# From E8 Root Vector Geometry to the LHC 

Frank Dodd (Tony) Smith, Jr. - 2017 - viXra 1701.0496


#### Abstract

This paper is intended to be a only rough semi-popular overview of how the 240 Root Vectors of E8 can be used to construct a useful Lagrangian describing Gravity and Dark Energy plus the Standard Model. For details and references, see viXra/1602.0319. The 240 Root Vectors of E8 represent the physical forces, particles, and spacetime that make up the construction of a realistic Lagrangian describing the Octonionic Inflation Era followed by a Quaternionic M4 x CP2 Kaluza-Klein Era in which the Hlggs emerges by the Mayer mechanism and 2nd and 3rd Generation Fermions appear. By generalizations of the Nambu-Jona-Lasinio models, the Higgs is seen to be a Truth Quark-AntiQuark Condensate giving 3 Mass States of the Higgs and 3 Mass States of the Truth Quark. My analysis of Fermilab and LHC observation data indicates that Fermilab has observed the 3 Truth Quark Mass States and LHC has observed the 3 Higgs Mass States. The Lagrangian, which is fundamentally classical, is constructed from E8 only and E 8 lives in $\mathrm{Cl}(16)=\mathrm{Cl}(8) \times \mathrm{Cl}(8)$ which corresponds to two copies of an E8 Lattice. A seperate paper discusses using a third copy of an E8 Lattice in connection with construction of a realistic Algebraic Quantum Field Theory related to the Leech Lattice.


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# The $\mathbf{2 4 0}$ root vectors of E8 are of equal length in 8 dimensions as they form the 240-vertex Witting-Gossett polytope so <br> you can in 8 dimensions visualize how they group together <br> If you look at the 240 vertices as points on an 8-dim sphere then <br> you can pick one point as the North Pole and see where the other points fall at their angle of latitude: 

1 is at North Pole

## 56 nearest neighbors of the North Pole are at North Temperate Latitude

## 126 2nd nearest neighbors of the North Pole are at the Equator

56 3rd nearest neighbors of the North Pole are at South Temperate Latitude

1 4th nearest neighbor of the North Pole is Anitpodal at the South Pole

Therefore you see that the 240 break down into $1+56+126+56+1$
but
what you need to see next is which root vector corresponds to which physics thing.

## Geometry of the E8 Lie Group gives you some ideas:

$56+56=112$ Temperate North and South is the D8 = Spin(16) subgroup of E8 and they correspond to Gravity + Dark Energy and the Standard Model gauge groups and to 8-dimensonal Spacetime position and momentum.

Each 56 breaks down into $24+32$.
North Temperate 24 = D4 Lie Algebra $=$ Spin $(2,6)$ which contains Conformal Spin $(2,4)$ which gives Gravity plus Conformal Dark Energy as well as Ghosts of Standard Model Gauge Bosons

South Temperate 24 = D4 Lie Algebra = Spin(8) which contains SU(4) which gives $\operatorname{SU}(3)$ of the Color Force which is the Global Group of Kaluza-Klein Internal Symmetry Space CP2 and $C P 2=S U(3) / S U(2) \times U(1)$ contains groups of Weak and Electromagnetic Forces as well as Ghosts of Gravity and Dark Energy

Symmetric space D8 / D4(gravity) x D4(standard model) is 112-28-28 = 64-dim and it corresponds to $64=8$-dim position $\times 8$-dim momentum of 8 -dim Spacetime which
8-dim Spacetime reduces to $4+4$ dim M4 x CP2 Kaluza-Klein spacetime

Symmetric space E8 / D8 is 128-dim Rosenfeld OctoOctonionic Projective Plane which is
$1+126+1$ of the North Pole, Equator, and South Pole
The 128 are the 8 Spacetime components of Fermions: 8 Particles and 8 AntiParticles for $8 x 8=64$ Particle components $+8 x 8=64$ AntiParticle components.
1 at North Pole $=$ time component of Neutrino
1 at South Pole $=$ time component of AntiNeutrino
126 at Equator $=$ other components of Leptons and Quarks $=$ root vectors of E7
Symmetric space E7 / D6xSU(2) = 64-dim Rosenfeld QuaterOctonionic Projective Plane corresponds to 8 components of (electron + rgb up quarks) $=8 \times 4=32$

$$
\text { plus } 8 \text { components of (positron }+ \text { rgb up antiquarks) }=8 \times 4=32
$$

D6 $x \mathrm{SU}(2)$ has $60+2=62$ root vectors so if you add $1+1$ North and South Poles you get 64 corresponding to 8 components of (neutrino + rgb down quarks) $=8 \times 4=32$ plus 8 components of (antineutrino + rgb down antiquarks $)=8 \times 4=32$

## 2-dim projection of 240 E8 Root Vectors

gives useful visualization of which root vector corresponds to which physics thing

In 2-dim Projection the Root Vectors no longer have the same distance from origin

but in this particular 2-dim projection the physical interpretations of each Root Vector becomes clear:

$\mathrm{E}=$ electron, $\mathrm{UQr}=$ red up quark, $\mathrm{UQg}=$ green up quark, $\mathrm{UQb}=$ blue up quark
$\mathrm{Nu}=$ neutrino, $\mathrm{DQr}=$ red down quark, $\mathrm{DQg}=$ green down quark, $\mathrm{DQb}=$ blue down quark
$\mathrm{P}=$ positron, aUQar = anti-red up antiquark,
aUQag = anti-green up antiquark, aUQab = anti-blue up antiquark
$\mathrm{aNu}=$ antineutrino, $\mathrm{aDQar}=$ anti-red down antiquark
white boxes enclose time components of neutrino and antineutrino
aDQag = anti-green down antiquark, aDQab = anti-blue down antiquark
Each Lepton and Quark has 8 components with respect to $4+4$ dim Kaluza-Klein
6 orange $\mathrm{SU}(3)$ and 2 orange $\mathrm{SU}(2)$ represent Standard Model root vectors
$24-6-2=16$ orange represent $\mathrm{U}(2,2)$ Conformal Gravity Ghosts
12 yellow $\operatorname{SU}(2,2)$ represent Conformal Gravity SU(2,2) root vectors
$24-12=12$ yellow represent Standard Model Ghosts
$32+32=64$ blue represent $4+4$ dim Kaluza-Klein spacetime position and momentum
Here is how the 2-dim physical interpretations correspond to the 8-dim Sphere Latitude decomposition:

1 is at North Pole

56 nearest neighbors of the North Pole are at North Temperate Latitude

126 2nd nearest neighbors of the North Pole are at the Equator

56 3rd nearest neighbors of the North Pole are at South Temperate Latitude

4th nearest neighbor of the North Pole is Anitpodal at the South Pole


## Recipe for constructing Lagrangian from E8 Root Vectors

My favorite Fundamental Structure of Physics is the Lagrangian.
In his Dirac Lecture, Steven Weinberg says "... Lagrangian density ...
you can think of it as the density of energy.
Energy is the quantity that ... tells us how the system evolves. ...".
The Lagrangian Density contains Boson terms and Fermion terms. To get the full Lagrangian, you integrate those terms over Spacetime.

The Code or Recipe just says:
put
the Gravity + Dark Energy Gauge Bosons and Standard Model Ghosts and
the Standard Model Gauge Bosons and Gravity-Dark Energy Ghosts into the Lagrangian Density Boson terms in accord with the standard way of constructing physics boson terms
and
put
the Fermion Particles and AntiParticles
into the Lagrangian Density Fermion terms in accord with the standard way of constructing physics fermion terms
and
put the Spacetime Root Vectors
into the Spacetime Base Manifold over which the Lagrangian Density is integrated.

In terms of the preceding pictures of physics of E8 Root Vectors the Code or Recipe gives a Lagrangian that is a realistic physics model.

Of course, to completely carry out the Code or Recipe you need to write out the Lagrangian terms in the math language of conventional physics and that is described in some of the long papers I have written (see my web site and my viXra papers).

Here I am just trying to show the basic underlying structure of E8 Geometry so I am not writing down the extensive details in this paper.


The fundamental Lagrangian formed by this structure is an Octonionic structure over 8-dim Spacetime and is effective during the Initial Big Bang and Inflation.


Since Octonionic Quantum Field Theory is NOT Unitary, Particle / AntiParticle Creation occurs during Inflation.

Inflation Ends when a preferred Quaternionic Subspacetime freezes out, converting 8 dim Spacetime into 4+4 dim M4 x CP2 Spacetime where

M4 = Physical Minkowski Spacetime and
CP2 = SU(3) / U(2) Internal Symmetry Space and
the Octonionic Integral becomes two Quaternionic Integrals


Here is how the Witting 240-Polytope splits into two 600-Cells:


In more detail, start with the North Pole.
Then the North Pole has 56 nearest neighbors that live on a North Temperate Zone which is a fixed Latitude Angle from the North Pole
and is a 6 -dim sphere Latitude subset of the 7 -dim sphere.
The 56 are of two kinds:
32 describing half of 8 -dim Spacetime for 4-dim Minkowski Physical Spacetime and 24 describing Gauge Bosons and Ghosts for Gravity and the Standard Model.
The 32 Spacetime-type vertices live on the Equator of the 6 -dim sphere and are distributed on that 5 -dim sphere as one half of the 64 vertices of a hypercube in 6 -dim space. 12 of the 24 live on a North Temperate Latitude of the 6 -dim sphere
The other 12 of the 24 live on a South Temperate Latitude of the 6 -dim sphere.
Then there are 126 next-nearest neighbors to the North Pole.
They live on the Equator of the 7 -dim sphere and are distributed on that 6-dim sphere as the Root Vectors of the E7 Lie Algebra


126 vertices of $2_{31}$ represent the
root vectors of $\mathrm{E}_{7}$
They correspond to 126 of the 128 components of $8+8$ Fermion Particles+AntiParticles.
Then are the 56 nearest neighbors of the South Pole that of a South Temperate Zone which is a fixed Latitude Angle from the South Pole
and is a 6 -dim sphere Latitude subset of the 7 -dim sphere.
The 56 are of two kinds:
32 describing half of 8 -dim Spacetime
for 4-dim CP2 Standard Model Internal Symmetry Space and
24 describing Gauge Bosons and Ghosts for the Standard Model and Gravity.
The 32 Spacetime-type vertices live on the Equator of the 6-dim sphere and
are distributed on that 5 -dim sphere as the other half of the 64 vertices of a hypercube in 6 -dim space.
12 of the 24 live on a North Temperate Latitude of the 6 -dim sphere
The other 12 of the 24 live on a South Temperate Latitude of the 6 -dim sphere.
Then there is finally the South Pole.The 240-Polytope decomposes into two 120-vertex 600-Cells

## The 240-Polytope splits into two 120-vertex 600-Cells:

Sadoc and Mosseri in their book "Geometrical Frustration" (Cambridge 1999, 2006), say: "...


Fig. A5.1. The $\{3,3,5\}$ polytope. Different flat sections in $S^{3}$ (with one site on top) give the following successive shells; (a) an icosahedral shell formed by the first 12 neighbours, (b) a dodecahedral shell, (c) a second and larger icosahedral shell, (d) an icosidodecahedral shell on the equatorial sphere. Then other shells are symmetrically disposed in the second 'south' hemi-hypersphere, relative to the equatorial sphere (e).

Table A5.1. Sections of the $\{3,3,5\}$ polytope (with an edge length equal to $2 \tau^{-1}$ ) beginning with a vertex

| Section | $x_{0}$ | $\left(x_{1}, x_{2}, x_{3}\right)^{1}$ | Vertex number | Shape |
| :---: | :---: | :---: | :---: | :---: |
| 0 | 2 | $(0,0,0)$ | 1 | point |
| 1 | $\tau$ | $\left(1,0, \tau^{-1}\right)$ | 12 | icosahedron <br> dodecahedron <br> 2 |
|  | 1 | $(1,1,1)$ | 20 | icosahedron |
| 3 | $\tau^{-1}$ | $\left(\tau, \tau^{-1}, 0\right)$ |  | $(\tau, 0,1)$ |
| 4 | 0 | $(2,0,0)$ | 30 | icosidodecahedron |
| 5 | $-\tau^{-1}$ | $\left(\tau, 1, \tau^{-1}\right)$ | $(\tau, 0,1)$ | 12 |
| 6 | -1 | $(1,1,1)$ | 20 | icosahedron |
| 7 | $-\tau$ | $\left(\tau, \tau^{-1}, 0\right)$ | $\left(1,0, \tau^{-1}\right)$ | 12 |
| 8 | -2 | $(0,0,0)$ | 1 | dodecahedron |

${ }^{\prime}$ Cyclic permutation with all possible changes of signs. $\tau=(1+\sqrt{5}) / 2$.

One 600-Cell represents M4 and the other 600-Cell represents CP2:


Splitting Octonionic Spacetime into Quaternionic M4 x CP2 Kaluza-Klein over CP2 produces
Higgs by the Mayer Mechanism and Second and Third Generation Fermions


By generalizations of the Nambu-Jona-Lasinio mechanism Higgs is a Fermion Particle-AntiParticle Condensate which, since the Truth Quark is by far the most massive Fermion, effectively means that Higgs is a Truth Quark - Truth AntiQuark Condensate.


Higgs - Truth Quark System has 3 mass states for Higgs and for Truth Quark that have (in my opinion) been by Fermilab and LHC experiments


## Semileptonic histograms of CDF and D0 show 3 Truth Quark Mass States



Higgs $->$ ZZ $->4$ I channel histogram of CMS shows 3 Higgs Mass States


