\end{aligned}$$

 $G_{32}^{(33)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= -1. & R_2(g_5) &= 1. & R_2(g_6) &= 1. \\
R_3(g_2) &= -1. & R_3(g_3) &= -1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. & R_3(g_6) &= 1. \\
R_4(g_2) &= -1. & R_4(g_3) &= 1. & R_4(g_4) &= -1. & R_4(g_5) &= 1. & R_4(g_6) &= 1. \\
R_5(g_2) &= -1. & R_5(g_3) &= 1. & R_5(g_4) &= 1. & R_5(g_5) &= 1. & R_5(g_6) &= 1. \\
R_6(g_2) &= 1. & R_6(g_3) &= -1. & R_6(g_4) &= -1. & R_6(g_5) &= 1. & R_6(g_6) &= 1. \\
R_7(g_2) &= 1. & R_7(g_3) &= -1. & R_7(g_4) &= 1. & R_7(g_5) &= 1. & R_7(g_6) &= 1. \\
R_8(g_2) &= 1. & R_8(g_3) &= 1. & R_8(g_4) &= -1. & R_8(g_5) &= 1. & R_8(g_6) &= 1. \\
R_9(g_2) &= \lambda. & R_9(g_3) &= -i\epsilon. & R_9(g_4) &= i\kappa. & R_9(g_5) &= \epsilon. & R_9(g_6) &= -\epsilon. \\
R_{10}(g_2) &= -\lambda. & R_{10}(g_3) &= i\epsilon. & R_{10}(g_4) &= -\phi. & R_{10}(g_5) &= \epsilon. & R_{10}(g_6) &= -\epsilon. \\
R_{11}(g_2) &= -\lambda. & R_{11}(g_3) &= \phi. & R_{11}(g_4) &= -i\phi. & R_{11}(g_5) &= -\epsilon. & R_{11}(g_6) &= -\epsilon. \\
R_{12}(g_2) &= \lambda. & R_{12}(g_3) &= \phi. & R_{12}(g_4) &= i\phi. & R_{12}(g_5) &= -\epsilon. & R_{12}(g_6) &= -\epsilon. \\
R_{13}(g_2) &= -\lambda. & R_{13}(g_3) &= i\phi. & R_{13}(g_4) &= -i\epsilon. & R_{13}(g_5) &= -\epsilon. & R_{13}(g_6) &= \epsilon. \\
R_{14}(g_2) &= -\lambda. & R_{14}(g_3) &= \kappa. & R_{14}(g_4) &= i\epsilon. & R_{14}(g_5) &= -\epsilon. & R_{14}(g_6) &= \epsilon.
\end{aligned}$$

$G_{32}^{(34)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= -1. & R_2(g_5) &= 1. & R_2(g_6) &= 1. \\
R_3(g_2) &= -1. & R_3(g_3) &= -1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. & R_3(g_6) &= 1. \\
R_4(g_2) &= -1. & R_4(g_3) &= 1. & R_4(g_4) &= -1. & R_4(g_5) &= 1. & R_4(g_6) &= 1. \\
R_5(g_2) &= -1. & R_5(g_3) &= 1. & R_5(g_4) &= 1. & R_5(g_5) &= 1. & R_5(g_6) &= 1. \\
R_6(g_2) &= 1. & R_6(g_3) &= -1. & R_6(g_4) &= -1. & R_6(g_5) &= 1. & R_6(g_6) &= 1. \\
R_7(g_2) &= 1. & R_7(g_3) &= -1. & R_7(g_4) &= 1. & R_7(g_5) &= 1. & R_7(g_6) &= 1. \\
R_8(g_2) &= 1. & R_8(g_3) &= 1. & R_8(g_4) &= -1. & R_8(g_5) &= 1. & R_8(g_6) &= 1. \\
R_9(g_2) &= -\lambda. & R_9(g_3) &= \epsilon. & R_9(g_4) &= \kappa. & R_9(g_5) &= \epsilon. & R_9(g_6) &= -\epsilon. \\
R_{10}(g_2) &= \lambda. & R_{10}(g_3) &= -\epsilon. & R_{10}(g_4) &= -\kappa. & R_{10}(g_5) &= \epsilon. & R_{10}(g_6) &= -\epsilon. \\
R_{11}(g_2) &= -\lambda. & R_{11}(g_3) &= -\kappa. & R_{11}(g_4) &= -\epsilon. & R_{11}(g_5) &= -\epsilon. & R_{11}(g_6) &= \epsilon. \\
R_{12}(g_2) &= -\lambda. & R_{12}(g_3) &= -\kappa. & R_{12}(g_4) &= -\kappa. & R_{12}(g_5) &= -\epsilon. & R_{12}(g_6) &= -\epsilon. \\
R_{13}(g_2) &= \lambda. & R_{13}(g_3) &= -\kappa. & R_{13}(g_4) &= \kappa. & R_{13}(g_5) &= -\epsilon. & R_{13}(g_6) &= -\epsilon. \\
R_{14}(g_2) &= \lambda. & R_{14}(g_3) &= \kappa. & R_{14}(g_4) &= \epsilon. & R_{14}(g_5) &= -\epsilon. & R_{14}(g_6) &= \epsilon.
\end{aligned}$$

 $G_{32}^{(35)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= -1. & R_2(g_5) &= 1. & R_2(g_6) &= 1. \\
R_3(g_2) &= -1. & R_3(g_3) &= -1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. & R_3(g_6) &= 1. \\
R_4(g_2) &= -1. & R_4(g_3) &= 1. & R_4(g_4) &= -1. & R_4(g_5) &= 1. & R_4(g_6) &= 1. \\
R_5(g_2) &= -1. & R_5(g_3) &= 1. & R_5(g_4) &= 1. & R_5(g_5) &= 1. & R_5(g_6) &= 1. \\
R_6(g_2) &= 1. & R_6(g_3) &= -1. & R_6(g_4) &= -1. & R_6(g_5) &= 1. & R_6(g_6) &= 1. \\
R_7(g_2) &= 1. & R_7(g_3) &= -1. & R_7(g_4) &= 1. & R_7(g_5) &= 1. & R_7(g_6) &= 1. \\
R_8(g_2) &= 1. & R_8(g_3) &= 1. & R_8(g_4) &= -1. & R_8(g_5) &= 1. & R_8(g_6) &= 1. \\
R_9(g_2) &= -\lambda. & R_9(g_3) &= \epsilon. & R_9(g_4) &= -\kappa. & R_9(g_5) &= \epsilon. & R_9(g_6) &= -\epsilon. \\
R_{10}(g_2) &= \lambda. & R_{10}(g_3) &= -\epsilon. & R_{10}(g_4) &= -\kappa. & R_{10}(g_5) &= \epsilon. & R_{10}(g_6) &= -\epsilon. \\
R_{11}(g_2) &= i\lambda. & R_{11}(g_3) &= i\phi. & R_{11}(g_4) &= -\epsilon. & R_{11}(g_5) &= -\epsilon. & R_{11}(g_6) &= \epsilon. \\
R_{12}(g_2) &= -i\lambda. & R_{12}(g_3) &= i\phi. & R_{12}(g_4) &= i\phi. & R_{12}(g_5) &= -\epsilon. & R_{12}(g_6) &= -\epsilon. \\
R_{13}(g_2) &= i\lambda. & R_{13}(g_3) &= -\kappa. & R_{13}(g_4) &= \kappa. & R_{13}(g_5) &= -\epsilon. & R_{13}(g_6) &= -\epsilon. \\
R_{14}(g_2) &= -i\lambda. & R_{14}(g_3) &= \kappa. & R_{14}(g_4) &= \epsilon. & R_{14}(g_5) &= -\epsilon. & R_{14}(g_6) &= \epsilon.
\end{aligned}$$

$G_{32}^{(36)}$

$$\begin{aligned}
 R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= -1. & R_2(g_5) &= 1. & R_2(g_6) &= 1. \\
 R_3(g_2) &= -1. & R_3(g_3) &= -1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. & R_3(g_6) &= 1. \\
 R_4(g_2) &= -1. & R_4(g_3) &= 1. & R_4(g_4) &= -1. & R_4(g_5) &= 1. & R_4(g_6) &= 1. \\
 R_5(g_2) &= -1. & R_5(g_3) &= 1. & R_5(g_4) &= 1. & R_5(g_5) &= 1. & R_5(g_6) &= 1. \\
 R_6(g_2) &= 1. & R_6(g_3) &= -1. & R_6(g_4) &= -1. & R_6(g_5) &= 1. & R_6(g_6) &= 1. \\
 R_7(g_2) &= 1. & R_7(g_3) &= -1. & R_7(g_4) &= 1. & R_7(g_5) &= 1. & R_7(g_6) &= 1. \\
 R_8(g_2) &= 1. & R_8(g_3) &= 1. & R_8(g_4) &= -1. & R_8(g_5) &= 1. & R_8(g_6) &= 1. \\
 R_9(g_2) &= -i. & R_9(g_3) &= -1. & R_9(g_4) &= -1. & R_9(g_5) &= -1. & R_9(g_6) &= 1. \\
 R_{10}(g_2) &= i. & R_{10}(g_3) &= -1. & R_{10}(g_4) &= -1. & R_{10}(g_5) &= -1. & R_{10}(g_6) &= 1. \\
 R_{11}(g_2) &= -i. & R_{11}(g_3) &= -1. & R_{11}(g_4) &= 1. & R_{11}(g_5) &= -1. & R_{11}(g_6) &= 1. \\
 R_{12}(g_2) &= i. & R_{12}(g_3) &= -1. & R_{12}(g_4) &= 1. & R_{12}(g_5) &= -1. & R_{12}(g_6) &= 1. \\
 R_{13}(g_2) &= -i. & R_{13}(g_3) &= 1. & R_{13}(g_4) &= -1. & R_{13}(g_5) &= -1. & R_{13}(g_6) &= 1. \\
 R_{14}(g_2) &= i. & R_{14}(g_3) &= 1. & R_{14}(g_4) &= -1. & R_{14}(g_5) &= -1. & R_{14}(g_6) &= 1. \\
 R_{15}(g_2) &= -i. & R_{15}(g_3) &= 1. & R_{15}(g_4) &= 1. & R_{15}(g_5) &= -1. & R_{15}(g_6) &= 1. \\
 R_{16}(g_2) &= i. & R_{16}(g_3) &= 1. & R_{16}(g_4) &= 1. & R_{16}(g_5) &= -1. & R_{16}(g_6) &= 1. \\
 R_{17}(g_2) &= -e_8. & R_{17}(g_3) &= -1. & R_{17}(g_4) &= -1. & R_{17}(g_5) &= i. & R_{17}(g_6) &= -1. \\
 R_{18}(g_2) &= -e_8^3. & R_{18}(g_3) &= -1. & R_{18}(g_4) &= -1. & R_{18}(g_5) &= -i. & R_{18}(g_6) &= -1. \\
 R_{19}(g_2) &= e_8^3. & R_{19}(g_3) &= -1. & R_{19}(g_4) &= -1. & R_{19}(g_5) &= -i. & R_{19}(g_6) &= -1. \\
 R_{20}(g_2) &= e_8. & R_{20}(g_3) &= -1. & R_{20}(g_4) &= -1. & R_{20}(g_5) &= i. & R_{20}(g_6) &= -1. \\
 R_{21}(g_2) &= -e_8. & R_{21}(g_3) &= -1. & R_{21}(g_4) &= 1. & R_{21}(g_5) &= i. & R_{21}(g_6) &= -1. \\
 R_{22}(g_2) &= -e_8^3. & R_{22}(g_3) &= -1. & R_{22}(g_4) &= 1. & R_{22}(g_5) &= -i. & R_{22}(g_6) &= -1. \\
 R_{23}(g_2) &= e_8^3. & R_{23}(g_3) &= -1. & R_{23}(g_4) &= 1. & R_{23}(g_5) &= -i. & R_{23}(g_6) &= -1. \\
 R_{24}(g_2) &= e_8. & R_{24}(g_3) &= -1. & R_{24}(g_4) &= 1. & R_{24}(g_5) &= i. & R_{24}(g_6) &= -1. \\
 R_{25}(g_2) &= -e_8. & R_{25}(g_3) &= 1. & R_{25}(g_4) &= -1. & R_{25}(g_5) &= i. & R_{25}(g_6) &= -1. \\
 R_{26}(g_2) &= -e_8^3. & R_{26}(g_3) &= 1. & R_{26}(g_4) &= -1. & R_{26}(g_5) &= -i. & R_{26}(g_6) &= -1. \\
 R_{27}(g_2) &= e_8^3. & R_{27}(g_3) &= 1. & R_{27}(g_4) &= -1. & R_{27}(g_5) &= -i. & R_{27}(g_6) &= -1. \\
 R_{28}(g_2) &= e_8. & R_{28}(g_3) &= 1. & R_{28}(g_4) &= -1. & R_{28}(g_5) &= i. & R_{28}(g_6) &= -1. \\
 R_{29}(g_2) &= -e_8. & R_{29}(g_3) &= 1. & R_{29}(g_4) &= 1. & R_{29}(g_5) &= i. & R_{29}(g_6) &= -1. \\
 R_{30}(g_2) &= -e_8^3. & R_{30}(g_3) &= 1. & R_{30}(g_4) &= 1. & R_{30}(g_5) &= -i. & R_{30}(g_6) &= -1. \\
 R_{31}(g_2) &= e_8^3. & R_{31}(g_3) &= 1. & R_{31}(g_4) &= 1. & R_{31}(g_5) &= -i. & R_{31}(g_6) &= -1. \\
 R_{32}(g_2) &= e_8. & R_{32}(g_3) &= 1. & R_{32}(g_4) &= 1. & R_{32}(g_5) &= i. & R_{32}(g_6) &= -1.
 \end{aligned}$$

$G_{32}^{(37)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= -1. & R_2(g_5) &= 1. & R_2(g_6) &= 1. \\
R_3(g_2) &= -1. & R_3(g_3) &= -1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. & R_3(g_6) &= 1. \\
R_4(g_2) &= -1. & R_4(g_3) &= 1. & R_4(g_4) &= -1. & R_4(g_5) &= 1. & R_4(g_6) &= 1. \\
R_5(g_2) &= -1. & R_5(g_3) &= 1. & R_5(g_4) &= 1. & R_5(g_5) &= 1. & R_5(g_6) &= 1. \\
R_6(g_2) &= 1. & R_6(g_3) &= -1. & R_6(g_4) &= -1. & R_6(g_5) &= 1. & R_6(g_6) &= 1. \\
R_7(g_2) &= 1. & R_7(g_3) &= -1. & R_7(g_4) &= 1. & R_7(g_5) &= 1. & R_7(g_6) &= 1. \\
R_8(g_2) &= 1. & R_8(g_3) &= 1. & R_8(g_4) &= -1. & R_8(g_5) &= 1. & R_8(g_6) &= 1. \\
R_9(g_2) &= -i. & R_9(g_3) &= -1. & R_9(g_4) &= -1. & R_9(g_5) &= -1. & R_9(g_6) &= 1. \\
R_{10}(g_2) &= i. & R_{10}(g_3) &= -1. & R_{10}(g_4) &= -1. & R_{10}(g_5) &= -1. & R_{10}(g_6) &= 1. \\
R_{11}(g_2) &= -i. & R_{11}(g_3) &= -1. & R_{11}(g_4) &= 1. & R_{11}(g_5) &= -1. & R_{11}(g_6) &= 1. \\
R_{12}(g_2) &= i. & R_{12}(g_3) &= -1. & R_{12}(g_4) &= 1. & R_{12}(g_5) &= -1. & R_{12}(g_6) &= 1. \\
R_{13}(g_2) &= -i. & R_{13}(g_3) &= 1. & R_{13}(g_4) &= -1. & R_{13}(g_5) &= -1. & R_{13}(g_6) &= 1. \\
R_{14}(g_2) &= i. & R_{14}(g_3) &= 1. & R_{14}(g_4) &= -1. & R_{14}(g_5) &= -1. & R_{14}(g_6) &= 1. \\
R_{15}(g_2) &= -i. & R_{15}(g_3) &= 1. & R_{15}(g_4) &= 1. & R_{15}(g_5) &= -1. & R_{15}(g_6) &= 1. \\
R_{16}(g_2) &= i. & R_{16}(g_3) &= 1. & R_{16}(g_4) &= 1. & R_{16}(g_5) &= -1. & R_{16}(g_6) &= 1. \\
R_{17}(g_2) &= \begin{pmatrix} -e_8^3 & 0 \\ 0 & e_8^3 \end{pmatrix}. & R_{17}(g_3) &= \begin{pmatrix} 0 & e_8 \\ -e_8^3 & 0 \end{pmatrix}. & R_{17}(g_4) &= -\epsilon. & R_{17}(g_5) &= -i\epsilon. & R_{17}(g_6) &= -\epsilon. \\
R_{18}(g_2) &= \begin{pmatrix} e_8 & 0 \\ 0 & -e_8 \end{pmatrix}. & R_{18}(g_3) &= \begin{pmatrix} 0 & -e_8 \\ e_8^3 & 0 \end{pmatrix}. & R_{18}(g_4) &= -\epsilon. & R_{18}(g_5) &= i\epsilon. & R_{18}(g_6) &= -\epsilon. \\
R_{19}(g_2) &= \begin{pmatrix} e_8^3 & 0 \\ 0 & -e_8^3 \end{pmatrix}. & R_{19}(g_3) &= -\phi. & R_{19}(g_4) &= \epsilon. & R_{19}(g_5) &= -i\epsilon. & R_{19}(g_6) &= -\epsilon. \\
R_{20}(g_2) &= \begin{pmatrix} -e_8 & 0 \\ 0 & e_8 \end{pmatrix}. & R_{20}(g_3) &= i\kappa. & R_{20}(g_4) &= \epsilon. & R_{20}(g_5) &= i\epsilon. & R_{20}(g_6) &= -\epsilon.
\end{aligned}$$

 $G_{32}^{(38)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= -1. & R_2(g_5) &= 1. & R_2(g_6) &= 1. \\
R_3(g_2) &= -1. & R_3(g_3) &= -1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. & R_3(g_6) &= 1. \\
R_4(g_2) &= -1. & R_4(g_3) &= 1. & R_4(g_4) &= -1. & R_4(g_5) &= 1. & R_4(g_6) &= 1. \\
R_5(g_2) &= -1. & R_5(g_3) &= 1. & R_5(g_4) &= 1. & R_5(g_5) &= 1. & R_5(g_6) &= 1. \\
R_6(g_2) &= 1. & R_6(g_3) &= -1. & R_6(g_4) &= -1. & R_6(g_5) &= 1. & R_6(g_6) &= 1. \\
R_7(g_2) &= 1. & R_7(g_3) &= -1. & R_7(g_4) &= 1. & R_7(g_5) &= 1. & R_7(g_6) &= 1. \\
R_8(g_2) &= 1. & R_8(g_3) &= 1. & R_8(g_4) &= -1. & R_8(g_5) &= 1. & R_8(g_6) &= 1. \\
R_9(g_2) &= -i. & R_9(g_3) &= -1. & R_9(g_4) &= -1. & R_9(g_5) &= -1. & R_9(g_6) &= 1. \\
R_{10}(g_2) &= i. & R_{10}(g_3) &= -1. & R_{10}(g_4) &= -1. & R_{10}(g_5) &= -1. & R_{10}(g_6) &= 1. \\
R_{11}(g_2) &= -i. & R_{11}(g_3) &= -1. & R_{11}(g_4) &= 1. & R_{11}(g_5) &= -1. & R_{11}(g_6) &= 1. \\
R_{12}(g_2) &= i. & R_{12}(g_3) &= -1. & R_{12}(g_4) &= 1. & R_{12}(g_5) &= -1. & R_{12}(g_6) &= 1. \\
R_{13}(g_2) &= -i. & R_{13}(g_3) &= 1. & R_{13}(g_4) &= -1. & R_{13}(g_5) &= -1. & R_{13}(g_6) &= 1. \\
R_{14}(g_2) &= i. & R_{14}(g_3) &= 1. & R_{14}(g_4) &= -1. & R_{14}(g_5) &= -1. & R_{14}(g_6) &= 1. \\
R_{15}(g_2) &= -i. & R_{15}(g_3) &= 1. & R_{15}(g_4) &= 1. & R_{15}(g_5) &= -1. & R_{15}(g_6) &= 1. \\
R_{16}(g_2) &= i. & R_{16}(g_3) &= 1. & R_{16}(g_4) &= 1. & R_{16}(g_5) &= -1. & R_{16}(g_6) &= 1.
\end{aligned}$$

$$R_{17}(g_2) = \begin{pmatrix} -e_8 & 0 \\ 0 & -e_8 \end{pmatrix}. \quad R_{17}(g_3) = \lambda. \quad R_{17}(g_4) = \phi. \quad R_{17}(g_5) = i\epsilon. \quad R_{17}(g_6) = -\epsilon.$$

$$R_{18}(g_2) = \begin{pmatrix} -e_8^3 & 0 \\ 0 & -e_8^3 \end{pmatrix}. \quad R_{18}(g_3) = -\lambda. \quad R_{18}(g_4) = -i\kappa. \quad R_{18}(g_5) = -i\epsilon. \quad R_{18}(g_6) = -\epsilon.$$

$$R_{19}(g_2) = \begin{pmatrix} e_8^3 & 0 \\ 0 & e_8^3 \end{pmatrix}. \quad R_{19}(g_3) = -\lambda. \quad R_{19}(g_4) = -\phi. \quad R_{19}(g_5) = -i\epsilon. \quad R_{19}(g_6) = -\epsilon.$$

$$R_{20}(g_2) = \begin{pmatrix} e_8 & 0 \\ 0 & e_8 \end{pmatrix}. \quad R_{20}(g_3) = -\lambda. \quad R_{20}(g_4) = \begin{pmatrix} 0 & -e_8^3 \\ e_8 & 0 \end{pmatrix}. \quad R_{20}(g_5) = i\epsilon. \quad R_{20}(g_6) = -\epsilon.$$

 $G_{32}^{(39)}$

$$R_2(g_2) = -1. \quad R_2(g_3) = -1. \quad R_2(g_4) = -1. \quad R_2(g_5) = 1. \quad R_2(g_6) = 1.$$

$$R_3(g_2) = -1. \quad R_3(g_3) = -1. \quad R_3(g_4) = 1. \quad R_3(g_5) = 1. \quad R_3(g_6) = 1.$$

$$R_4(g_2) = -1. \quad R_4(g_3) = 1. \quad R_4(g_4) = -1. \quad R_4(g_5) = 1. \quad R_4(g_6) = 1.$$

$$R_5(g_2) = -1. \quad R_5(g_3) = 1. \quad R_5(g_4) = 1. \quad R_5(g_5) = 1. \quad R_5(g_6) = 1.$$

$$R_6(g_2) = 1. \quad R_6(g_3) = -1. \quad R_6(g_4) = -1. \quad R_6(g_5) = 1. \quad R_6(g_6) = 1.$$

$$R_7(g_2) = 1. \quad R_7(g_3) = -1. \quad R_7(g_4) = 1. \quad R_7(g_5) = 1. \quad R_7(g_6) = 1.$$

$$R_8(g_2) = 1. \quad R_8(g_3) = 1. \quad R_8(g_4) = -1. \quad R_8(g_5) = 1. \quad R_8(g_6) = 1.$$

$$R_9(g_2) = \lambda. \quad R_9(g_3) = \phi. \quad R_9(g_4) = -\epsilon. \quad R_9(g_5) = -\epsilon. \quad R_9(g_6) = \epsilon.$$

$$R_{10}(g_2) = \lambda. \quad R_{10}(g_3) = -\phi. \quad R_{10}(g_4) = \epsilon. \quad R_{10}(g_5) = -\epsilon. \quad R_{10}(g_6) = \epsilon.$$

$$R_{11}(g_2) = \begin{pmatrix} 1 & 0 \\ -\sqrt{2}i & -1 \end{pmatrix}. \quad R_{11}(g_3) = \phi. \quad R_{11}(g_4) = -\epsilon. \quad R_{11}(g_5) = \begin{pmatrix} 1 & \sqrt{2} \\ -\sqrt{2}i & -1 \end{pmatrix}. \quad R_{11}(g_6) = -\epsilon.$$

$$R_{12}(g_2) = \begin{pmatrix} -1 & -\sqrt{2}i \\ 0 & 1 \end{pmatrix}. \quad R_{12}(g_3) = -\phi. \quad R_{12}(g_4) = -\epsilon. \quad R_{12}(g_5) = \begin{pmatrix} -1 & -\sqrt{2}i \\ \sqrt{2} & 1 \end{pmatrix}. \quad R_{12}(g_6) = -\epsilon.$$

$$R_{13}(g_2) = \begin{pmatrix} -1 & -\sqrt{2}i \\ 0 & 1 \end{pmatrix}. \quad R_{13}(g_3) = \begin{pmatrix} \sqrt{2} & 1 \\ -1 & -\sqrt{2}i \end{pmatrix}. \quad R_{13}(g_4) = \epsilon.$$

$$R_{13}(g_5) = \begin{pmatrix} 1 & \sqrt{2} \\ -\sqrt{2}i & -1 \end{pmatrix}. \quad R_{13}(g_6) = -\epsilon.$$

$$R_{14}(g_2) = \begin{pmatrix} 1 & 0 \\ \sqrt{2} & -1 \end{pmatrix}. \quad R_{14}(g_3) = \begin{pmatrix} \sqrt{2} & -1 \\ 1 & -\sqrt{2}i \end{pmatrix}. \quad R_{14}(g_4) = \epsilon.$$

$$R_{14}(g_5) = \begin{pmatrix} -1 & \sqrt{2} \\ -\sqrt{2}i & 1 \end{pmatrix}. \quad R_{14}(g_6) = -\epsilon.$$

 $G_{32}^{(40)}$

$$R_2(g_2) = -1. \quad R_2(g_3) = -1. \quad R_2(g_4) = -1. \quad R_2(g_5) = 1. \quad R_2(g_6) = 1.$$

$$R_3(g_2) = -1. \quad R_3(g_3) = -1. \quad R_3(g_4) = 1. \quad R_3(g_5) = 1. \quad R_3(g_6) = 1.$$

$$R_4(g_2) = -1. \quad R_4(g_3) = 1. \quad R_4(g_4) = -1. \quad R_4(g_5) = 1. \quad R_4(g_6) = 1.$$

$$R_5(g_2) = -1. \quad R_5(g_3) = 1. \quad R_5(g_4) = 1. \quad R_5(g_5) = 1. \quad R_5(g_6) = 1.$$

$$R_6(g_2) = 1. \quad R_6(g_3) = -1. \quad R_6(g_4) = -1. \quad R_6(g_5) = 1. \quad R_6(g_6) = 1.$$

$$R_7(g_2) = 1. \quad R_7(g_3) = -1. \quad R_7(g_4) = 1. \quad R_7(g_5) = 1. \quad R_7(g_6) = 1.$$

$$R_8(g_2) = 1. \quad R_8(g_3) = 1. \quad R_8(g_4) = -1. \quad R_8(g_5) = 1. \quad R_8(g_6) = 1.$$

$$R_9(g_2) = -\lambda. \quad R_9(g_3) = -\phi. \quad R_9(g_4) = -\epsilon. \quad R_9(g_5) = -\epsilon. \quad R_9(g_6) = \epsilon.$$

$$R_{10}(g_2) = \lambda. \quad R_{10}(g_3) = -\phi. \quad R_{10}(g_4) = \epsilon. \quad R_{10}(g_5) = -\epsilon. \quad R_{10}(g_6) = \epsilon.$$

$$R_{11}(g_2) = \begin{pmatrix} i & 0 \\ \sqrt{2} & -i \end{pmatrix}. \quad R_{11}(g_3) = \begin{pmatrix} -\sqrt{2}i & i \\ i & \sqrt{2} \end{pmatrix}. \quad R_{11}(g_4) = -\epsilon.$$

$$R_{11}(g_5) = \begin{pmatrix} -1 & \sqrt{2}i \\ \sqrt{2}i & 1 \end{pmatrix}. \quad R_{11}(g_6) = -\epsilon.$$

$$R_{12}(g_2) = -i\lambda. \quad R_{12}(g_3) = \begin{pmatrix} -1/\sqrt{2} & -1/\sqrt{2} \\ -1/\sqrt{2} & 1/\sqrt{2} \end{pmatrix}. \quad R_{12}(g_4) = -\epsilon. \quad R_{12}(g_5) = -\kappa. \quad R_{12}(g_6) = -\epsilon.$$

$$R_{13}(g_2) = -i\phi. \quad R_{13}(g_3) = \begin{pmatrix} -1/\sqrt{2} & 1/\sqrt{2} \\ 1/\sqrt{2} & 1/\sqrt{2} \end{pmatrix}. \quad R_{13}(g_4) = \epsilon. \quad R_{13}(g_5) = -\kappa. \quad R_{13}(g_6) = -\epsilon.$$

$$R_{14}(g_2) = \begin{pmatrix} -i & 0 \\ -\sqrt{2}i & i \end{pmatrix}. \quad R_{14}(g_3) = \begin{pmatrix} -\sqrt{2}i & i \\ i & \sqrt{2} \end{pmatrix}. \quad R_{14}(g_4) = \epsilon.$$

$$R_{14}(g_5) = \begin{pmatrix} -1 & \sqrt{2}i \\ \sqrt{2}i & 1 \end{pmatrix}. \quad R_{14}(g_6) = -\epsilon.$$

 $G_{32}^{(41)}$

$$R_2(g_2) = -1. \quad R_2(g_3) = -1. \quad R_2(g_4) = -1. \quad R_2(g_5) = 1. \quad R_2(g_6) = 1.$$

$$R_3(g_2) = -1. \quad R_3(g_3) = -1. \quad R_3(g_4) = 1. \quad R_3(g_5) = 1. \quad R_3(g_6) = 1.$$

$$R_4(g_2) = -1. \quad R_4(g_3) = 1. \quad R_4(g_4) = -1. \quad R_4(g_5) = 1. \quad R_4(g_6) = 1.$$

$$R_5(g_2) = -1. \quad R_5(g_3) = 1. \quad R_5(g_4) = 1. \quad R_5(g_5) = 1. \quad R_5(g_6) = 1.$$

$$R_6(g_2) = 1. \quad R_6(g_3) = -1. \quad R_6(g_4) = -1. \quad R_6(g_5) = 1. \quad R_6(g_6) = 1.$$

$$R_7(g_2) = 1. \quad R_7(g_3) = -1. \quad R_7(g_4) = 1. \quad R_7(g_5) = 1. \quad R_7(g_6) = 1.$$

$$R_8(g_2) = 1. \quad R_8(g_3) = 1. \quad R_8(g_4) = -1. \quad R_8(g_5) = 1. \quad R_8(g_6) = 1.$$

$$R_9(g_2) = \lambda. \quad R_9(g_3) = \phi. \quad R_9(g_4) = -\epsilon. \quad R_9(g_5) = -\epsilon. \quad R_9(g_6) = \epsilon.$$

$$R_{10}(g_2) = -\lambda. \quad R_{10}(g_3) = -\phi. \quad R_{10}(g_4) = \epsilon. \quad R_{10}(g_5) = -\epsilon. \quad R_{10}(g_6) = \epsilon.$$

$$R_{11}(g_2) = \begin{pmatrix} -i & \sqrt{2}i \\ 0 & i \end{pmatrix}. \quad R_{11}(g_3) = \begin{pmatrix} -\sqrt{2}i & i \\ -i & \sqrt{2}i \end{pmatrix}. \quad R_{11}(g_4) = -\epsilon.$$

$$R_{11}(g_5) = \begin{pmatrix} 1 & -\sqrt{2}i \\ \sqrt{2} & -1 \end{pmatrix}. \quad R_{11}(g_6) = -\epsilon.$$

$$R_{12}(g_2) = \begin{pmatrix} i & 0 \\ -\sqrt{2}i & -i \end{pmatrix}. \quad R_{12}(g_3) = \begin{pmatrix} -\sqrt{2}i & -i \\ i & \sqrt{2}i \end{pmatrix}. \quad R_{12}(g_4) = -\epsilon.$$

$$R_{12}(g_5) = \begin{pmatrix} -1 & -\sqrt{2}i \\ \sqrt{2} & 1 \end{pmatrix}. \quad R_{12}(g_6) = -\epsilon.$$

$$R_{13}(g_2) = \begin{pmatrix} -i & -\sqrt{2}i \\ 0 & i \end{pmatrix}. \quad R_{13}(g_3) = \begin{pmatrix} -\sqrt{2}i & -i \\ i & \sqrt{2}i \end{pmatrix}. \quad R_{13}(g_4) = \epsilon.$$

$$R_{13}(g_5) = \begin{pmatrix} 1 & \sqrt{2} \\ -\sqrt{2}i & -1 \end{pmatrix}. \quad R_{13}(g_6) = -\epsilon.$$

$$\begin{aligned}
 R_{14}(g_2) &= \begin{pmatrix} -i & 0 \\ -\sqrt{2}i & i \end{pmatrix}. & R_{14}(g_3) &= \begin{pmatrix} \sqrt{2}i & -i \\ i & -\sqrt{2}i \end{pmatrix}. & R_{14}(g_4) &= \epsilon. \\
 R_{14}(g_5) &= \begin{pmatrix} -1 & \sqrt{2} \\ -\sqrt{2}i & 1 \end{pmatrix}. & R_{14}(g_6) &= -\epsilon.
 \end{aligned}$$

 $G_{32}^{(42)}$

$$\begin{aligned}
 R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= -1. & R_2(g_5) &= 1. & R_2(g_6) &= 1. \\
 R_3(g_2) &= -1. & R_3(g_3) &= -1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. & R_3(g_6) &= 1. \\
 R_4(g_2) &= -1. & R_4(g_3) &= 1. & R_4(g_4) &= -1. & R_4(g_5) &= 1. & R_4(g_6) &= 1. \\
 R_5(g_2) &= -1. & R_5(g_3) &= 1. & R_5(g_4) &= 1. & R_5(g_5) &= 1. & R_5(g_6) &= 1. \\
 R_6(g_2) &= 1. & R_6(g_3) &= -1. & R_6(g_4) &= -1. & R_6(g_5) &= 1. & R_6(g_6) &= 1. \\
 R_7(g_2) &= 1. & R_7(g_3) &= -1. & R_7(g_4) &= 1. & R_7(g_5) &= 1. & R_7(g_6) &= 1. \\
 R_8(g_2) &= 1. & R_8(g_3) &= 1. & R_8(g_4) &= -1. & R_8(g_5) &= 1. & R_8(g_6) &= 1. \\
 R_9(g_2) &= \lambda. & R_9(g_3) &= \phi. & R_9(g_4) &= -\epsilon. & R_9(g_5) &= -\epsilon. & R_9(g_6) &= \epsilon. \\
 R_{10}(g_2) &= -\lambda. & R_{10}(g_3) &= -\phi. & R_{10}(g_4) &= \epsilon. & R_{10}(g_5) &= -\epsilon. & R_{10}(g_6) &= \epsilon. \\
 R_{11}(g_2) &= \lambda. & R_{11}(g_3) &= \begin{pmatrix} -1/\sqrt{2} & -1/\sqrt{2} \\ i/\sqrt{2} & 1/\sqrt{2} \end{pmatrix}. & R_{11}(g_4) &= -i\epsilon. & R_{11}(g_5) &= -i\phi. & R_{11}(g_6) &= -\epsilon. \\
 R_{12}(g_2) &= \lambda. & R_{12}(g_3) &= \begin{pmatrix} 1/\sqrt{2} & -1/\sqrt{2} \\ i/\sqrt{2} & -1/\sqrt{2} \end{pmatrix}. & R_{12}(g_4) &= -i\epsilon. & R_{12}(g_5) &= i\phi. & R_{12}(g_6) &= -\epsilon. \\
 R_{13}(g_2) &= \begin{pmatrix} 1 & \sqrt{2}i \\ 0 & -1 \end{pmatrix}. & R_{13}(g_3) &= \begin{pmatrix} -\sqrt{2}i & -i \\ -i & \sqrt{2} \end{pmatrix}. & R_{13}(g_4) &= i\epsilon. \\
 R_{13}(g_5) &= \begin{pmatrix} 1 & \sqrt{2}i \\ \sqrt{2}i & -1 \end{pmatrix}. & R_{13}(g_6) &= -\epsilon. \\
 R_{14}(g_2) &= -\lambda. & R_{14}(g_3) &= \begin{pmatrix} -1/\sqrt{2} & -1/\sqrt{2} \\ i/\sqrt{2} & 1/\sqrt{2} \end{pmatrix}. & R_{14}(g_4) &= i\epsilon. & R_{14}(g_5) &= -i\phi. & R_{14}(g_6) &= -\epsilon.
 \end{aligned}$$

 $G_{32}^{(43)}$

$$\begin{aligned}
 R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= -1. & R_2(g_5) &= 1. & R_2(g_6) &= 1. \\
 R_3(g_2) &= -1. & R_3(g_3) &= -1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. & R_3(g_6) &= 1. \\
 R_4(g_2) &= -1. & R_4(g_3) &= 1. & R_4(g_4) &= -1. & R_4(g_5) &= 1. & R_4(g_6) &= 1. \\
 R_5(g_2) &= -1. & R_5(g_3) &= 1. & R_5(g_4) &= 1. & R_5(g_5) &= 1. & R_5(g_6) &= 1. \\
 R_6(g_2) &= 1. & R_6(g_3) &= -1. & R_6(g_4) &= -1. & R_6(g_5) &= 1. & R_6(g_6) &= 1. \\
 R_7(g_2) &= 1. & R_7(g_3) &= -1. & R_7(g_4) &= 1. & R_7(g_5) &= 1. & R_7(g_6) &= 1. \\
 R_8(g_2) &= 1. & R_8(g_3) &= 1. & R_8(g_4) &= -1. & R_8(g_5) &= 1. & R_8(g_6) &= 1. \\
 R_9(g_2) &= \lambda. & R_9(g_3) &= \phi. & R_9(g_4) &= \epsilon. & R_9(g_5) &= -\epsilon. & R_9(g_6) &= \epsilon. \\
 R_{10}(g_2) &= \lambda. & R_{10}(g_3) &= \phi. & R_{10}(g_4) &= -\epsilon. & R_{10}(g_5) &= -\epsilon. & R_{10}(g_6) &= \epsilon.
 \end{aligned}$$

$$\begin{aligned}
R_{11}(g_2) &= \begin{pmatrix} 0 & e_8 & 0 & 0 \\ -e_8^3 & 0 & 0 & 0 \\ 0 & 0 & 0 & e_8^3 \\ 0 & 0 & -e_8 & 0 \end{pmatrix}, & R_{11}(g_3) &= \begin{pmatrix} 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & -i \\ 0 & 0 & i & 0 \end{pmatrix}. \\
R_{11}(g_4) &= \begin{pmatrix} 0 & 0 & -i & 0 \\ 0 & 0 & 0 & -1 \\ i & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \end{pmatrix}, & R_{11}(g_5) &= \begin{pmatrix} -i & 0 & 0 & 0 \\ 0 & i & 0 & 0 \\ 0 & 0 & -i & 0 \\ 0 & 0 & 0 & i \end{pmatrix}. \\
& & R_{11}(g_6) &= \begin{pmatrix} -1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & -1 \end{pmatrix}.
\end{aligned}$$

 $G_{32}^{(44)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= -1. & R_2(g_5) &= 1. & R_2(g_6) &= 1. \\
R_3(g_2) &= -1. & R_3(g_3) &= -1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. & R_3(g_6) &= 1. \\
R_4(g_2) &= -1. & R_4(g_3) &= 1. & R_4(g_4) &= -1. & R_4(g_5) &= 1. & R_4(g_6) &= 1. \\
R_5(g_2) &= -1. & R_5(g_3) &= 1. & R_5(g_4) &= 1. & R_5(g_5) &= 1. & R_5(g_6) &= 1. \\
R_6(g_2) &= 1. & R_6(g_3) &= -1. & R_6(g_4) &= -1. & R_6(g_5) &= 1. & R_6(g_6) &= 1. \\
R_7(g_2) &= 1. & R_7(g_3) &= -1. & R_7(g_4) &= 1. & R_7(g_5) &= 1. & R_7(g_6) &= 1. \\
R_8(g_2) &= 1. & R_8(g_3) &= 1. & R_8(g_4) &= -1. & R_8(g_5) &= 1. & R_8(g_6) &= 1. \\
R_9(g_2) &= \lambda. & R_9(g_3) &= \phi. & R_9(g_4) &= \epsilon. & R_9(g_5) &= -\epsilon. & R_9(g_6) &= \epsilon. \\
R_{10}(g_2) &= \lambda. & R_{10}(g_3) &= -\phi. & R_{10}(g_4) &= -\epsilon. & R_{10}(g_5) &= -\epsilon. & R_{10}(g_6) &= \epsilon.
\end{aligned}$$

$$\begin{aligned}
R_{11}(g_2) &= \begin{pmatrix} 0 & 0 & 0 & -e_8 \\ 0 & 0 & i & 0 \\ 0 & -i & 0 & 0 \\ e_8^3 & 0 & 0 & 0 \end{pmatrix}, & R_{11}(g_3) &= \begin{pmatrix} 0 & 0 & 0 & 1 \\ 0 & 0 & -e_8^3 & 0 \\ 0 & -e_8 & 0 & 0 \\ -1 & 0 & 0 & 0 \end{pmatrix}. \\
R_{11}(g_4) &= \begin{pmatrix} 0 & 0 & -e_8^3 & 0 \\ 0 & 0 & 0 & -1 \\ e_8 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \end{pmatrix}, & R_{11}(g_5) &= \begin{pmatrix} i & 0 & 0 & 0 \\ 0 & -i & 0 & 0 \\ 0 & 0 & i & 0 \\ 0 & 0 & 0 & -i \end{pmatrix}. \\
& & R_{11}(g_6) &= \begin{pmatrix} -1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & -1 \end{pmatrix}.
\end{aligned}$$

 $G_{32}^{(45)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= -1. & R_2(g_5) &= -1. & R_2(g_6) &= 1. \\
R_3(g_2) &= -1. & R_3(g_3) &= -1. & R_3(g_4) &= -1. & R_3(g_5) &= 1. & R_3(g_6) &= 1. \\
R_4(g_2) &= -1. & R_4(g_3) &= -1. & R_4(g_4) &= 1. & R_4(g_5) &= -1. & R_4(g_6) &= 1. \\
R_5(g_2) &= -1. & R_5(g_3) &= -1. & R_5(g_4) &= 1. & R_5(g_5) &= 1. & R_5(g_6) &= 1. \\
R_6(g_2) &= -1. & R_6(g_3) &= 1. & R_6(g_4) &= -1. & R_6(g_5) &= -1. & R_6(g_6) &= 1. \\
R_7(g_2) &= -1. & R_7(g_3) &= 1. & R_7(g_4) &= -1. & R_7(g_5) &= 1. & R_7(g_6) &= 1.
\end{aligned}$$

$$\begin{aligned}
 R_8(g_2) &= -1. & R_8(g_3) &= 1. & R_8(g_4) &= 1. & R_8(g_5) &= -1. & R_8(g_6) &= 1. \\
 R_9(g_2) &= -1. & R_9(g_3) &= 1. & R_9(g_4) &= 1. & R_9(g_5) &= 1. & R_9(g_6) &= 1. \\
 R_{10}(g_2) &= 1. & R_{10}(g_3) &= -1. & R_{10}(g_4) &= -1. & R_{10}(g_5) &= -1. & R_{10}(g_6) &= 1. \\
 R_{11}(g_2) &= 1. & R_{11}(g_3) &= -1. & R_{11}(g_4) &= -1. & R_{11}(g_5) &= 1. & R_{11}(g_6) &= 1. \\
 R_{12}(g_2) &= 1. & R_{12}(g_3) &= -1. & R_{12}(g_4) &= 1. & R_{12}(g_5) &= -1. & R_{12}(g_6) &= 1. \\
 R_{13}(g_2) &= 1. & R_{13}(g_3) &= -1. & R_{13}(g_4) &= 1. & R_{13}(g_5) &= 1. & R_{13}(g_6) &= 1. \\
 R_{14}(g_2) &= 1. & R_{14}(g_3) &= 1. & R_{14}(g_4) &= -1. & R_{14}(g_5) &= -1. & R_{14}(g_6) &= 1. \\
 R_{15}(g_2) &= 1. & R_{15}(g_3) &= 1. & R_{15}(g_4) &= -1. & R_{15}(g_5) &= 1. & R_{15}(g_6) &= 1. \\
 R_{16}(g_2) &= 1. & R_{16}(g_3) &= 1. & R_{16}(g_4) &= 1. & R_{16}(g_5) &= -1. & R_{16}(g_6) &= 1. \\
 R_{17}(g_2) &= -i. & R_{17}(g_3) &= -1. & R_{17}(g_4) &= -1. & R_{17}(g_5) &= -1. & R_{17}(g_6) &= -1. \\
 R_{18}(g_2) &= i. & R_{18}(g_3) &= -1. & R_{18}(g_4) &= -1. & R_{18}(g_5) &= -1. & R_{18}(g_6) &= -1. \\
 R_{19}(g_2) &= -i. & R_{19}(g_3) &= -1. & R_{19}(g_4) &= -1. & R_{19}(g_5) &= 1. & R_{19}(g_6) &= -1. \\
 R_{20}(g_2) &= i. & R_{20}(g_3) &= -1. & R_{20}(g_4) &= -1. & R_{20}(g_5) &= 1. & R_{20}(g_6) &= -1. \\
 R_{21}(g_2) &= -i. & R_{21}(g_3) &= -1. & R_{21}(g_4) &= 1. & R_{21}(g_5) &= -1. & R_{21}(g_6) &= -1. \\
 R_{22}(g_2) &= i. & R_{22}(g_3) &= -1. & R_{22}(g_4) &= 1. & R_{22}(g_5) &= -1. & R_{22}(g_6) &= -1. \\
 R_{23}(g_2) &= -i. & R_{23}(g_3) &= -1. & R_{23}(g_4) &= 1. & R_{23}(g_5) &= 1. & R_{23}(g_6) &= -1. \\
 R_{24}(g_2) &= i. & R_{24}(g_3) &= -1. & R_{24}(g_4) &= 1. & R_{24}(g_5) &= 1. & R_{24}(g_6) &= -1. \\
 R_{25}(g_2) &= -i. & R_{25}(g_3) &= 1. & R_{25}(g_4) &= -1. & R_{25}(g_5) &= -1. & R_{25}(g_6) &= -1. \\
 R_{26}(g_2) &= i. & R_{26}(g_3) &= 1. & R_{26}(g_4) &= -1. & R_{26}(g_5) &= -1. & R_{26}(g_6) &= -1. \\
 R_{27}(g_2) &= -i. & R_{27}(g_3) &= 1. & R_{27}(g_4) &= -1. & R_{27}(g_5) &= 1. & R_{27}(g_6) &= -1. \\
 R_{28}(g_2) &= i. & R_{28}(g_3) &= 1. & R_{28}(g_4) &= -1. & R_{28}(g_5) &= 1. & R_{28}(g_6) &= -1. \\
 R_{29}(g_2) &= -i. & R_{29}(g_3) &= 1. & R_{29}(g_4) &= 1. & R_{29}(g_5) &= -1. & R_{29}(g_6) &= -1. \\
 R_{30}(g_2) &= i. & R_{30}(g_3) &= 1. & R_{30}(g_4) &= 1. & R_{30}(g_5) &= -1. & R_{30}(g_6) &= -1. \\
 R_{31}(g_2) &= -i. & R_{31}(g_3) &= 1. & R_{31}(g_4) &= 1. & R_{31}(g_5) &= 1. & R_{31}(g_6) &= -1. \\
 R_{32}(g_2) &= i. & R_{32}(g_3) &= 1. & R_{32}(g_4) &= 1. & R_{32}(g_5) &= 1. & R_{32}(g_6) &= -1.
 \end{aligned}$$

 $G_{32}^{(46)}$

$$\begin{aligned}
 R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= -1. & R_2(g_5) &= -1. & R_2(g_6) &= 1. \\
 R_3(g_2) &= -1. & R_3(g_3) &= -1. & R_3(g_4) &= -1. & R_3(g_5) &= 1. & R_3(g_6) &= 1. \\
 R_4(g_2) &= -1. & R_4(g_3) &= -1. & R_4(g_4) &= 1. & R_4(g_5) &= -1. & R_4(g_6) &= 1. \\
 R_5(g_2) &= -1. & R_5(g_3) &= -1. & R_5(g_4) &= 1. & R_5(g_5) &= 1. & R_5(g_6) &= 1. \\
 R_6(g_2) &= -1. & R_6(g_3) &= 1. & R_6(g_4) &= -1. & R_6(g_5) &= -1. & R_6(g_6) &= 1. \\
 R_7(g_2) &= -1. & R_7(g_3) &= 1. & R_7(g_4) &= -1. & R_7(g_5) &= 1. & R_7(g_6) &= 1. \\
 R_8(g_2) &= -1. & R_8(g_3) &= 1. & R_8(g_4) &= 1. & R_8(g_5) &= -1. & R_8(g_6) &= 1. \\
 R_9(g_2) &= -1. & R_9(g_3) &= 1. & R_9(g_4) &= 1. & R_9(g_5) &= 1. & R_9(g_6) &= 1. \\
 R_{10}(g_2) &= 1. & R_{10}(g_3) &= -1. & R_{10}(g_4) &= -1. & R_{10}(g_5) &= -1. & R_{10}(g_6) &= 1. \\
 R_{11}(g_2) &= 1. & R_{11}(g_3) &= -1. & R_{11}(g_4) &= -1. & R_{11}(g_5) &= 1. & R_{11}(g_6) &= 1. \\
 R_{12}(g_2) &= 1. & R_{12}(g_3) &= -1. & R_{12}(g_4) &= 1. & R_{12}(g_5) &= -1. & R_{12}(g_6) &= 1. \\
 R_{13}(g_2) &= 1. & R_{13}(g_3) &= -1. & R_{13}(g_4) &= 1. & R_{13}(g_5) &= 1. & R_{13}(g_6) &= 1. \\
 R_{14}(g_2) &= 1. & R_{14}(g_3) &= 1. & R_{14}(g_4) &= -1. & R_{14}(g_5) &= -1. & R_{14}(g_6) &= 1. \\
 R_{15}(g_2) &= 1. & R_{15}(g_3) &= 1. & R_{15}(g_4) &= -1. & R_{15}(g_5) &= 1. & R_{15}(g_6) &= 1.
 \end{aligned}$$

$$\begin{aligned}
 R_{15}(g_2) &= 1. & R_{15}(g_3) &= 1. & R_{15}(g_4) &= -1. & R_{15}(g_5) &= 1. & R_{15}(g_6) &= 1. \\
 R_{16}(g_2) &= 1. & R_{16}(g_3) &= 1. & R_{16}(g_4) &= 1. & R_{16}(g_5) &= -1. & R_{16}(g_6) &= 1. \\
 R_{17}(g_2) &= -\lambda. & R_{17}(g_3) &= -i\kappa. & R_{17}(g_4) &= -i\epsilon. & R_{17}(g_5) &= -\epsilon. & R_{17}(g_6) &= -\epsilon. \\
 R_{18}(g_2) &= \lambda. & R_{18}(g_3) &= \phi. & R_{18}(g_4) &= i\epsilon. & R_{18}(g_5) &= -\epsilon. & R_{18}(g_6) &= -\epsilon. \\
 R_{19}(g_2) &= -\lambda. & R_{19}(g_3) &= -\phi. & R_{19}(g_4) &= -i\epsilon. & R_{19}(g_5) &= \epsilon. & R_{19}(g_6) &= -\epsilon. \\
 R_{20}(g_2) &= -\lambda. & R_{20}(g_3) &= -i\kappa. & R_{20}(g_4) &= i\epsilon. & R_{20}(g_5) &= \epsilon. & R_{20}(g_6) &= -\epsilon.
 \end{aligned}$$

 $G_{32}^{(49)}$

$$\begin{aligned}
 R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= -1. & R_2(g_5) &= -1. & R_2(g_6) &= 1. \\
 R_3(g_2) &= -1. & R_3(g_3) &= -1. & R_3(g_4) &= -1. & R_3(g_5) &= 1. & R_3(g_6) &= 1. \\
 R_4(g_2) &= -1. & R_4(g_3) &= -1. & R_4(g_4) &= 1. & R_4(g_5) &= -1. & R_4(g_6) &= 1. \\
 R_5(g_2) &= -1. & R_5(g_3) &= -1. & R_5(g_4) &= 1. & R_5(g_5) &= 1. & R_5(g_6) &= 1. \\
 R_6(g_2) &= -1. & R_6(g_3) &= 1. & R_6(g_4) &= -1. & R_6(g_5) &= -1. & R_6(g_6) &= 1. \\
 R_7(g_2) &= -1. & R_7(g_3) &= 1. & R_7(g_4) &= -1. & R_7(g_5) &= 1. & R_7(g_6) &= 1. \\
 R_8(g_2) &= -1. & R_8(g_3) &= 1. & R_8(g_4) &= 1. & R_8(g_5) &= -1. & R_8(g_6) &= 1. \\
 R_9(g_2) &= -1. & R_9(g_3) &= 1. & R_9(g_4) &= 1. & R_9(g_5) &= 1. & R_9(g_6) &= 1. \\
 R_{10}(g_2) &= 1. & R_{10}(g_3) &= -1. & R_{10}(g_4) &= -1. & R_{10}(g_5) &= -1. & R_{10}(g_6) &= 1. \\
 R_{11}(g_2) &= 1. & R_{11}(g_3) &= -1. & R_{11}(g_4) &= -1. & R_{11}(g_5) &= 1. & R_{11}(g_6) &= 1. \\
 R_{12}(g_2) &= 1. & R_{12}(g_3) &= -1. & R_{12}(g_4) &= 1. & R_{12}(g_5) &= -1. & R_{12}(g_6) &= 1. \\
 R_{13}(g_2) &= 1. & R_{13}(g_3) &= -1. & R_{13}(g_4) &= 1. & R_{13}(g_5) &= 1. & R_{13}(g_6) &= 1. \\
 R_{14}(g_2) &= 1. & R_{14}(g_3) &= 1. & R_{14}(g_4) &= -1. & R_{14}(g_5) &= -1. & R_{14}(g_6) &= 1. \\
 R_{15}(g_2) &= 1. & R_{15}(g_3) &= 1. & R_{15}(g_4) &= -1. & R_{15}(g_5) &= 1. & R_{15}(g_6) &= 1. \\
 R_{16}(g_2) &= 1. & R_{16}(g_3) &= 1. & R_{16}(g_4) &= 1. & R_{16}(g_5) &= -1. & R_{16}(g_6) &= 1.
 \end{aligned}$$

$$\begin{aligned}
 R_{17}(g_2) &= \begin{pmatrix} 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & -1 \\ -1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \end{pmatrix}. & R_{17}(g_3) &= \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & -1 \end{pmatrix}. \\
 R_{17}(g_4) &= \begin{pmatrix} 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & -1 \\ 1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \end{pmatrix}. & R_{17}(g_5) &= \begin{pmatrix} 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & -1 \\ 0 & 0 & -1 & 0 \end{pmatrix}. \\
 & & R_{17}(g_6) &= \begin{pmatrix} -1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & -1 \end{pmatrix}.
 \end{aligned}$$

$G_{32}^{(50)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= -1. & R_2(g_5) &= -1. & R_2(g_6) &= 1. \\
R_3(g_2) &= -1. & R_3(g_3) &= -1. & R_3(g_4) &= -1. & R_3(g_5) &= 1. & R_3(g_6) &= 1. \\
R_4(g_2) &= -1. & R_4(g_3) &= -1. & R_4(g_4) &= 1. & R_4(g_5) &= -1. & R_4(g_6) &= 1. \\
R_5(g_2) &= -1. & R_5(g_3) &= -1. & R_5(g_4) &= 1. & R_5(g_5) &= 1. & R_5(g_6) &= 1. \\
R_6(g_2) &= -1. & R_6(g_3) &= 1. & R_6(g_4) &= -1. & R_6(g_5) &= -1. & R_6(g_6) &= 1. \\
R_7(g_2) &= -1. & R_7(g_3) &= 1. & R_7(g_4) &= -1. & R_7(g_5) &= 1. & R_7(g_6) &= 1. \\
R_8(g_2) &= -1. & R_8(g_3) &= 1. & R_8(g_4) &= 1. & R_8(g_5) &= -1. & R_8(g_6) &= 1. \\
R_9(g_2) &= -1. & R_9(g_3) &= 1. & R_9(g_4) &= 1. & R_9(g_5) &= 1. & R_9(g_6) &= 1. \\
R_{10}(g_2) &= 1. & R_{10}(g_3) &= -1. & R_{10}(g_4) &= -1. & R_{10}(g_5) &= -1. & R_{10}(g_6) &= 1. \\
R_{11}(g_2) &= 1. & R_{11}(g_3) &= -1. & R_{11}(g_4) &= -1. & R_{11}(g_5) &= 1. & R_{11}(g_6) &= 1. \\
R_{12}(g_2) &= 1. & R_{12}(g_3) &= -1. & R_{12}(g_4) &= 1. & R_{12}(g_5) &= -1. & R_{12}(g_6) &= 1. \\
R_{13}(g_2) &= 1. & R_{13}(g_3) &= -1. & R_{13}(g_4) &= 1. & R_{13}(g_5) &= 1. & R_{13}(g_6) &= 1. \\
R_{14}(g_2) &= 1. & R_{14}(g_3) &= 1. & R_{14}(g_4) &= -1. & R_{14}(g_5) &= -1. & R_{14}(g_6) &= 1. \\
R_{15}(g_2) &= 1. & R_{15}(g_3) &= 1. & R_{15}(g_4) &= -1. & R_{15}(g_5) &= 1. & R_{15}(g_6) &= 1. \\
R_{16}(g_2) &= 1. & R_{16}(g_3) &= 1. & R_{16}(g_4) &= 1. & R_{16}(g_5) &= -1. & R_{16}(g_6) &= 1.
\end{aligned}$$

$$\begin{aligned}
R_{17}(g_2) &= \begin{pmatrix} 0 & 0 & 0 & -i \\ 0 & 0 & i & 0 \\ 0 & -i & 0 & 0 \\ i & 0 & 0 & 0 \end{pmatrix}. & R_{17}(g_3) &= \begin{pmatrix} -i & 0 & 0 & 0 \\ 0 & i & 0 & 0 \\ 0 & 0 & -i & 0 \\ 0 & 0 & 0 & i \end{pmatrix}. \\
R_{17}(g_4) &= \begin{pmatrix} 0 & 0 & 0 & -1 \\ 0 & 0 & -1 & 0 \\ 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 \end{pmatrix}. & R_{17}(g_5) &= \begin{pmatrix} 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & -1 \\ 1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \end{pmatrix}. \\
& & R_{17}(g_6) &= \begin{pmatrix} -1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & -1 \end{pmatrix}.
\end{aligned}$$

 $G_{32}^{(51)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= -1. & R_2(g_5) &= -1. & R_2(g_6) &= -1. \\
R_3(g_2) &= -1. & R_3(g_3) &= -1. & R_3(g_4) &= -1. & R_3(g_5) &= -1. & R_3(g_6) &= 1. \\
R_4(g_2) &= -1. & R_4(g_3) &= -1. & R_4(g_4) &= -1. & R_4(g_5) &= 1. & R_4(g_6) &= -1. \\
R_5(g_2) &= -1. & R_5(g_3) &= -1. & R_5(g_4) &= -1. & R_5(g_5) &= 1. & R_5(g_6) &= 1. \\
R_6(g_2) &= -1. & R_6(g_3) &= -1. & R_6(g_4) &= 1. & R_6(g_5) &= -1. & R_6(g_6) &= -1. \\
R_7(g_2) &= -1. & R_7(g_3) &= -1. & R_7(g_4) &= 1. & R_7(g_5) &= -1. & R_7(g_6) &= 1. \\
R_8(g_2) &= -1. & R_8(g_3) &= -1. & R_8(g_4) &= 1. & R_8(g_5) &= 1. & R_8(g_6) &= -1. \\
R_9(g_2) &= -1. & R_9(g_3) &= -1. & R_9(g_4) &= 1. & R_9(g_5) &= 1. & R_9(g_6) &= 1. \\
R_{10}(g_2) &= -1. & R_{10}(g_3) &= 1. & R_{10}(g_4) &= -1. & R_{10}(g_5) &= -1. & R_{10}(g_6) &= -1. \\
R_{11}(g_2) &= -1. & R_{11}(g_3) &= 1. & R_{11}(g_4) &= -1. & R_{11}(g_5) &= -1. & R_{11}(g_6) &= 1. \\
R_{12}(g_2) &= -1. & R_{12}(g_3) &= 1. & R_{12}(g_4) &= -1. & R_{12}(g_5) &= 1. & R_{12}(g_6) &= -1.
\end{aligned}$$

$$\begin{aligned}
R_{13}(g_2) &= -1. & R_{13}(g_3) &= 1. & R_{13}(g_4) &= -1. & R_{13}(g_5) &= 1. & R_{13}(g_6) &= 1. \\
R_{14}(g_2) &= -1. & R_{14}(g_3) &= 1. & R_{14}(g_4) &= 1. & R_{14}(g_5) &= -1. & R_{14}(g_6) &= -1. \\
R_{15}(g_2) &= -1. & R_{15}(g_3) &= 1. & R_{15}(g_4) &= 1. & R_{15}(g_5) &= -1. & R_{15}(g_6) &= 1. \\
R_{16}(g_2) &= -1. & R_{16}(g_3) &= 1. & R_{16}(g_4) &= 1. & R_{16}(g_5) &= 1. & R_{16}(g_6) &= -1. \\
R_{17}(g_2) &= -1. & R_{17}(g_3) &= 1. & R_{17}(g_4) &= 1. & R_{17}(g_5) &= 1. & R_{17}(g_6) &= 1. \\
R_{18}(g_2) &= 1. & R_{18}(g_3) &= -1. & R_{18}(g_4) &= -1. & R_{18}(g_5) &= -1. & R_{18}(g_6) &= -1. \\
R_{19}(g_2) &= 1. & R_{19}(g_3) &= -1. & R_{19}(g_4) &= -1. & R_{19}(g_5) &= -1. & R_{19}(g_6) &= 1. \\
R_{20}(g_2) &= 1. & R_{20}(g_3) &= -1. & R_{20}(g_4) &= -1. & R_{20}(g_5) &= 1. & R_{20}(g_6) &= -1. \\
R_{21}(g_2) &= 1. & R_{21}(g_3) &= -1. & R_{21}(g_4) &= -1. & R_{21}(g_5) &= 1. & R_{21}(g_6) &= 1. \\
R_{22}(g_2) &= 1. & R_{22}(g_3) &= -1. & R_{22}(g_4) &= 1. & R_{22}(g_5) &= -1. & R_{22}(g_6) &= -1. \\
R_{23}(g_2) &= 1. & R_{23}(g_3) &= -1. & R_{23}(g_4) &= 1. & R_{23}(g_5) &= -1. & R_{23}(g_6) &= 1. \\
R_{24}(g_2) &= 1. & R_{24}(g_3) &= -1. & R_{24}(g_4) &= 1. & R_{24}(g_5) &= 1. & R_{24}(g_6) &= -1. \\
R_{25}(g_2) &= 1. & R_{25}(g_3) &= -1. & R_{25}(g_4) &= 1. & R_{25}(g_5) &= 1. & R_{25}(g_6) &= 1. \\
R_{26}(g_2) &= 1. & R_{26}(g_3) &= 1. & R_{26}(g_4) &= -1. & R_{26}(g_5) &= -1. & R_{26}(g_6) &= -1. \\
R_{27}(g_2) &= 1. & R_{27}(g_3) &= 1. & R_{27}(g_4) &= -1. & R_{27}(g_5) &= -1. & R_{27}(g_6) &= 1. \\
R_{28}(g_2) &= 1. & R_{28}(g_3) &= 1. & R_{28}(g_4) &= -1. & R_{28}(g_5) &= 1. & R_{28}(g_6) &= -1. \\
R_{29}(g_2) &= 1. & R_{29}(g_3) &= 1. & R_{29}(g_4) &= -1. & R_{29}(g_5) &= 1. & R_{29}(g_6) &= 1. \\
R_{30}(g_2) &= 1. & R_{30}(g_3) &= 1. & R_{30}(g_4) &= 1. & R_{30}(g_5) &= -1. & R_{30}(g_6) &= -1. \\
R_{31}(g_2) &= 1. & R_{31}(g_3) &= 1. & R_{31}(g_4) &= 1. & R_{31}(g_5) &= -1. & R_{31}(g_6) &= 1. \\
R_{32}(g_2) &= 1. & R_{32}(g_3) &= 1. & R_{32}(g_4) &= 1. & R_{32}(g_5) &= 1. & R_{32}(g_6) &= -1.
\end{aligned}$$

2.33. Order 33. $G_{33}^{(1)}$

$$\begin{aligned}
R_2(g_2) &= 1. & R_2(g_3) &= e_{11}^{10}. \\
R_3(g_2) &= 1. & R_3(g_3) &= e_{11}^9. \\
R_4(g_2) &= 1. & R_4(g_3) &= e_{11}^8. \\
R_5(g_2) &= 1. & R_5(g_3) &= e_{11}^7. \\
R_6(g_2) &= 1. & R_6(g_3) &= e_{11}^6. \\
R_7(g_2) &= 1. & R_7(g_3) &= e_{11}^5. \\
R_8(g_2) &= 1. & R_8(g_3) &= e_{11}^4. \\
R_9(g_2) &= 1. & R_9(g_3) &= e_{11}^3. \\
R_{10}(g_2) &= 1. & R_{10}(g_3) &= e_{11}^2. \\
R_{11}(g_2) &= 1. & R_{11}(g_3) &= e_{11}. \\
R_{12}(g_2) &= e_3^2. & R_{12}(g_3) &= 1. \\
R_{13}(g_2) &= e_3. & R_{13}(g_3) &= 1. \\
R_{14}(g_2) &= e_3^2. & R_{14}(g_3) &= e_{11}^{10}. \\
R_{15}(g_2) &= e_3^2. & R_{15}(g_3) &= e_{11}^9. \\
R_{16}(g_2) &= e_3^2. & R_{16}(g_3) &= e_{11}^8. \\
R_{17}(g_2) &= e_3^2. & R_{17}(g_3) &= e_{11}^7. \\
R_{18}(g_2) &= e_3^2. & R_{18}(g_3) &= e_{11}^6. \\
R_{19}(g_2) &= e_3^2. & R_{19}(g_3) &= e_{11}^5.
\end{aligned}$$

$$\begin{aligned}
R_{20}(g_2) &= e_3^2. & R_{20}(g_3) &= e_{11}^4. \\
R_{21}(g_2) &= e_3^2. & R_{21}(g_3) &= e_{11}^3. \\
R_{22}(g_2) &= e_3^2. & R_{22}(g_3) &= e_{11}^2. \\
R_{23}(g_2) &= e_3^2. & R_{23}(g_3) &= e_{11}. \\
R_{24}(g_2) &= e_3. & R_{24}(g_3) &= e_{11}^{10}. \\
R_{25}(g_2) &= e_3. & R_{25}(g_3) &= e_{11}^9. \\
R_{26}(g_2) &= e_3. & R_{26}(g_3) &= e_{11}^8. \\
R_{27}(g_2) &= e_3. & R_{27}(g_3) &= e_{11}^7. \\
R_{28}(g_2) &= e_3. & R_{28}(g_3) &= e_{11}^6. \\
R_{29}(g_2) &= e_3. & R_{29}(g_3) &= e_{11}^5. \\
R_{30}(g_2) &= e_3. & R_{30}(g_3) &= e_{11}^4. \\
R_{31}(g_2) &= e_3. & R_{31}(g_3) &= e_{11}^3. \\
R_{32}(g_2) &= e_3. & R_{32}(g_3) &= e_{11}^2. \\
R_{33}(g_2) &= e_3. & R_{33}(g_3) &= e_{11}.
\end{aligned}$$

2.34. **Order 34.** $G_{34}^{(1)}$

$$R_2(g_2) = -1. \quad R_2(g_3) = 1.$$

$$R_3(g_2) = \begin{pmatrix} \alpha_{34,1} & \alpha_{34,2} \\ -\alpha_{34,1} & -\alpha_{34,1} \end{pmatrix}. \quad R_3(g_3) = \begin{pmatrix} -e_{17}^4 - e_{17}^{13} & \alpha_{34,3} \\ -\alpha_{34,3} & e_{17}^4 + e_{17}^5 + e_{17}^{12} + e_{17}^{13} \end{pmatrix}.$$

Constants:

$$\begin{aligned}
\alpha_{34,1} &\equiv e_{17}^3 + e_{17}^4 + e_{17}^5 + e_{17}^6 + e_{17}^{11} + e_{17}^{12} + e_{17}^{13} + e_{17}^{14}; \\
\alpha_{34,2} &\equiv e_{17}^2 + e_{17}^3 + e_{17}^4 + e_{17}^5 + e_{17}^6 + e_{17}^{11} + e_{17}^{12} + e_{17}^{13} + e_{17}^{14} + e_{17}^{15}; \\
\alpha_{34,3} &\equiv -e_{17} - e_{17}^2 - e_{17}^3 - e_{17}^4 - e_{17}^5 - e_{17}^6 - e_{17}^7 - e_{17}^{10} - e_{17}^{11} - e_{17}^{12} - e_{17}^{13} - e_{17}^{14} - e_{17}^{15} - e_{17}^{16}.
\end{aligned}$$

$$R_4(g_2) = \begin{pmatrix} \alpha_{34,4} & \alpha_{34,5} \\ -\alpha_{34,4} & -\alpha_{34,4} \end{pmatrix}. \quad R_4(g_3) = \begin{pmatrix} \alpha_{34,6} & -e_{17}^7 - e_{17}^{10} \\ e_{17}^7 + e_{17}^{10} & -1 \end{pmatrix}.$$

Constants:

$$\begin{aligned}
\alpha_{34,4} &\equiv e_{17} + e_{17}^2 + e_{17}^4 + e_{17}^7 + e_{17}^{10} + e_{17}^{13} + e_{17}^{15} + e_{17}^{16}; \\
\alpha_{34,5} &\equiv e_{17} + e_{17}^2 + e_{17}^4 + e_{17}^5 + e_{17}^7 + e_{17}^{10} + e_{17}^{12} + e_{17}^{13} + e_{17}^{15} + e_{17}^{16}; \\
\alpha_{34,6} &\equiv -e_{17} - e_{17}^2 - e_{17}^4 - e_{17}^5 - e_{17}^6 - e_{17}^7 - e_{17}^8 - e_{17}^9 - e_{17}^{10} - e_{17}^{11} - e_{17}^{12} - e_{17}^{13} - e_{17}^{15} - e_{17}^{16}.
\end{aligned}$$

$$\begin{aligned}
R_5(g_2) &= \begin{pmatrix} \alpha_{34,7} & e_{17}^2 + e_{17}^3 + e_{17}^8 + e_{17}^9 + e_{17}^{14} + e_{17}^{15} \\ -e_{17}^3 - e_{17}^8 - e_{17}^9 - e_{17}^{14} & -\alpha_{34,7} \end{pmatrix}. \\
R_5(g_3) &= \begin{pmatrix} -1 & e_{17}^3 + e_{17}^{14} \\ -e_{17}^3 - e_{17}^{14} & \alpha_{34,8} \end{pmatrix}.
\end{aligned}$$

Constants:

$$\begin{aligned}
\alpha_{34,7} &\equiv e_{17} + e_{17}^2 + e_{17}^3 + e_{17}^4 + e_{17}^7 + e_{17}^8 + e_{17}^9 + e_{17}^{10} + e_{17}^{13} + e_{17}^{14} + e_{17}^{15} + e_{17}^{16}; \\
\alpha_{34,8} &\equiv -e_{17} - e_{17}^2 - e_{17}^3 - e_{17}^4 - e_{17}^5 - e_{17}^7 - e_{17}^8 - e_{17}^9 - e_{17}^{10} - e_{17}^{12} - e_{17}^{13} - e_{17}^{14} - e_{17}^{15} - e_{17}^{16}.
\end{aligned}$$

$$R_6(g_2) = \begin{pmatrix} \alpha_{34,9} & e_7^7 + e_{17}^8 + e_{17}^9 + e_{17}^{10} \\ -e_{17}^8 - e_{17}^9 & -\alpha_{34,9} \end{pmatrix}.$$

$$R_6(g_3) = \begin{pmatrix} \alpha_{34,10} & -e_7^7 - e_{17}^8 - e_{17}^9 - e_{17}^{10} \\ e_7^7 + e_{17}^8 + e_{17}^9 + e_{17}^{10} & \alpha_{34,9} \end{pmatrix}.$$

Constants:

$$\alpha_{34,9} \equiv e_{17}^2 + e_{17}^3 + e_{17}^4 + e_{17}^5 + e_{17}^6 + e_{17}^7 + e_{17}^8 + e_{17}^9 + e_{17}^{10} + e_{17}^{11} + e_{17}^{12} + e_{17}^{13} + e_{17}^{14} + e_{17}^{15};$$

$$\alpha_{34,10} \equiv -e_{17}^3 - e_{17}^4 - e_{17}^5 - e_{17}^6 - e_{17}^7 - e_{17}^8 - e_{17}^9 - e_{17}^{10} - e_{17}^{11} - e_{17}^{12} - e_{17}^{13} - e_{17}^{14}.$$

$$R_7(g_2) = \begin{pmatrix} \alpha_{34,11} & -e_{17} - e_{17}^{16} \\ e_{17} + e_{17}^3 + e_{17}^{14} + e_{17}^{16} & -\alpha_{34,11} \end{pmatrix}.$$

$$R_7(g_3) = \begin{pmatrix} -e_{17} - e_{17}^3 - e_{17}^5 - e_{17}^{12} - e_{17}^{14} - e_{17}^{16} & \alpha_{34,12} \\ -\alpha_{34,12} & e_{17} + e_{17}^3 + e_{17}^5 + e_{17}^7 + e_{17}^{10} + e_{17}^{12} + e_{17}^{14} + e_{17}^{16} \end{pmatrix}.$$

Constants:

$$\alpha_{34,11} \equiv -e_{17} - e_{17}^3 - e_{17}^4 - e_{17}^5 - e_{17}^6 - e_{17}^7 - e_{17}^8 - e_{17}^9 - e_{17}^{10} - e_{17}^{11} - e_{17}^{12} - e_{17}^{13} - e_{17}^{14} - e_{17}^{16};$$

$$\alpha_{34,12} \equiv -e_{17} - e_{17}^3 - e_{17}^5 - e_{17}^7 - e_{17}^8 - e_{17}^9 - e_{17}^{10} - e_{17}^{12} - e_{17}^{14} - e_{17}^{16}.$$

$$R_8(g_2) = \begin{pmatrix} 1 & 0 \\ e_{17}^4 + e_{17}^{13} & -1 \end{pmatrix}, \quad R_8(g_3) = \begin{pmatrix} -1 & e_{17}^4 + e_{17}^{13} \\ -e_{17}^4 - e_{17}^{13} & \alpha_{34,3} \end{pmatrix}.$$

$$R_9(g_2) = \begin{pmatrix} \alpha_{34,13} & -e_{17} - e_{17}^3 - e_{17}^{14} - e_{17}^{16} \\ e_{17} + e_{17}^3 + e_{17}^5 + e_{17}^{12} + e_{17}^{14} + e_{17}^{16} & -\alpha_{34,13} \end{pmatrix}.$$

$$R_9(g_3) = \begin{pmatrix} -\alpha_{34,11} & e_{17} + e_{17}^3 + e_{17}^{14} + e_{17}^{16} \\ -e_{17} - e_{17}^3 - e_{17}^{14} - e_{17}^{16} & \alpha_{34,13} \end{pmatrix}.$$

Constants:

$$\alpha_{34,13} \equiv -e_{17} - e_{17}^3 - e_{17}^5 - e_{17}^6 - e_{17}^7 - e_{17}^8 - e_{17}^9 - e_{17}^{10} - e_{17}^{11} - e_{17}^{12} - e_{17}^{14} - e_{17}^{16}.$$

$$R_{10}(g_2) = \begin{pmatrix} \alpha_{34,8} & -e_{17}^3 - e_{17}^{14} \\ e_{17}^3 + e_{17}^8 + e_{17}^9 + e_{17}^{14} & -\alpha_{34,8} \end{pmatrix}.$$

$$R_{10}(g_3) = \begin{pmatrix} \alpha_{34,15} & -e_{17}^2 - e_{17}^3 - e_{17}^8 - e_{17}^9 - e_{17}^{14} - e_{17}^{15} \\ e_{17}^2 + e_{17}^3 + e_{17}^8 + e_{17}^9 + e_{17}^{14} + e_{17}^{15} & \alpha_{34,7} \end{pmatrix}.$$

Constants:

$$\alpha_{34,14} \equiv -e_{17}^2 - e_{17}^3 - e_{17}^4 - e_{17}^7 - e_{17}^8 - e_{17}^9 - e_{17}^{10} - e_{17}^{13} - e_{17}^{14} - e_{17}^{15}.$$

$G_{34}^{(2)}$

$$R_2(g_2) = -1. \quad R_2(g_3) = 1.$$

$$R_3(g_2) = -1. \quad R_3(g_3) = e_{17}^{16}.$$

$$R_4(g_2) = -1. \quad R_4(g_3) = e_{17}^{15}.$$

$$R_5(g_2) = -1. \quad R_5(g_3) = e_{17}^{14}.$$

$$R_6(g_2) = -1. \quad R_6(g_3) = e_{17}^{13}.$$

$$\begin{aligned}
R_7(g_2) &= -1. & R_7(g_3) &= e_{17}^{12}. \\
R_8(g_2) &= -1. & R_8(g_3) &= e_{17}^{11}. \\
R_9(g_2) &= -1. & R_9(g_3) &= e_{17}^{10}. \\
R_{10}(g_2) &= -1. & R_{10}(g_3) &= e_{17}^9. \\
R_{11}(g_2) &= -1. & R_{11}(g_3) &= e_{17}^8. \\
R_{12}(g_2) &= -1. & R_{12}(g_3) &= e_{17}^7. \\
R_{13}(g_2) &= -1. & R_{13}(g_3) &= e_{17}^6. \\
R_{14}(g_2) &= -1. & R_{14}(g_3) &= e_{17}^5. \\
R_{15}(g_2) &= -1. & R_{15}(g_3) &= e_{17}^4. \\
R_{16}(g_2) &= -1. & R_{16}(g_3) &= e_{17}^3. \\
R_{17}(g_2) &= -1. & R_{17}(g_3) &= e_{17}^2. \\
R_{18}(g_2) &= -1. & R_{18}(g_3) &= e_{17}. \\
R_{19}(g_2) &= 1. & R_{19}(g_3) &= e_{17}^{16}. \\
R_{20}(g_2) &= 1. & R_{20}(g_3) &= e_{17}^{15}. \\
R_{21}(g_2) &= 1. & R_{21}(g_3) &= e_{17}^{14}. \\
R_{22}(g_2) &= 1. & R_{22}(g_3) &= e_{17}^{13}. \\
R_{23}(g_2) &= 1. & R_{23}(g_3) &= e_{17}^{12}. \\
R_{24}(g_2) &= 1. & R_{24}(g_3) &= e_{17}^{11}. \\
R_{25}(g_2) &= 1. & R_{25}(g_3) &= e_{17}^{10}. \\
R_{26}(g_2) &= 1. & R_{26}(g_3) &= e_{17}^9. \\
R_{27}(g_2) &= 1. & R_{27}(g_3) &= e_{17}^8. \\
R_{28}(g_2) &= 1. & R_{28}(g_3) &= e_{17}^7. \\
R_{29}(g_2) &= 1. & R_{29}(g_3) &= e_{17}^6. \\
R_{30}(g_2) &= 1. & R_{30}(g_3) &= e_{17}^5. \\
R_{31}(g_2) &= 1. & R_{31}(g_3) &= e_{17}^4. \\
R_{32}(g_2) &= 1. & R_{32}(g_3) &= e_{17}^3. \\
R_{33}(g_2) &= 1. & R_{33}(g_3) &= e_{17}^2. \\
R_{34}(g_2) &= 1. & R_{34}(g_3) &= e_{17}.
\end{aligned}$$

2.35. Order 35. $G_{35}^{(1)}$

$$\begin{aligned}
R_2(g_2) &= 1. & R_2(g_3) &= e_7^6. \\
R_3(g_2) &= 1. & R_3(g_3) &= e_7^5. \\
R_4(g_2) &= 1. & R_4(g_3) &= e_7^4. \\
R_5(g_2) &= 1. & R_5(g_3) &= e_7^3. \\
R_6(g_2) &= 1. & R_6(g_3) &= e_7^2. \\
R_7(g_2) &= 1. & R_7(g_3) &= e_7. \\
R_8(g_2) &= e_5^4. & R_8(g_3) &= 1. \\
R_9(g_2) &= e_5^3. & R_9(g_3) &= 1. \\
R_{10}(g_2) &= e_5^2. & R_{10}(g_3) &= 1. \\
R_{11}(g_2) &= e_5. & R_{11}(g_3) &= 1. \\
R_{12}(g_2) &= e_5^4. & R_{12}(g_3) &= e_7^6. \\
R_{13}(g_2) &= e_5^4. & R_{13}(g_3) &= e_7^5. \\
R_{14}(g_2) &= e_5^4. & R_{14}(g_3) &= e_7^4. \\
R_{15}(g_2) &= e_5^4. & R_{15}(g_3) &= e_7^3. \\
R_{16}(g_2) &= e_5^4. & R_{16}(g_3) &= e_7^2. \\
R_{17}(g_2) &= e_5^4. & R_{17}(g_3) &= e_7. \\
R_{18}(g_2) &= e_5^3. & R_{18}(g_3) &= e_7^6. \\
R_{19}(g_2) &= e_5^3. & R_{19}(g_3) &= e_7^5. \\
R_{20}(g_2) &= e_5^3. & R_{20}(g_3) &= e_7^4. \\
R_{21}(g_2) &= e_5^3. & R_{21}(g_3) &= e_7^3. \\
R_{22}(g_2) &= e_5^3. & R_{22}(g_3) &= e_7^2. \\
R_{23}(g_2) &= e_5^3. & R_{23}(g_3) &= e_7. \\
R_{24}(g_2) &= e_5^2. & R_{24}(g_3) &= e_7^6. \\
R_{25}(g_2) &= e_5^2. & R_{25}(g_3) &= e_7^5. \\
R_{26}(g_2) &= e_5^2. & R_{26}(g_3) &= e_7^4. \\
R_{27}(g_2) &= e_5^2. & R_{27}(g_3) &= e_7^3. \\
R_{28}(g_2) &= e_5^2. & R_{28}(g_3) &= e_7^2. \\
R_{29}(g_2) &= e_5^2. & R_{29}(g_3) &= e_7. \\
R_{30}(g_2) &= e_5. & R_{30}(g_3) &= e_7^6. \\
R_{31}(g_2) &= e_5. & R_{31}(g_3) &= e_7^5. \\
R_{32}(g_2) &= e_5. & R_{32}(g_3) &= e_7^4. \\
R_{33}(g_2) &= e_5. & R_{33}(g_3) &= e_7^3. \\
R_{34}(g_2) &= e_5. & R_{34}(g_3) &= e_7^2. \\
R_{35}(g_2) &= e_5. & R_{35}(g_3) &= e_7.
\end{aligned}$$

2.36. **Order 36.** $G_{36}^{(1)}$

$$R_2(g_2) = -1. \quad R_2(g_3) = 1. \quad R_2(g_4) = 1. \quad R_2(g_5) = 1.$$

$$R_3(g_2) = -i. \quad R_3(g_3) = -1. \quad R_3(g_4) = 1. \quad R_3(g_5) = 1.$$

$$R_4(g_2) = i. \quad R_4(g_3) = -1. \quad R_4(g_4) = 1. \quad R_4(g_5) = 1.$$

$$R_5(g_2) = \begin{pmatrix} -1 & -1 \\ 0 & 1 \end{pmatrix}. \quad R_5(g_3) = \epsilon. \quad R_5(g_4) = \begin{pmatrix} -1 & -1 \\ 1 & 0 \end{pmatrix}. \quad R_5(g_5) = \epsilon.$$

$$R_6(g_2) = \begin{pmatrix} -i & -1 \\ 0 & i \end{pmatrix}. \quad R_6(g_3) = -\epsilon. \quad R_6(g_4) = \begin{pmatrix} 0 & -i \\ -i & -1 \end{pmatrix}. \quad R_6(g_5) = \epsilon.$$

$$R_7(g_2) = \begin{pmatrix} -e_9^3 + e_9^4 + e_9^5 - e_9^6 & -e_9^2 - e_9^7 \\ e_9^2 + e_9^3 + e_9^6 + e_9^7 & e_9^3 - e_9^4 - e_9^5 + e_9^6 \end{pmatrix}. \quad R_7(g_3) = \epsilon.$$

$$R_7(g_4) = \begin{pmatrix} e_9^2 + e_9^7 & -1 \\ 1 & 0 \end{pmatrix}. \quad R_7(g_5) = \begin{pmatrix} -e_9^2 - e_9^7 & -e_9^3 + e_9^4 + e_9^5 - e_9^6 \\ e_9^3 - e_9^4 - e_9^5 + e_9^6 & e_9^2 + e_9^3 + e_9^6 + e_9^7 \end{pmatrix}.$$

$$R_8(g_2) = \begin{pmatrix} 1 & 0 \\ -1 & -1 \end{pmatrix}. \quad R_8(g_3) = \epsilon.$$

$$R_8(g_4) = \begin{pmatrix} (-2e_9^2 - e_9^4 - e_9^5 - 2e_9^7)/3 & -2(\Re e_9^2 + \Re e_{18})/3 \\ (e_9^2 - e_9^4 - e_9^5 + e_9^7)/3 & (-e_9^2 - 2e_9^4 - 2e_9^5 - e_9^7)/3 \end{pmatrix}. \quad R_8(g_5) = \begin{pmatrix} 0 & 1 \\ -1 & -1 \end{pmatrix}.$$

$$R_9(g_2) = \begin{pmatrix} -e_9^2 - e_9^7 & -e_9^3 + e_9^4 + e_9^5 - e_9^6 \\ -1 & e_9^2 + e_9^7 \end{pmatrix}. \quad R_9(g_3) = \epsilon.$$

$$R_9(g_4) = \begin{pmatrix} -e_9^3 + e_9^4 + e_9^5 - e_9^6 & -e_9^2 - e_9^7 \\ e_9^2 + e_9^7 & -1 \end{pmatrix}. \quad R_9(g_5) = \begin{pmatrix} e_9^2 + e_9^3 + e_9^6 + e_9^7 & e_9^3 - e_9^4 - e_9^5 + e_9^6 \\ -e_9^3 + e_9^4 + e_9^5 - e_9^6 & -e_9^2 - e_9^7 \end{pmatrix}.$$

$$R_{10}(g_2) = \begin{pmatrix} i & 0 \\ i & -i \end{pmatrix}. \quad R_{10}(g_3) = -\epsilon.$$

$$R_{10}(g_4) = \begin{pmatrix} (2e_9^2 + e_9^4 + e_9^5 + 2e_9^7)/3 & (-e_9^2 - 2e_9^4 - 2e_9^5 - e_9^7)/3 \\ (e_9^2 + 2e_9^4 + 2e_9^5 + e_9^7)/3 & (e_9^2 - e_9^4 - e_9^5 + e_9^7)/3 \end{pmatrix}. \quad R_{10}(g_5) = \begin{pmatrix} -1 & 1 \\ -1 & 0 \end{pmatrix}.$$

$$R_{11}(g_2) = \begin{pmatrix} i & 0 \\ -e_{36} - e_{36}^{17} & -i \end{pmatrix}. \quad R_{11}(g_3) = -\epsilon.$$

$$R_{11}(g_4) = \begin{pmatrix} -e_9^2 - e_9^3 - e_9^6 - e_9^7 & e_9^2 + e_9^3 + e_9^6 + e_9^7 \\ -e_9^2 - e_9^3 - e_9^6 - e_9^7 & e_9^3 - e_9^4 - e_9^5 + e_9^6 \end{pmatrix}.$$

$$R_{11}(g_5) = \begin{pmatrix} -e_9^2 - e_9^7 & e_9^3 - e_9^4 - e_9^5 + e_9^6 \\ -e_9^3 + e_9^4 + e_9^5 - e_9^6 & e_9^2 + e_9^3 + e_9^6 + e_9^7 \end{pmatrix}.$$

$$R_{12}(g_2) = \begin{pmatrix} i & 0 \\ -e_9^4 - e_9^5 & -i \end{pmatrix}. \quad R_{12}(g_3) = -\epsilon. \quad R_{12}(g_4) = \begin{pmatrix} e_9^4 + e_9^5 & i \\ i & 0 \end{pmatrix}.$$

$$R_{12}(g_5) = \begin{pmatrix} -e_9^4 - e_9^5 & e_{36} + e_{36}^{17} + e_{36}^{21} + e_{36}^{25} + e_{36}^{29} + e_{36}^{33} \\ e_{36} + e_{36}^{17} + e_{36}^{21} + e_{36}^{25} + e_{36}^{29} + e_{36}^{33} & e_9^3 + e_9^4 + e_9^5 + e_9^6 \end{pmatrix}.$$

$G_{36}^{(2)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= 1. & R_2(g_4) &= 1. & R_2(g_5) &= 1. \\
R_3(g_2) &= -1. & R_3(g_3) &= e_3^2. & R_3(g_4) &= 1. & R_3(g_5) &= 1. \\
R_4(g_2) &= -1. & R_4(g_3) &= e_3. & R_4(g_4) &= 1. & R_4(g_5) &= 1. \\
R_5(g_2) &= -1. & R_5(g_3) &= -e_9^2 - e_9^5. & R_5(g_4) &= 1. & R_5(g_5) &= e_3^2. \\
R_6(g_2) &= -1. & R_6(g_3) &= -e_9^4 - e_9^7. & R_6(g_4) &= 1. & R_6(g_5) &= e_3. \\
R_7(g_2) &= -1. & R_7(g_3) &= e_9^7. & R_7(g_4) &= 1. & R_7(g_5) &= e_3. \\
R_8(g_2) &= -1. & R_8(g_3) &= e_9^5. & R_8(g_4) &= 1. & R_8(g_5) &= e_3^2. \\
R_9(g_2) &= -1. & R_9(g_3) &= e_9^4. & R_9(g_4) &= 1. & R_9(g_5) &= e_3. \\
R_{10}(g_2) &= -1. & R_{10}(g_3) &= e_9^2. & R_{10}(g_4) &= 1. & R_{10}(g_5) &= e_3^2. \\
R_{11}(g_2) &= 1. & R_{11}(g_3) &= e_3^2. & R_{11}(g_4) &= 1. & R_{11}(g_5) &= 1. \\
R_{12}(g_2) &= 1. & R_{12}(g_3) &= e_3. & R_{12}(g_4) &= 1. & R_{12}(g_5) &= 1. \\
R_{13}(g_2) &= 1. & R_{13}(g_3) &= -e_9^2 - e_9^5. & R_{13}(g_4) &= 1. & R_{13}(g_5) &= e_3^2. \\
R_{14}(g_2) &= 1. & R_{14}(g_3) &= -e_9^4 - e_9^7. & R_{14}(g_4) &= 1. & R_{14}(g_5) &= e_3. \\
R_{15}(g_2) &= 1. & R_{15}(g_3) &= e_9^7. & R_{15}(g_4) &= 1. & R_{15}(g_5) &= e_3. \\
R_{16}(g_2) &= 1. & R_{16}(g_3) &= e_9^5. & R_{16}(g_4) &= 1. & R_{16}(g_5) &= e_3^2. \\
R_{17}(g_2) &= 1. & R_{17}(g_3) &= e_9^4. & R_{17}(g_4) &= 1. & R_{17}(g_5) &= e_3. \\
R_{18}(g_2) &= 1. & R_{18}(g_3) &= e_9^2. & R_{18}(g_4) &= 1. & R_{18}(g_5) &= e_3^2. \\
R_{19}(g_2) &= -i. & R_{19}(g_3) &= 1. & R_{19}(g_4) &= -1. & R_{19}(g_5) &= 1. \\
R_{20}(g_2) &= i. & R_{20}(g_3) &= 1. & R_{20}(g_4) &= -1. & R_{20}(g_5) &= 1. \\
R_{21}(g_2) &= -i. & R_{21}(g_3) &= e_3^2. & R_{21}(g_4) &= -1. & R_{21}(g_5) &= 1. \\
R_{22}(g_2) &= -i. & R_{22}(g_3) &= e_3. & R_{22}(g_4) &= -1. & R_{22}(g_5) &= 1. \\
R_{23}(g_2) &= i. & R_{23}(g_3) &= e_3^2. & R_{23}(g_4) &= -1. & R_{23}(g_5) &= 1. \\
R_{24}(g_2) &= i. & R_{24}(g_3) &= e_3. & R_{24}(g_4) &= -1. & R_{24}(g_5) &= 1. \\
R_{25}(g_2) &= -i. & R_{25}(g_3) &= -e_9^2 - e_9^5. & R_{25}(g_4) &= -1. & R_{25}(g_5) &= e_3^2. \\
R_{26}(g_2) &= -i. & R_{26}(g_3) &= -e_9^4 - e_9^7. & R_{26}(g_4) &= -1. & R_{26}(g_5) &= e_3. \\
R_{27}(g_2) &= -i. & R_{27}(g_3) &= e_9^7. & R_{27}(g_4) &= -1. & R_{27}(g_5) &= e_3. \\
R_{28}(g_2) &= -i. & R_{28}(g_3) &= e_9^5. & R_{28}(g_4) &= -1. & R_{28}(g_5) &= e_3^2. \\
R_{29}(g_2) &= -i. & R_{29}(g_3) &= e_9^4. & R_{29}(g_4) &= -1. & R_{29}(g_5) &= e_3. \\
R_{30}(g_2) &= -i. & R_{30}(g_3) &= e_9^2. & R_{30}(g_4) &= -1. & R_{30}(g_5) &= e_3^2. \\
R_{31}(g_2) &= i. & R_{31}(g_3) &= -e_9^2 - e_9^5. & R_{31}(g_4) &= -1. & R_{31}(g_5) &= e_3^2. \\
R_{32}(g_2) &= i. & R_{32}(g_3) &= -e_9^4 - e_9^7. & R_{32}(g_4) &= -1. & R_{32}(g_5) &= e_3. \\
R_{33}(g_2) &= i. & R_{33}(g_3) &= e_9^7. & R_{33}(g_4) &= -1. & R_{33}(g_5) &= e_3. \\
R_{34}(g_2) &= i. & R_{34}(g_3) &= e_9^5. & R_{34}(g_4) &= -1. & R_{34}(g_5) &= e_3^2. \\
R_{35}(g_2) &= i. & R_{35}(g_3) &= e_9^4. & R_{35}(g_4) &= -1. & R_{35}(g_5) &= e_3. \\
R_{36}(g_2) &= i. & R_{36}(g_3) &= e_9^2. & R_{36}(g_4) &= -1. & R_{36}(g_5) &= e_3^2.
\end{aligned}$$

$G_{36}^{(3)}$

$$R_2(g_2) = e_3^2. \quad R_2(g_3) = 1. \quad R_2(g_4) = 1. \quad R_2(g_5) = 1.$$

$$R_3(g_2) = e_3. \quad R_3(g_3) = 1. \quad R_3(g_4) = 1. \quad R_3(g_5) = 1.$$

$$R_4(g_2) = -e_9^2 - e_9^5. \quad R_4(g_3) = e_3^2. \quad R_4(g_4) = 1. \quad R_4(g_5) = 1.$$

$$R_5(g_2) = -e_9^4 - e_9^7. \quad R_5(g_3) = e_3. \quad R_5(g_4) = 1. \quad R_5(g_5) = 1.$$

$$R_6(g_2) = e_9^7. \quad R_6(g_3) = e_3. \quad R_6(g_4) = 1. \quad R_6(g_5) = 1.$$

$$R_7(g_2) = e_9^5. \quad R_7(g_3) = e_3^2. \quad R_7(g_4) = 1. \quad R_7(g_5) = 1.$$

$$R_8(g_2) = e_9^4. \quad R_8(g_3) = e_3. \quad R_8(g_4) = 1. \quad R_8(g_5) = 1.$$

$$R_9(g_2) = e_9^2. \quad R_9(g_3) = e_3^2. \quad R_9(g_4) = 1. \quad R_9(g_5) = 1.$$

$$R_{10}(g_2) = \begin{pmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 1 & 0 & 0 \end{pmatrix}. \quad R_{10}(g_3) = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}.$$

$$R_{10}(g_4) = \begin{pmatrix} -1 & -1 & -1 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix}. \quad R_{10}(g_5) = \begin{pmatrix} 0 & 0 & 1 \\ -1 & -1 & -1 \\ 1 & 0 & 0 \end{pmatrix}.$$

$$R_{11}(g_2) = \begin{pmatrix} 0 & 0 & -e_9^2 - e_9^5 \\ e_3 & 0 & 0 \\ 0 & -e_9^4 - e_9^7 & 0 \end{pmatrix}. \quad R_{11}(g_3) = \begin{pmatrix} e_3 & 0 & 0 \\ 0 & e_3 & 0 \\ 0 & 0 & e_3 \end{pmatrix}.$$

$$R_{11}(g_4) = \begin{pmatrix} 0 & e_9^7 & 0 \\ e_9^2 & 0 & 0 \\ -e_9^2 & -1 & -1 \end{pmatrix}. \quad R_{11}(g_5) = \begin{pmatrix} 0 & 0 & e_9^7 \\ -e_9^2 & -1 & -1 \\ e_9^2 & 0 & 0 \end{pmatrix}.$$

$$R_{12}(g_2) = \begin{pmatrix} -e_9^2 & e_9^2 + e_9^5 & -e_9^4 \\ e_9^5 & 0 & 0 \\ 0 & 0 & e_9^2 \end{pmatrix}. \quad R_{12}(g_3) = \begin{pmatrix} e_3^2 & 0 & 0 \\ 0 & e_3^2 & 0 \\ 0 & 0 & e_3^2 \end{pmatrix}.$$

$$R_{12}(g_4) = \begin{pmatrix} -1 & -e_3^2 & -e_9^2 \\ 0 & 0 & e_9^5 \\ 0 & e_9^4 & 0 \end{pmatrix}. \quad R_{12}(g_5) = \begin{pmatrix} 0 & 0 & e_9^2 \\ -e_3 & -1 & -e_9^5 \\ e_9^7 & 0 & 0 \end{pmatrix}.$$

 $G_{36}^{(4)}$

$$R_2(g_2) = -1. \quad R_2(g_3) = -1. \quad R_2(g_4) = 1. \quad R_2(g_5) = 1.$$

$$R_3(g_2) = -1. \quad R_3(g_3) = 1. \quad R_3(g_4) = 1. \quad R_3(g_5) = 1.$$

$$R_4(g_2) = 1. \quad R_4(g_3) = -1. \quad R_4(g_4) = 1. \quad R_4(g_5) = 1.$$

$$R_5(g_2) = \phi. \quad R_5(g_3) = \epsilon. \quad R_5(g_4) = \begin{pmatrix} 0 & 1 \\ -1 & -1 \end{pmatrix}. \quad R_5(g_5) = \epsilon.$$

$$R_6(g_2) = \begin{pmatrix} 1 & 0 \\ -1 & -1 \end{pmatrix}. \quad R_6(g_3) = -\epsilon. \quad R_6(g_4) = \begin{pmatrix} 0 & 1 \\ -1 & -1 \end{pmatrix}. \quad R_6(g_5) = \epsilon.$$

$$R_7(g_2) = \begin{pmatrix} (-2e_9^2 - e_9^4 - e_9^5 - 2e_9^7)/3 & -2(\Re e_9^2 + \Re e_{18})/3 \\ (e_9^2 + 2e_9^4 + 2e_9^5 + e_9^7)/3 & (2e_9^2 + e_9^4 + e_9^5 + 2e_9^7)/3 \end{pmatrix}. \quad R_7(g_3) = \epsilon.$$

$$R_7(g_4) = \begin{pmatrix} (e_9^2 - e_9^4 - e_9^5 + e_9^7)/3 & (-e_9^2 - 2e_9^4 - 2e_9^5 - e_9^7)/3 \\ (e_9^2 + 2e_9^4 + 2e_9^5 + e_9^7)/3 & (2e_9^2 + 3e_9^4 + 3e_9^5 + 2e_9^7)/3 \end{pmatrix}. \quad R_7(g_5) = \begin{pmatrix} 0 & 1 \\ -1 & -1 \end{pmatrix}.$$

$$R_8(g_2) = \begin{pmatrix} -1 & e_9^2 + e_9^7 \\ 0 & 1 \end{pmatrix}. \quad R_8(g_3) = \epsilon.$$

$$R_8(g_4) = \begin{pmatrix} -1 & e_9^2 + e_9^7 \\ -e_9^2 - e_9^7 & -e_9^3 + e_9^4 + e_9^5 - e_9^6 \end{pmatrix}. \quad R_8(g_5) = \begin{pmatrix} -e_9^2 - e_9^7 & -e_9^3 + e_9^4 + e_9^5 - e_9^6 \\ e_9^3 - e_9^4 - e_9^5 + e_9^6 & e_9^2 + e_9^3 + e_9^6 + e_9^7 \end{pmatrix}.$$

$$R_9(g_2) = \begin{pmatrix} \Re e_{18}^7 & 1 - 2\Re e_9 + 2\Re e_{18}^2 \\ -1 & -\Re e_{18}^7 \end{pmatrix}. \quad R_9(g_3) = \epsilon.$$

$$R_9(g_4) = \begin{pmatrix} 0 & 1 \\ -1 & -\Re e_{18}^7 \end{pmatrix}. \quad R_9(g_5) = \begin{pmatrix} 1/(2c_{18}) & -1 + 2\Re e_9 - 2\Re e_{18}^2 \\ 1 - 2\Re e_9 + 2\Re e_{18}^2 & \Re e_{18}^7 \end{pmatrix}.$$

$$R_{10}(g_2) = \begin{pmatrix} (-e_9^2 - 2e_9^4 - 2e_9^5 - e_9^7)/3 & -2(\Re e_9^2 + \Re e_{18})/3 \\ (-2e_9^2 - e_9^4 - e_9^5 - 2e_9^7)/3 & (e_9^2 + 2e_9^4 + 2e_9^5 + e_9^7)/3 \end{pmatrix}. \quad R_{10}(g_3) = -\epsilon.$$

$$R_{10}(g_4) = \begin{pmatrix} (e_9^2 - e_9^4 - e_9^5 + e_9^7)/3 & (e_9^2 + 2e_9^4 + 2e_9^5 + e_9^7)/3 \\ (-e_9^2 - 2e_9^4 - 2e_9^5 - e_9^7)/3 & (2e_9^2 + e_9^4 + e_9^5 + 2e_9^7)/3 \end{pmatrix}. \quad R_{10}(g_5) = \begin{pmatrix} 0 & -1 \\ 1 & -1 \end{pmatrix}.$$

$$R_{11}(g_2) = \begin{pmatrix} (e_9^2 + 2e_9^4 + 2e_9^5 + e_9^7)/3 & (2e_9^2 + e_9^4 + e_9^5 + 2e_9^7)/3 \\ (e_9^2 - e_9^4 - e_9^5 + e_9^7)/3 & (-e_9^2 - 2e_9^4 - 2e_9^5 - e_9^7)/3 \end{pmatrix}. \quad R_{11}(g_3) = -\epsilon.$$

$$R_{11}(g_4) = \begin{pmatrix} -2(\Re e_9^2 + \Re e_{18})/3 & (-2e_9^2 - e_9^4 - e_9^5 - 2e_9^7)/3 \\ (2e_9^2 + e_9^4 + e_9^5 + 2e_9^7)/3 & (e_9^2 + 2e_9^4 + 2e_9^5 + e_9^7)/3 \end{pmatrix}. \quad R_{11}(g_5) = \begin{pmatrix} -1 & -1 \\ 1 & 0 \end{pmatrix}.$$

$$R_{12}(g_2) = \begin{pmatrix} (e_9^2 - e_9^4 - e_9^5 + e_9^7)/3 & (e_9^2 + 2e_9^4 + 2e_9^5 + e_9^7)/3 \\ (2e_9^2 + e_9^4 + e_9^5 + 2e_9^7)/3 & -2(\Re e_9^2 + \Re e_{18})/3 \end{pmatrix}. \quad R_{12}(g_3) = -\epsilon.$$

$$R_{12}(g_4) = \begin{pmatrix} (-e_9^2 - 2e_9^4 - 2e_9^5 - e_9^7)/3 & -2(\Re e_9^2 + \Re e_{18})/3 \\ (e_9^2 - e_9^4 - e_9^5 + e_9^7)/3 & (-2e_9^2 - e_9^4 - e_9^5 - 2e_9^7)/3 \end{pmatrix}. \quad R_{12}(g_5) = \begin{pmatrix} -1 & 1 \\ -1 & 0 \end{pmatrix}.$$

$G_{36}^{(5)}$

$$R_2(g_2) = -1. \quad R_2(g_3) = -1. \quad R_2(g_4) = 1. \quad R_2(g_5) = 1.$$

$$R_3(g_2) = -1. \quad R_3(g_3) = 1. \quad R_3(g_4) = 1. \quad R_3(g_5) = 1.$$

$$R_4(g_2) = 1. \quad R_4(g_3) = -1. \quad R_4(g_4) = 1. \quad R_4(g_5) = 1.$$

$$R_5(g_2) = -1. \quad R_5(g_3) = -1. \quad R_5(g_4) = e_3^2. \quad R_5(g_5) = 1.$$

$$R_6(g_2) = -1. \quad R_6(g_3) = -1. \quad R_6(g_4) = e_3. \quad R_6(g_5) = 1.$$

$$R_7(g_2) = -1. \quad R_7(g_3) = -1. \quad R_7(g_4) = -e_9^2 - e_9^5. \quad R_7(g_5) = e_3^2.$$

$$R_8(g_2) = -1. \quad R_8(g_3) = -1. \quad R_8(g_4) = -e_9^4 - e_9^7. \quad R_8(g_5) = e_3.$$

$$R_9(g_2) = -1. \quad R_9(g_3) = -1. \quad R_9(g_4) = e_9^7. \quad R_9(g_5) = e_3.$$

$$R_{10}(g_2) = -1. \quad R_{10}(g_3) = -1. \quad R_{10}(g_4) = e_9^5. \quad R_{10}(g_5) = e_3^2.$$

$$R_{11}(g_2) = -1. \quad R_{11}(g_3) = -1. \quad R_{11}(g_4) = e_9^4. \quad R_{11}(g_5) = e_3.$$

$$R_{12}(g_2) = -1. \quad R_{12}(g_3) = -1. \quad R_{12}(g_4) = e_9^2. \quad R_{12}(g_5) = e_3^2.$$

$$R_{13}(g_2) = -1. \quad R_{13}(g_3) = 1. \quad R_{13}(g_4) = e_3^2. \quad R_{13}(g_5) = 1.$$

$$R_{14}(g_2) = -1. \quad R_{14}(g_3) = 1. \quad R_{14}(g_4) = e_3. \quad R_{14}(g_5) = 1.$$

$$R_{15}(g_2) = -1. \quad R_{15}(g_3) = 1. \quad R_{15}(g_4) = -e_9^2 - e_9^5. \quad R_{15}(g_5) = e_3^2.$$

$$R_{16}(g_2) = -1. \quad R_{16}(g_3) = 1. \quad R_{16}(g_4) = -e_9^4 - e_9^7. \quad R_{16}(g_5) = e_3.$$

$$R_{17}(g_2) = -1. \quad R_{17}(g_3) = 1. \quad R_{17}(g_4) = e_9^7. \quad R_{17}(g_5) = e_3.$$

$$R_{18}(g_2) = -1. \quad R_{18}(g_3) = 1. \quad R_{18}(g_4) = e_9^5. \quad R_{18}(g_5) = e_3^2.$$

$$R_{19}(g_2) = -1. \quad R_{19}(g_3) = 1. \quad R_{19}(g_4) = e_9^4. \quad R_{19}(g_5) = e_3.$$

$$\begin{aligned}
R_{20}(g_2) &= -1. & R_{20}(g_3) &= 1. & R_{20}(g_4) &= e_9^2. & R_{20}(g_5) &= e_3^2. \\
R_{21}(g_2) &= 1. & R_{21}(g_3) &= -1. & R_{21}(g_4) &= e_3^2. & R_{21}(g_5) &= 1. \\
R_{22}(g_2) &= 1. & R_{22}(g_3) &= -1. & R_{22}(g_4) &= e_3. & R_{22}(g_5) &= 1. \\
R_{23}(g_2) &= 1. & R_{23}(g_3) &= -1. & R_{23}(g_4) &= -e_9^2 - e_9^5. & R_{23}(g_5) &= e_3^2. \\
R_{24}(g_2) &= 1. & R_{24}(g_3) &= -1. & R_{24}(g_4) &= -e_9^4 - e_9^7. & R_{24}(g_5) &= e_3. \\
R_{25}(g_2) &= 1. & R_{25}(g_3) &= -1. & R_{25}(g_4) &= e_9^7. & R_{25}(g_5) &= e_3. \\
R_{26}(g_2) &= 1. & R_{26}(g_3) &= -1. & R_{26}(g_4) &= e_9^5. & R_{26}(g_5) &= e_3^2. \\
R_{27}(g_2) &= 1. & R_{27}(g_3) &= -1. & R_{27}(g_4) &= e_9^4. & R_{27}(g_5) &= e_3. \\
R_{28}(g_2) &= 1. & R_{28}(g_3) &= -1. & R_{28}(g_4) &= e_9^2. & R_{28}(g_5) &= e_3^2. \\
R_{29}(g_2) &= 1. & R_{29}(g_3) &= 1. & R_{29}(g_4) &= e_3^2. & R_{29}(g_5) &= 1. \\
R_{30}(g_2) &= 1. & R_{30}(g_3) &= 1. & R_{30}(g_4) &= e_3. & R_{30}(g_5) &= 1. \\
R_{31}(g_2) &= 1. & R_{31}(g_3) &= 1. & R_{31}(g_4) &= -e_9^2 - e_9^5. & R_{31}(g_5) &= e_3^2. \\
R_{32}(g_2) &= 1. & R_{32}(g_3) &= 1. & R_{32}(g_4) &= -e_9^4 - e_9^7. & R_{32}(g_5) &= e_3. \\
R_{33}(g_2) &= 1. & R_{33}(g_3) &= 1. & R_{33}(g_4) &= e_9^7. & R_{33}(g_5) &= e_3. \\
R_{34}(g_2) &= 1. & R_{34}(g_3) &= 1. & R_{34}(g_4) &= e_9^5. & R_{34}(g_5) &= e_3^2. \\
R_{35}(g_2) &= 1. & R_{35}(g_3) &= 1. & R_{35}(g_4) &= e_9^4. & R_{35}(g_5) &= e_3. \\
R_{36}(g_2) &= 1. & R_{36}(g_3) &= 1. & R_{36}(g_4) &= e_9^2. & R_{36}(g_5) &= e_3^2.
\end{aligned}$$

 $G_{36}^{(6)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= 1. & R_2(g_4) &= 1. & R_2(g_5) &= 1. \\
R_3(g_2) &= -1. & R_3(g_3) &= e_3^2. & R_3(g_4) &= 1. & R_3(g_5) &= 1. \\
R_4(g_2) &= -1. & R_4(g_3) &= e_3. & R_4(g_4) &= 1. & R_4(g_5) &= 1. \\
R_5(g_2) &= 1. & R_5(g_3) &= e_3^2. & R_5(g_4) &= 1. & R_5(g_5) &= 1. \\
R_6(g_2) &= 1. & R_6(g_3) &= e_3. & R_6(g_4) &= 1. & R_6(g_5) &= 1. \\
R_7(g_2) &= -i. & R_7(g_3) &= 1. & R_7(g_4) &= -1. & R_7(g_5) &= 1. \\
R_8(g_2) &= i. & R_8(g_3) &= 1. & R_8(g_4) &= -1. & R_8(g_5) &= 1. \\
R_9(g_2) &= -i. & R_9(g_3) &= e_3^2. & R_9(g_4) &= -1. & R_9(g_5) &= 1. \\
R_{10}(g_2) &= -i. & R_{10}(g_3) &= e_3. & R_{10}(g_4) &= -1. & R_{10}(g_5) &= 1. \\
R_{11}(g_2) &= i. & R_{11}(g_3) &= e_3^2. & R_{11}(g_4) &= -1. & R_{11}(g_5) &= 1. \\
R_{12}(g_2) &= i. & R_{12}(g_3) &= e_3. & R_{12}(g_4) &= -1. & R_{12}(g_5) &= 1. \\
R_{13}(g_2) &= \begin{pmatrix} i & 0 \\ -1 & -i \end{pmatrix}. & R_{13}(g_3) &= \epsilon. & R_{13}(g_4) &= -\epsilon. & R_{13}(g_5) &= \begin{pmatrix} 0 & i \\ i & -1 \end{pmatrix}. \\
R_{14}(g_2) &= \phi. & R_{14}(g_3) &= \epsilon. & R_{14}(g_4) &= \epsilon. & R_{14}(g_5) &= \begin{pmatrix} -1 & -1 \\ 1 & 0 \end{pmatrix}. \\
R_{15}(g_2) &= \begin{pmatrix} -i & e_3 \\ 0 & i \end{pmatrix}. & R_{15}(g_3) &= \begin{pmatrix} e_3^2 & 0 \\ 0 & e_3^2 \end{pmatrix}. & R_{15}(g_4) &= -\epsilon. & R_{15}(g_5) &= \begin{pmatrix} -1 & -e_{12}^7 \\ -e_{12}^{11} & 0 \end{pmatrix}. \\
R_{16}(g_2) &= \begin{pmatrix} 0 & -e_3^2 \\ e_3 & 0 \end{pmatrix}. & R_{16}(g_3) &= \begin{pmatrix} e_3 & 0 \\ 0 & e_3 \end{pmatrix}. & R_{16}(g_4) &= -\epsilon. & R_{16}(g_5) &= \begin{pmatrix} 0 & e_{12}^{11} \\ e_{12}^7 & -1 \end{pmatrix}. \\
R_{17}(g_2) &= \begin{pmatrix} -1 & -e_3^2 \\ 0 & 1 \end{pmatrix}. & R_{17}(g_3) &= \begin{pmatrix} e_3^2 & 0 \\ 0 & e_3^2 \end{pmatrix}. & R_{17}(g_4) &= \epsilon. & R_{17}(g_5) &= \begin{pmatrix} -1 & -e_3^2 \\ e_3 & 0 \end{pmatrix}. \\
R_{18}(g_2) &= \begin{pmatrix} 1 & 0 \\ -e_3 & -1 \end{pmatrix}. & R_{18}(g_3) &= \begin{pmatrix} e_3 & 0 \\ 0 & e_3 \end{pmatrix}. & R_{18}(g_4) &= \epsilon. & R_{18}(g_5) &= \begin{pmatrix} -1 & -e_3^2 \\ e_3 & 0 \end{pmatrix}.
\end{aligned}$$

$G_{36}^{(7)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= 1. & R_2(g_4) &= 1. & R_2(g_5) &= 1. \\
R_3(g_2) &= -i. & R_3(g_3) &= -1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. \\
R_4(g_2) &= i. & R_4(g_3) &= -1. & R_4(g_4) &= 1. & R_4(g_5) &= 1. \\
R_5(g_2) &= \phi. & R_5(g_3) &= \epsilon. & R_5(g_4) &= \epsilon. & R_5(g_5) &= \begin{pmatrix} -1 & -1 \\ 1 & 0 \end{pmatrix}. \\
R_6(g_2) &= \begin{pmatrix} i & 0 \\ 1 & -i \end{pmatrix}. & R_6(g_3) &= -\epsilon. & R_6(g_4) &= \epsilon. & R_6(g_5) &= \begin{pmatrix} 0 & -i \\ -i & -1 \end{pmatrix}. \\
R_7(g_2) &= \begin{pmatrix} -1 & -1 \\ 0 & 1 \end{pmatrix}. & R_7(g_3) &= \epsilon. & R_7(g_4) &= \begin{pmatrix} -1 & -1 \\ 1 & 0 \end{pmatrix}. & R_7(g_5) &= \epsilon. \\
R_8(g_2) &= \begin{pmatrix} -i & -i \\ 0 & i \end{pmatrix}. & R_8(g_3) &= -\epsilon. & R_8(g_4) &= \begin{pmatrix} 0 & 1 \\ -1 & -1 \end{pmatrix}. & R_8(g_5) &= \epsilon. \\
R_9(g_2) &= -\kappa. & R_9(g_3) &= -\epsilon. & R_9(g_4) &= \begin{pmatrix} 0 & i \\ i & -1 \end{pmatrix}. & R_9(g_5) &= \begin{pmatrix} 0 & i \\ i & -1 \end{pmatrix}. \\
R_{10}(g_2) &= -\kappa. & R_{10}(g_3) &= -\epsilon. & R_{10}(g_4) &= \begin{pmatrix} -1 & -i \\ -i & 0 \end{pmatrix}. & R_{10}(g_5) &= \begin{pmatrix} 0 & i \\ i & -1 \end{pmatrix}. \\
R_{11}(g_2) &= \begin{pmatrix} -1 & -1 \\ 0 & 1 \end{pmatrix}. & R_{11}(g_3) &= \epsilon. & R_{11}(g_4) &= \begin{pmatrix} 0 & 1 \\ -1 & -1 \end{pmatrix}. & R_{11}(g_5) &= \begin{pmatrix} 0 & 1 \\ -1 & -1 \end{pmatrix}. \\
R_{12}(g_2) &= \begin{pmatrix} -1 & -1 \\ 0 & 1 \end{pmatrix}. & R_{12}(g_3) &= \epsilon. & R_{12}(g_4) &= \begin{pmatrix} 0 & 1 \\ -1 & -1 \end{pmatrix}. & R_{12}(g_5) &= \begin{pmatrix} -1 & -1 \\ 1 & 0 \end{pmatrix}.
\end{aligned}$$

 $G_{36}^{(8)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= 1. & R_2(g_4) &= 1. & R_2(g_5) &= 1. \\
R_3(g_2) &= -1. & R_3(g_3) &= 1. & R_3(g_4) &= e_3^2. & R_3(g_5) &= 1. \\
R_4(g_2) &= -1. & R_4(g_3) &= 1. & R_4(g_4) &= e_3. & R_4(g_5) &= 1. \\
R_5(g_2) &= -1. & R_5(g_3) &= e_3^2. & R_5(g_4) &= 1. & R_5(g_5) &= 1. \\
R_6(g_2) &= -1. & R_6(g_3) &= e_3. & R_6(g_4) &= 1. & R_6(g_5) &= 1. \\
R_7(g_2) &= -1. & R_7(g_3) &= e_3^2. & R_7(g_4) &= e_3^2. & R_7(g_5) &= 1. \\
R_8(g_2) &= -1. & R_8(g_3) &= e_3. & R_8(g_4) &= e_3. & R_8(g_5) &= 1. \\
R_9(g_2) &= -1. & R_9(g_3) &= e_3^2. & R_9(g_4) &= e_3. & R_9(g_5) &= 1. \\
R_{10}(g_2) &= -1. & R_{10}(g_3) &= e_3. & R_{10}(g_4) &= e_3^2. & R_{10}(g_5) &= 1. \\
R_{11}(g_2) &= 1. & R_{11}(g_3) &= 1. & R_{11}(g_4) &= e_3^2. & R_{11}(g_5) &= 1. \\
R_{12}(g_2) &= 1. & R_{12}(g_3) &= 1. & R_{12}(g_4) &= e_3. & R_{12}(g_5) &= 1. \\
R_{13}(g_2) &= 1. & R_{13}(g_3) &= e_3^2. & R_{13}(g_4) &= 1. & R_{13}(g_5) &= 1. \\
R_{14}(g_2) &= 1. & R_{14}(g_3) &= e_3. & R_{14}(g_4) &= 1. & R_{14}(g_5) &= 1. \\
R_{15}(g_2) &= 1. & R_{15}(g_3) &= e_3^2. & R_{15}(g_4) &= e_3^2. & R_{15}(g_5) &= 1. \\
R_{16}(g_2) &= 1. & R_{16}(g_3) &= e_3. & R_{16}(g_4) &= e_3. & R_{16}(g_5) &= 1. \\
R_{17}(g_2) &= 1. & R_{17}(g_3) &= e_3^2. & R_{17}(g_4) &= e_3. & R_{17}(g_5) &= 1. \\
R_{18}(g_2) &= 1. & R_{18}(g_3) &= e_3. & R_{18}(g_4) &= e_3^2. & R_{18}(g_5) &= 1. \\
R_{19}(g_2) &= -i. & R_{19}(g_3) &= 1. & R_{19}(g_4) &= 1. & R_{19}(g_5) &= -1. \\
R_{20}(g_2) &= i. & R_{20}(g_3) &= 1. & R_{20}(g_4) &= 1. & R_{20}(g_5) &= -1. \\
R_{21}(g_2) &= -i. & R_{21}(g_3) &= 1. & R_{21}(g_4) &= e_3^2. & R_{21}(g_5) &= -1.
\end{aligned}$$

$$\begin{aligned}
R_{22}(g_2) &= -i. & R_{22}(g_3) &= 1. & R_{22}(g_4) &= e_3. & R_{22}(g_5) &= -1. \\
R_{23}(g_2) &= i. & R_{23}(g_3) &= 1. & R_{23}(g_4) &= e_3^2. & R_{23}(g_5) &= -1. \\
R_{24}(g_2) &= i. & R_{24}(g_3) &= 1. & R_{24}(g_4) &= e_3. & R_{24}(g_5) &= -1. \\
R_{25}(g_2) &= -i. & R_{25}(g_3) &= e_3^2. & R_{25}(g_4) &= 1. & R_{25}(g_5) &= -1. \\
R_{26}(g_2) &= -i. & R_{26}(g_3) &= e_3. & R_{26}(g_4) &= 1. & R_{26}(g_5) &= -1. \\
R_{27}(g_2) &= i. & R_{27}(g_3) &= e_3^2. & R_{27}(g_4) &= 1. & R_{27}(g_5) &= -1. \\
R_{28}(g_2) &= i. & R_{28}(g_3) &= e_3. & R_{28}(g_4) &= 1. & R_{28}(g_5) &= -1. \\
R_{29}(g_2) &= -i. & R_{29}(g_3) &= e_3^2. & R_{29}(g_4) &= e_3^2. & R_{29}(g_5) &= -1. \\
R_{30}(g_2) &= -i. & R_{30}(g_3) &= e_3. & R_{30}(g_4) &= e_3. & R_{30}(g_5) &= -1. \\
R_{31}(g_2) &= i. & R_{31}(g_3) &= e_3^2. & R_{31}(g_4) &= e_3^2. & R_{31}(g_5) &= -1. \\
R_{32}(g_2) &= i. & R_{32}(g_3) &= e_3. & R_{32}(g_4) &= e_3. & R_{32}(g_5) &= -1. \\
R_{33}(g_2) &= -i. & R_{33}(g_3) &= e_3^2. & R_{33}(g_4) &= e_3. & R_{33}(g_5) &= -1. \\
R_{34}(g_2) &= -i. & R_{34}(g_3) &= e_3. & R_{34}(g_4) &= e_3^2. & R_{34}(g_5) &= -1. \\
R_{35}(g_2) &= i. & R_{35}(g_3) &= e_3^2. & R_{35}(g_4) &= e_3. & R_{35}(g_5) &= -1. \\
R_{36}(g_2) &= i. & R_{36}(g_3) &= e_3. & R_{36}(g_4) &= e_3^2. & R_{36}(g_5) &= -1.
\end{aligned}$$

 $G_{36}^{(9)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= 1. & R_2(g_4) &= 1. & R_2(g_5) &= 1. \\
R_3(g_2) &= -i. & R_3(g_3) &= -1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. \\
R_4(g_2) &= i. & R_4(g_3) &= -1. & R_4(g_4) &= 1. & R_4(g_5) &= 1.
\end{aligned}$$

$$\begin{aligned}
R_5(g_2) &= \begin{pmatrix} -1 & 1 & 1 & 0 \\ -1 & 0 & 0 & -1 \\ 0 & 0 & 1 & 0 \\ 1 & 0 & 0 & 0 \end{pmatrix}. & R_5(g_3) &= \begin{pmatrix} 0 & -1 & 0 & -1 \\ 0 & -1 & -1 & 0 \\ 0 & 0 & 1 & 0 \\ -1 & 1 & 1 & 0 \end{pmatrix}. \\
R_5(g_4) &= \begin{pmatrix} 1 & 0 & -1 & 1 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ -1 & 1 & 1 & 0 \end{pmatrix}. & R_5(g_5) &= \begin{pmatrix} 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \\ 0 & -1 & -1 & 0 \\ -1 & 0 & 0 & -1 \end{pmatrix}.
\end{aligned}$$

$$\begin{aligned}
R_6(g_2) &= \begin{pmatrix} 0 & 0 & 0 & 1 \\ -1 & -1 & 1 & -1 \\ 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \end{pmatrix}. & R_6(g_3) &= \begin{pmatrix} 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ -1 & -1 & 1 & -1 \end{pmatrix}. \\
R_6(g_4) &= \begin{pmatrix} -1 & -1 & 1 & -1 \\ 0 & -1 & 0 & -1 \\ -1 & 0 & 0 & -1 \\ 0 & 1 & 0 & 0 \end{pmatrix}. & R_6(g_5) &= \begin{pmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 1 & 0 & 0 & 0 \\ 1 & 0 & -1 & 1 \end{pmatrix}.
\end{aligned}$$

$G_{36}^{(10)}$

$$R_2(g_2) = -1. \quad R_2(g_3) = -1. \quad R_2(g_4) = 1. \quad R_2(g_5) = 1.$$

$$R_3(g_2) = -1. \quad R_3(g_3) = 1. \quad R_3(g_4) = 1. \quad R_3(g_5) = 1.$$

$$R_4(g_2) = 1. \quad R_4(g_3) = -1. \quad R_4(g_4) = 1. \quad R_4(g_5) = 1.$$

$$R_5(g_2) = -\phi. \quad R_5(g_3) = -\epsilon. \quad R_5(g_4) = \epsilon. \quad R_5(g_5) = \begin{pmatrix} 0 & -1 \\ 1 & -1 \end{pmatrix}.$$

$$R_6(g_2) = \begin{pmatrix} 1 & 0 \\ -1 & -1 \end{pmatrix}. \quad R_6(g_3) = \epsilon. \quad R_6(g_4) = \epsilon. \quad R_6(g_5) = \begin{pmatrix} 0 & 1 \\ -1 & -1 \end{pmatrix}.$$

$$R_7(g_2) = -\epsilon. \quad R_7(g_3) = \phi. \quad R_7(g_4) = \begin{pmatrix} 0 & 1 \\ -1 & -1 \end{pmatrix}. \quad R_7(g_5) = \epsilon.$$

$$R_8(g_2) = \epsilon. \quad R_8(g_3) = \begin{pmatrix} 1 & 0 \\ -1 & -1 \end{pmatrix}. \quad R_8(g_4) = \begin{pmatrix} 0 & 1 \\ -1 & -1 \end{pmatrix}. \quad R_8(g_5) = \epsilon.$$

$$R_9(g_2) = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \\ -e_3^2 & 0 & 0 & -1 \end{pmatrix}. \quad R_9(g_3) = \begin{pmatrix} 0 & -e_3 & -e_3 & 0 \\ 0 & 0 & 0 & 1 \\ -e_3^2 & 0 & 0 & -1 \\ 0 & 1 & 0 & 0 \end{pmatrix}.$$

$$R_9(g_4) = \begin{pmatrix} e_3^2 & 0 & 0 & 0 \\ 0 & e_3 & 0 & 0 \\ 0 & 0 & e_3 & 0 \\ 0 & 0 & 0 & e_3^2 \end{pmatrix}. \quad R_9(g_5) = \begin{pmatrix} -1 & 0 & 0 & -e_3 \\ 0 & -1 & -1 & 0 \\ 0 & 1 & 0 & 0 \\ e_3^2 & 0 & 0 & 0 \end{pmatrix}.$$

 $G_{36}^{(11)}$

$$R_2(g_2) = 1. \quad R_2(g_3) = e_3^2. \quad R_2(g_4) = 1. \quad R_2(g_5) = 1.$$

$$R_3(g_2) = 1. \quad R_3(g_3) = e_3. \quad R_3(g_4) = 1. \quad R_3(g_5) = 1.$$

$$R_4(g_2) = e_3^2. \quad R_4(g_3) = 1. \quad R_4(g_4) = 1. \quad R_4(g_5) = 1.$$

$$R_5(g_2) = e_3. \quad R_5(g_3) = 1. \quad R_5(g_4) = 1. \quad R_5(g_5) = 1.$$

$$R_6(g_2) = e_3^2. \quad R_6(g_3) = e_3^2. \quad R_6(g_4) = 1. \quad R_6(g_5) = 1.$$

$$R_7(g_2) = e_3. \quad R_7(g_3) = e_3. \quad R_7(g_4) = 1. \quad R_7(g_5) = 1.$$

$$R_8(g_2) = e_3^2. \quad R_8(g_3) = e_3. \quad R_8(g_4) = 1. \quad R_8(g_5) = 1.$$

$$R_9(g_2) = e_3. \quad R_9(g_3) = e_3^2. \quad R_9(g_4) = 1. \quad R_9(g_5) = 1.$$

$$R_{10}(g_2) = \begin{pmatrix} -1 & -1 & -1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{pmatrix}. \quad R_{10}(g_3) = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}.$$

$$R_{10}(g_4) = \begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ -1 & -1 & -1 \end{pmatrix}. \quad R_{10}(g_5) = \begin{pmatrix} 0 & 0 & 1 \\ -1 & -1 & -1 \\ 1 & 0 & 0 \end{pmatrix}.$$

$$\begin{aligned}
R_{11}(g_2) &= \begin{pmatrix} -1 & -e_3 & -e_3^2 \\ e_3^2 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix}, & R_{11}(g_3) &= \begin{pmatrix} e_3 & 0 & 0 \\ 0 & e_3 & 0 \\ 0 & 0 & e_3 \end{pmatrix}. \\
R_{11}(g_4) &= \begin{pmatrix} 0 & e_3 & 0 \\ e_3^2 & 0 & 0 \\ -e_3 & -e_3^2 & -1 \end{pmatrix}, & R_{11}(g_5) &= \begin{pmatrix} -1 & -e_3 & -e_3^2 \\ 0 & 0 & e_3 \\ 0 & e_3^2 & 0 \end{pmatrix}. \\
R_{12}(g_2) &= \begin{pmatrix} 0 & e_3 & 0 \\ -e_3^2 & -1 & -1 \\ 0 & 0 & 1 \end{pmatrix}, & R_{12}(g_3) &= \begin{pmatrix} e_3^2 & 0 & 0 \\ 0 & e_3^2 & 0 \\ 0 & 0 & e_3^2 \end{pmatrix}. \\
R_{12}(g_4) &= \begin{pmatrix} 0 & 0 & e_3 \\ -e_3^2 & -1 & -1 \\ e_3^2 & 0 & 0 \end{pmatrix}, & R_{12}(g_5) &= \begin{pmatrix} -1 & -e_3 & -e_3 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix}.
\end{aligned}$$

 $G_{36}^{(12)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= 1. & R_2(g_5) &= 1. \\
R_3(g_2) &= -1. & R_3(g_3) &= 1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. \\
R_4(g_2) &= 1. & R_4(g_3) &= -1. & R_4(g_4) &= 1. & R_4(g_5) &= 1. \\
R_5(g_2) &= -1. & R_5(g_3) &= -1. & R_5(g_4) &= e_3^2. & R_5(g_5) &= 1. \\
R_6(g_2) &= -1. & R_6(g_3) &= -1. & R_6(g_4) &= e_3. & R_6(g_5) &= 1. \\
R_7(g_2) &= -1. & R_7(g_3) &= 1. & R_7(g_4) &= e_3^2. & R_7(g_5) &= 1. \\
R_8(g_2) &= -1. & R_8(g_3) &= 1. & R_8(g_4) &= e_3. & R_8(g_5) &= 1. \\
R_9(g_2) &= 1. & R_9(g_3) &= -1. & R_9(g_4) &= e_3^2. & R_9(g_5) &= 1. \\
R_{10}(g_2) &= 1. & R_{10}(g_3) &= -1. & R_{10}(g_4) &= e_3. & R_{10}(g_5) &= 1. \\
R_{11}(g_2) &= 1. & R_{11}(g_3) &= 1. & R_{11}(g_4) &= e_3^2. & R_{11}(g_5) &= 1. \\
R_{12}(g_2) &= 1. & R_{12}(g_3) &= 1. & R_{12}(g_4) &= e_3. & R_{12}(g_5) &= 1. \\
R_{13}(g_2) &= -\phi. & R_{13}(g_3) &= -\epsilon. & R_{13}(g_4) &= \epsilon. & R_{13}(g_5) &= \begin{pmatrix} 0 & -1 \\ 1 & -1 \end{pmatrix}. \\
R_{14}(g_2) &= \phi. & R_{14}(g_3) &= \epsilon. & R_{14}(g_4) &= \epsilon. & R_{14}(g_5) &= \begin{pmatrix} 0 & 1 \\ -1 & -1 \end{pmatrix}. \\
R_{15}(g_2) &= \begin{pmatrix} 1 & 0 \\ e_3^2 & -1 \end{pmatrix}. & R_{15}(g_3) &= -\epsilon. & R_{15}(g_4) &= \begin{pmatrix} e_3^2 & 0 \\ 0 & e_3^2 \end{pmatrix}. & R_{15}(g_5) &= \begin{pmatrix} 0 & -e_3 \\ e_3^2 & -1 \end{pmatrix}. \\
R_{16}(g_2) &= \begin{pmatrix} -1 & -1 \\ 0 & 1 \end{pmatrix}. & R_{16}(g_3) &= -\epsilon. & R_{16}(g_4) &= \begin{pmatrix} e_3 & 0 \\ 0 & e_3 \end{pmatrix}. & R_{16}(g_5) &= \begin{pmatrix} -1 & -1 \\ 1 & 0 \end{pmatrix}. \\
R_{17}(g_2) &= \begin{pmatrix} 1 & 0 \\ -e_3 & -1 \end{pmatrix}. & R_{17}(g_3) &= \epsilon. & R_{17}(g_4) &= \begin{pmatrix} e_3^2 & 0 \\ 0 & e_3^2 \end{pmatrix}. & R_{17}(g_5) &= \begin{pmatrix} 0 & e_3^2 \\ -e_3 & -1 \end{pmatrix}. \\
R_{18}(g_2) &= \begin{pmatrix} 1 & 0 \\ -e_3 & -1 \end{pmatrix}. & R_{18}(g_3) &= \epsilon. & R_{18}(g_4) &= \begin{pmatrix} e_3 & 0 \\ 0 & e_3 \end{pmatrix}. & R_{18}(g_5) &= \begin{pmatrix} -1 & -e_3^2 \\ e_3 & 0 \end{pmatrix}.
\end{aligned}$$

$G_{36}^{(13)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= 1. & R_2(g_5) &= 1. \\
R_3(g_2) &= -1. & R_3(g_3) &= 1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. \\
R_4(g_2) &= 1. & R_4(g_3) &= -1. & R_4(g_4) &= 1. & R_4(g_5) &= 1. \\
R_5(g_2) &= \phi. & R_5(g_3) &= \epsilon. & R_5(g_4) &= \epsilon. & R_5(g_5) &= \begin{pmatrix} 0 & 1 \\ -1 & -1 \end{pmatrix}. \\
R_6(g_2) &= \phi. & R_6(g_3) &= -\epsilon. & R_6(g_4) &= \epsilon. & R_6(g_5) &= \begin{pmatrix} -1 & -1 \\ 1 & 0 \end{pmatrix}. \\
R_7(g_2) &= \begin{pmatrix} -1 & -1 \\ 0 & 1 \end{pmatrix}. & R_7(g_3) &= \epsilon. & R_7(g_4) &= \begin{pmatrix} 0 & 1 \\ -1 & -1 \end{pmatrix}. & R_7(g_5) &= \epsilon. \\
R_8(g_2) &= -\phi. & R_8(g_3) &= -\epsilon. & R_8(g_4) &= \begin{pmatrix} 0 & -1 \\ 1 & -1 \end{pmatrix}. & R_8(g_5) &= \epsilon. \\
R_9(g_2) &= \phi. & R_9(g_3) &= -\epsilon. & R_9(g_4) &= \begin{pmatrix} 0 & 1 \\ -1 & -1 \end{pmatrix}. & R_9(g_5) &= \begin{pmatrix} 0 & 1 \\ -1 & -1 \end{pmatrix}. \\
R_{10}(g_2) &= \phi. & R_{10}(g_3) &= -\epsilon. & R_{10}(g_4) &= \begin{pmatrix} 0 & 1 \\ -1 & -1 \end{pmatrix}. & R_{10}(g_5) &= \begin{pmatrix} -1 & -1 \\ 1 & 0 \end{pmatrix}. \\
R_{11}(g_2) &= \phi. & R_{11}(g_3) &= \epsilon. & R_{11}(g_4) &= \begin{pmatrix} -1 & -1 \\ 1 & 0 \end{pmatrix}. & R_{11}(g_5) &= \begin{pmatrix} -1 & -1 \\ 1 & 0 \end{pmatrix}. \\
R_{12}(g_2) &= \begin{pmatrix} -1 & -1 \\ 0 & 1 \end{pmatrix}. & R_{12}(g_3) &= \epsilon. & R_{12}(g_4) &= \begin{pmatrix} -1 & -1 \\ 1 & 0 \end{pmatrix}. & R_{12}(g_5) &= \begin{pmatrix} 0 & 1 \\ -1 & -1 \end{pmatrix}.
\end{aligned}$$

 $G_{36}^{(14)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= 1. & R_2(g_5) &= 1. \\
R_3(g_2) &= -1. & R_3(g_3) &= 1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. \\
R_4(g_2) &= 1. & R_4(g_3) &= -1. & R_4(g_4) &= 1. & R_4(g_5) &= 1. \\
R_5(g_2) &= -1. & R_5(g_3) &= -1. & R_5(g_4) &= 1. & R_5(g_5) &= e_3^2. \\
R_6(g_2) &= -1. & R_6(g_3) &= -1. & R_6(g_4) &= 1. & R_6(g_5) &= e_3. \\
R_7(g_2) &= -1. & R_7(g_3) &= -1. & R_7(g_4) &= e_3^2. & R_7(g_5) &= 1. \\
R_8(g_2) &= -1. & R_8(g_3) &= -1. & R_8(g_4) &= e_3. & R_8(g_5) &= 1. \\
R_9(g_2) &= -1. & R_9(g_3) &= -1. & R_9(g_4) &= e_3^2. & R_9(g_5) &= e_3^2. \\
R_{10}(g_2) &= -1. & R_{10}(g_3) &= -1. & R_{10}(g_4) &= e_3. & R_{10}(g_5) &= e_3. \\
R_{11}(g_2) &= -1. & R_{11}(g_3) &= -1. & R_{11}(g_4) &= e_3^2. & R_{11}(g_5) &= e_3. \\
R_{12}(g_2) &= -1. & R_{12}(g_3) &= -1. & R_{12}(g_4) &= e_3. & R_{12}(g_5) &= e_3^2. \\
R_{13}(g_2) &= -1. & R_{13}(g_3) &= 1. & R_{13}(g_4) &= 1. & R_{13}(g_5) &= e_3^2. \\
R_{14}(g_2) &= -1. & R_{14}(g_3) &= 1. & R_{14}(g_4) &= 1. & R_{14}(g_5) &= e_3. \\
R_{15}(g_2) &= -1. & R_{15}(g_3) &= 1. & R_{15}(g_4) &= e_3^2. & R_{15}(g_5) &= 1. \\
R_{16}(g_2) &= -1. & R_{16}(g_3) &= 1. & R_{16}(g_4) &= e_3. & R_{16}(g_5) &= 1. \\
R_{17}(g_2) &= -1. & R_{17}(g_3) &= 1. & R_{17}(g_4) &= e_3^2. & R_{17}(g_5) &= e_3^2. \\
R_{18}(g_2) &= -1. & R_{18}(g_3) &= 1. & R_{18}(g_4) &= e_3. & R_{18}(g_5) &= e_3. \\
R_{19}(g_2) &= -1. & R_{19}(g_3) &= 1. & R_{19}(g_4) &= e_3^2. & R_{19}(g_5) &= e_3. \\
R_{20}(g_2) &= -1. & R_{20}(g_3) &= 1. & R_{20}(g_4) &= e_3. & R_{20}(g_5) &= e_3^2. \\
R_{21}(g_2) &= 1. & R_{21}(g_3) &= -1. & R_{21}(g_4) &= 1. & R_{21}(g_5) &= e_3^2.
\end{aligned}$$

$$\begin{aligned}
R_{22}(g_2) &= 1. & R_{22}(g_3) &= -1. & R_{22}(g_4) &= 1. & R_{22}(g_5) &= e_3. \\
R_{23}(g_2) &= 1. & R_{23}(g_3) &= -1. & R_{23}(g_4) &= e_3^2. & R_{23}(g_5) &= 1. \\
R_{24}(g_2) &= 1. & R_{24}(g_3) &= -1. & R_{24}(g_4) &= e_3. & R_{24}(g_5) &= 1. \\
R_{25}(g_2) &= 1. & R_{25}(g_3) &= -1. & R_{25}(g_4) &= e_3^2. & R_{25}(g_5) &= e_3^2. \\
R_{26}(g_2) &= 1. & R_{26}(g_3) &= -1. & R_{26}(g_4) &= e_3. & R_{26}(g_5) &= e_3. \\
R_{27}(g_2) &= 1. & R_{27}(g_3) &= -1. & R_{27}(g_4) &= e_3^2. & R_{27}(g_5) &= e_3. \\
R_{28}(g_2) &= 1. & R_{28}(g_3) &= -1. & R_{28}(g_4) &= e_3. & R_{28}(g_5) &= e_3^2. \\
R_{29}(g_2) &= 1. & R_{29}(g_3) &= 1. & R_{29}(g_4) &= 1. & R_{29}(g_5) &= e_3^2. \\
R_{30}(g_2) &= 1. & R_{30}(g_3) &= 1. & R_{30}(g_4) &= 1. & R_{30}(g_5) &= e_3. \\
R_{31}(g_2) &= 1. & R_{31}(g_3) &= 1. & R_{31}(g_4) &= e_3^2. & R_{31}(g_5) &= 1. \\
R_{32}(g_2) &= 1. & R_{32}(g_3) &= 1. & R_{32}(g_4) &= e_3. & R_{32}(g_5) &= 1. \\
R_{33}(g_2) &= 1. & R_{33}(g_3) &= 1. & R_{33}(g_4) &= e_3^2. & R_{33}(g_5) &= e_3^2. \\
R_{34}(g_2) &= 1. & R_{34}(g_3) &= 1. & R_{34}(g_4) &= e_3. & R_{34}(g_5) &= e_3. \\
R_{35}(g_2) &= 1. & R_{35}(g_3) &= 1. & R_{35}(g_4) &= e_3^2. & R_{35}(g_5) &= e_3. \\
R_{36}(g_2) &= 1. & R_{36}(g_3) &= 1. & R_{36}(g_4) &= e_3. & R_{36}(g_5) &= e_3^2.
\end{aligned}$$

2.37. **Order 37.** $G_{37}^{(1)}$

$$R_j(g_2) = e_{37}^{j-1}, \quad j = 1, \dots, 37.$$

2.38. **Order 38.** $G_{38}^{(1)}$

$$R_2(g_2) = -1. \quad R_2(g_3) = 1.$$

$$\begin{aligned}
R_3(g_2) &= \begin{pmatrix} & & & \alpha_{38,1} & & & & & \alpha_{38,1} \\ -e_{19} - e_{19}^4 - e_{19}^6 - e_{19}^8 - e_{19}^{11} - e_{19}^{13} - e_{19}^{15} - e_{19}^{18} & & & & & & & & -\alpha_{38,1} \end{pmatrix}. \\
R_3(g_3) &= \begin{pmatrix} e_{19}^6 + e_{19}^{13} & -1 \\ 1 & 0 \end{pmatrix}.
\end{aligned}$$

Constants:

$$\alpha_{38,1} \equiv e_{19} + e_{19}^3 + e_{19}^4 + e_{19}^6 + e_{19}^8 + e_{19}^{11} + e_{19}^{13} + e_{19}^{15} + e_{19}^{16} + e_{19}^{18}.$$

$$\begin{aligned}
R_4(g_2) &= \begin{pmatrix} e_{19}^5 + e_{19}^8 + e_{19}^{11} + e_{19}^{14} & & \alpha_{38,2} \\ \alpha_{38,3} & & -e_{19}^5 - e_{19}^8 - e_{19}^{11} - e_{19}^{14} \end{pmatrix}. \\
R_4(g_3) &= \begin{pmatrix} e_{19}^2 + e_{19}^5 + e_{19}^8 + e_{19}^{11} + e_{19}^{14} + e_{19}^{17} & & -\alpha_{38,3} \\ \alpha_{38,3} & & -e_{19}^5 - e_{19}^8 - e_{19}^{11} - e_{19}^{14} \end{pmatrix}.
\end{aligned}$$

Constants:

$$\alpha_{38,2} \equiv e_{19} + e_{19}^2 + e_{19}^4 + e_{19}^5 + e_{19}^6 + e_{19}^7 + e_{19}^8 + e_{19}^9 + e_{19}^{10} + e_{19}^{11} + e_{19}^{12} + e_{19}^{13} + e_{19}^{14} + e_{19}^{15} + e_{19}^{17} + e_{19}^{18};$$

$$\alpha_{38,3} \equiv -e_{19} - e_{19}^2 - e_{19}^4 - e_{19}^5 - e_{19}^7 - e_{19}^8 - e_{19}^9 - e_{19}^{10} - e_{19}^{11} - e_{19}^{12} - e_{19}^{14} - e_{19}^{15} - e_{19}^{17} - e_{19}^{18}.$$

$$R_5(g_2) = \begin{pmatrix} -e_{19}^2 - e_{19}^6 - e_{19}^{13} - e_{19}^{17} & \alpha_{38,4} \\ \alpha_{38,5} & e_{19}^2 + e_{19}^6 + e_{19}^{13} + e_{19}^{17} \end{pmatrix}.$$

$$R_5(g_3) = \begin{pmatrix} -\alpha_{38,4} & \alpha_{38,6} \\ -\alpha_{38,6} & -e_{19} - e_{19}^2 - e_{19}^3 - e_{19}^5 - e_{19}^6 - e_{19}^9 - e_{19}^{10} - e_{19}^{13} - e_{19}^{14} - e_{19}^{16} - e_{19}^{17} - e_{19}^{18} \end{pmatrix}.$$

Constants:

$$\alpha_{38,4} \equiv -e_{19} - e_{19}^2 - e_{19}^3 - e_{19}^5 - e_{19}^6 - e_{19}^7 - e_{19}^9 - e_{19}^{10} - e_{19}^{12} - e_{19}^{13} - e_{19}^{14} - e_{19}^{16} - e_{19}^{17} - e_{19}^{18};$$

$$\alpha_{38,5} \equiv e_{19} + e_{19}^2 + e_{19}^3 + e_{19}^5 + e_{19}^6 + e_{19}^7 + e_{19}^8 + e_{19}^9 + e_{19}^{10} + e_{19}^{11} + e_{19}^{12} + e_{19}^{13} + e_{19}^{14} + e_{19}^{16} + e_{19}^{17} + e_{19}^{18};$$

$$\alpha_{38,6} \equiv e_{19}^2 + e_{19}^6 + e_{19}^9 + e_{19}^{10} + e_{19}^{13} + e_{19}^{17}.$$

$$R_6(g_2) = \begin{pmatrix} -1 & e_{19}^7 + e_{19}^{12} \\ 0 & 1 \end{pmatrix}, \quad R_6(g_3) = \begin{pmatrix} -1 & e_{19}^7 + e_{19}^{12} \\ -e_{19}^7 - e_{19}^{12} & \alpha_{38,7} \end{pmatrix}.$$

Constants:

$$\alpha_{38,7} \equiv -e_{19} - e_{19}^2 - e_{19}^3 - e_{19}^4 - e_{19}^6 - e_{19}^7 - e_{19}^8 - e_{19}^9 - e_{19}^{10} - e_{19}^{11} - e_{19}^{12} - e_{19}^{13} - e_{19}^{15} - e_{19}^{16} - e_{19}^{17} - e_{19}^{18}.$$

$$R_7(g_2) = \begin{pmatrix} -e_{19}^8 - e_{19}^9 - e_{19}^{10} - e_{19}^{11} & \alpha_{38,8} \\ \alpha_{38,9} & e_{19}^8 + e_{19}^9 + e_{19}^{10} + e_{19}^{11} \end{pmatrix}.$$

$$R_7(g_3) = \begin{pmatrix} -e_{19}^5 - e_{19}^6 - e_{19}^7 - e_{19}^8 - e_{19}^9 - e_{19}^{10} - e_{19}^{11} - e_{19}^{12} - e_{19}^{13} - e_{19}^{14} & \alpha_{38,10} \\ -\alpha_{38,10} & \alpha_{38,11} \end{pmatrix}.$$

Constants:

$$\alpha_{38,8} \equiv -e_{19}^3 - e_{19}^4 - e_{19}^5 - e_{19}^6 - e_{19}^7 - e_{19}^8 - e_{19}^9 - e_{19}^{10} - e_{19}^{11} - e_{19}^{12} - e_{19}^{13} - e_{19}^{14} - e_{19}^{15} - e_{19}^{16};$$

$$\alpha_{38,9} \equiv e_{19}^2 + e_{19}^3 + e_{19}^4 + e_{19}^5 + e_{19}^6 + e_{19}^7 + e_{19}^8 + e_{19}^9 + e_{19}^{10} + e_{19}^{11} + e_{19}^{12} + e_{19}^{13} + e_{19}^{14} + e_{19}^{15} + e_{19}^{16} + e_{19}^{17};$$

$$\alpha_{38,10} \equiv -e_{19}^6 - e_{19}^7 - e_{19}^8 - e_{19}^9 - e_{19}^{10} - e_{19}^{11} - e_{19}^{12} - e_{19}^{13};$$

$$\alpha_{38,11} \equiv e_{19}^4 + e_{19}^5 + e_{19}^6 + e_{19}^7 + e_{19}^8 + e_{19}^9 + e_{19}^{10} + e_{19}^{11} + e_{19}^{12} + e_{19}^{13} + e_{19}^{14} + e_{19}^{15}.$$

$$R_8(g_2) = \begin{pmatrix} -e_{19}^3 - e_{19}^{16} & \alpha_{38,12} \\ -1 & e_{19}^3 + e_{19}^{16} \end{pmatrix}.$$

$$R_8(g_3) = \begin{pmatrix} -e_{19}^2 - e_{19}^3 - e_{19}^4 - e_{19}^9 - e_{19}^{10} - e_{19}^{15} - e_{19}^{16} - e_{19}^{17} & \alpha_{38,13} \\ -\alpha_{38,13} & -\alpha_{38,13} \end{pmatrix}.$$

Constants:

$$\alpha_{38,12} \equiv -e_{19} - e_{19}^2 - e_{19}^3 - e_{19}^4 - e_{19}^5 - e_{19}^7 - e_{19}^8 - e_{19}^9 - e_{19}^{10} - e_{19}^{11} - e_{19}^{12} - e_{19}^{14} - e_{19}^{15} - e_{19}^{16} - e_{19}^{17} - e_{19}^{18};$$

$$\alpha_{38,13} \equiv -e_{19}^2 - e_{19}^3 - e_{19}^4 - e_{19}^8 - e_{19}^9 - e_{19}^{10} - e_{19}^{11} - e_{19}^{15} - e_{19}^{16} - e_{19}^{17}.$$

$$R_9(g_2) = \begin{pmatrix} \alpha_{38,14} & e_{19}^2 + e_{19}^3 + e_{19}^7 + e_{19}^{12} + e_{19}^{16} + e_{19}^{17} \\ -e_{19}^2 - e_{19}^7 - e_{19}^{12} - e_{19}^{17} & -\alpha_{38,14} \end{pmatrix}.$$

$$R_9(g_3) = \begin{pmatrix} \alpha_{38,15} & \alpha_{38,16} \\ -\alpha_{38,16} & -e_{19}^2 - e_{19}^3 - e_{19}^6 - e_{19}^7 - e_{19}^8 - e_{19}^{11} - e_{19}^{12} - e_{19}^{13} - e_{19}^{16} - e_{19}^{17} \end{pmatrix}.$$

Constants:

$$\alpha_{38,14} \equiv e_{19} + e_{19}^2 + e_{19}^3 + e_{19}^4 + e_{19}^6 + e_{19}^7 + e_{19}^8 + e_{19}^{11} + e_{19}^{12} + e_{19}^{13} + e_{19}^{15} + e_{19}^{16} + e_{19}^{17} + e_{19}^{18};$$

$$\begin{aligned}\alpha_{38,15} &\equiv e_{19} + e_{19}^2 + e_{19}^3 + e_{19}^6 + e_{19}^7 + e_{19}^8 + e_{19}^{11} + e_{19}^{12} + e_{19}^{13} + e_{19}^{16} + e_{19}^{17} + e_{19}^{18}; \\ \alpha_{38,16} &\equiv e_{19}^2 + e_{19}^3 + e_{19}^7 + e_{19}^8 + e_{19}^{11} + e_{19}^{12} + e_{19}^{16} + e_{19}^{17}.\end{aligned}$$

$$\begin{aligned}R_{10}(g_2) &= \begin{pmatrix} -\alpha_{38,8} & e_{19}^7 + e_{19}^8 + e_{19}^9 + e_{19}^{10} + e_{19}^{11} + e_{19}^{12} \\ -e_{19}^8 - e_{19}^9 - e_{19}^{10} - e_{19}^{11} & \alpha_{38,8} \end{pmatrix}. \\ R_{10}(g_3) &= \begin{pmatrix} 0 & 1 \\ -1 & e_{19}^9 + e_{19}^{10} \end{pmatrix}.\end{aligned}$$

$$R_{11}(g_2) = \begin{pmatrix} -e_{19}^5 - e_{19}^{14} & \alpha_{38,16} \\ -1 & e_{19}^5 + e_{19}^{14} \end{pmatrix}.$$

$$R_{11}(g_3) = \begin{pmatrix} e_{19}^3 + e_{19}^4 + e_{19}^5 + e_{19}^6 + e_{19}^{13} + e_{19}^{14} + e_{19}^{15} + e_{19}^{16} & \alpha_{38,17} \\ -\alpha_{38,17} & -e_{19}^4 - e_{19}^5 - e_{19}^6 - e_{19}^{13} - e_{19}^{14} - e_{19}^{15} \end{pmatrix}.$$

Constants:

$$\begin{aligned}\alpha_{38,16} &\equiv -e_{19} - e_{19}^2 - e_{19}^3 - e_{19}^4 - e_{19}^5 - e_{19}^6 - e_{19}^7 - e_{19}^8 - e_{19}^{11} - e_{19}^{12} - e_{19}^{13} - e_{19}^{14} - e_{19}^{15} - e_{19}^{16} - e_{19}^{17} - e_{19}^{18}; \\ \alpha_{38,17} &\equiv e_{19}^2 + e_{19}^3 + e_{19}^4 + e_{19}^5 + e_{19}^6 + e_{19}^7 + e_{19}^{12} + e_{19}^{13} + e_{19}^{14} + e_{19}^{15} + e_{19}^{16} + e_{19}^{17}.\end{aligned}$$

$G_{38}^{(2)}$

$$\begin{aligned}R_2(g_2) &= -1. & R_2(g_3) &= 1. \\ R_3(g_2) &= -1. & R_3(g_3) &= e_{19}^{18}. \\ R_4(g_2) &= -1. & R_4(g_3) &= e_{19}^{17}. \\ R_5(g_2) &= -1. & R_5(g_3) &= e_{19}^{16}. \\ R_6(g_2) &= -1. & R_6(g_3) &= e_{19}^{15}. \\ R_7(g_2) &= -1. & R_7(g_3) &= e_{19}^{14}. \\ R_8(g_2) &= -1. & R_8(g_3) &= e_{19}^{13}. \\ R_9(g_2) &= -1. & R_9(g_3) &= e_{19}^{12}. \\ R_{10}(g_2) &= -1. & R_{10}(g_3) &= e_{19}^{11}. \\ R_{11}(g_2) &= -1. & R_{11}(g_3) &= e_{19}^{10}. \\ R_{12}(g_2) &= -1. & R_{12}(g_3) &= e_{19}^9. \\ R_{13}(g_2) &= -1. & R_{13}(g_3) &= e_{19}^8. \\ R_{14}(g_2) &= -1. & R_{14}(g_3) &= e_{19}^7. \\ R_{15}(g_2) &= -1. & R_{15}(g_3) &= e_{19}^6. \\ R_{16}(g_2) &= -1. & R_{16}(g_3) &= e_{19}^5. \\ R_{17}(g_2) &= -1. & R_{17}(g_3) &= e_{19}^4. \\ R_{18}(g_2) &= -1. & R_{18}(g_3) &= e_{19}^3. \\ R_{19}(g_2) &= -1. & R_{19}(g_3) &= e_{19}^2. \\ R_{20}(g_2) &= -1. & R_{20}(g_3) &= e_{19}. \\ R_{21}(g_2) &= 1. & R_{21}(g_3) &= e_{19}^{18}. \\ R_{22}(g_2) &= 1. & R_{22}(g_3) &= e_{19}^{17}. \\ R_{23}(g_2) &= 1. & R_{23}(g_3) &= e_{19}^{16}. \\ R_{24}(g_2) &= 1. & R_{24}(g_3) &= e_{19}^{15}.\end{aligned}$$

$$\begin{aligned}
 R_{25}(g_2) &= 1. & R_{25}(g_3) &= e_{19}^{14}. \\
 R_{26}(g_2) &= 1. & R_{26}(g_3) &= e_{19}^{13}. \\
 R_{27}(g_2) &= 1. & R_{27}(g_3) &= e_{19}^{12}. \\
 R_{28}(g_2) &= 1. & R_{28}(g_3) &= e_{19}^{11}. \\
 R_{29}(g_2) &= 1. & R_{29}(g_3) &= e_{19}^{10}. \\
 R_{30}(g_2) &= 1. & R_{30}(g_3) &= e_{19}^9. \\
 R_{31}(g_2) &= 1. & R_{31}(g_3) &= e_{19}^8. \\
 R_{32}(g_2) &= 1. & R_{32}(g_3) &= e_{19}^7. \\
 R_{33}(g_2) &= 1. & R_{33}(g_3) &= e_{19}^6. \\
 R_{34}(g_2) &= 1. & R_{34}(g_3) &= e_{19}^5. \\
 R_{35}(g_2) &= 1. & R_{35}(g_3) &= e_{19}^4. \\
 R_{36}(g_2) &= 1. & R_{36}(g_3) &= e_{19}^3. \\
 R_{37}(g_2) &= 1. & R_{37}(g_3) &= e_{19}^2. \\
 R_{38}(g_2) &= 1. & R_{38}(g_3) &= e_{19}.
 \end{aligned}$$

2.39. Order 39. $G_{39}^{(1)}$

$$\begin{aligned}
 R_2(g_2) &= e_3^2. & R_2(g_3) &= 1. \\
 R_3(g_2) &= e_3. & R_3(g_3) &= 1.
 \end{aligned}$$

$$\begin{aligned}
 R_4(g_2) &= \begin{pmatrix} -e_{13}^7 - e_{13}^8 - e_{13}^{11} & \alpha_{39,1} & \alpha_{39,2} \\ e_{13}^7 + e_{13}^8 + e_{13}^{11} & 1 & -e_{13}^2 - e_{13}^5 - e_{13}^6 \\ \alpha_{39,2} & -e_{13}^2 - e_{13}^5 - e_{13}^6 & \alpha_{39,1} \end{pmatrix}. \\
 R_4(g_3) &= \begin{pmatrix} \alpha_{39,3} & \alpha_{39,2} & -e_{13}^4 - 2e_{13}^7 - 2e_{13}^8 - e_{13}^{10} - 2e_{13}^{11} - e_{13}^{12} \\ -e_{13}^2 - e_{13}^5 - e_{13}^6 & e_{13} + e_{13}^2 + e_{13}^3 + e_{13}^5 + e_{13}^6 + e_{13}^9 & -\alpha_{39,1} \\ \alpha_{39,2} & -e_{13}^2 - e_{13}^5 - e_{13}^6 & \alpha_{39,1} \end{pmatrix}.
 \end{aligned}$$

Constants:

$$\begin{aligned}
 \alpha_{39,1} &\equiv e_{13} + e_{13}^2 + e_{13}^3 + e_{13}^4 + e_{13}^5 + e_{13}^6 + 2e_{13}^7 + 2e_{13}^8 + e_{13}^9 + e_{13}^{10} + 2e_{13}^{11} + e_{13}^{12}; \\
 \alpha_{39,2} &\equiv e_{13} + 2e_{13}^2 + e_{13}^3 + e_{13}^4 + 2e_{13}^5 + 2e_{13}^6 + e_{13}^7 + e_{13}^8 + e_{13}^9 + e_{13}^{10} + e_{13}^{11} + e_{13}^{12}; \\
 \alpha_{39,3} &\equiv -e_{13} - 2e_{13}^2 - e_{13}^3 - e_{13}^4 - 2e_{13}^5 - 2e_{13}^6 - 2e_{13}^7 - 2e_{13}^8 - e_{13}^9 - e_{13}^{10} - 2e_{13}^{11} - e_{13}^{12}.
 \end{aligned}$$

$$\begin{aligned}
 R_5(g_2) &= \begin{pmatrix} -e_{13}^4 - e_{13}^{10} - e_{13}^{12} & e_{13} + e_{13}^3 + e_{13}^9 & 1 \\ \alpha_{39,4} & \alpha_{39,5} & -e_{13}^4 - e_{13}^{10} - e_{13}^{12} \\ 0 & 0 & 1 \end{pmatrix}. \\
 R_5(g_3) &= \begin{pmatrix} \alpha_{39,4} & \alpha_{39,5} & -e_{13}^4 - e_{13}^{10} - e_{13}^{12} \\ \alpha_{39,7} & \alpha_{39,6} & \alpha_{39,5} \\ -\alpha_{39,4} & -e_{13}^4 - e_{13}^{10} - e_{13}^{12} & e_{13}^2 + e_{13}^4 + e_{13}^5 + e_{13}^6 + e_{13}^{10} + e_{13}^{12} \end{pmatrix}.
 \end{aligned}$$

Constants:

$$\begin{aligned}
 \alpha_{39,4} &\equiv 2e_{13} + e_{13}^2 + 2e_{13}^3 + e_{13}^4 + e_{13}^5 + e_{13}^6 + e_{13}^7 + e_{13}^8 + 2e_{13}^9 + e_{13}^{10} + e_{13}^{11} + e_{13}^{12}; \\
 \alpha_{39,5} &\equiv e_{13} + e_{13}^2 + e_{13}^3 + 2e_{13}^4 + e_{13}^5 + e_{13}^6 + e_{13}^7 + e_{13}^8 + e_{13}^9 + 2e_{13}^{10} + e_{13}^{11} + 2e_{13}^{12}; \\
 \alpha_{39,6} &\equiv -2e_{13} - e_{13}^2 - 2e_{13}^3 - 2e_{13}^4 - e_{13}^5 - e_{13}^6 - e_{13}^7 - e_{13}^8 - 2e_{13}^9 - 2e_{13}^{10} - e_{13}^{11} - 2e_{13}^{12};
 \end{aligned}$$

$$\alpha_{39,7} \equiv -2e_{13} - 2e_{13}^3 - e_{13}^7 - e_{13}^8 - 2e_{13}^9 - e_{13}^{11}.$$

$$R_6(g_2) = \begin{pmatrix} -\alpha_{39,6} & e_{13}^2 + e_{13}^4 + e_{13}^5 + e_{13}^6 + e_{13}^{10} + e_{13}^{12} & e_{13} + e_{13}^3 + e_{13}^9 \\ \alpha_{39,7} & \alpha_{39,6} & \alpha_{39,5} \\ 1 & 0 & 0 \end{pmatrix}.$$

$$R_6(g_3) = \begin{pmatrix} 0 & 0 & 1 \\ 1 & 0 & 0 \\ -e_{13} - e_{13}^3 - e_{13}^9 & 1 & e_{13}^4 + e_{13}^{10} + e_{13}^{12} \end{pmatrix}.$$

$$R_7(g_2) = \begin{pmatrix} -e_{13} - e_{13}^3 - e_{13}^9 & 1 & e_{13}^4 + e_{13}^{10} + e_{13}^{12} \\ 0 & 1 & 0 \\ \alpha_{39,5} & -e_{13} - e_{13}^3 - e_{13}^9 & \alpha_{39,4} \end{pmatrix}.$$

$$R_7(g_3) = \begin{pmatrix} -e_{13}^2 - 2e_{13}^4 - e_{13}^5 - e_{13}^6 - 2e_{13}^{10} - 2e_{13}^{12} & \alpha_{39,4} & \alpha_{39,6} \\ \alpha_{39,5} & -e_{13} - e_{13}^3 - e_{13}^9 & \alpha_{39,4} \\ \alpha_{39,7} & \alpha_{39,6} & \alpha_{39,5} \end{pmatrix}.$$

 $G_{39}^{(2)}$

$$\begin{aligned} R_2(g_2) &= 1. & R_2(g_3) &= e_{13}^{12}. \\ R_3(g_2) &= 1. & R_3(g_3) &= e_{13}^{11}. \\ R_4(g_2) &= 1. & R_4(g_3) &= e_{13}^{10}. \\ R_5(g_2) &= 1. & R_5(g_3) &= e_{13}^9. \\ R_6(g_2) &= 1. & R_6(g_3) &= e_{13}^8. \\ R_7(g_2) &= 1. & R_7(g_3) &= e_{13}^7. \\ R_8(g_2) &= 1. & R_8(g_3) &= e_{13}^6. \\ R_9(g_2) &= 1. & R_9(g_3) &= e_{13}^5. \\ R_{10}(g_2) &= 1. & R_{10}(g_3) &= e_{13}^4. \\ R_{11}(g_2) &= 1. & R_{11}(g_3) &= e_{13}^3. \\ R_{12}(g_2) &= 1. & R_{12}(g_3) &= e_{13}^2. \\ R_{13}(g_2) &= 1. & R_{13}(g_3) &= e_{13}. \\ R_{14}(g_2) &= e_3^2. & R_{14}(g_3) &= 1. \\ R_{15}(g_2) &= e_3. & R_{15}(g_3) &= 1. \\ R_{16}(g_2) &= e_3^2. & R_{16}(g_3) &= e_{13}^{12}. \\ R_{17}(g_2) &= e_3^2. & R_{17}(g_3) &= e_{13}^{11}. \\ R_{18}(g_2) &= e_3^2. & R_{18}(g_3) &= e_{13}^{10}. \\ R_{19}(g_2) &= e_3^2. & R_{19}(g_3) &= e_{13}^9. \\ R_{20}(g_2) &= e_3^2. & R_{20}(g_3) &= e_{13}^8. \\ R_{21}(g_2) &= e_3^2. & R_{21}(g_3) &= e_{13}^7. \\ R_{22}(g_2) &= e_3^2. & R_{22}(g_3) &= e_{13}^6. \\ R_{23}(g_2) &= e_3^2. & R_{23}(g_3) &= e_{13}^5. \\ R_{24}(g_2) &= e_3^2. & R_{24}(g_3) &= e_{13}^4. \\ R_{25}(g_2) &= e_3^2. & R_{25}(g_3) &= e_{13}^3. \end{aligned}$$

$$\begin{aligned}
R_{26}(g_2) &= e_3^2. & R_{26}(g_3) &= e_{13}^2. \\
R_{27}(g_2) &= e_3^2. & R_{27}(g_3) &= e_{13}. \\
R_{28}(g_2) &= e_3. & R_{28}(g_3) &= e_{13}^{12}. \\
R_{29}(g_2) &= e_3. & R_{29}(g_3) &= e_{13}^{11}. \\
R_{30}(g_2) &= e_3. & R_{30}(g_3) &= e_{13}^{10}. \\
R_{31}(g_2) &= e_3. & R_{31}(g_3) &= e_{13}^9. \\
R_{32}(g_2) &= e_3. & R_{32}(g_3) &= e_{13}^8. \\
R_{33}(g_2) &= e_3. & R_{33}(g_3) &= e_{13}^7. \\
R_{34}(g_2) &= e_3. & R_{34}(g_3) &= e_{13}^6. \\
R_{35}(g_2) &= e_3. & R_{35}(g_3) &= e_{13}^5. \\
R_{36}(g_2) &= e_3. & R_{36}(g_3) &= e_{13}^4. \\
R_{37}(g_2) &= e_3. & R_{37}(g_3) &= e_{13}^3. \\
R_{38}(g_2) &= e_3. & R_{38}(g_3) &= e_{13}^2. \\
R_{39}(g_2) &= e_3. & R_{39}(g_3) &= e_{13}.
\end{aligned}$$

2.40. **Order 40.** $G_{40}^{(1)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= 1. & R_2(g_4) &= 1. & R_2(g_5) &= 1. \\
R_3(g_2) &= -i. & R_3(g_3) &= -1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. \\
R_4(g_2) &= i. & R_4(g_3) &= -1. & R_4(g_4) &= 1. & R_4(g_5) &= 1. \\
R_5(g_2) &= -e_8. & R_5(g_3) &= i. & R_5(g_4) &= -1. & R_5(g_5) &= 1. \\
R_6(g_2) &= -e_8^3. & R_6(g_3) &= -i. & R_6(g_4) &= -1. & R_6(g_5) &= 1. \\
R_7(g_2) &= e_8^3. & R_7(g_3) &= -i. & R_7(g_4) &= -1. & R_7(g_5) &= 1. \\
R_8(g_2) &= e_8. & R_8(g_3) &= i. & R_8(g_4) &= -1. & R_8(g_5) &= 1. \\
R_9(g_2) &= \begin{pmatrix} i & 0 \\ 2\Re e_5 & -i \end{pmatrix}. & R_9(g_3) &= -\epsilon. & R_9(g_4) &= \epsilon. & R_9(g_5) &= \begin{pmatrix} -1 & e_{20} + e_{20}^9 \\ e_{20} + e_{20}^9 & -2\Re e_5 \end{pmatrix}. \\
R_{10}(g_2) &= -\kappa. & R_{10}(g_3) &= -\epsilon. & R_{10}(g_4) &= \epsilon. & R_{10}(g_5) &= \begin{pmatrix} 0 & i \\ i & 2\Re e_5 \end{pmatrix}. \\
R_{11}(g_2) &= \begin{pmatrix} \varphi & -1 \\ -\varphi & -\varphi \end{pmatrix}. & R_{11}(g_3) &= \epsilon. & R_{11}(g_4) &= \epsilon. & R_{11}(g_5) &= \begin{pmatrix} 0 & 1 \\ -1 & \varphi \end{pmatrix}. \\
R_{12}(g_2) &= \begin{pmatrix} -2\Re e_5 & -2\Re e_5 \\ -1 & 2\Re e_5 \end{pmatrix}. & R_{12}(g_3) &= \epsilon. & R_{12}(g_4) &= \epsilon. & R_{12}(g_5) &= \begin{pmatrix} 0 & 1 \\ -1 & 2\Re e_5 \end{pmatrix}. \\
R_{13}(g_2) &= \begin{pmatrix} -e_{40}^{31} - e_{40}^{39} & e_{40}^{31} + e_{40}^{39} \\ e_8^3 & e_{40}^{31} + e_{40}^{39} \end{pmatrix}. & R_{13}(g_3) &= -i\epsilon. & R_{13}(g_4) &= -\epsilon. & R_{13}(g_5) &= \begin{pmatrix} 0 & -1 \\ 1 & \varphi \end{pmatrix}. \\
R_{14}(g_2) &= \begin{pmatrix} 0 & -i \\ 1 & 0 \end{pmatrix}. & R_{14}(g_3) &= -i\epsilon. & R_{14}(g_4) &= -\epsilon. & R_{14}(g_5) &= \begin{pmatrix} -\varphi & -e_{40}^{31} - e_{40}^{39} \\ -e_{40}^{21} - e_{40}^{29} & -1 \end{pmatrix}. \\
R_{15}(g_2) &= \begin{pmatrix} e_8 & 0 \\ e_{40}^7 + e_{40}^{23} & -e_8 \end{pmatrix}. & R_{15}(g_3) &= i\epsilon. & R_{15}(g_4) &= -\epsilon. & R_{15}(g_5) &= \begin{pmatrix} -1 & -e_{20} - e_{20}^9 \\ -e_{20} - e_{20}^9 & -2\Re e_5 \end{pmatrix}. \\
R_{16}(g_2) &= \begin{pmatrix} 0 & -i \\ -1 & 0 \end{pmatrix}. & R_{16}(g_3) &= i\epsilon. & R_{16}(g_4) &= -\epsilon. & R_{16}(g_5) &= \begin{pmatrix} 2\Re e_5 & e_8 \\ e_8^3 & 0 \end{pmatrix}.
\end{aligned}$$

$G_{40}^{(2)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= 1. & R_2(g_4) &= 1. & R_2(g_5) &= 1. \\
R_3(g_2) &= -1. & R_3(g_3) &= e_5^4. & R_3(g_4) &= 1. & R_3(g_5) &= 1. \\
R_4(g_2) &= -1. & R_4(g_3) &= e_5^3. & R_4(g_4) &= 1. & R_4(g_5) &= 1. \\
R_5(g_2) &= -1. & R_5(g_3) &= e_5^2. & R_5(g_4) &= 1. & R_5(g_5) &= 1. \\
R_6(g_2) &= -1. & R_6(g_3) &= e_5. & R_6(g_4) &= 1. & R_6(g_5) &= 1. \\
R_7(g_2) &= 1. & R_7(g_3) &= e_5^4. & R_7(g_4) &= 1. & R_7(g_5) &= 1. \\
R_8(g_2) &= 1. & R_8(g_3) &= e_5^3. & R_8(g_4) &= 1. & R_8(g_5) &= 1. \\
R_9(g_2) &= 1. & R_9(g_3) &= e_5^2. & R_9(g_4) &= 1. & R_9(g_5) &= 1. \\
R_{10}(g_2) &= 1. & R_{10}(g_3) &= e_5. & R_{10}(g_4) &= 1. & R_{10}(g_5) &= 1. \\
R_{11}(g_2) &= -i. & R_{11}(g_3) &= 1. & R_{11}(g_4) &= -1. & R_{11}(g_5) &= 1. \\
R_{12}(g_2) &= i. & R_{12}(g_3) &= 1. & R_{12}(g_4) &= -1. & R_{12}(g_5) &= 1. \\
R_{13}(g_2) &= -i. & R_{13}(g_3) &= e_5^4. & R_{13}(g_4) &= -1. & R_{13}(g_5) &= 1. \\
R_{14}(g_2) &= -i. & R_{14}(g_3) &= e_5^3. & R_{14}(g_4) &= -1. & R_{14}(g_5) &= 1. \\
R_{15}(g_2) &= -i. & R_{15}(g_3) &= e_5^2. & R_{15}(g_4) &= -1. & R_{15}(g_5) &= 1. \\
R_{16}(g_2) &= -i. & R_{16}(g_3) &= e_5. & R_{16}(g_4) &= -1. & R_{16}(g_5) &= 1. \\
R_{17}(g_2) &= i. & R_{17}(g_3) &= e_5^4. & R_{17}(g_4) &= -1. & R_{17}(g_5) &= 1. \\
R_{18}(g_2) &= i. & R_{18}(g_3) &= e_5^3. & R_{18}(g_4) &= -1. & R_{18}(g_5) &= 1. \\
R_{19}(g_2) &= i. & R_{19}(g_3) &= e_5^2. & R_{19}(g_4) &= -1. & R_{19}(g_5) &= 1. \\
R_{20}(g_2) &= i. & R_{20}(g_3) &= e_5. & R_{20}(g_4) &= -1. & R_{20}(g_5) &= 1. \\
R_{21}(g_2) &= -e_8. & R_{21}(g_3) &= 1. & R_{21}(g_4) &= i. & R_{21}(g_5) &= -1. \\
R_{22}(g_2) &= -e_8^3. & R_{22}(g_3) &= 1. & R_{22}(g_4) &= -i. & R_{22}(g_5) &= -1. \\
R_{23}(g_2) &= e_8^3. & R_{23}(g_3) &= 1. & R_{23}(g_4) &= -i. & R_{23}(g_5) &= -1. \\
R_{24}(g_2) &= e_8. & R_{24}(g_3) &= 1. & R_{24}(g_4) &= i. & R_{24}(g_5) &= -1. \\
R_{25}(g_2) &= -e_8. & R_{25}(g_3) &= e_5^4. & R_{25}(g_4) &= i. & R_{25}(g_5) &= -1. \\
R_{26}(g_2) &= -e_8. & R_{26}(g_3) &= e_5^3. & R_{26}(g_4) &= i. & R_{26}(g_5) &= -1. \\
R_{27}(g_2) &= -e_8. & R_{27}(g_3) &= e_5^2. & R_{27}(g_4) &= i. & R_{27}(g_5) &= -1. \\
R_{28}(g_2) &= -e_8. & R_{28}(g_3) &= e_5. & R_{28}(g_4) &= i. & R_{28}(g_5) &= -1. \\
R_{29}(g_2) &= -e_8^3. & R_{29}(g_3) &= e_5^4. & R_{29}(g_4) &= -i. & R_{29}(g_5) &= -1. \\
R_{30}(g_2) &= -e_8^3. & R_{30}(g_3) &= e_5^3. & R_{30}(g_4) &= -i. & R_{30}(g_5) &= -1. \\
R_{31}(g_2) &= -e_8^3. & R_{31}(g_3) &= e_5^2. & R_{31}(g_4) &= -i. & R_{31}(g_5) &= -1. \\
R_{32}(g_2) &= -e_8^3. & R_{32}(g_3) &= e_5. & R_{32}(g_4) &= -i. & R_{32}(g_5) &= -1. \\
R_{33}(g_2) &= e_8^3. & R_{33}(g_3) &= e_5^4. & R_{33}(g_4) &= -i. & R_{33}(g_5) &= -1. \\
R_{34}(g_2) &= e_8^3. & R_{34}(g_3) &= e_5^3. & R_{34}(g_4) &= -i. & R_{34}(g_5) &= -1. \\
R_{35}(g_2) &= e_8^3. & R_{35}(g_3) &= e_5^2. & R_{35}(g_4) &= -i. & R_{35}(g_5) &= -1. \\
R_{36}(g_2) &= e_8^3. & R_{36}(g_3) &= e_5. & R_{36}(g_4) &= -i. & R_{36}(g_5) &= -1. \\
R_{37}(g_2) &= e_8. & R_{37}(g_3) &= e_5^4. & R_{37}(g_4) &= i. & R_{37}(g_5) &= -1. \\
R_{38}(g_2) &= e_8. & R_{38}(g_3) &= e_5^3. & R_{38}(g_4) &= i. & R_{38}(g_5) &= -1. \\
R_{39}(g_2) &= e_8. & R_{39}(g_3) &= e_5^2. & R_{39}(g_4) &= i. & R_{39}(g_5) &= -1. \\
R_{40}(g_2) &= e_8. & R_{40}(g_3) &= e_5. & R_{40}(g_4) &= i. & R_{40}(g_5) &= -1.
\end{aligned}$$

$G_{40}^{(3)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= 1. & R_2(g_4) &= 1. & R_2(g_5) &= 1. \\
R_3(g_2) &= -i. & R_3(g_3) &= -1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. \\
R_4(g_2) &= i. & R_4(g_3) &= -1. & R_4(g_4) &= 1. & R_4(g_5) &= 1. \\
R_5(g_2) &= -e_8. & R_5(g_3) &= i. & R_5(g_4) &= -1. & R_5(g_5) &= 1. \\
R_6(g_2) &= -e_8^3. & R_6(g_3) &= -i. & R_6(g_4) &= -1. & R_6(g_5) &= 1. \\
R_7(g_2) &= e_8^3. & R_7(g_3) &= -i. & R_7(g_4) &= -1. & R_7(g_5) &= 1. \\
R_8(g_2) &= e_8. & R_8(g_3) &= i. & R_8(g_4) &= -1. & R_8(g_5) &= 1.
\end{aligned}$$

$$\begin{aligned}
R_9(g_2) &= \begin{pmatrix} -e_8 & -e_8^3 & e_8^3 & -1 \\ 0 & e_8 & 0 & 0 \\ 0 & 0 & 0 & i \\ i & 0 & 0 & 0 \end{pmatrix}. & R_9(g_3) &= \begin{pmatrix} 0 & 0 & 1 & 0 \\ 0 & i & 0 & 0 \\ -1 & 0 & 0 & 0 \\ -e_8^3 & e_8 & -e_8 & -i \end{pmatrix}. \\
R_9(g_4) &= \begin{pmatrix} -1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & -1 \end{pmatrix}. & R_9(g_5) &= \begin{pmatrix} 0 & 0 & 0 & -e_8^3 \\ i & -1 & 1 & e_8 \\ i & 0 & 0 & 0 \\ 0 & e_8^3 & 0 & 0 \end{pmatrix}.
\end{aligned}$$

$$\begin{aligned}
R_{10}(g_2) &= \begin{pmatrix} -1 & -1 & -1 & -1 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \\ 1 & 0 & 0 & 0 \end{pmatrix}. & R_{10}(g_3) &= \begin{pmatrix} 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ -1 & -1 & -1 & -1 \end{pmatrix}. \\
R_{10}(g_4) &= \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}. & R_{10}(g_5) &= \begin{pmatrix} 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 \\ -1 & -1 & -1 & -1 \\ 0 & 0 & 1 & 0 \end{pmatrix}.
\end{aligned}$$

 $G_{40}^{(4)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= 1. & R_2(g_5) &= 1. \\
R_3(g_2) &= -1. & R_3(g_3) &= 1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. \\
R_4(g_2) &= 1. & R_4(g_3) &= -1. & R_4(g_4) &= 1. & R_4(g_5) &= 1. \\
R_5(g_2) &= -i\lambda. & R_5(g_3) &= -i\phi. & R_5(g_4) &= -\epsilon. & R_5(g_5) &= \epsilon.
\end{aligned}$$

$$R_6(g_2) = \begin{pmatrix} -2\Re e_5 & 2\Re e_5 \\ 1 & 2\Re e_5 \end{pmatrix}. \quad R_6(g_3) = -\epsilon. \quad R_6(g_4) = \epsilon. \quad R_6(g_5) = \begin{pmatrix} -2\Re e_5 & 2\Re e_5 \\ -2\Re e_5 & -1 \end{pmatrix}.$$

$$R_7(g_2) = \begin{pmatrix} 2\Re e_5 & 1 \\ 2\Re e_5 & -2\Re e_5 \end{pmatrix}. \quad R_7(g_3) = -\epsilon. \quad R_7(g_4) = \epsilon. \quad R_7(g_5) = \begin{pmatrix} 0 & -1 \\ 1 & 2\Re e_5 \end{pmatrix}.$$

$$\begin{aligned}
R_8(g_2) &= \begin{pmatrix} i & 0 \\ -2\Re e_5 & -i \end{pmatrix}. & R_8(g_3) &= \begin{pmatrix} -e_{20} + e_{20}^9 + e_{20}^{13} - e_{20}^{17} & 2e_5^2 + 2e_5^3 \\ -2e_5^2 - 2e_5^3 & e_{20} - e_{20}^9 - e_{20}^{13} + e_{20}^{17} \end{pmatrix}. \\
R_8(g_4) &= -\epsilon. & R_8(g_5) &= \begin{pmatrix} 1 & e_{20} - e_{20}^9 \\ -e_{20} + e_{20}^9 & e_5 + 2e_5^2 + 2e_5^3 + e_5^4 \end{pmatrix}.
\end{aligned}$$

$$R_9(g_2) = -i\phi. \quad R_9(g_3) = \begin{pmatrix} (-e_{20} + e_{20}^9 - 3e_{20}^{13} + 3e_{20}^{17})/5 & (4e_{20} - 4e_{20}^9 + 2e_{20}^{13} - 2e_{20}^{17})/5 \\ (-4e_{20} + 4e_{20}^9 - 2e_{20}^{13} + 2e_{20}^{17})/5 & (e_{20} - e_{20}^9 + 3e_{20}^{13} - 3e_{20}^{17})/5 \end{pmatrix}.$$

$$R_9(g_4) = -\epsilon. \quad R_9(g_5) = \begin{pmatrix} -2\Re e_5 & 2\Re e_5 \\ -2\Re e_5 & -1 \end{pmatrix}.$$

$$R_{10}(g_2) = \begin{pmatrix} i & 0 \\ e_{20}^{13} + e_{20}^{17} & -i \end{pmatrix}.$$

$$R_{10}(g_3) = \begin{pmatrix} (-3e_{20} + 3e_{20}^9 + e_{20}^{13} - e_{20}^{17})/5 & (-2e_{20} + 2e_{20}^9 + 4e_{20}^{13} - 4e_{20}^{17})/5 \\ (2e_{20} - 2e_{20}^9 - 4e_{20}^{13} + 4e_{20}^{17})/5 & (3e_{20} - 3e_{20}^9 - e_{20}^{13} + e_{20}^{17})/5 \end{pmatrix}.$$

$$R_{10}(g_4) = -\epsilon. \quad R_{10}(g_5) = \begin{pmatrix} -1 & \varphi \\ -\varphi & -\varphi \end{pmatrix}.$$

$$R_{11}(g_2) = \begin{pmatrix} e_{20} + e_{20}^9 & -i \\ -e_{20} - e_{20}^9 & -e_{20} - e_{20}^9 \end{pmatrix}.$$

$$R_{11}(g_3) = \begin{pmatrix} (e_{20} - e_{20}^9 + 3e_{20}^{13} - 3e_{20}^{17})/5 & (4e_{20} - 4e_{20}^9 + 2e_{20}^{13} - 2e_{20}^{17})/5 \\ (-4e_{20} + 4e_{20}^9 - 2e_{20}^{13} + 2e_{20}^{17})/5 & (-e_{20} + e_{20}^9 - 3e_{20}^{13} + 3e_{20}^{17})/5 \end{pmatrix}.$$

$$R_{11}(g_4) = -\epsilon. \quad R_{11}(g_5) = \begin{pmatrix} 2\Re e_5 & -1 \\ 1 & 0 \end{pmatrix}.$$

$$R_{12}(g_2) = \begin{pmatrix} 1 & 0 \\ 2\Re e_5 & -1 \end{pmatrix}. \quad R_{12}(g_3) = \epsilon. \quad R_{12}(g_4) = \epsilon. \quad R_{12}(g_5) = \begin{pmatrix} -2\Re e_5 & -2\Re e_5 \\ 2\Re e_5 & -1 \end{pmatrix}.$$

$$R_{13}(g_2) = \begin{pmatrix} -2\Re e_5 & -2\Re e_5 \\ -1 & 2\Re e_5 \end{pmatrix}. \quad R_{13}(g_3) = \epsilon. \quad R_{13}(g_4) = \epsilon. \quad R_{13}(g_5) = \begin{pmatrix} 2\Re e_5 & -1 \\ 1 & 0 \end{pmatrix}.$$

 $G_{40}^{(5)}$

$$R_2(g_2) = -1. \quad R_2(g_3) = -1. \quad R_2(g_4) = 1. \quad R_2(g_5) = 1.$$

$$R_3(g_2) = -1. \quad R_3(g_3) = 1. \quad R_3(g_4) = 1. \quad R_3(g_5) = 1.$$

$$R_4(g_2) = 1. \quad R_4(g_3) = -1. \quad R_4(g_4) = 1. \quad R_4(g_5) = 1.$$

$$R_5(g_2) = -1. \quad R_5(g_3) = -i. \quad R_5(g_4) = -1. \quad R_5(g_5) = 1.$$

$$R_6(g_2) = -1. \quad R_6(g_3) = i. \quad R_6(g_4) = -1. \quad R_6(g_5) = 1.$$

$$R_7(g_2) = 1. \quad R_7(g_3) = -i. \quad R_7(g_4) = -1. \quad R_7(g_5) = 1.$$

$$R_8(g_2) = 1. \quad R_8(g_3) = i. \quad R_8(g_4) = -1. \quad R_8(g_5) = 1.$$

$$R_9(g_2) = \begin{pmatrix} 1 & 0 \\ 2\Re e_5 & -1 \end{pmatrix}. \quad R_9(g_3) = -\epsilon. \quad R_9(g_4) = \epsilon. \quad R_9(g_5) = \begin{pmatrix} -1 & 2\Re e_5 \\ -2\Re e_5 & -2\Re e_5 \end{pmatrix}.$$

$$R_{10}(g_2) = \begin{pmatrix} -1 & \varphi \\ 0 & 1 \end{pmatrix}. \quad R_{10}(g_3) = -\epsilon. \quad R_{10}(g_4) = \epsilon. \quad R_{10}(g_5) = \begin{pmatrix} -1 & \varphi \\ -\varphi & -\varphi \end{pmatrix}.$$

$$R_{11}(g_2) = \begin{pmatrix} 1 & 0 \\ 2\Re e_5 & -1 \end{pmatrix}. \quad R_{11}(g_3) = \epsilon. \quad R_{11}(g_4) = \epsilon. \quad R_{11}(g_5) = \begin{pmatrix} -2\Re e_5 & -2\Re e_5 \\ 2\Re e_5 & -1 \end{pmatrix}.$$

$$R_{12}(g_2) = \begin{pmatrix} 2\Re e_5 & -1 \\ -2\Re e_5 & -2\Re e_5 \end{pmatrix}. \quad R_{12}(g_3) = \epsilon. \quad R_{12}(g_4) = \epsilon. \quad R_{12}(g_5) = \begin{pmatrix} 0 & 1 \\ -1 & 2\Re e_5 \end{pmatrix}.$$

$$R_{13}(g_2) = \phi. \quad R_{13}(g_3) = -i\epsilon. \quad R_{13}(g_4) = -\epsilon. \quad R_{13}(g_5) = \begin{pmatrix} -2\Re e_5 & -2\Re e_5 \\ 2\Re e_5 & -1 \end{pmatrix}.$$

$$R_{14}(g_2) = \begin{pmatrix} 1 & 0 \\ -e_{20}^{13} - e_{20}^{17} & -1 \end{pmatrix}. \quad R_{14}(g_3) = -i\epsilon. \quad R_{14}(g_4) = -\epsilon.$$

$$R_{14}(g_5) = \begin{pmatrix} -1 & e_{20}^{13} + e_{20}^{17} \\ e_{20}^{13} + e_{20}^{17} & -\varphi \end{pmatrix}.$$

$$R_{15}(g_2) = \begin{pmatrix} -\varphi & e_{20}^{13} + e_{20}^{17} \\ -i & \varphi \end{pmatrix}. \quad R_{15}(g_3) = i\epsilon. \quad R_{15}(g_4) = -\epsilon. \quad R_{15}(g_5) = \begin{pmatrix} 0 & -i \\ -i & \varphi \end{pmatrix}.$$

$$R_{16}(g_2) = \begin{pmatrix} 2\Re e_5 & -i \\ e_{20} + e_{20}^9 & -2\Re e_5 \end{pmatrix}. \quad R_{16}(g_3) = i\epsilon. \quad R_{16}(g_4) = -\epsilon. \quad R_{16}(g_5) = \begin{pmatrix} 0 & i \\ i & 2\Re e_5 \end{pmatrix}.$$

$G_{40}^{(6)}$

$$R_2(g_2) = -1. \quad R_2(g_3) = -1. \quad R_2(g_4) = 1. \quad R_2(g_5) = 1.$$

$$R_3(g_2) = -1. \quad R_3(g_3) = 1. \quad R_3(g_4) = 1. \quad R_3(g_5) = 1.$$

$$R_4(g_2) = 1. \quad R_4(g_3) = -1. \quad R_4(g_4) = 1. \quad R_4(g_5) = 1.$$

$$R_5(g_2) = \lambda. \quad R_5(g_3) = -\kappa. \quad R_5(g_4) = -\epsilon. \quad R_5(g_5) = \epsilon.$$

$$R_6(g_2) = \begin{pmatrix} -1 & -\varphi \\ 0 & 1 \end{pmatrix}. \quad R_6(g_3) = -\epsilon. \quad R_6(g_4) = \epsilon. \quad R_6(g_5) = \begin{pmatrix} 0 & -1 \\ 1 & \varphi \end{pmatrix}.$$

$$R_7(g_2) = \begin{pmatrix} \varphi & -1 \\ -\varphi & -\varphi \end{pmatrix}. \quad R_7(g_3) = -\epsilon. \quad R_7(g_4) = \epsilon. \quad R_7(g_5) = \begin{pmatrix} -1 & \varphi \\ -\varphi & -\varphi \end{pmatrix}.$$

$$R_8(g_2) = \begin{pmatrix} (-e_5^2 - e_5^3)/2 & (e_{20}^{13} - e_{20}^{17})/2 \\ (e_{20}^{13} - e_{20}^{17})/2 & 2\Re e_{10} \end{pmatrix}. \quad R_8(g_3) = \kappa. \quad R_8(g_4) = -\epsilon.$$

$$R_8(g_5) = \begin{pmatrix} 2\Re e_{10} & (e_{20}^{13} - e_{20}^{17})/2 \\ (-e_{20}^{13} + e_{20}^{17})/2 & 2\Re e_{10} \end{pmatrix}.$$

$$R_9(g_2) = \begin{pmatrix} (-e_5^2 - e_5^3)/2 & (e_{20}^{13} - e_{20}^{17})/2 \\ (e_{20}^{13} - e_{20}^{17})/2 & 2\Re e_{10} \end{pmatrix}. \quad R_9(g_3) = \kappa. \quad R_9(g_4) = -\epsilon.$$

$$R_9(g_5) = \begin{pmatrix} 2\Re e_{10} & (-e_{20}^{13} + e_{20}^{17})/2 \\ (e_{20}^{13} - e_{20}^{17})/2 & 2\Re e_{10} \end{pmatrix}.$$

$$R_{10}(g_2) = \begin{pmatrix} -e_5 - 2e_5^2 - 2e_5^3 - e_5^4 & -e_{20} + e_{20}^9 \\ e_{20} - e_{20}^9 - e_{20}^{13} + e_{20}^{17} & e_5 + 2e_5^2 + 2e_5^3 + e_5^4 \end{pmatrix}.$$

$$R_{10}(g_3) = \begin{pmatrix} e_{20} - e_{20}^9 - e_{20}^{13} + e_{20}^{17} & 2e_5^2 + 2e_5^3 \\ -2e_5^2 - 2e_5^3 & -e_{20} + e_{20}^9 + e_{20}^{13} - e_{20}^{17} \end{pmatrix}.$$

$$R_{10}(g_4) = -\epsilon. \quad R_{10}(g_5) = \begin{pmatrix} -2e_5^2 - 2e_5^3 & -e_{20} + e_{20}^9 + e_{20}^{13} - e_{20}^{17} \\ e_{20} - e_{20}^9 - e_{20}^{13} + e_{20}^{17} & e_5 + 2e_5^2 + 2e_5^3 + e_5^4 \end{pmatrix}.$$

$$R_{11}(g_2) = \begin{pmatrix} 2\Re e_5 & -2\Re e_5 \\ -1 & -2\Re e_5 \end{pmatrix}.$$

$$R_{11}(g_3) = \begin{pmatrix} (-e_{20} + e_{20}^9 - 3e_{20}^{13} + 3e_{20}^{17})/5 & (4e_{20} - 4e_{20}^9 + 2e_{20}^{13} - 2e_{20}^{17})/5 \\ (-4e_{20} + 4e_{20}^9 - 2e_{20}^{13} + 2e_{20}^{17})/5 & (e_{20} - e_{20}^9 + 3e_{20}^{13} - 3e_{20}^{17})/5 \end{pmatrix}.$$

$$R_{11}(g_4) = -\epsilon. \quad R_{11}(g_5) = \begin{pmatrix} 0 & -1 \\ 1 & 2\Re e_5 \end{pmatrix}.$$

$$R_{12}(g_2) = \begin{pmatrix} -2\Re e_5 & -2\Re e_5 \\ -1 & 2\Re e_5 \end{pmatrix}. \quad R_{12}(g_3) = \epsilon. \quad R_{12}(g_4) = \epsilon. \quad R_{12}(g_5) = \begin{pmatrix} -2\Re e_5 & -2\Re e_5 \\ 2\Re e_5 & -1 \end{pmatrix}.$$

$$R_{13}(g_2) = \begin{pmatrix} 1 & 0 \\ \varphi & -1 \end{pmatrix}. \quad R_{13}(g_3) = \epsilon. \quad R_{13}(g_4) = \epsilon. \quad R_{13}(g_5) = \begin{pmatrix} -1 & \varphi \\ -\varphi & -\varphi \end{pmatrix}.$$

$$G_{40}^{(7)}$$

$$R_2(g_2) = -1. \quad R_2(g_3) = -1. \quad R_2(g_4) = 1. \quad R_2(g_5) = 1.$$

$$R_3(g_2) = -1. \quad R_3(g_3) = 1. \quad R_3(g_4) = 1. \quad R_3(g_5) = 1.$$

$$R_4(g_2) = 1. \quad R_4(g_3) = -1. \quad R_4(g_4) = 1. \quad R_4(g_5) = 1.$$

$$R_5(g_2) = -i. \quad R_5(g_3) = -1. \quad R_5(g_4) = -1. \quad R_5(g_5) = 1.$$

$$R_6(g_2) = i. \quad R_6(g_3) = -1. \quad R_6(g_4) = -1. \quad R_6(g_5) = 1.$$

$$R_7(g_2) = -i. \quad R_7(g_3) = 1. \quad R_7(g_4) = -1. \quad R_7(g_5) = 1.$$

$$R_8(g_2) = i. \quad R_8(g_3) = 1. \quad R_8(g_4) = -1. \quad R_8(g_5) = 1.$$

$$R_9(g_2) = -i\phi. \quad R_9(g_3) = -\epsilon. \quad R_9(g_4) = -\epsilon. \quad R_9(g_5) = \begin{pmatrix} -1 & -2\Re e_5 \\ 2\Re e_5 & -2\Re e_5 \end{pmatrix}.$$

$$R_{10}(g_2) = i\phi. \quad R_{10}(g_3) = -\epsilon. \quad R_{10}(g_4) = -\epsilon. \quad R_{10}(g_5) = \begin{pmatrix} 2\Re e_5 & -1 \\ 1 & 0 \end{pmatrix}.$$

$$R_{11}(g_2) = \begin{pmatrix} -2\Re e_5 & 2\Re e_5 \\ 1 & 2\Re e_5 \end{pmatrix}. \quad R_{11}(g_3) = -\epsilon. \quad R_{11}(g_4) = \epsilon. \quad R_{11}(g_5) = \begin{pmatrix} -1 & -2\Re e_5 \\ 2\Re e_5 & -2\Re e_5 \end{pmatrix}.$$

$$R_{12}(g_2) = \begin{pmatrix} -\varphi & -\varphi \\ -1 & \varphi \end{pmatrix}. \quad R_{12}(g_3) = -\epsilon. \quad R_{12}(g_4) = \epsilon. \quad R_{12}(g_5) = \begin{pmatrix} -1 & \varphi \\ -\varphi & -\varphi \end{pmatrix}.$$

$$R_{13}(g_2) = \begin{pmatrix} i & 0 \\ 2\Re e_5 & -i \end{pmatrix}. \quad R_{13}(g_3) = \epsilon. \quad R_{13}(g_4) = -\epsilon. \quad R_{13}(g_5) = \begin{pmatrix} -1 & e_{20} + e_{20}^9 \\ e_{20} + e_{20}^9 & -2\Re e_5 \end{pmatrix}.$$

$$R_{14}(g_2) = \begin{pmatrix} e_{20} + e_{20}^9 & -i \\ -e_{20} - e_{20}^9 & -e_{20} - e_{20}^9 \end{pmatrix}. \quad R_{14}(g_3) = \epsilon. \quad R_{14}(g_4) = -\epsilon. \quad R_{14}(g_5) = \begin{pmatrix} 2\Re e_5 & -1 \\ 1 & 0 \end{pmatrix}.$$

$$R_{15}(g_2) = \begin{pmatrix} 1 & 0 \\ \varphi & -1 \end{pmatrix}. \quad R_{15}(g_3) = \epsilon. \quad R_{15}(g_4) = \epsilon. \quad R_{15}(g_5) = \begin{pmatrix} 0 & 1 \\ -1 & \varphi \end{pmatrix}.$$

$$R_{16}(g_2) = \phi. \quad R_{16}(g_3) = \epsilon. \quad R_{16}(g_4) = \epsilon. \quad R_{16}(g_5) = \begin{pmatrix} 0 & 1 \\ -1 & 2\Re e_5 \end{pmatrix}.$$

$$G_{40}^{(8)}$$

$$R_2(g_2) = -1. \quad R_2(g_3) = -1. \quad R_2(g_4) = 1. \quad R_2(g_5) = 1.$$

$$R_3(g_2) = -1. \quad R_3(g_3) = 1. \quad R_3(g_4) = 1. \quad R_3(g_5) = 1.$$

$$R_4(g_2) = 1. \quad R_4(g_3) = -1. \quad R_4(g_4) = 1. \quad R_4(g_5) = 1.$$

$$R_5(g_2) = -\lambda. \quad R_5(g_3) = -\phi. \quad R_5(g_4) = -\epsilon. \quad R_5(g_5) = \epsilon.$$

$$R_6(g_2) = \begin{pmatrix} 1 & 0 \\ 2\Re e_5 & -1 \end{pmatrix}. \quad R_6(g_3) = -\epsilon. \quad R_6(g_4) = \epsilon. \quad R_6(g_5) = \begin{pmatrix} -1 & 2\Re e_5 \\ -2\Re e_5 & -2\Re e_5 \end{pmatrix}.$$

$$R_7(g_2) = \begin{pmatrix} -\varphi & -\varphi \\ -1 & \varphi \end{pmatrix}. \quad R_7(g_3) = -\epsilon. \quad R_7(g_4) = \epsilon. \quad R_7(g_5) = \begin{pmatrix} -\varphi & -\varphi \\ \varphi & -1 \end{pmatrix}.$$

$$R_8(g_2) = \begin{pmatrix} \varphi & \varphi \\ 1 & -\varphi \end{pmatrix}.$$

$$R_8(g_3) = \begin{pmatrix} (3e_5 + e_5^2 - e_5^3 - 3e_5^4)/5 & (2e_5 + 4e_5^2 - 4e_5^3 - 2e_5^4)/5 \\ (-2e_5 - 4e_5^2 + 4e_5^3 + 2e_5^4)/5 & (-3e_5 - e_5^2 + e_5^3 + 3e_5^4)/5 \end{pmatrix}. \quad R_8(g_4) = -\epsilon. \quad R_8(g_5) = \begin{pmatrix} 0 & 1 \\ -1 & \varphi \end{pmatrix}$$

$$R_9(g_2) = \begin{pmatrix} 2\Re e_{10} & (e_5^2 - e_5^3)/2 \\ -2\Re e_{10} & (-e_5^2 - e_5^3)/2 \end{pmatrix}. \quad R_9(g_3) = -\phi. \quad R_9(g_4) = -\epsilon.$$

$$R_9(g_5) = \begin{pmatrix} 2\Re e_{10} & -2\Re e_{10} \\ -2\Re e_{10} & 2\Re e_{10} \end{pmatrix}.$$

$$R_{10}(g_2) = \begin{pmatrix} -1 & 0 \\ -\varphi & 1 \end{pmatrix}. \quad R_{10}(g_3) = \begin{pmatrix} (-3e_5 - e_5^2 + e_5^3 + 3e_5^4)/5 & (-2e_5 - 4e_5^2 + 4e_5^3 + 2e_5^4)/5 \\ (2e_5 + 4e_5^2 - 4e_5^3 - 2e_5^4)/5 & (3e_5 + e_5^2 - e_5^3 - 3e_5^4)/5 \end{pmatrix}.$$

$$R_{10}(g_4) = -\epsilon. \quad R_{10}(g_5) = \begin{pmatrix} -1 & \varphi \\ -\varphi & -\varphi \end{pmatrix}.$$

$$R_{11}(g_2) = \begin{pmatrix} -1 & 2\Re e_5 \\ 0 & 1 \end{pmatrix}. \quad R_{11}(g_3) = \begin{pmatrix} (e_5 - 3e_5^2 + 3e_5^3 - e_5^4)/5 & (4e_5 - 2e_5^2 + 2e_5^3 - 4e_5^4)/5 \\ (-4e_5 + 2e_5^2 - 2e_5^3 + 4e_5^4)/5 & (-e_5 + 3e_5^2 - 3e_5^3 + e_5^4)/5 \end{pmatrix}.$$

$$R_{11}(g_4) = -\epsilon. \quad R_{11}(g_5) = \begin{pmatrix} 2\Re e_5 & -1 \\ 1 & 0 \end{pmatrix}.$$

$$R_{12}(g_2) = \begin{pmatrix} 2\Re e_5 & -1 \\ -2\Re e_5 & -2\Re e_5 \end{pmatrix}. \quad R_{12}(g_3) = \epsilon. \quad R_{12}(g_4) = \epsilon. \quad R_{12}(g_5) = \begin{pmatrix} -1 & 2\Re e_5 \\ -2\Re e_5 & -2\Re e_5 \end{pmatrix}.$$

$$R_{13}(g_2) = \begin{pmatrix} \varphi & -1 \\ -\varphi & -\varphi \end{pmatrix}. \quad R_{13}(g_3) = \epsilon. \quad R_{13}(g_4) = \epsilon. \quad R_{13}(g_5) = \begin{pmatrix} -1 & \varphi \\ -\varphi & -\varphi \end{pmatrix}.$$

 $G_{40}^{(9)}$

$$R_2(g_2) = -1. \quad R_2(g_3) = -1. \quad R_2(g_4) = 1. \quad R_2(g_5) = 1.$$

$$R_3(g_2) = -1. \quad R_3(g_3) = 1. \quad R_3(g_4) = 1. \quad R_3(g_5) = 1.$$

$$R_4(g_2) = 1. \quad R_4(g_3) = -1. \quad R_4(g_4) = 1. \quad R_4(g_5) = 1.$$

$$R_5(g_2) = -1. \quad R_5(g_3) = -1. \quad R_5(g_4) = e_5^4. \quad R_5(g_5) = 1.$$

$$R_6(g_2) = -1. \quad R_6(g_3) = -1. \quad R_6(g_4) = e_5^3. \quad R_6(g_5) = 1.$$

$$R_7(g_2) = -1. \quad R_7(g_3) = -1. \quad R_7(g_4) = e_5^2. \quad R_7(g_5) = 1.$$

$$R_8(g_2) = -1. \quad R_8(g_3) = -1. \quad R_8(g_4) = e_5. \quad R_8(g_5) = 1.$$

$$R_9(g_2) = -1. \quad R_9(g_3) = 1. \quad R_9(g_4) = e_5^4. \quad R_9(g_5) = 1.$$

$$R_{10}(g_2) = -1. \quad R_{10}(g_3) = 1. \quad R_{10}(g_4) = e_5^3. \quad R_{10}(g_5) = 1.$$

$$R_{11}(g_2) = -1. \quad R_{11}(g_3) = 1. \quad R_{11}(g_4) = e_5^2. \quad R_{11}(g_5) = 1.$$

$$R_{12}(g_2) = -1. \quad R_{12}(g_3) = 1. \quad R_{12}(g_4) = e_5. \quad R_{12}(g_5) = 1.$$

$$R_{13}(g_2) = 1. \quad R_{13}(g_3) = -1. \quad R_{13}(g_4) = e_5^4. \quad R_{13}(g_5) = 1.$$

$$R_{14}(g_2) = 1. \quad R_{14}(g_3) = -1. \quad R_{14}(g_4) = e_5^3. \quad R_{14}(g_5) = 1.$$

$$R_{15}(g_2) = 1. \quad R_{15}(g_3) = -1. \quad R_{15}(g_4) = e_5^2. \quad R_{15}(g_5) = 1.$$

$$R_{16}(g_2) = 1. \quad R_{16}(g_3) = -1. \quad R_{16}(g_4) = e_5. \quad R_{16}(g_5) = 1.$$

$$R_{17}(g_2) = 1. \quad R_{17}(g_3) = 1. \quad R_{17}(g_4) = e_5^4. \quad R_{17}(g_5) = 1.$$

$$R_{18}(g_2) = 1. \quad R_{18}(g_3) = 1. \quad R_{18}(g_4) = e_5^3. \quad R_{18}(g_5) = 1.$$

$$R_{19}(g_2) = 1. \quad R_{19}(g_3) = 1. \quad R_{19}(g_4) = e_5^2. \quad R_{19}(g_5) = 1.$$

$$R_{20}(g_2) = 1. \quad R_{20}(g_3) = 1. \quad R_{20}(g_4) = e_5. \quad R_{20}(g_5) = 1.$$

$$R_{21}(g_2) = -i. \quad R_{21}(g_3) = -1. \quad R_{21}(g_4) = 1. \quad R_{21}(g_5) = -1.$$

$$R_{22}(g_2) = i. \quad R_{22}(g_3) = -1. \quad R_{22}(g_4) = 1. \quad R_{22}(g_5) = -1.$$

$$R_{23}(g_2) = -i. \quad R_{23}(g_3) = -1. \quad R_{23}(g_4) = e_5^4. \quad R_{23}(g_5) = -1.$$

$$R_{24}(g_2) = -i. \quad R_{24}(g_3) = -1. \quad R_{24}(g_4) = e_5^3. \quad R_{24}(g_5) = -1.$$

$$\begin{aligned}
R_{25}(g_2) &= -i. & R_{25}(g_3) &= -1. & R_{25}(g_4) &= e_5^2. & R_{25}(g_5) &= -1. \\
R_{26}(g_2) &= -i. & R_{26}(g_3) &= -1. & R_{26}(g_4) &= e_5. & R_{26}(g_5) &= -1. \\
R_{27}(g_2) &= i. & R_{27}(g_3) &= -1. & R_{27}(g_4) &= e_5^4. & R_{27}(g_5) &= -1. \\
R_{28}(g_2) &= i. & R_{28}(g_3) &= -1. & R_{28}(g_4) &= e_5^3. & R_{28}(g_5) &= -1. \\
R_{29}(g_2) &= i. & R_{29}(g_3) &= -1. & R_{29}(g_4) &= e_5^2. & R_{29}(g_5) &= -1. \\
R_{30}(g_2) &= i. & R_{30}(g_3) &= -1. & R_{30}(g_4) &= e_5. & R_{30}(g_5) &= -1. \\
R_{31}(g_2) &= -i. & R_{31}(g_3) &= 1. & R_{31}(g_4) &= 1. & R_{31}(g_5) &= -1. \\
R_{32}(g_2) &= i. & R_{32}(g_3) &= 1. & R_{32}(g_4) &= 1. & R_{32}(g_5) &= -1. \\
R_{33}(g_2) &= -i. & R_{33}(g_3) &= 1. & R_{33}(g_4) &= e_5^4. & R_{33}(g_5) &= -1. \\
R_{34}(g_2) &= -i. & R_{34}(g_3) &= 1. & R_{34}(g_4) &= e_5^3. & R_{34}(g_5) &= -1. \\
R_{35}(g_2) &= -i. & R_{35}(g_3) &= 1. & R_{35}(g_4) &= e_5^2. & R_{35}(g_5) &= -1. \\
R_{36}(g_2) &= -i. & R_{36}(g_3) &= 1. & R_{36}(g_4) &= e_5. & R_{36}(g_5) &= -1. \\
R_{37}(g_2) &= i. & R_{37}(g_3) &= 1. & R_{37}(g_4) &= e_5^4. & R_{37}(g_5) &= -1. \\
R_{38}(g_2) &= i. & R_{38}(g_3) &= 1. & R_{38}(g_4) &= e_5^3. & R_{38}(g_5) &= -1. \\
R_{39}(g_2) &= i. & R_{39}(g_3) &= 1. & R_{39}(g_4) &= e_5^2. & R_{39}(g_5) &= -1. \\
R_{40}(g_2) &= i. & R_{40}(g_3) &= 1. & R_{40}(g_4) &= e_5. & R_{40}(g_5) &= -1.
\end{aligned}$$

 $G_{40}^{(10)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= 1. & R_2(g_5) &= 1. \\
R_3(g_2) &= -1. & R_3(g_3) &= 1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. \\
R_4(g_2) &= 1. & R_4(g_3) &= -1. & R_4(g_4) &= 1. & R_4(g_5) &= 1. \\
R_5(g_2) &= -1. & R_5(g_3) &= -1. & R_5(g_4) &= e_5^4. & R_5(g_5) &= 1. \\
R_6(g_2) &= -1. & R_6(g_3) &= -1. & R_6(g_4) &= e_5^3. & R_6(g_5) &= 1. \\
R_7(g_2) &= -1. & R_7(g_3) &= -1. & R_7(g_4) &= e_5^2. & R_7(g_5) &= 1. \\
R_8(g_2) &= -1. & R_8(g_3) &= -1. & R_8(g_4) &= e_5. & R_8(g_5) &= 1. \\
R_9(g_2) &= -1. & R_9(g_3) &= 1. & R_9(g_4) &= e_5^4. & R_9(g_5) &= 1. \\
R_{10}(g_2) &= -1. & R_{10}(g_3) &= 1. & R_{10}(g_4) &= e_5^3. & R_{10}(g_5) &= 1. \\
R_{11}(g_2) &= -1. & R_{11}(g_3) &= 1. & R_{11}(g_4) &= e_5^2. & R_{11}(g_5) &= 1. \\
R_{12}(g_2) &= -1. & R_{12}(g_3) &= 1. & R_{12}(g_4) &= e_5. & R_{12}(g_5) &= 1. \\
R_{13}(g_2) &= 1. & R_{13}(g_3) &= -1. & R_{13}(g_4) &= e_5^4. & R_{13}(g_5) &= 1. \\
R_{14}(g_2) &= 1. & R_{14}(g_3) &= -1. & R_{14}(g_4) &= e_5^3. & R_{14}(g_5) &= 1. \\
R_{15}(g_2) &= 1. & R_{15}(g_3) &= -1. & R_{15}(g_4) &= e_5^2. & R_{15}(g_5) &= 1. \\
R_{16}(g_2) &= 1. & R_{16}(g_3) &= -1. & R_{16}(g_4) &= e_5. & R_{16}(g_5) &= 1. \\
R_{17}(g_2) &= 1. & R_{17}(g_3) &= 1. & R_{17}(g_4) &= e_5^4. & R_{17}(g_5) &= 1. \\
R_{18}(g_2) &= 1. & R_{18}(g_3) &= 1. & R_{18}(g_4) &= e_5^3. & R_{18}(g_5) &= 1. \\
R_{19}(g_2) &= 1. & R_{19}(g_3) &= 1. & R_{19}(g_4) &= e_5^2. & R_{19}(g_5) &= 1. \\
R_{20}(g_2) &= 1. & R_{20}(g_3) &= 1. & R_{20}(g_4) &= e_5. & R_{20}(g_5) &= 1. \\
R_{21}(g_2) &= -\lambda. & R_{21}(g_3) &= -\phi. & R_{21}(g_4) &= \epsilon. & R_{21}(g_5) &= -\epsilon. \\
R_{22}(g_2) &= \lambda. & R_{22}(g_3) &= \begin{pmatrix} 0 & -e_5^3 \\ -e_5^2 & 0 \end{pmatrix}. & R_{22}(g_4) &= \begin{pmatrix} e_5^4 & 0 \\ 0 & e_5^4 \end{pmatrix}. & R_{22}(g_5) &= -\epsilon.
\end{aligned}$$

$$\begin{aligned}
R_{23}(g_2) &= -\lambda. & R_{23}(g_3) &= \begin{pmatrix} 0 & e_5^4 \\ e_5 & 0 \end{pmatrix}. & R_{23}(g_4) &= \begin{pmatrix} e_5^3 & 0 \\ 0 & e_5^3 \end{pmatrix}. & R_{23}(g_5) &= -\epsilon. \\
R_{24}(g_2) &= \lambda. & R_{24}(g_3) &= \begin{pmatrix} 0 & -e_5^3 \\ -e_5^2 & 0 \end{pmatrix}. & R_{24}(g_4) &= \begin{pmatrix} e_5^2 & 0 \\ 0 & e_5^2 \end{pmatrix}. & R_{24}(g_5) &= -\epsilon. \\
R_{25}(g_2) &= -\lambda. & R_{25}(g_3) &= -\phi. & R_{25}(g_4) &= \begin{pmatrix} e_5 & 0 \\ 0 & e_5 \end{pmatrix}. & R_{25}(g_5) &= -\epsilon.
\end{aligned}$$

 $G_{40}^{(11)}$

$$\begin{aligned}
R_2(g_2) &= -1. & R_2(g_3) &= -1. & R_2(g_4) &= 1. & R_2(g_5) &= 1. \\
R_3(g_2) &= -1. & R_3(g_3) &= 1. & R_3(g_4) &= 1. & R_3(g_5) &= 1. \\
R_4(g_2) &= 1. & R_4(g_3) &= -1. & R_4(g_4) &= 1. & R_4(g_5) &= 1. \\
R_5(g_2) &= -1. & R_5(g_3) &= -1. & R_5(g_4) &= e_5^4. & R_5(g_5) &= 1. \\
R_6(g_2) &= -1. & R_6(g_3) &= -1. & R_6(g_4) &= e_5^3. & R_6(g_5) &= 1. \\
R_7(g_2) &= -1. & R_7(g_3) &= -1. & R_7(g_4) &= e_5^2. & R_7(g_5) &= 1. \\
R_8(g_2) &= -1. & R_8(g_3) &= -1. & R_8(g_4) &= e_5. & R_8(g_5) &= 1. \\
R_9(g_2) &= -1. & R_9(g_3) &= 1. & R_9(g_4) &= e_5^4. & R_9(g_5) &= 1. \\
R_{10}(g_2) &= -1. & R_{10}(g_3) &= 1. & R_{10}(g_4) &= e_5^3. & R_{10}(g_5) &= 1. \\
R_{11}(g_2) &= -1. & R_{11}(g_3) &= 1. & R_{11}(g_4) &= e_5^2. & R_{11}(g_5) &= 1. \\
R_{12}(g_2) &= -1. & R_{12}(g_3) &= 1. & R_{12}(g_4) &= e_5. & R_{12}(g_5) &= 1. \\
R_{13}(g_2) &= 1. & R_{13}(g_3) &= -1. & R_{13}(g_4) &= e_5^4. & R_{13}(g_5) &= 1. \\
R_{14}(g_2) &= 1. & R_{14}(g_3) &= -1. & R_{14}(g_4) &= e_5^3. & R_{14}(g_5) &= 1. \\
R_{15}(g_2) &= 1. & R_{15}(g_3) &= -1. & R_{15}(g_4) &= e_5^2. & R_{15}(g_5) &= 1. \\
R_{16}(g_2) &= 1. & R_{16}(g_3) &= -1. & R_{16}(g_4) &= e_5. & R_{16}(g_5) &= 1. \\
R_{17}(g_2) &= 1. & R_{17}(g_3) &= 1. & R_{17}(g_4) &= e_5^4. & R_{17}(g_5) &= 1. \\
R_{18}(g_2) &= 1. & R_{18}(g_3) &= 1. & R_{18}(g_4) &= e_5^3. & R_{18}(g_5) &= 1. \\
R_{19}(g_2) &= 1. & R_{19}(g_3) &= 1. & R_{19}(g_4) &= e_5^2. & R_{19}(g_5) &= 1. \\
R_{20}(g_2) &= 1. & R_{20}(g_3) &= 1. & R_{20}(g_4) &= e_5. & R_{20}(g_5) &= 1. \\
R_{21}(g_2) &= -i\lambda. & R_{21}(g_3) &= -i\phi. & R_{21}(g_4) &= \epsilon. & R_{21}(g_5) &= -\epsilon. \\
R_{22}(g_2) &= i\lambda. & R_{22}(g_3) &= \begin{pmatrix} 0 & -e_5^2 \\ e_5^3 & 0 \end{pmatrix}. & R_{22}(g_4) &= \begin{pmatrix} e_5^4 & 0 \\ 0 & e_5^4 \end{pmatrix}. & R_{22}(g_5) &= -\epsilon. \\
R_{23}(g_2) &= i\lambda. & R_{23}(g_3) &= \begin{pmatrix} 0 & e_5 \\ -e_5^4 & 0 \end{pmatrix}. & R_{23}(g_4) &= \begin{pmatrix} e_5^3 & 0 \\ 0 & e_5^3 \end{pmatrix}. & R_{23}(g_5) &= -\epsilon. \\
R_{24}(g_2) &= -i\lambda. & R_{24}(g_3) &= \begin{pmatrix} 0 & e_{20}^{17} \\ e_{20}^{13} & 0 \end{pmatrix}. & R_{24}(g_4) &= \begin{pmatrix} e_5^2 & 0 \\ 0 & e_5^2 \end{pmatrix}. & R_{24}(g_5) &= -\epsilon. \\
R_{25}(g_2) &= -i\lambda. & R_{25}(g_3) &= \begin{pmatrix} 0 & -e_5 \\ e_5^4 & 0 \end{pmatrix}. & R_{25}(g_4) &= \begin{pmatrix} e_5 & 0 \\ 0 & e_5 \end{pmatrix}. & R_{25}(g_5) &= -\epsilon.
\end{aligned}$$

$G_{40}^{(12)}$

$$R_2(g_2) = -1. \quad R_2(g_3) = -1. \quad R_2(g_4) = 1. \quad R_2(g_5) = 1.$$

$$R_3(g_2) = -1. \quad R_3(g_3) = 1. \quad R_3(g_4) = 1. \quad R_3(g_5) = 1.$$

$$R_4(g_2) = 1. \quad R_4(g_3) = -1. \quad R_4(g_4) = 1. \quad R_4(g_5) = 1.$$

$$R_5(g_2) = -i. \quad R_5(g_3) = -1. \quad R_5(g_4) = -1. \quad R_5(g_5) = 1.$$

$$R_6(g_2) = i. \quad R_6(g_3) = -1. \quad R_6(g_4) = -1. \quad R_6(g_5) = 1.$$

$$R_7(g_2) = -i. \quad R_7(g_3) = 1. \quad R_7(g_4) = -1. \quad R_7(g_5) = 1.$$

$$R_8(g_2) = i. \quad R_8(g_3) = 1. \quad R_8(g_4) = -1. \quad R_8(g_5) = 1.$$

$$R_9(g_2) = \begin{pmatrix} 0 & 0 & 1 & 0 \\ 1 & -1 & 1 & -1 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}. \quad R_9(g_3) = \begin{pmatrix} -1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & -1 \end{pmatrix}.$$

$$R_9(g_4) = \begin{pmatrix} 0 & -1 & 0 & 0 \\ -1 & 0 & 0 & 0 \\ -1 & 1 & -1 & 1 \\ 0 & 0 & 0 & 1 \end{pmatrix}. \quad R_9(g_5) = \begin{pmatrix} 0 & 0 & 0 & -1 \\ 1 & -1 & 1 & -1 \\ 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{pmatrix}.$$

$$R_{10}(g_2) = \begin{pmatrix} 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{pmatrix}. \quad R_{10}(g_3) = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}.$$

$$R_{10}(g_4) = \begin{pmatrix} 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{pmatrix}. \quad R_{10}(g_5) = \begin{pmatrix} -1 & -1 & -1 & -1 \\ 0 & 0 & 0 & 1 \\ 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 \end{pmatrix}.$$

 $G_{40}^{(13)}$

$$R_2(g_2) = -1. \quad R_2(g_3) = -1. \quad R_2(g_4) = -1. \quad R_2(g_5) = 1.$$

$$R_3(g_2) = -1. \quad R_3(g_3) = -1. \quad R_3(g_4) = 1. \quad R_3(g_5) = 1.$$

$$R_4(g_2) = -1. \quad R_4(g_3) = 1. \quad R_4(g_4) = -1. \quad R_4(g_5) = 1.$$

$$R_5(g_2) = -1. \quad R_5(g_3) = 1. \quad R_5(g_4) = 1. \quad R_5(g_5) = 1.$$

$$R_6(g_2) = 1. \quad R_6(g_3) = -1. \quad R_6(g_4) = -1. \quad R_6(g_5) = 1.$$

$$R_7(g_2) = 1. \quad R_7(g_3) = -1. \quad R_7(g_4) = 1. \quad R_7(g_5) = 1.$$

$$R_8(g_2) = 1. \quad R_8(g_3) = 1. \quad R_8(g_4) = -1. \quad R_8(g_5) = 1.$$

$$R_9(g_2) = \begin{pmatrix} -2\Re e_5 & 2\Re e_5 \\ 1 & 2\Re e_5 \end{pmatrix}. \quad R_9(g_3) = -\epsilon. \quad R_9(g_4) = -\epsilon. \quad R_9(g_5) = \begin{pmatrix} -2\Re e_5 & 2\Re e_5 \\ -2\Re e_5 & -1 \end{pmatrix}.$$

$$R_{10}(g_2) = \begin{pmatrix} -1 & 2\Re e_5 \\ 0 & 1 \end{pmatrix}. \quad R_{10}(g_3) = -\epsilon. \quad R_{10}(g_4) = -\epsilon. \quad R_{10}(g_5) = \begin{pmatrix} 0 & 1 \\ -1 & 2\Re e_5 \end{pmatrix}.$$

$$R_{11}(g_2) = \begin{pmatrix} -1 & \varphi \\ 0 & 1 \end{pmatrix}. \quad R_{11}(g_3) = -\epsilon. \quad R_{11}(g_4) = \epsilon. \quad R_{11}(g_5) = \begin{pmatrix} 0 & 1 \\ -1 & \varphi \end{pmatrix}.$$

$$R_{12}(g_2) = \begin{pmatrix} \varphi & 1 \\ \varphi & -\varphi \end{pmatrix}. \quad R_{12}(g_3) = -\epsilon. \quad R_{12}(g_4) = \epsilon. \quad R_{12}(g_5) = \begin{pmatrix} -\varphi & \varphi \\ -\varphi & -1 \end{pmatrix}.$$

$$\begin{aligned}
 R_{13}(g_2) &= \begin{pmatrix} 1 & 0 \\ 2\Re e_5 & -1 \end{pmatrix}. \quad R_{13}(g_3) = \epsilon. \quad R_{13}(g_4) = -\epsilon. \quad R_{13}(g_5) = \begin{pmatrix} -2\Re e_5 & -2\Re e_5 \\ 2\Re e_5 & -1 \end{pmatrix}. \\
 R_{14}(g_2) &= \begin{pmatrix} 2\Re e_5 & -1 \\ -2\Re e_5 & -2\Re e_5 \end{pmatrix}. \quad R_{14}(g_3) = \epsilon. \quad R_{14}(g_4) = -\epsilon. \quad R_{14}(g_5) = \begin{pmatrix} 0 & 1 \\ -1 & 2\Re e_5 \end{pmatrix}. \\
 R_{15}(g_2) &= \begin{pmatrix} \varphi & -1 \\ -\varphi & -\varphi \end{pmatrix}. \quad R_{15}(g_3) = \epsilon. \quad R_{15}(g_4) = \epsilon. \quad R_{15}(g_5) = \begin{pmatrix} \varphi & -1 \\ 1 & 0 \end{pmatrix}. \\
 R_{16}(g_2) &= \begin{pmatrix} \varphi & -1 \\ -\varphi & -\varphi \end{pmatrix}. \quad R_{16}(g_3) = \epsilon. \quad R_{16}(g_4) = \epsilon. \quad R_{16}(g_5) = \begin{pmatrix} -\varphi & -\varphi \\ \varphi & -1 \end{pmatrix}.
 \end{aligned}$$

 $G_{40}^{(14)}$

$$\begin{aligned}
 R_2(g_2) &= -1. \quad R_2(g_3) = -1. \quad R_2(g_4) = -1. \quad R_2(g_5) = 1. \\
 R_3(g_2) &= -1. \quad R_3(g_3) = -1. \quad R_3(g_4) = 1. \quad R_3(g_5) = 1. \\
 R_4(g_2) &= -1. \quad R_4(g_3) = 1. \quad R_4(g_4) = -1. \quad R_4(g_5) = 1. \\
 R_5(g_2) &= -1. \quad R_5(g_3) = 1. \quad R_5(g_4) = 1. \quad R_5(g_5) = 1. \\
 R_6(g_2) &= 1. \quad R_6(g_3) = -1. \quad R_6(g_4) = -1. \quad R_6(g_5) = 1. \\
 R_7(g_2) &= 1. \quad R_7(g_3) = -1. \quad R_7(g_4) = 1. \quad R_7(g_5) = 1. \\
 R_8(g_2) &= 1. \quad R_8(g_3) = 1. \quad R_8(g_4) = -1. \quad R_8(g_5) = 1. \\
 R_9(g_2) &= -1. \quad R_9(g_3) = -1. \quad R_9(g_4) = -1. \quad R_9(g_5) = e_5^4. \\
 R_{10}(g_2) &= -1. \quad R_{10}(g_3) = -1. \quad R_{10}(g_4) = -1. \quad R_{10}(g_5) = e_5^3. \\
 R_{11}(g_2) &= -1. \quad R_{11}(g_3) = -1. \quad R_{11}(g_4) = -1. \quad R_{11}(g_5) = e_5^2. \\
 R_{12}(g_2) &= -1. \quad R_{12}(g_3) = -1. \quad R_{12}(g_4) = -1. \quad R_{12}(g_5) = e_5. \\
 R_{13}(g_2) &= -1. \quad R_{13}(g_3) = -1. \quad R_{13}(g_4) = 1. \quad R_{13}(g_5) = e_5^4. \\
 R_{14}(g_2) &= -1. \quad R_{14}(g_3) = -1. \quad R_{14}(g_4) = 1. \quad R_{14}(g_5) = e_5^3. \\
 R_{15}(g_2) &= -1. \quad R_{15}(g_3) = -1. \quad R_{15}(g_4) = 1. \quad R_{15}(g_5) = e_5^2. \\
 R_{16}(g_2) &= -1. \quad R_{16}(g_3) = -1. \quad R_{16}(g_4) = 1. \quad R_{16}(g_5) = e_5. \\
 R_{17}(g_2) &= -1. \quad R_{17}(g_3) = 1. \quad R_{17}(g_4) = -1. \quad R_{17}(g_5) = e_5^4. \\
 R_{18}(g_2) &= -1. \quad R_{18}(g_3) = 1. \quad R_{18}(g_4) = -1. \quad R_{18}(g_5) = e_5^3. \\
 R_{19}(g_2) &= -1. \quad R_{19}(g_3) = 1. \quad R_{19}(g_4) = -1. \quad R_{19}(g_5) = e_5^2. \\
 R_{20}(g_2) &= -1. \quad R_{20}(g_3) = 1. \quad R_{20}(g_4) = -1. \quad R_{20}(g_5) = e_5. \\
 R_{21}(g_2) &= -1. \quad R_{21}(g_3) = 1. \quad R_{21}(g_4) = 1. \quad R_{21}(g_5) = e_5^4. \\
 R_{22}(g_2) &= -1. \quad R_{22}(g_3) = 1. \quad R_{22}(g_4) = 1. \quad R_{22}(g_5) = e_5^3. \\
 R_{23}(g_2) &= -1. \quad R_{23}(g_3) = 1. \quad R_{23}(g_4) = 1. \quad R_{23}(g_5) = e_5^2. \\
 R_{24}(g_2) &= -1. \quad R_{24}(g_3) = 1. \quad R_{24}(g_4) = 1. \quad R_{24}(g_5) = e_5. \\
 R_{25}(g_2) &= 1. \quad R_{25}(g_3) = -1. \quad R_{25}(g_4) = -1. \quad R_{25}(g_5) = e_5^4. \\
 R_{26}(g_2) &= 1. \quad R_{26}(g_3) = -1. \quad R_{26}(g_4) = -1. \quad R_{26}(g_5) = e_5^3. \\
 R_{27}(g_2) &= 1. \quad R_{27}(g_3) = -1. \quad R_{27}(g_4) = -1. \quad R_{27}(g_5) = e_5^2. \\
 R_{28}(g_2) &= 1. \quad R_{28}(g_3) = -1. \quad R_{28}(g_4) = -1. \quad R_{28}(g_5) = e_5. \\
 R_{29}(g_2) &= 1. \quad R_{29}(g_3) = -1. \quad R_{29}(g_4) = 1. \quad R_{29}(g_5) = e_5^4. \\
 R_{30}(g_2) &= 1. \quad R_{30}(g_3) = -1. \quad R_{30}(g_4) = 1. \quad R_{30}(g_5) = e_5^3. \\
 R_{31}(g_2) &= 1. \quad R_{31}(g_3) = -1. \quad R_{31}(g_4) = 1. \quad R_{31}(g_5) = e_5^2. \\
 R_{32}(g_2) &= 1. \quad R_{32}(g_3) = -1. \quad R_{32}(g_4) = 1. \quad R_{32}(g_5) = e_5. \\
 R_{33}(g_2) &= 1. \quad R_{33}(g_3) = 1. \quad R_{33}(g_4) = -1. \quad R_{33}(g_5) = e_5^4.
 \end{aligned}$$

$$\begin{aligned}
R_{34}(g_2) &= 1. & R_{34}(g_3) &= 1. & R_{34}(g_4) &= -1. & R_{34}(g_5) &= e_5^3. \\
R_{35}(g_2) &= 1. & R_{35}(g_3) &= 1. & R_{35}(g_4) &= -1. & R_{35}(g_5) &= e_5^2. \\
R_{36}(g_2) &= 1. & R_{36}(g_3) &= 1. & R_{36}(g_4) &= -1. & R_{36}(g_5) &= e_5. \\
R_{37}(g_2) &= 1. & R_{37}(g_3) &= 1. & R_{37}(g_4) &= 1. & R_{37}(g_5) &= e_5^4. \\
R_{38}(g_2) &= 1. & R_{38}(g_3) &= 1. & R_{38}(g_4) &= 1. & R_{38}(g_5) &= e_5^3. \\
R_{39}(g_2) &= 1. & R_{39}(g_3) &= 1. & R_{39}(g_4) &= 1. & R_{39}(g_5) &= e_5^2. \\
R_{40}(g_2) &= 1. & R_{40}(g_3) &= 1. & R_{40}(g_4) &= 1. & R_{40}(g_5) &= e_5.
\end{aligned}$$

REFERENCES

1. László Babai and Lajos Rónyai, *Computing irreducible representations of finite groups*, Math. Comp. **55** (1990), 705–722. MR 1035925
2. Christopher John Bradley and Arthur P. Cracknell, *The mathematical theory of the symmetry in solids*, Clarendon Press, Oxford, 1972.
3. John D. Dixon, *Computing irreducible representations of groups*, Math. Comp. **24** (1970), no. 111, 707–712. MR 0280611
4. The GAP Group, *GAP – groups, algorithms, and programming, version 4.7.4*, 2015.
5. Noboru Itô, *On the degrees of irreducible representations of a finite group*, Nagoya Math. J. **3** (1951), no. 1, 5–6. MR 0044528
6. Richard J. Mathar, *Plots of cycle graphs of the finite groups up to order 36*, vixra:1406.0183 (2014).
7. Gerhard J. A. Schneider, *Dixon’s character table algorithm revisited*, J. Symbolic Comput **9** (1990), no. 5–6, 601–606.
URL: <http://www.mpia.de/~mathar>

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