

# A New Boundary for Heisenberg's Uncertainty Principle Good Bye to the Point Particle Hypothesis?

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## Abstract

In this paper we are combining Heisenberg's uncertainty principle with Haug's new insight on the maximum velocity for anything with rest-mass; see [1, 2, 3]. This leads to a new and exact boundary condition on Heisenberg's uncertainty principle. The uncertainty in position at the potential maximum momentum for subatomic particles as derived from the maximum velocity is half of the Planck length.

Perhaps Einstein was right after all when he stated, "God does not play dice." Or at least the dice may have a stricter boundary on possible outcomes than we have previously thought.

We also show how this new boundary condition seems to make big  $G$  consistent with Heisenberg's uncertainty principle. We obtain a mathematical expression for big  $G$  that is fully in line with empirical observations.

Hopefully our analysis can be a small step in better understanding Heisenberg's uncertainty principle and its interpretations and by extension, the broader implications for the quantum world.

**Key words:** Heisenberg's uncertainty principle, maximum velocity matter, point particle, boundary condition, big  $G$ , Planck mass particle, Planck length, reduced Compton wavelength.

## 1 Introduction

Haug [1, 2, 3] has recently introduced a new maximum velocity for subatomic particles (anything with mass) that is just below the speed of light. The formula is given by

$$v_{max} = c\sqrt{1 - \frac{l_p^2}{\bar{\lambda}^2}} \quad (1)$$

where  $\bar{\lambda}$  is the reduced Compton wavelength of the particle we are trying to accelerate and  $l_p$  is the Planck length [4]. This maximum velocity puts an upper boundary condition on the kinetic energy, the momentum, and the relativistic mass, as well as on the relativistic Doppler shift in relation to subatomic particles. Basically, no fundamental particle can attain a relativistic mass higher than the Planck mass, and the shortest reduced Compton wavelength we can observe from length contraction is the Planck length. In addition, the maximum frequency is limited to the Planck frequency, the Planck particle mass is invariant, and so is the Planck length (when related to the reduced Compton wavelength). Here we will combine this equation with Heisenberg's uncertainty principle.

## 2 Heisenberg's Uncertainty Principle in relation to Maximum Momentum

Heisenberg's uncertainty principle [5] is given by<sup>1</sup>

$$\sigma_x \sigma_p \geq \frac{\hbar}{2} \quad (2)$$

where  $\sigma_x$  is considered to be the uncertainty in the position,  $\sigma_p$  is the uncertainty in the momentum, and  $\hbar$  is the reduced Planck constant.

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<sup>1</sup>See also Kennard [6] that was the first to "prove" this modern inequality based on the work of Heisenberg.

Haug [1] has shown that the maximum momentum for a fundamental particle likely is given by

$$\begin{aligned}
p_{max} &= \frac{mv_{max}}{\sqrt{1 - \frac{v_{max}^2}{c^2}}} \\
p_{max} &= \frac{mv_{max}}{\sqrt{1 - \frac{\left(c\sqrt{1 - \frac{l_p^2}{\lambda^2}}\right)^2}{c^2}}} \\
p_{max} &= \frac{mv_{max}}{\sqrt{1 - \frac{c^2 + c^2 \frac{l_p^2}{\lambda^2}}{c^2}}} \\
p_{max} &= \frac{mc\sqrt{1 - \frac{l_p^2}{\lambda^2}}}{\frac{l_p}{\lambda}} \\
p_{max} &= m_p c \sqrt{1 - \frac{l_p^2}{\lambda^2}} \tag{3}
\end{aligned}$$

Based on this we can find a lower boundary in the uncertainty of the position,  $\sigma_x$ , for of any fundamental particle when assuming the  $\sigma_p$  is limited to the maximum momentum for the subatomic particle in question. From this we get

$$\begin{aligned}
\sigma_x \sigma_p &\geq \frac{\hbar}{2} \\
\sigma_x \frac{mv_{max}}{\sqrt{1 - \frac{v_{max}^2}{c^2}}} &\geq \frac{\hbar}{2} \\
\sigma_x m_p v_{max} &\geq \frac{\hbar}{2} \\
\sigma_x m_p c \sqrt{1 - \frac{l_p^2}{\lambda^2}} &\geq \frac{\hbar}{2} \\
\sigma_x &\geq \frac{\hbar}{2m_p c \sqrt{1 - \frac{l_p^2}{\lambda^2}}} \tag{4}
\end{aligned}$$

and since the Planck mass can be written as  $m_p = \frac{\hbar}{l_p c}$ , we can rewrite this as

$$\begin{aligned}
\sigma_x &\geq \frac{\hbar}{2 \frac{\hbar}{l_p c} c \sqrt{1 - \frac{l_p^2}{\lambda^2}}} \\
\sigma_x &\geq \frac{l_p}{2\sqrt{1 - \frac{l_p^2}{\lambda^2}}} \tag{5}
\end{aligned}$$

For any known fundamental particle,  $\bar{\lambda} \gg l_p$  so we can use the first term of a series expansion:  $\sqrt{1 - \frac{l_p^2}{\lambda^2}} \approx 1 - \frac{1}{2} \frac{l_p^2}{\lambda^2}$ . This gives us

$$\begin{aligned}
\sigma_x &\geq \frac{l_p}{2\left(1 - \frac{1}{2} \frac{l_p^2}{\lambda^2}\right)} \\
\sigma_x &\geq \frac{l_p}{2 - \frac{l_p^2}{\lambda^2}} \tag{6}
\end{aligned}$$

and when  $\bar{\lambda} \gg l_p$  we have a very good approximation by

$$\sigma_x \geq \frac{l_p}{2} \tag{7}$$

In other words, the maximum uncertainty in the position of any fundamental subatomic particle (when assuming  $\sigma_p$  is equal to the maximum momentum of the particle) is half the Planck length. This lies in strong contrast to standard physics, where there is basically no boundary on the maximum momentum a fundamental particle can achieve as long as it is below infinite. Therefore, in the standard theory there



We are not the only ones to suggest an absolute minimum uncertainty in the position of any particle, such as an electron. Adler and Santiago [9] have, based on assumed gravitational interaction of the photon and the particle being observed, modified the uncertainty principle with an additional term. By doing this they find a minimum uncertainty in the position that is not far from our prediction. The strength in our result is that no additional terms in the Heisenberg principle are needed to get a minimum uncertainty in the position of any particle, and thereby also a maximum limit in the uncertainty of the momentum.

### 3 Time and Energy

Heisenberg's uncertainty principle in terms of time and energy can be written as

$$\sigma_t \sigma_E \geq \frac{\hbar}{2} \quad (10)$$

Haug [1] has shown that the maximum kinetic energy of a fundamental particle with reduced Compton wavelength of  $\bar{\lambda}$  is given by

$$\begin{aligned} E_{k,max} &= \frac{mc^2}{\sqrt{1 - \frac{v_{max}^2}{c^2}}} - mc^2 \\ E_{k,max} &= \frac{mc^2}{\sqrt{1 - \frac{\left(c\sqrt{1 - \frac{l_p^2}{\bar{\lambda}^2}}\right)^2}{c^2}}} - mc^2 \\ E_{k,max} &= \frac{mc^2}{\sqrt{1 - \frac{c^2\left(1 - \frac{l_p^2}{\bar{\lambda}^2}\right)}{c^2}}} - mc^2 \\ E_{k,max} &= \frac{mc^2}{\frac{l_p}{\bar{\lambda}}} - mc^2 \\ E_{k,max} &= \frac{\bar{\lambda}}{l_p} mc^2 - mc^2 \\ E_{k,max} &= \frac{\bar{\lambda}}{l_p} \frac{\hbar}{\bar{\lambda}} \frac{1}{c} c^2 - \frac{\hbar}{\bar{\lambda}} \frac{1}{c} c^2 \\ E_{k,max} &= \frac{\hbar}{l_p} c - \frac{\hbar}{\bar{\lambda}} c \\ E_{k,max} &= \hbar c \left( \frac{1}{l_p} - \frac{1}{\bar{\lambda}} \right) \end{aligned} \quad (11)$$

We can use this result in Heisenberg's time energy uncertainty inequality equation

$$\begin{aligned} \sigma_t \sigma_E &\geq \frac{\hbar}{2} \\ \sigma_t \hbar c \left( \frac{1}{l_p} - \frac{1}{\bar{\lambda}} \right) &\geq \frac{\hbar}{2} \\ \sigma_t &\geq \frac{\hbar}{2\hbar c \left( \frac{1}{l_p} - \frac{1}{\bar{\lambda}} \right)} \\ \sigma_t &\geq \frac{1}{2c \left( \frac{1}{l_p} - \frac{1}{\bar{\lambda}} \right)} \end{aligned} \quad (12)$$

and when  $\bar{\lambda} \gg l_p$ , we have a very good approximation by

$$\sigma_t \geq \frac{1}{2} \frac{l_p}{c} \quad (13)$$

Which is half a Planck second. It is worth mentioning that the half Planck second and half Planck length found as boundary conditions here are exactly the same as the results we obtained when looking at the Lorentz transformation in the limit of the maximum velocity of mass [10].

## 4 Big G and Heisenberg's Uncertainty Principle

As shown in [3], the maximum velocity can also be written as

$$v_{max} = c\sqrt{1 - \frac{l_p^2}{\lambda^2}} = c\sqrt{1 - \frac{Gm^2}{\hbar c}} \quad (14)$$

where  $G$  is Newton's gravitational constant [11] and  $m$  is the mass of a fundamental particle. It is important to understand  $m$  in this context is not just any mass; this mass must have a reduced Compton wavelength. In other words, it is the mass of fundamental particles. Based on this observation, we can assess whether or not we can use this in combination with Heisenberg's uncertainty principle to derive a theoretical value of big  $G$ . We are not the first to suggest that Heisenberg's uncertainty principle could be related to Newtonian gravity. McCulloch [12] has shown that Newton's gravity formula basically can be derived from Heisenberg's uncertainty principle. However, he has not shown how big  $G$  also can be derived from it.

We could also say that this is just another way to show the maximum velocity for matter may be consistent with Heisenberg's uncertainty principle, although this should not be considered as evidence that we will get big  $G$  from Heisenberg's uncertainty principle. We have

$$\begin{aligned} \sigma_x \sigma_p &\geq \frac{\hbar}{2} \\ \sigma_x \frac{mv_{max}}{\sqrt{1 - \frac{v_{max}^2}{c^2}}} &\geq \frac{\hbar}{2} \\ \sigma_x m_p v_{max} &\geq \frac{\hbar}{2} \\ \sigma_x m_p c \sqrt{1 - \frac{Gm^2}{\hbar c}} &\geq \frac{\hbar}{2} \\ \sqrt{1 - \frac{Gm^2}{\hbar c}} &\geq \frac{\hbar}{2\sigma_x m_p c} \\ 1 - \frac{Gm^2}{\hbar c} &\geq \frac{\hbar^2}{4\sigma_x^2 m_p^2 c^2} \\ G &\geq \frac{\hbar c}{m^2} - \frac{\hbar^2 \hbar c}{4\sigma_x^2 m_p^2 c^2 m^2} \\ G &\geq \frac{\hbar c}{\frac{\hbar^2}{\bar{\lambda}^2} \frac{1}{c^2}} - \frac{\hbar^2 \hbar c}{4 \frac{\hbar^2}{4m_p^2 v_{max}^2} m_p^2 c^2 m^2} \\ G &\geq \frac{\bar{\lambda}^2 c^3}{\hbar} - \frac{\hbar c v_{max}^2}{m^2 c^2} \\ G &\geq \frac{\bar{\lambda}^2 c^3}{\hbar} - \frac{\hbar c^2 \left(1 - \frac{l_p^2}{\lambda^2}\right)}{m^2 c^2} \\ G &\geq \frac{\bar{\lambda}^2 c^3}{\hbar} - \frac{\hbar c \left(1 - \frac{l_p^2}{\lambda^2}\right)}{\frac{\hbar^2}{\bar{\lambda}^2} \frac{1}{c^2}} \\ G &\geq \frac{\bar{\lambda}^2 c^3}{\hbar} - \frac{\bar{\lambda}^2 c^3 \left(1 - \frac{l_p^2}{\lambda^2}\right)}{\hbar} \\ G &\geq \frac{l_p^2 c^3}{\hbar} \approx 6.67384 \times 10^{-11} \end{aligned} \quad (15)$$

To write the gravitational constant as  $G = \frac{l_p^2 c^3}{\hbar}$  has already been suggested by Haug [13, 14] in order to simplify a series of expressions in Newton and Einstein gravity end results. It has also been derived by dimensional analysis [3] and used to simplify the equation form of the Planck units. Further, Haug has suggested that the Planck length (at least in a thought experiment) can be found independent of  $G$  based on the maximum velocity formula.

This gives the same value as the gravitational constant, as is known from experiments. However, there is still considerable uncertainty about the exact measurement of the gravitational constant. Experimentally, substantial progress has been made in recent years based on various methods. See, for example,

[15, 16, 17, 18, 19]. In the formula presented here, the uncertainty lies in the exact value of the Planck length, as well as in  $\hbar$ ; the speed of light  $c = 299792458$  is exact per definition. At the moment, the Planck length can only be found from  $G$ , but if we had access to much more advanced particle accelerators than the Large Hadron Collider, we could expect to detect  $v_{max}$  and then back the Planck length out from there. We claim that big  $G$  is indeed a universal constant, but it is a composite constant that is dependent on three even more fundamental constants, namely  $\hbar$ ,  $l_p$ , and  $c$ .

## 5 Conclusion

By combining Heisenberg's uncertainty principle with the newly introduced maximum velocity on mass, we have shown that the smallest location uncertainty of a fundamental particle is related to half the Planck length, and that the shortest time interval is related to half the Planck time. This is the "same" finding as we obtained when combining this maximum velocity with the Lorentz transformation [10].

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