

Refutation of the language of sets for model theory = universal algebra + mathematical logic

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Abstract: A first order language of sets is proposed, but the first example $A \subset B$ iff $(x \in A \text{ then } x \in B)$ is *not* tautologous. This refutes the conjecture of model theory = universal algebra + mathematical logic, which forms a *non* tautologous fragment of the universal logic $\forall\exists\Delta$.

We assume the method and apparatus of Meth8/ $\forall\exists\Delta$ with Tautology as the designated proof value, **F** as contradiction, **N** as truthity (non-contingency), and **C** as falsity (contingency). The 16-valued truth table is row-major and horizontal, or repeating fragments of 128-tables, sometimes with table counts, for more variables. (See ersatz-systems.com.)

LET \sim Not, \neg ; + Or, \vee , \cup , \sqcup ; - Not Or; & And, \wedge , \cap , \sqcap , $;$; \ Not And;
 $>$ Imply, greater than, \rightarrow , \Rightarrow , \mapsto , $>$, \supset , \rightsquigarrow ;
 $<$ Not Imply, less than, \in , $<$, \subset , \prec , \preceq , \ll , \leq ;
 $=$ Equivalent, \equiv , $:=$, \Leftrightarrow , \leftrightarrow , \triangleq , \approx , \simeq ; @ Not Equivalent, \neq ;
 $\%$ possibility, for one or some, \exists , \diamond , M ; # necessity, for every or all, \forall , \square , L ;
 $(z=z)$ **T** as tautology, \top , ordinal 3; $(z@z)$ **F** as contradiction, \emptyset , Null, \perp , zero;
 $(\%z\>\#z)$ **N** as non-contingency, Δ , ordinal 1;
 $(\%z\<\#z)$ **C** as contingency, ∇ , ordinal 2;
 $\sim(y < x)$ $(x \leq y)$, $(x \subseteq y)$; $(A=B)$ $(A\sim B)$; $(B>A)$ $(A\vdash B)$; $(B>A)$ $(A\neq B)$.
 Note for clarity, we usually distribute quantifiers onto each designated variable.

From: Torres, J. (2019). Model theory, arithmetic & algebraic geometry.
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1.1. **What is Model Theory?** ... Model Theory introduces Mathematical Logic in the practice of Universal Algebra, so we can think it like Model Theory = Universal Algebra + Mathematical Logic. (1.1.1)

1.2. **Languages.** To start we fix a first order language L which contains exactly those symbols that we request in our interest and nothing else. ... A simple example of a language is $L_{\text{sets}} = \{\in\}$ the language of sets, note that we can define other symbols in Set Theory from \in , for example $A \subset B$ iff $(x \in A \text{ then } x \in B)$ (1.2.1.1)

LET p, q, r: A, B, x.

$$((r < p) > (r < q)) > (p < q); \quad \mathbf{FTFF \ FTFF \ FTFF \ FTFF} \quad (1.2.1.2)$$

Eq. 1.2.1.2 as rendered is *not* tautologous to refute the first order language of sets as proposed. What follows is that Eq. 1.1.1 model theory = universal algebra + mathematical logic is also refuted.