

# Proof of Fermat's last theorem (Part I of III)

$$a^n + b^n = c^n \quad (n > 1 \text{ and odd})$$

Objet: Proof of Fermat's last theorem with conventional means.

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## 1) Introduction :

- ✓ I am not a professional of mathematics.
- ✓ My English is poor. I use **google translate** to write these pages.

## 2) I prove that $c < (a + b)$

$$(a + b)^n = a^n + b^n + \sum_{k=1}^n \binom{n}{k} a^k b^{n-k}$$

$$\text{Then } (a + b)^n > (a^n + b^n)$$

$$\text{Then } (a + b)^n > c^n \text{ because } c^n = a^n + b^n$$

$$\text{Then } (a + b) > c$$

$d$  is a natural number. It is the complement of  $c$  to  $(a + b)$ .

$$c + d = a + b$$

$$c = a + b - d$$

$$c - b = a - d$$

$$c - a = b - d$$

## 3) I prove a parity of $d$

Whatever the parity of  $a$ ,  $b$  and  $c$ , we can easily verify that  $d$  is always even.

<b>a</b>	<b>b</b>	<b>c</b>	<b>d</b>
even	even	even	even
even	odd	odd	even
odd	even	odd	even
odd	odd	even	even

$2^n$  divide  $d^n$ .

4) Conditions (supposition) to prove Fermat's last theorem :

- ✓ a, b, c, d and n are non-zero positive integers
- ✓ a, b and c are pairwise coprime
- ✓  $n > 1$  and odd
- ✓  $a^n + b^n = c^n$
- ✓  $a + b = c + d$
- ✓  $a < b$

5) I prove that c is not coprime with d

$$d^n = d^n$$

$$c^n - a^n - b^n = 0$$

$$d^n = d^n + c^n - a^n - b^n$$

$$d^n = (d^n + c^n) - (a^n + b^n)$$

$$(c + d) \text{ divide } (d^n + c^n)$$

$$(a + b) \text{ divide } (a^n + b^n)$$

$$(c + d) = (a + b)$$

$$(c + d) \text{ divide } d^n$$

Any integer which divide  $(c + d)$  divide  $d^n$

Any prime number which divide  $(c + d)$  divide  $d^n$

Any prime number which divide  $(c + d)$  divide  $d$

Any prime number which divide  $[(c + d) \text{ and } d]$  divide  $c$

***c is not coprime with d***

$$(c + d) = (a + b)$$

$$(a + b) \text{ divide } d^n$$

Any prime number which divide  $(a + b)$  divide  $d$

6) I prove that a is not coprime with d

$$d^n = d^n$$

$$c^n - a^n - b^n = 0$$

$$d^n = d^n + c^n - a^n - b^n$$

$$d^n = (c^n - b^n) - (a^n - d^n)$$

$$(c - b) \text{ divide } (c^n - b^n)$$

$$(a - d) \text{ divide } (a^n - d^n)$$

$$(c - b) = (a - d)$$

$$(a - d) \text{ divide } d^n$$

$$(c - b) \text{ divide } d^n$$

Any integer which divide  $(a - d)$  divide  $d^n$   
 Any prime number divide  $(a - d)$  divide  $d^n$   
 Any prime number divide  $(a - d)$  divide  $d$   
 Any prime number divide  $[(a - d) \text{ and } d]$  divide  $a$   
 **$a$  is not coprime with  $d$  (Except if  $(a - d) = 1$ ).**

$$(c - b) = (a - d)$$

$$(c - b) \text{ divide } d^n$$

Any prime number which divide  $(c - b)$  divide  $d$ .

7) I prove that b is not coprime with d

$$d^n = d^n$$

$$c^n - a^n - b^n = 0$$

$$d^n = d^n + c^n - a^n - b^n$$

$$d^n = (c^n - a^n) - (b^n - d^n)$$

$$(c - a) \text{ divide } (c^n - a^n)$$

$$(b - d) \text{ divide } (b^n - d^n)$$

$$(c - a) = (b - d)$$

$$(b - d) \text{ divide } d^n$$

$$(c - a) \text{ divide } d^n$$

Any integer which divide  $(b - d)$  divide  $d^n$

Any prime number divide  $(b - d)$  divide  $d^n$

Any prime number divide  $(b - d)$  divide  $d$

Any prime number divide  $[(b - d) \text{ and } d]$  divide  $b$

**$b$  is not coprime with  $d$**

$$(c - a) = (b - d)$$

$$(c - a) \text{ divide } d^n$$

Any prime number which divide  $(c - a)$  divide  $d$

## 8) Contradictions

I proved that:

1. Any prime number which divide  $(a + b)$  *divide d.*
2. Any prime number which divide  $(c + d)$  *divide d.*
3. Any prime number which divide  $(a - d)$  *divide d.*
4. Any prime number which divide  $(c - b)$  *divide d.*
5. Any prime number which divide  $(b - d)$  *divide d.*
6. Any prime number which divide  $(c - a)$  *divide d.*

Proof 1 and proof 3

Any prime number that divide  $(d$  and  $a)$  must necessarily divide  $b$ ; **but  $a$  and  $b$  are hypothetically pairwise coprime.**

Proof 2 and proof 6

Any prime number that divide  $(c$  and  $d)$  must necessarily divide  $a$ ; **but  $c$  and  $a$  are hypothetically pairwise coprime.**

Proof 2 and proof 4

Any prime number that divide  $(c$  and  $d)$  must necessarily divide  $b$ ; **but  $c$  and  $b$  are hypothetically pairwise coprime.**

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