

Refutation of the quantifier Most

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Abstract: We evaluate two equivalent semantics for "Most A are B" which while logically equivalent are neither tautologous. Hence the quantifier Most is refuted.

We assume the method and apparatus of Meth8/VL4 with Tautology as the designated *proof* value, **F** as contradiction, **N** as truthity (non-contingency), and **C** as falsity (contingency). For results, the 16-valued truth table is row-major and horizontal, or repeating fragments of 128-tables, sometimes with table counts, for more variables. Reproducible transcripts for results are available. (See ersatz-systems.com.)

LET $p, q, r, s: A, B, C, s;$
 \sim Not, \neg ; $+$ Or, \vee, \cup ; $-$ Not Or; $\&$ And, \wedge, \cap ; \setminus Not And;
 $>$ Imply, greater than, $\rightarrow, \mapsto, \succ, \supset, \vdash, \models$; $<$ Not Imply, less than, \in, \prec, \subset ;
 $=$ Equivalent, $\equiv, :=, \iff, \leftrightarrow, \triangleq$ $@$ Not Equivalent, \neq ;
 $\%$ possibility, for one or some, \exists, \diamond, M ; $\#$ necessity, for every or all, \forall, \square, L ;
 $(z=z)$ **T** as tautology, \top , ordinal 3; $(z@z)$ **F** as contradiction, $\emptyset, \text{Null}, \perp$, zero;
 $(\%z>\#z)$ **N** as non-contingency, ∇ , ordinal 1; $(\%z<\#z)$ **C** as contingency, Δ , ordinal 2;
 $\sim(y < x)$ ($x \leq y$), ($x \subseteq y$); $(A=B)$ ($A \sim B$).

From: Topal, S. (2019). Natural density and the quantifier most.
 arxiv.org/pdf/1901.10394.pdf s.topal@beu.edu.tr

Two different but equivalent semantics are for Most A are B as

$$(i) C(A \cap B) > C(A \setminus B) \text{ and} \tag{1.1}$$

$$((r \& (p \& q)) > (r \& (p \setminus q))) > ((r \& p) = q); \quad \mathbf{TTF\!F \ TFF\!T \ TTF\!F \ TFF\!T} \tag{1.2}$$

$$(ii) C(A \cap B) > C(A)/2 \tag{2.1}$$

$$((r \& (p \& q)) > ((r \& p) \setminus (\%s < \#s))) > ((r \& p) = q); \quad \mathbf{TTF\!F \ TFF\!T \ TTF\!F \ TFF\!T} \tag{2.2}$$

While Eqs. 1.2 and 2.2 as rendered share the same truth table result, being logically equivalent, neither is tautologous. The means the quantifier Most is refuted.