

Proof of Fermat's last theorem (Part II of III)

$$a^n + b^n = c^n \quad (n > 1 \text{ and odd})$$

Objet: Proof of Fermat's last theorem with conventional means.

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Another way to approach research proof

$$a^n + b^n = c^n$$

$$(a + b)^n = (c + d)^n$$

$$a^n + b^n + \sum_{k=1}^n \binom{n}{k} a^k b^{n-k} = c^n + d^n + \sum_{k=1}^n \binom{n}{k} c^k d^{n-k}$$

$$a^n + b^n + \sum_{k=1}^n \binom{n}{k} a^k b^{n-k} = c^n + d^n + \sum_{k=1}^n \binom{n}{k} c^k d^{n-k}$$

$$\sum_{k=1}^n \binom{n}{k} a^k b^{n-k} = d^n + \sum_{k=1}^n \binom{n}{k} c^k d^{n-k}$$

$$d^n = \sum_{k=1}^n \binom{n}{k} a^k b^{n-k} - \sum_{k=1}^n \binom{n}{k} c^k d^{n-k}$$

$$d^n = \sum_{k=1}^n \binom{n}{k} (a^k b^{n-k} - c^k d^{n-k})$$

I prove that $ab - cd = (a - d)(b - d)$

$$c = a + b - d$$

$$ab - cd = ab - (a + b - d)d$$

$$ab - cd = ab - ad - bd + d^2$$

$$ab - cd = a(b - d) - d(b - d)$$

$$ab - cd = (a - d)(b - d)$$

For $n = 1, 2$ or 3

$n = 1$	$(c + d)^1 = (a + b)^1$ $d^1 = a^1 + b^1 - c^1$ $d^1 = 0.$
$n = 2$	$(c + d)^2 = (a + b)^2$ $c^2 + 2cd + d^2 = a^2 + 2ab + b^2$ $d^2 = a^2 + b^2 - c^2 + 2ab - 2cd$ $d^2 = 2ab - 2cd$ $d^2 = 2(a - d)(b - d)$
$n = 3$	$(c + d)^3 = (a + b)^3$ $c^3 + 3c^2d + 3cd^2 + d^3 = a^3 + 3a^2b + 3ab^2 + b^3$ $d^3 = a^3 + b^3 - c^3 + 3a^2b + 3ab^2 - 3c^2d - 3cd^2$ $d^3 = 3(a^2b + ab^2 - c^2d - cd^2)$ $d^3 = 3(ab(a + b) - cd(c + d))$ $d^3 = 3(a + b)(ab - cd)$ $d^3 = 3(a + b)(a - d)(b - d)$