# Analyzing some parts of Ramanujan's Manuscripts: Mathematical connections between several Ramanujan's equations, the Rogers-Ramanujan continued fractions and some sectors of Cosmology and Theoretical Physics. II 

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#### Abstract

In this research thesis, we have analyzed some parts of Ramanujan's Manuscripts and obtained new mathematical connections between several Ramanujan's equations, the Rogers-Ramanujan continued fractions and some sectors of Cosmology and Theoretical Physics .


[^0]
http://esciencecommons.blogspot.com/2012/12/math-formula-gives-new-glimpse-into.html
"...Expansion of modular forms is one of the fundamental tools for computing the entropy of a modular black hole. Some black holes, however, are not modular, but the new formula based on Ramanujan's vision may allow physicists to compute their entropy as though they were....."


[^1]From:

## Manuscript Book 2 of Srinivasa Ramanujan

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$1 /(((324 \mathrm{Pi}) * \mathrm{sqrt}(3)))+25 / 756-\mathrm{Pi} /(54 * \operatorname{sqrt}(3))+(((\mathrm{Pi} /(18 * \operatorname{sqrt}(3)))))^{*}$ 1/(14* $\left.\cosh \left(3 \mathrm{Pi}^{*} \mathrm{sqrt}(3)\right)\right)$

## Input:

$\frac{1}{(324 \pi) \sqrt{3}}+\frac{25}{756}-\frac{\pi}{54 \sqrt{3}}+\frac{\pi}{18 \sqrt{3}} \times \frac{1}{14 \cosh (3 \pi \sqrt{3})}$
$\cosh (x)$ is the hyperbolic cosine function

## Exact result:

$$
\frac{25}{756}+\frac{1}{324 \sqrt{3} \pi}-\frac{\pi}{54 \sqrt{3}}+\frac{\pi \operatorname{sech}(3 \sqrt{3} \pi)}{252 \sqrt{3}}
$$

## Decimal approximation:

$0.000047117922509775900865462588584753873831033642776814532 \ldots$

## Result:

$4.7117922509775900865462588584753873831033642776814532 \times 10^{-5}$
$4.71179225 \ldots * 10^{-5}$

## Alternate forms:

$\frac{7 \sqrt{3}+3 \pi(75+\sqrt{3} \pi(3 \operatorname{sech}(3 \sqrt{3} \pi)-14))}{6804 \pi}$
$\underline{7 \sqrt{3}+225 \pi-42 \sqrt{3} \pi^{2}+9 \sqrt{3} \pi^{2} \operatorname{sech}(3 \sqrt{3} \pi)}$

$$
6804 \pi
$$

$$
\frac{25}{756}+\frac{1}{324 \sqrt{3} \pi}-\frac{\pi}{54 \sqrt{3}}+\frac{\pi}{126 \sqrt{3}\left(e^{-3 \sqrt{3} \pi}+e^{3 \sqrt{3} \pi}\right)}
$$

## Alternative representations:

$$
\begin{aligned}
& \frac{1}{\sqrt{3} 324 \pi}+\frac{25}{756}-\frac{\pi}{54 \sqrt{3}}+\frac{\pi}{(14 \cosh (3 \pi \sqrt{3}))(18 \sqrt{3})}= \\
& \frac{25}{756}+\frac{\pi}{(14 \cos (-3 i \pi \sqrt{3}))(18 \sqrt{3})}-\frac{\pi}{54 \sqrt{3}}+\frac{1}{324 \pi \sqrt{3}} \\
& \frac{1}{\sqrt{3} 324 \pi}+\frac{25}{756}-\frac{\pi}{54 \sqrt{3}}+\frac{\pi}{(14 \cosh (3 \pi \sqrt{3}))(18 \sqrt{3})}= \\
& \frac{25}{756}+\frac{\pi}{(14 \cos (3 i \pi \sqrt{3}))(18 \sqrt{3})}-\frac{\pi}{54 \sqrt{3}}+\frac{1}{324 \pi \sqrt{3}} \\
& \frac{1}{\sqrt{3} 324 \pi}+\frac{25}{756}-\frac{\pi}{54 \sqrt{3}}+\frac{\pi}{(14 \cosh (3 \pi \sqrt{3}))(18 \sqrt{3})}= \\
& \frac{25}{756}+\frac{\pi}{\left(7\left(e^{-3 \pi \sqrt{3}}+e^{3 \pi \sqrt{3}}\right)\right)(18 \sqrt{3})}-\frac{\pi}{54 \sqrt{3}}+\frac{1}{324 \pi \sqrt{3}}
\end{aligned}
$$

## Series representations:

$$
\begin{aligned}
& \frac{1}{\sqrt{3} 324 \pi}+\frac{25}{756}-\frac{\pi}{54 \sqrt{3}}+\frac{\pi}{(14 \cosh (3 \pi \sqrt{3}))(18 \sqrt{3})}= \\
& \frac{25}{756}+\frac{1}{324 \sqrt{3} \pi}-\frac{\pi}{54 \sqrt{3}}+\frac{\sum_{k=0}^{\infty} \frac{(-1)^{k}(1+2 k)}{109+4 k+4 k^{2}}}{63 \sqrt{3}} \\
& \frac{1}{\sqrt{3} 324 \pi}+\frac{25}{756}-\frac{\pi}{54 \sqrt{3}}+\frac{\pi}{(14 \cosh (3 \pi \sqrt{3}))(18 \sqrt{3})}= \\
& \frac{25}{756}+\frac{1}{324 \sqrt{3} \pi}-\frac{\pi}{54 \sqrt{3}}-\frac{\pi \sum_{k=1}^{\infty}(-1)^{k} q^{-1+2 k}}{126 \sqrt{3}} \text { for } q=e^{3 \sqrt{3} \pi}
\end{aligned}
$$

$$
\begin{aligned}
& \frac{1}{\sqrt{3} 324 \pi}+\frac{25}{756}-\frac{\pi}{54 \sqrt{3}}+\frac{\pi}{(14 \cosh (3 \pi \sqrt{3}))(18 \sqrt{3})}= \\
& \frac{25}{756}+\frac{1}{324 \sqrt{3} \pi}-\frac{\pi}{54 \sqrt{3}}+\frac{e^{-3 \sqrt{3} \pi} \pi \sum_{k=0}^{\infty}(-1)^{k} e^{-6 \sqrt{3} k \pi}}{126 \sqrt{3}}
\end{aligned}
$$

## Integral representation:

$$
\begin{aligned}
& \frac{1}{\sqrt{3} 324 \pi}+\frac{25}{756}-\frac{\pi}{54 \sqrt{3}}+\frac{\pi}{(14 \cosh (3 \pi \sqrt{3}))(18 \sqrt{3})}= \\
& \frac{25}{756}+\frac{1}{324 \sqrt{3} \pi}-\frac{\pi}{54 \sqrt{3}}+\frac{1}{126 \sqrt{3}} \int_{0}^{\infty} \frac{t^{6 i \sqrt{3}}}{1+t^{2}} d t
\end{aligned}
$$

$\left(\left(\left(\left((1 /(((324 \mathrm{Pi}) * \operatorname{sqrt}(3)))+25 / 756-\mathrm{Pi} /(54 * \operatorname{sqrt}(3))+(((\mathrm{Pi} /(18 * \operatorname{sqrt}(3))))))^{*}\right.\right.\right.\right.$ $\left.\left.\left.\left.\left.1 /\left(14^{*} \cosh \left(3 \mathrm{Pi}^{*} \operatorname{sqrt}(3)\right)\right)\right)\right)\right)\right)\right)^{\wedge} 1 / 1024$

## Input:

$$
\sqrt[1024]{\frac{1}{(324 \pi) \sqrt{3}}+\frac{25}{756}-\frac{\pi}{54 \sqrt{3}}+\frac{\pi}{18 \sqrt{3}} \times \frac{1}{14 \cosh (3 \pi \sqrt{3})}}
$$

## Exact result:

$$
\sqrt[1024]{\frac{25}{756}+\frac{1}{324 \sqrt{3} \pi}-\frac{\pi}{54 \sqrt{3}}+\frac{\pi \operatorname{sech}(3 \sqrt{3} \pi)}{252 \sqrt{3}}}
$$

## Decimal approximation:

$0.990317824381383794203738279426892199335057434473544561135 \ldots$
$0.990317824 \ldots$. result very near to the value of the following Rogers-Ramanujan continued fraction:
$\frac{\mathrm{e}^{-\frac{\pi}{\sqrt{5}}}}{\frac{\sqrt{5}}{1+\sqrt[5]{\sqrt{\varphi^{5 \sqrt[4]{5^{3}}}-1}}-\varphi+1}=1-\frac{\mathrm{e}^{-\pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-2 \pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-3 \pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-4 \pi \sqrt{5}}}{1+\ldots}}}} \approx 0.9991104684 .10 .}$
and to the dilaton value $\mathbf{0 . 9 8 9 1 1 7 3 5 2 2 4 3}=\boldsymbol{\phi}$

## Alternate forms:

$$
\sqrt[1024]{\frac{25}{756}+\frac{1}{324 \sqrt{3} \pi}-\frac{\pi}{54 \sqrt{3}}+\frac{\pi}{126 \sqrt{3}\left(e^{-3 \sqrt{3} \pi}+e^{3 \sqrt{3} \pi}\right)}}
$$

$$
\sqrt[1024]{\frac{25}{756}+\frac{1}{324 \sqrt{3} \pi}-\frac{\pi}{54 \sqrt{3}}+\frac{\pi \cosh (3 \sqrt{3} \pi)}{126 \sqrt{3}(1+\cosh (6 \sqrt{3} \pi))}}
$$

1
$\sqrt[512]{2} 3^{5 / 1024} 1024 \sqrt{\frac{7 \pi}{7 \sqrt{3}+225 \pi-42 \sqrt{3} \pi^{2}+9 \sqrt{3} \pi^{2} \operatorname{sech}(3 \sqrt{3} \pi)}}$

All 1024th roots of $25 / 756+1 /(324 \operatorname{sqrt}(3) \pi)-\pi /(54 \operatorname{sqrt}(3))+(\pi \operatorname{sech}(3 \operatorname{sqrt}(3)$ $\pi)$ )/(252 sqrt(3)):
$e^{0} 1024 \sqrt{\frac{25}{756}+\frac{1}{324 \sqrt{3} \pi}-\frac{\pi}{54 \sqrt{3}}+\frac{\pi \operatorname{sech}(3 \sqrt{3} \pi)}{252 \sqrt{3}}} \approx 0.9903$ (real, principal root)

$$
e^{(i \pi) / 512} 1024 \sqrt{\frac{25}{756}+\frac{1}{324 \sqrt{3} \pi}-\frac{\pi}{54 \sqrt{3}}+\frac{\pi \operatorname{sech}(3 \sqrt{3} \pi)}{252 \sqrt{3}}} \approx 0.9903+0.006076 i
$$

$$
e^{(i \pi) / 256} \sqrt[1024]{\frac{25}{756}+\frac{1}{324 \sqrt{3} \pi}-\frac{\pi}{54 \sqrt{3}}+\frac{\pi \operatorname{sech}(3 \sqrt{3} \pi)}{252 \sqrt{3}}} \approx 0.9902+0.012153 i
$$

$$
e^{(3 i \pi) / 512} 1024 \sqrt{\frac{25}{756}+\frac{1}{324 \sqrt{3} \pi}-\frac{\pi}{54 \sqrt{3}}+\frac{\pi \operatorname{sech}(3 \sqrt{3} \pi)}{252 \sqrt{3}}} \approx 0.9902+0.018229 i
$$

$$
e^{(i \pi / 128} \sqrt[1024]{\frac{25}{756}+\frac{1}{324 \sqrt{3} \pi}-\frac{\pi}{54 \sqrt{3}}+\frac{\pi \operatorname{sech}(3 \sqrt{3} \pi)}{252 \sqrt{3}}} \approx 0.9900+0.02430 i
$$

## Alternative representations:

$$
\begin{gathered}
\sqrt[1024]{\frac{1}{\sqrt{3} 324 \pi}+\frac{25}{756}-\frac{\pi}{54 \sqrt{3}}+\frac{\pi}{(14 \cosh (3 \pi \sqrt{3}))(18 \sqrt{3})}}= \\
\sqrt[1024]{\frac{25}{756}+\frac{\pi}{(14 \cos (-3 i \pi \sqrt{3}))(18 \sqrt{3})}-\frac{\pi}{54 \sqrt{3}}+\frac{1}{324 \pi \sqrt{3}}}
\end{gathered}
$$

$$
\sqrt[1024]{\frac{1}{\sqrt{3} 324 \pi}+\frac{25}{756}-\frac{\pi}{54 \sqrt{3}}+\frac{\pi}{(14 \cosh (3 \pi \sqrt{3}))(18 \sqrt{3})}}=
$$

$$
\sqrt[1024]{\frac{25}{756}+\frac{\pi}{(14 \cos (3 i \pi \sqrt{3}))(18 \sqrt{3})}-\frac{\pi}{54 \sqrt{3}}+\frac{1}{324 \pi \sqrt{3}}}
$$

$$
\sqrt[1024]{\frac{1}{\sqrt{3} 324 \pi}+\frac{25}{756}-\frac{\pi}{54 \sqrt{3}}+\frac{\pi}{(14 \cosh (3 \pi \sqrt{3}))(18 \sqrt{3})}}=
$$

$$
\sqrt[1024]{\frac{25}{756}+\frac{\pi}{\frac{14(18 \sqrt{3})}{\operatorname{soc}(3 i \pi \sqrt{3})}}-\frac{\pi}{54 \sqrt{3}}+\frac{1}{324 \pi \sqrt{3}}}
$$

## Series representations:

$$
\begin{aligned}
& \sqrt[1024]{\frac{1}{\sqrt{3} 324 \pi}+\frac{25}{756}-\frac{\pi}{54 \sqrt{3}}+\frac{\pi}{(14 \cosh (3 \pi \sqrt{3}))(18 \sqrt{3})}}= \\
& \sqrt[1024]{\frac{25}{756}+\frac{1}{324 \sqrt{3} \pi}-\frac{\pi}{54 \sqrt{3}}-\frac{\pi \sum_{k=1}^{\infty}(-1)^{k} q^{-1+2 k}}{126 \sqrt{3}}} \text { for } q=e^{3 \sqrt{3} \pi} \\
& \sqrt[1024]{\frac{1}{\sqrt{3} 324 \pi}+\frac{25}{756}-\frac{\pi}{54 \sqrt{3}}+\frac{1}{(14 \cosh (3 \pi \sqrt{3}))(18 \sqrt{3})}}= \\
& \sqrt[1024]{\frac{25}{756}+\frac{1}{324 \sqrt{3} \pi}-\frac{\pi}{54 \sqrt{3}}+\frac{e^{-3 \sqrt{3} \pi \pi \sum_{k=0}^{\infty}(-1)^{k} e^{-6 \sqrt{3} k \pi}}}{1024 \sqrt{3}}} \\
& \sqrt[1024]{\frac{1}{\sqrt{3} 324 \pi}+\frac{25}{756}-\frac{\pi}{54 \sqrt{3}}+\frac{25}{(14 \operatorname{cosh(3\pi \sqrt {3}))(18\sqrt {3}})}}= \\
& \sqrt{356}+\frac{1}{324 \sqrt{3} \pi}-\frac{\pi}{54 \sqrt{3}}+\frac{\pi^{2}}{\pi^{2} \sum_{k=0}^{\infty} \frac{(-1)^{k}(1+2 k)}{27 \pi^{2}+\left(\frac{1}{2}+k\right)^{2} \pi^{2}}}
\end{aligned}
$$

## Integral representation:

$$
\begin{gathered}
\sqrt[1024]{\frac{1}{\sqrt{3} 324 \pi}+\frac{25}{756}-\frac{\pi}{54 \sqrt{3}}+\frac{\pi}{(14 \cosh (3 \pi \sqrt{3}))(18 \sqrt{3})}} \\
\sqrt[1024]{\frac{25}{756}+\frac{1}{324 \sqrt{3} \pi}-\frac{\pi}{54 \sqrt{3}}+\frac{1}{126 \sqrt{3}} \int_{0}^{\infty} \frac{t^{6 i \sqrt{3}}}{1+t^{2}} d t}
\end{gathered}
$$

$-782-8+(7 / 2) * 1 /(((((1 /(((324 \mathrm{Pi}) * \operatorname{sqrt}(3)))+25 / 756-$
$\left.\left.\left.\left.\left.\mathrm{Pi} /(54 * \operatorname{sqrt}(3))+(((\mathrm{Pi} /(18 * \operatorname{sqrt}(3))))))^{*} 1 /\left(14^{*} \cosh \left(3 \mathrm{Pi}^{*} \operatorname{sqrt}(3)\right)\right)\right)\right)\right)\right)\right)$

## Input:

$-782-8+\frac{7}{2} \times \frac{1}{\frac{1}{(324 \pi) \sqrt{3}}+\frac{25}{756}-\frac{\pi}{54 \sqrt{3}}+\frac{\pi}{18 \sqrt{3}} \times \frac{1}{14 \cosh (3 \pi \sqrt{3})}}$

## Exact result:

$\frac{7}{2\left(\frac{25}{756}+\frac{1}{324 \sqrt{3} \pi}-\frac{\pi}{54 \sqrt{3}}+\frac{\pi \operatorname{sech}(3 \sqrt{3} \pi)}{252 \sqrt{3}}\right)}-790$

## Decimal approximation:

73491.71306308824072153249106940347306025593211382945287718...
73491.713063...

## Alternate forms:

$\frac{23814 \pi}{7 \sqrt{3}+225 \pi+3 \sqrt{3} \pi^{2}(3 \operatorname{sech}(3 \sqrt{3} \pi)-14)}-790$
$\frac{23814 \pi}{7 \sqrt{3}+225 \pi-42 \sqrt{3} \pi^{2}+9 \sqrt{3} \pi^{2} \operatorname{sech}(3 \sqrt{3} \pi)}-790$
$\frac{7}{2\left(\frac{25}{756}+\frac{1}{324 \sqrt{3} \pi}-\frac{\pi}{54 \sqrt{3}}+\frac{\pi}{126 \sqrt{3}\left(e^{-3 \sqrt{3} \pi}+e^{3 \sqrt{3} \pi}\right)}\right)}-790$

## Alternative representations:

$$
\begin{aligned}
& -782-8+\frac{7}{\left(\frac{1}{(324 \pi) \sqrt{3}}+\frac{25}{756}-\frac{\pi}{54 \sqrt{3}}+\frac{\pi}{(18 \sqrt{3})(14 \cosh (3 \pi \sqrt{3}))}\right) 2}= \\
& -790+\frac{7}{2\left(\frac{25}{756}+\frac{\pi}{(14 \cos (-3 i \pi \sqrt{3}))(18 \sqrt{3})}-\frac{\pi}{54 \sqrt{3}}+\frac{1}{324 \pi \sqrt{3}}\right)} \\
& \begin{array}{l}
-782-8+\frac{7}{\left(\frac{1}{(324 \pi) \sqrt{3}}+\frac{25}{756}-\frac{\pi}{54 \sqrt{3}}+\frac{7}{(18 \sqrt{3})(14 \cosh (3 \pi \sqrt{3}))}\right)} 2 \\
-790+\frac{7}{2\left(\frac{25}{756}+\frac{\pi}{(14 \cos (3 i \pi \sqrt{3}))(18 \sqrt{3})}-\frac{\pi}{54 \sqrt{3}}+\frac{1}{324 \pi \sqrt{3}}\right)}
\end{array}= \\
& -782-8+\frac{7}{\left(\frac{1}{(324 \pi) \sqrt{3}}+\frac{25}{756}-\frac{\pi}{54 \sqrt{3}}+\frac{\pi}{(18 \sqrt{3})(14 \cosh (3 \pi \sqrt{3}))}\right) 2}= \\
& \left.-790+\frac{7}{2\left(\frac{25}{756}+\frac{\pi}{\frac{14(18 \sqrt{3})}{\operatorname{sed}(3 i \pi \sqrt{3})}}-\frac{\pi}{54 \sqrt{3}}+\frac{1}{324 \pi \sqrt{3}}\right.}\right)
\end{aligned}
$$

## Series representations:

$$
\begin{aligned}
& -782-8+\frac{7}{\left(\frac{1}{(324 \pi) \sqrt{3}}+\frac{25}{756}-\frac{\pi}{54 \sqrt{3}}+\frac{\pi}{(18 \sqrt{3})(14 \cosh (3 \pi \sqrt{3}))}\right) 2}= \\
& -790-\frac{23814 \pi}{-7 \sqrt{3}-225 \pi+42 \sqrt{3} \pi^{2}+18 \sqrt{3} \pi^{2} \sum_{k=1}^{\infty}(-1)^{k} q^{-1+2 k}} \text { for } q=e^{3 \sqrt{3} \pi} \\
& -782-8+\frac{7}{\left(\frac{1}{(324 \pi) \sqrt{3}}+\frac{25}{756}-\frac{\pi}{54 \sqrt{3}}+\frac{\pi}{(18 \sqrt{3})(14 \cosh (3 \pi \sqrt{3}))}\right) 2}= \\
& -790+\frac{23814 \pi}{7 \sqrt{3}+225 \pi-42 \sqrt{3} \pi^{2}+36 \sqrt{3} \pi \sum_{k=0}^{\infty} \frac{(-1)^{k}(1+2 k)}{109+4 k+4 k^{2}}}
\end{aligned}
$$

$$
\begin{aligned}
& -782-8+\frac{7}{\left(\frac{1}{(324 \pi) \sqrt{3}}+\frac{25}{756}-\frac{\pi}{54 \sqrt{3}}+\frac{\pi}{(18 \sqrt{3})(14 \cosh (3 \pi \sqrt{3}))}\right) 2}= \\
& -790+\frac{23814}{225+\frac{7 \sqrt{3}}{\pi}-42 \sqrt{3} \pi+18 \sqrt{3} e^{-3 \sqrt{3} \pi} \pi \sum_{k=0}^{\infty}(-1)^{k} e^{-6 \sqrt{3} k \pi}}
\end{aligned}
$$

## Integral representation:

$$
\begin{aligned}
& -782-8+\frac{7}{\left(\frac{1}{(324 \pi) \sqrt{3}}+\frac{25}{756}-\frac{\pi}{54 \sqrt{3}}+\frac{\pi}{(18 \sqrt{3})(14 \cosh (3 \pi \sqrt{3}))}\right) 2}= \\
& -790+\frac{7}{2\left(\frac{25}{756}+\frac{1}{324 \sqrt{3} \pi}-\frac{\pi}{54 \sqrt{3}}+\frac{1}{126 \sqrt{3}} \int_{0}^{\infty} \frac{t^{6 i \sqrt{3}}}{1+t^{2}} d t\right)}
\end{aligned}
$$

Thence, we have the following mathematical connection:

$$
\begin{aligned}
& \left(\frac{7}{2\left(\frac{25}{756}+\frac{1}{324 \sqrt{3} \pi}-\frac{\pi}{54 \sqrt{3}}+\frac{\pi \operatorname{sech}(3 \sqrt{3} \pi)}{252 \sqrt{3}}\right)}-790\right)=73491.713063 \ldots \Rightarrow
\end{aligned}
$$

$$
\begin{aligned}
& -3927+2 \sqrt[13]{2.2983717437 \times 10^{59}+2.0823329825883 \times 10^{59}} \\
& =73490.8437525 \ldots . \Rightarrow \\
& \Rightarrow\left(A(r) \times \frac{1}{B(r)}\left(-\frac{1}{\phi(r)}\right) \times \frac{1}{e^{\Lambda(r)}}\right) \Rightarrow
\end{aligned}
$$

$$
\begin{aligned}
& \Rightarrow\left(-0.000029211892 \times \frac{1}{0.0003644621}\left(-\frac{1}{0.0005946833}\right) \times \frac{1}{0.00183393}\right)= \\
& =73491.78832548118710549159572042220548025195726563413398700 \ldots \\
& =73491.7883254 \ldots \Rightarrow
\end{aligned}
$$

$$
\begin{gathered}
\binom{I_{21} \leqslant \int_{-\infty}^{+\infty} \exp \left(-\left(\frac{t}{H}\right)^{2}\right)\left|\sum_{\lambda \leqslant P^{1-\varepsilon_{4}}} \frac{a(\lambda)}{\sqrt{\lambda}} B(\lambda) \lambda^{-i(T+t)}\right|^{2} d t \leqslant}{\leqslant H\left\{\left(\frac{4}{\varepsilon_{2} \log T}\right)^{2 r}(\log T)(\log X)^{-2 \beta}+\left(\varepsilon_{2}^{-2 r}(\log T)^{-2 r}+\varepsilon_{2}^{-r} h_{1}^{r}(\log T)^{-r}\right) T^{-\varepsilon_{1}}\right\}} / \\
\quad /(26 \times 4)^{2}-24=\left(\frac{7.9313976505275 \times 10^{8}}{(26 \times 4)^{2}-24}\right)=73493.30662 \ldots
\end{gathered}
$$

Mathematical connections with the boundary state corresponding to the NSNS-sector of N Dp-branes in the limit of $u \rightarrow \infty$, with the ratio concerning the general asymptotically flat solution of the equations of motion of the $p$-brane and with the Karatsuba's equation concerning the zeros of a special type of function connected with Dirichlet series.

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We have:
sqrt(21) $\left.1 / 2((((3-\operatorname{sqrt}(7)) / \operatorname{sqrt}(2))))^{\wedge} 2(((\operatorname{sqrt}(((5+\operatorname{sqrt}(7))) / 4)))-\operatorname{sqrt}(((1+\operatorname{sqrt}(7)) / 4)))\right)^{\wedge} 4$ $(((\operatorname{sqrt}(((3+\operatorname{sqrt}(7)) / 4)))-\operatorname{sqrt}(((\operatorname{sqrt}(7)+1)) / 4)))^{\wedge} 4(1 / 2 * \operatorname{sqrt}(7)-\operatorname{sqrt}(3))^{\wedge} 2$

## Input:

$\sqrt{21}\left(\frac{1}{2}\left(\frac{3-\sqrt{7}}{\sqrt{2}}\right)^{2}\right)\left(\sqrt{\frac{1}{4}(5+\sqrt{7})}-\sqrt{\frac{1}{4}(1+\sqrt{7})}\right)^{4}$
$\left(\sqrt{\frac{1}{4}(3+\sqrt{7})}-\sqrt{\frac{1}{4}(\sqrt{7}+1)}\right)^{4}\left(\frac{1}{2} \sqrt{7}-\sqrt{3}\right)^{2}$

## Result:

$$
\begin{aligned}
& \frac{1}{4} \sqrt{21}(3-\sqrt{7})^{2}\left(\frac{\sqrt{7}}{2}-\sqrt{3}\right)^{2} \\
& \left(\frac{\sqrt{3+\sqrt{7}}}{2}-\frac{1}{2} \sqrt{1+\sqrt{7}}\right)^{4}\left(\frac{\sqrt{5+\sqrt{7}}}{2}-\frac{1}{2} \sqrt{1+\sqrt{7}}\right)^{4}
\end{aligned}
$$

## Decimal approximation:

$2.3915524816624164664374098055386443887961318323545792 \ldots \times 10^{-6}$
$2.3915524816 \ldots * 10^{-6}$

## Alternate forms:

$$
\begin{aligned}
& \frac{1}{2048}(-32 \sqrt{2(5+\sqrt{7})(11+5 \sqrt{7})}+48 \sqrt{7}+12 \sqrt{14(5+\sqrt{7})(11+5 \sqrt{7})}- \\
& 32 \sqrt{2(1+\sqrt{7})(115+41 \sqrt{7})}+12 \sqrt{14(1+\sqrt{7})(115+41 \sqrt{7})-112)} \\
& (\sqrt{3+\sqrt{7}}-\sqrt{1+\sqrt{7}})^{4}(19 \sqrt{21}-84) \\
& \frac{\sqrt{21}(2 \sqrt{3}-\sqrt{7})^{2}(\sqrt{7}-3)^{2}(\sqrt{1+\sqrt{7}}-\sqrt{3+\sqrt{7}})^{4}(\sqrt{1+\sqrt{7}}-\sqrt{5+\sqrt{7}})^{4}}{4096}
\end{aligned}
$$

```
root of 1208925819614629174706176 x 16 +
    1066272572900102932090847232 x 15 +
    52042471479879261245210099712 x 14 +
    11466902464047792010302125506560 x 13 +
    268522316518239021476930106949632 x (12 +
    46911589457958527140659385941884928 \mp@subsup{x}{}{11}
    808765686867360903096041774996520960 x 10 +
    57518512275172950055158185352757248 x -
    2273601509826907571634757618498535424 x -
    1188432066556571834863445242753843200 x % -
    2576436753017819098275602371706880000 x' -
    4456804560805111404527207055360000000 x 5 -
    414358661156186273863724236800000000 \mp@subsup{x}{}{4}+
    9347379325695247854366720000000000 x -
    16871240529992096010000000000000 x 2-
    2372911639160737500000000000x+
    5 7 7 1 3 1 0 3 2 7 3 0 1 0 2 5 3 9 0 6 2 5 ~ n e a r ~ x ~ = ~ 2 . 3 9 1 5 5 \times 1 0 ^ { - 6 }
```


## Minimal polynomial:

$1208925819614629174706176 x^{16}+1066272572900102932090847232 x^{15}+$ $52042471479879261245210099712 x^{14}+$ $11466902464047792010302125506560 x^{13}+$ $268522316518239021476930106949632 x^{12}+$ $46911589457958527140659385941884928 x^{11}-$ $808765686867360903096041774996520960 x^{10}+$ $57518512275172950055158185352757248 x^{9}-$ $2273601509826907571634757618498535424 x^{8}-$ $1188432066556571834863445242753843200 x^{7}-$ $2576436753017819098275602371706880000 x^{6}-$ $4456804560805111404527207055360000000 x^{5}-$ $414358661156186273863724236800000000 x^{4}+$ $9347379325695247854366720000000000 x^{3}$ $16871240529992096010000000000000 x^{2}$ $2372911639160737500000000000 x+5771310327301025390625$
sqrt(33) $1 / 2$ * $\left(\left((2-\operatorname{sqrt}(3))^{\wedge} 3(((\operatorname{sqrt}(((7+3 * \operatorname{sqrt}(3)) / 4)))-\operatorname{sqrt}(((3+3 \operatorname{sqrt}(3)) / 4))))^{\wedge} 4\right.\right.$ $\left.\left.(((\operatorname{sqrt}(((5+\operatorname{sqrt}(3)) / 4)))-\operatorname{sqrt}(((1+\operatorname{sqrt}(3))) / 4)))^{\wedge} 4\left((((\operatorname{sqrt}(3)-2)) /(\operatorname{sqrt}(2)))^{\wedge} 2\right)\right)\right)$

## Input:

$$
\begin{gathered}
\sqrt{33} \times \frac{1}{2}\left((2-\sqrt{3})^{3}\left(\sqrt{\frac{1}{4}(7+3 \sqrt{3})}-\sqrt{\frac{1}{4}(3+3 \sqrt{3})}\right)^{4}\right. \\
\left.\left(\sqrt{\frac{1}{4}(5+\sqrt{3})}-\sqrt{\frac{1}{4}(1+\sqrt{3})}\right)^{4}\left(\frac{\sqrt{3}-2}{\sqrt{2}}\right)^{2}\right)
\end{gathered}
$$

## Exact result:

$$
\begin{aligned}
& \frac{1}{4} \sqrt{33}(2-\sqrt{3})^{3}(\sqrt{3}-2)^{2} \\
& \left(\frac{\sqrt{5+\sqrt{3}}}{2}-\frac{1}{2} \sqrt{1+\sqrt{3}}\right)^{4}\left(\frac{1}{2} \sqrt{7+3 \sqrt{3}}-\frac{1}{2} \sqrt{3+3 \sqrt{3}}\right)^{4}
\end{aligned}
$$

## Decimal approximation:

$9.5641535164851598615720165586116228685173468809096524 \ldots \times 10^{-7}$
$9.5641535 \ldots * 10^{-7}$

## Alternate forms:

$$
\begin{aligned}
& \text { root of } 65536 x^{8}+51904512 x^{7}+141384105984 x^{6}+ \\
& 55824100687872 x^{5}+76366762805380608 x^{4}- \\
& 314341398791202816 x^{3}-3256884091099584 x^{2}- \\
& 1236849191424 x+1185921 \text { near } x=9.56415 \times 10^{-7}
\end{aligned}
$$

$$
-\frac{\sqrt{33}(\sqrt{3}-2)^{5}(\sqrt{1+\sqrt{3}}-\sqrt{5+\sqrt{3}})^{4}(\sqrt{3(1+\sqrt{3})}-\sqrt{7+3 \sqrt{3}})^{4}}{1024}
$$

$$
-\frac{9 \sqrt{33}(\sqrt{3}-2)^{5}(1+\sqrt{3})^{2}(\sqrt{1+\sqrt{3}}-\sqrt{5+\sqrt{3}})^{4}}{1024}-
$$

$$
\frac{9}{512} \sqrt{33}(\sqrt{3}-2)^{5}(1+\sqrt{3})(7+3 \sqrt{3})(\sqrt{1+\sqrt{3}}-\sqrt{5+\sqrt{3}})^{4}+
$$

$$
\frac{3}{256}(\sqrt{3}-2)^{5} \sqrt{11(1+\sqrt{3})}(7+3 \sqrt{3})^{3 / 2}(\sqrt{1+\sqrt{3}}-\sqrt{5+\sqrt{3}})^{4}-
$$

$$
\frac{\sqrt{33}(\sqrt{3}-2)^{5}(7+3 \sqrt{3})^{2}(\sqrt{1+\sqrt{3}}-\sqrt{5+\sqrt{3}})^{4}}{1024}+
$$

$$
\frac{9}{256}(\sqrt{3}-2)^{5}(1+\sqrt{3})^{3 / 2} \sqrt{11(7+3 \sqrt{3})}(\sqrt{1+\sqrt{3}}-\sqrt{5+\sqrt{3}})^{4}
$$

## Minimal polynomial:

$65536 x^{8}+51904512 x^{7}+141384105984 x^{6}+55824100687872 x^{5}+$ $76366762805380608 x^{4}-314341398791202816 x^{3}-$ $3256884091099584 x^{2}-1236849191424 x+1185921$
$\operatorname{sqrt}(45) 1 / 2 *(\operatorname{sqrt}(5)-2) \wedge 3(((\operatorname{sqrt}(((7+3 * \operatorname{sqrt}(5)) / 4)))-\operatorname{sqrt}(((3+3 \operatorname{sqrt}(5)) / 4)))))^{\wedge} 4$ $\left.(((\operatorname{sqrt}(((3+\operatorname{sqrt}(5)) / 2)))-\operatorname{sqrt}(((1+\operatorname{sqrt}(5))) / 2)))^{\wedge} 4(((\operatorname{sqrt}(5)-\operatorname{sqrt}(3)) /(\operatorname{sqrt}(2))))\right)^{\wedge} 4$

## Input:

$$
\begin{aligned}
& \sqrt{45}\left(\frac{1}{2}(\sqrt{5}-2)^{3}\right)\left(\sqrt{\frac{1}{4}(7+3 \sqrt{5})}-\sqrt{\frac{1}{4}(3+3 \sqrt{5})}\right)^{4} \\
& \left(\sqrt{\frac{1}{2}(3+\sqrt{5})}-\sqrt{\left.\frac{1}{2}(1+\sqrt{5})\right)^{4}\left(\frac{\sqrt{5}-\sqrt{3}}{\sqrt{2}}\right)^{4}}\right.
\end{aligned}
$$

## Exact result:

$\frac{3}{8} \sqrt{5}(\sqrt{5}-2)^{3}(\sqrt{5}-\sqrt{3})^{4}$
$\left(\sqrt{\frac{1}{2}(3+\sqrt{5})}-\sqrt{\frac{1}{2}(1+\sqrt{5})}\right)^{4}\left(\frac{1}{2} \sqrt{7+3 \sqrt{5}}-\frac{1}{2} \sqrt{3+3 \sqrt{5}}\right)^{4}$

## Decimal approximation:

$7.5545989655538975680277255117978988700650564261449067 \ldots \times 10^{-8}$
7.5545989... * $10^{-8}$
$\left.\operatorname{sqrt}(15) * 1 / 16^{*}((((\operatorname{sqrt}(5)-1)) / 2))^{\wedge} 4 *((2-\operatorname{sqrt}(3)))\right)^{\wedge} 2 *((4-\operatorname{sqrt}(15)))$

## Input:

$\sqrt{15} \times \frac{1}{16}\left(\frac{1}{2}(\sqrt{5}-1)\right)^{4}(2-\sqrt{3})^{2}(4-\sqrt{15})$

## Result:

$\frac{1}{256} \sqrt{15}(2-\sqrt{3})^{2}(\sqrt{5}-1)^{4}(4-\sqrt{15})$

## Decimal approximation:

$0.000322062869471454321112479786299775908555054150731656741 \ldots$

## Result:

$3.22062869471454321112479786299775908555054150731656741 \times 10^{-4}$
$3.220628694 \ldots * 10^{-4}$

Alternate forms:
$\frac{1}{32}(7-3 \sqrt{5})(7-4 \sqrt{3})(4 \sqrt{15}-15)$
$\frac{1}{32}(-15-21 \sqrt{5}+16 \sqrt{15})$
$-\frac{15}{32}-\frac{21 \sqrt{5}}{32}+\frac{\sqrt{15}}{2}$
Minimal polynomial:
$65536 x^{4}+122880 x^{3}-687360 x^{2}-698400 x+225$

Now, we have that:
$-1024+24 /\left(\left(\left(\left(\operatorname{sqrt}(15) * 1 / 16 *((((\operatorname{sqrt}(5)-1)) / 2))^{\wedge} 4 *((2-\operatorname{sqrt}(3)))\right)^{\wedge} 2 *((4-\right.\right.\right.$ $\operatorname{sqrt(15)))))))}$

## Input:

$-1024+\frac{24}{\sqrt{15} \times \frac{1}{16}\left(\frac{1}{2}(\sqrt{5}-1)\right)^{4}(2-\sqrt{3})^{2}(4-\sqrt{15})}$

## Result:

$\frac{2048 \sqrt{\frac{3}{5}}}{(2-\sqrt{3})^{2}(\sqrt{5}-1)^{4}(4-\sqrt{15})}-1024$

## Decimal approximation:

73495.61177451787222723623392674785115106531233916750239826...
73495.6117745...

Alternate forms:

$$
\begin{aligned}
& -\frac{1}{55}(67840+6720 \sqrt{3}+5376 \sqrt{5}+3136 \sqrt{15}) \\
& \frac{256}{5}\left(\frac{1}{1+\frac{\sqrt{15}}{7 \sqrt{3}-16}}-21\right)
\end{aligned}
$$

$$
17600+24064 \sqrt{\frac{3}{5}}+\frac{1}{2} \sqrt{\frac{13879885824}{5}+3583770624 \sqrt{\frac{3}{5}}}
$$

## Minimal polynomial:

$25 x^{4}-1760000 x^{3}-5607997440 x^{2}-5841134551040 x-2018181241634816$

Thence, we have the following mathematical connection:

$$
\binom{I_{21} \leqslant \int_{-\infty}^{+\infty} \exp \left(-\left(\frac{t}{H}\right)^{2}\right)\left|\sum_{\lambda \leqslant P^{1-\varepsilon},} \frac{a(\lambda)}{\sqrt{\lambda}} B(\lambda) \lambda^{-i\left(\tau^{r}+t\right)}\right|^{2} d t \ll}{\leqslant H\left\{\left(\frac{4}{\varepsilon_{2} \log T}\right)^{2 r}(\log T)(\log X)^{-2 \beta}+\left(\varepsilon_{2}^{-2 r}(\log T)^{-2 r}+\varepsilon_{2}^{-r} h_{1}^{r}(\log T)^{-r}\right) T^{-\varepsilon_{1}}\right\}} /
$$

$$
\begin{aligned}
& \left(\frac{2048 \sqrt{\frac{3}{5}}}{(2-\sqrt{3})^{2}(\sqrt{5}-1)^{4}(4-\sqrt{15})}-1024\right)=73495.6117745 \ldots \Rightarrow \\
& \Rightarrow-3927+2\binom{13 \sqrt{N \exp \left[\int d \hat{\sigma}\left(-\frac{1}{4 u^{2}} \mathbf{P}_{i} D \mathbf{P}_{i}\right)\right]|B p\rangle_{\mathrm{NS}}+}}{\int\left[d \mathbf{X}^{\mu}\right] \exp \left\{\int d \widehat{\sigma}\left(-\frac{1}{4 v^{2}} D \mathbf{X}^{\mu} D^{2} \mathbf{X}^{\mu}\right)\right\}\left|\mathbf{X}^{\mu}, \mathbf{X}^{i}=0\right\rangle_{\mathrm{NS}}}= \\
& -3927+2 \sqrt[13]{2.2983717437 \times 10^{59}+2.0823329825883 \times 10^{59}} \\
& =73490.8437525 \ldots \Rightarrow \\
& \Rightarrow\left(A(r) \times \frac{1}{B(r)}\left(-\frac{1}{\phi(r)}\right) \times \frac{1}{e^{\Lambda(r)}}\right) \Rightarrow \\
& \Rightarrow\left(-0.000029211892 \times \frac{1}{0.0003644621}\left(-\frac{1}{0.0005946833}\right) \times \frac{1}{0.00183393}\right)= \\
& =73491.78832548118710549159572042220548025195726563413398700 \ldots \\
& =73491.7883254 \ldots \Rightarrow
\end{aligned}
$$

$$
/(26 \times 4)^{2}-24=\left(\frac{7.9313976505275 \times 10^{8}}{(26 \times 4)^{2}-24}\right)=73493.30662 \ldots
$$

Mathematical connections with the boundary state corresponding to the NSNS-sector of N Dp-branes in the limit of $u \rightarrow \infty$, with the ratio concerning the general asymptotically flat solution of the equations of motion of the p-brane and with the Karatsuba's equation concerning the zeros of a special type of function connected with Dirichlet series.

Now, we have:
$\left.\left.\left(\left(\left(\left(\operatorname{sqrt}(15) * 1 / 16^{*}((((\operatorname{sqrt}(5)-1)) / 2))^{\wedge} 4 *((2-\operatorname{sqrt}(3)))\right)^{\wedge} 2 *((4-\operatorname{sqrt}(15)))\right)\right)\right)\right)\right)^{\wedge} 1 / 1024$

## Input:

$$
\sqrt[1024]{\sqrt{15} \times \frac{1}{16}\left(\frac{1}{2}(\sqrt{5}-1)\right)^{4}(2-\sqrt{3})^{2}(4-\sqrt{15})}
$$

## Exact result:

```
\(\frac{\sqrt[2048]{15} \sqrt[512]{2-\sqrt{3}} \sqrt[256]{\sqrt{5}-1} \sqrt[1024]{4-\sqrt{15}}}{\sqrt[128]{2}}\)
```


## Decimal approximation:

0.992178440454249520310411311750776776068998591904671813514
$0.9921784404 \ldots$. result very near to the value of the following Rogers-Ramanujan continued fraction:
$\frac{\mathrm{e}^{-\frac{\pi}{\sqrt{5}}}}{\frac{\sqrt{5}}{1+\sqrt[5]{\sqrt{\varphi^{5 \sqrt[4]{5^{3}}}-1}}-\varphi+1}=1-\frac{\mathrm{e}^{-\pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-2 \pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-3 \pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-4 \pi \sqrt{5}}}{1+\ldots}}}} \approx 0.9991104684 .10 .}$
and to the dilaton value $\mathbf{0 . 9 8 9 1 1 7 3 5 2 2 4 3 = \boldsymbol { \phi }}$
$\left(\left(\left(((\operatorname{sqrt}(21) 1 / 2((((3-\operatorname{sqrt}(7))) / \operatorname{sqrt}(2)))))^{\wedge} 2(((\operatorname{sqrt}(((5+\operatorname{sqrt}(7)) / 4)))-\right.\right.\right.$
$\operatorname{sqrt}(((1+\operatorname{sqrt}(7)) / 4))))^{\wedge} 4(((\operatorname{sqrt}(((3+\operatorname{sqrt}(7)) / 4)))-\operatorname{sqrt}(((\operatorname{sqrt}(7)+1)) / 4)))^{\wedge} 4(1 / 2 * \operatorname{sqrt}(7)-$ $\left.\left.\left.\left.\left.\operatorname{sqrt(3)})^{\wedge} 2\right)\right)\right)\right)\right)^{\wedge} 1 / 1024$

## Input:

$$
\begin{aligned}
& \left(\sqrt{21}\left(\frac{1}{2}\left(\frac{3-\sqrt{7}}{\sqrt{2}}\right)^{2}\right)\left(\sqrt{\frac{1}{4}(5+\sqrt{7})}-\sqrt{\frac{1}{4}(1+\sqrt{7})}\right)^{4}\right. \\
& \left.\quad\left(\sqrt{\frac{1}{4}(3+\sqrt{7})}-\sqrt{\frac{1}{4}(\sqrt{7}+1)}\right)^{4}\left(\frac{1}{2} \sqrt{7}-\sqrt{3}\right)^{2}\right) \wedge(1 / 1024)
\end{aligned}
$$

## Exact result:

$$
\begin{aligned}
& \frac{1}{\sqrt[512]{2}} \sqrt[2048]{21} \sqrt[512]{(3-\sqrt{7})\left(\sqrt{3}-\frac{\sqrt{7}}{2}\right)} \\
& \sqrt[256]{\left(\frac{\sqrt{3+\sqrt{7}}}{2}-\frac{1}{2} \sqrt{1+\sqrt{7}}\right)\left(\frac{\sqrt{5+\sqrt{7}}}{2}-\frac{1}{2} \sqrt{1+\sqrt{7}}\right)}
\end{aligned}
$$

## Decimal approximation:

$0.987439348870893804562981265483323778329220689630847778127 \ldots$
$0.987439348 \ldots$ result very near to the dilaton value $\mathbf{0 . 9 8 9 1 1 7 3 5 2 2 4 3}=\boldsymbol{\phi}$

## Alternate forms:

$$
\begin{aligned}
& \frac{1}{2^{3 / 256}} \sqrt[2048]{21} \sqrt[512]{(3-\sqrt{7})(2 \sqrt{3}-\sqrt{7})} \\
& \sqrt[256]{(\sqrt{3+\sqrt{7}}-\sqrt{1+\sqrt{7}})(\sqrt{5+\sqrt{7}}-\sqrt{1+\sqrt{7}})} \\
& \frac{1}{2^{3 / 256}} \sqrt[2048]{21} \sqrt[512]{7+6 \sqrt{3}-3 \sqrt{7}-2 \sqrt{21}} \\
& (1+\sqrt{7}-\sqrt{(1+\sqrt{7})(3+\sqrt{7})}-\sqrt{(1+\sqrt{7})(5+\sqrt{7})}+\sqrt{(3+\sqrt{7})(5+\sqrt{7})})
\end{aligned}
$$

$$
(1 / 256)
$$

$\left(\left(\left(\left(\left(\operatorname{sqrt}(33) 1 / 2 *\left(((2-\operatorname{sqrt}(3)) \wedge 3(((\operatorname{sqrt}(((7+3 * \operatorname{sqrt}(3)) / 4)))-\operatorname{sqrt}(((3+3 \operatorname{sqrt}(3)) / 4)))))^{\wedge} 4\right.\right.\right.\right.\right.\right.$ $(((\operatorname{sqrt}(((5+\operatorname{sqrt}(3)) / 4)))-\operatorname{sqrt}(((1+\operatorname{sqrt}(3))) / 4)))^{\wedge} 4 \quad((((\operatorname{sqrt}(3)-$
$\left.\left.\left.\left.\left.\left.\left.\left.2)) /((\operatorname{sqrt}(2)))^{\wedge} 2\right)\right)\right)\right)\right)\right)\right)\right)^{\wedge} 1 / 1024$

## Input:

$$
\begin{aligned}
&\left(\sqrt{33} \times \frac{1}{2}\left((2-\sqrt{3})^{3}\left(\sqrt{\frac{1}{4}(7+3 \sqrt{3})}-\sqrt{\frac{1}{4}(3+3 \sqrt{3})}\right)^{4}\right.\right. \\
&\left.\left.\left(\sqrt{\frac{1}{4}(5+\sqrt{3})}-\sqrt{\frac{1}{4}(1+\sqrt{3})}\right)^{4}\left(\frac{\sqrt{3}-2}{\sqrt{2}}\right)^{2}\right)\right) \wedge(1 / 1024)
\end{aligned}
$$

## Exact result:

$\frac{\left.\sqrt[2048]{33}(2-\sqrt{3})^{5 / 1024} \sqrt[256]{\left(\frac{\sqrt{5+\sqrt{3}}}{2}\right.}-\frac{1}{2} \sqrt{1+\sqrt{3}}\right)\left(\frac{1}{2} \sqrt{7+3 \sqrt{3}}-\frac{1}{2} \sqrt{3+3 \sqrt{3}}\right)}{\sqrt[512]{2}}$

## Decimal approximation:

0.986555961237011117594683147326554333473724037551432510022 ..
$0.986555961237 \ldots$. result very near to the dilaton value $\mathbf{0 . 9 8 9 1 1 7 3 5 2 2 4 3}=\boldsymbol{\phi}$
$\left(\left(\left(\left(\left(\left(\left(\operatorname{sqrt}(45) 1 / 2 *(\operatorname{sqrt}(5)-2)^{\wedge} 3(((\operatorname{sqrt}(((7+3 * \operatorname{sqrt}(5)) / 4)))-\operatorname{sqrt}(((3+3 \operatorname{sqrt}(5)) / 4))))^{\wedge} 4\right.\right.\right.\right.\right.\right.\right.$ $(((\operatorname{sqrt}(((3+\operatorname{sqrt}(5)) / 2)))-\operatorname{sqrt}(((1+\operatorname{sqrt}(5))) / 2)))^{\wedge} 4(((\operatorname{sqrt}(5)-$
$\left.\left.\left.\left.\left.\left.\left.\operatorname{sqrt}(3)) /((\operatorname{sqrt}(2)))))^{\wedge} 4\right)\right)\right)\right)\right)\right)\right)^{\wedge} 1 / 1024$

## Input:

$$
\begin{aligned}
& \left(\sqrt{45}\left(\frac{1}{2}(\sqrt{5}-2)^{3}\right)\left(\sqrt{\frac{1}{4}(7+3 \sqrt{5})}-\sqrt{\frac{1}{4}(3+3 \sqrt{5})}\right)^{4}\right. \\
& \left.\quad\left(\sqrt{\frac{1}{2}(3+\sqrt{5})}-\sqrt{\frac{1}{2}(1+\sqrt{5})}\right)^{4}\left(\frac{\sqrt{5}-\sqrt{3}}{\sqrt{2}}\right)^{4}\right) \wedge(1 / 1024)
\end{aligned}
$$

## Exact result:

$\frac{1}{2 / 3 / 1024} \sqrt[1024]{3} \sqrt[2048]{5}(\sqrt{5}-2)^{3 / 1024}$

$$
\sqrt[256]{(\sqrt{5}-\sqrt{3})\left(\sqrt{\frac{1}{2}(3+\sqrt{5})}-\sqrt{\frac{1}{2}(1+\sqrt{5})}\right)\left(\frac{1}{2} \sqrt{7+3 \sqrt{5}}-\frac{1}{2} \sqrt{3+3 \sqrt{5}}\right)}
$$

## Decimal approximation:

$0.98411336146 \ldots$ result very near to the dilaton value $\mathbf{0 . 9 8 9 1 1 7 3 5 2 2 4 3}=\boldsymbol{\phi}$

2207-1364-123-29+0.0055/((((sqrt(45)1/2 *(sqrt(5)-2)^3 (((sqrt(((7+3*sqrt(5)))/4)))$\operatorname{sqrt}(((3+3 \operatorname{sqrt}(5)) / 4))))^{\wedge} 4(((\operatorname{sqrt}(((3+\operatorname{sqrt}(5)) / 2)))-\operatorname{sqrt}(((1+\operatorname{sqrt}(5))) / 2)))^{\wedge} 4 \quad(((\operatorname{sqrt}(5)-$ $\operatorname{sqrt(3))/(\operatorname {sqrt}(2))))\wedge 4))))}$

Where 29, 123, 1364, 2207 are Lucas numbers and $0.0055=55 / 10^{4}$ where 55 is a Fibonacci number

## Input:

$$
\begin{aligned}
& 2207-1364-123-29+ \\
& 0.0055 /\left(\left(\sqrt{45} \times \frac{1}{2}(\sqrt{5}-2)^{3}\right)\left(\sqrt{\frac{1}{4}(7+3 \sqrt{5})}-\sqrt{\frac{1}{4}(3+3 \sqrt{5})}\right)^{4}\right. \\
& \left(\sqrt{\frac{1}{2}(3+\sqrt{5})}-\sqrt{\left.\left.\frac{1}{2}(1+\sqrt{5})\right)^{4}\left(\frac{\sqrt{5}-\sqrt{3}}{\sqrt{2}}\right)^{4}\right)}\right.
\end{aligned}
$$

## Result:

73494.3...
73494.3...

Thence, we have the following mathematical connection:

$$
\left(\begin{array}{c}
2207-1364-123-29+ \\
0.0055 /\left(\left(\sqrt{45} \times \frac{1}{2}(\sqrt{5}-2)^{3}\right)\left(\sqrt{\frac{1}{4}(7+3 \sqrt{5})}-\sqrt{\frac{1}{4}(3+3 \sqrt{5})}\right)^{4}\right. \\
\left(\sqrt{\frac{1}{2}(3+\sqrt{5})}-\sqrt{\left.\left.\frac{1}{2}(1+\sqrt{5})\right)^{4}\left(\frac{\sqrt{5}-\sqrt{3}}{\sqrt{2}}\right)^{4}\right)}\right.
\end{array}\right)=73494.3 \ldots \Rightarrow
$$

$$
\begin{aligned}
& \Rightarrow-3927+2\left(\begin{array}{l}
13\binom{N \exp \left[\int d \hat{\sigma}\left(-\frac{1}{4 u^{2}} P_{i} D \mathbf{P}_{i}\right)\right]|B p\rangle_{\mathrm{NS}}+}{\int\left[d \mathrm{X}^{\mu}\right] \exp \left\{\int d \hat{\sigma}\left(-\frac{1}{4 v^{2}} D \mathrm{X}^{\mu} D^{2} \mathrm{X}^{\mu}\right)\right\}\left|\mathrm{X}^{\mu}, \mathrm{X}^{i}=0\right\rangle_{\mathrm{NS}}}= \\
\\
-3927+2 \sqrt[13]{2.2983717437 \times 10^{59}+2.0823329825883 \times 10^{59}} \\
=73490.8437525 \ldots \Rightarrow \\
\Rightarrow\left(A(r) \times \frac{1}{B(r)}\left(-\frac{1}{\phi(r)}\right) \times \frac{1}{e^{\Lambda(r)}}\right) \Rightarrow \\
\Rightarrow\left(-0.000029211892 \times \frac{1}{0.0003644621}\left(-\frac{1}{0.0005946833}\right) \times \frac{1}{0.00183393}\right)= \\
=73491.78832548118710549159572042220548025195726563413398700 \ldots
\end{array}\right. \\
& =73491.7883254 \ldots \Rightarrow
\end{aligned}
$$

$$
\binom{I_{21} \leqslant \int_{-\infty}^{+\infty} \exp \left(-\left(\frac{t}{H}\right)^{2}\right)\left|\sum_{\lambda \leqslant P^{1-\varepsilon_{2}}} \frac{a(\lambda)}{\sqrt{\lambda}} B(\lambda) \lambda^{-i\left(T^{r}+t\right)}\right|^{2} d t \leqslant}{\leqslant H\left\{\left(\frac{4}{\varepsilon_{2} \log T}\right)^{2 r}(\log T)(\log X)^{-2 \beta}+\left(\varepsilon_{2}^{-2 r}(\log T)^{-2 r}+\varepsilon_{2}^{-r} h_{1}^{r}(\log T)^{-r}\right) T^{-\varepsilon_{1}}\right\}} /, ~\left(\frac{7.9313976505275 \times 10^{8}}{(26 \times 4)^{2}-24}\right)=73493.30662 \ldots .
$$

Mathematical connections with the boundary state corresponding to the NSNS-sector of N Dp-branes in the limit of $u \rightarrow \infty$, with the ratio concerning the general asymptotically flat solution of the equations of motion of the p-brane and with the Karatsuba's equation concerning the zeros of a special type of function connected with Dirichlet series.

From the results of the already analyzed expressions, we obtain:
$\left(2.39155248166 \times 10^{\wedge}-6\right) *\left(1 / 9.5641535164 \times 10^{\wedge}-7\right) *\left(1 / 7.5545989655 \times 10^{\wedge}-8\right)$ * (1/3.2206286947 * 10^-4)

## Input interpretation:

$2.39155248166 \times 10^{-6} \times \frac{1}{9.5641535164 \times 10^{-7}} \times \frac{1}{7.5545989655 \times 10^{-8}} \times \frac{\frac{1}{3.2206286947}}{10^{4}}$

## Result:

1027.735372756695967150068231886714891405595570757250597699...
1027.7353727...

And:
$(1 / 2.39155248166 \mathrm{e}-6) *(1 / 9.5641535164 \mathrm{e}-7) *(1 / 7.5545989655 \mathrm{e}-8) *(1 /$ $3.2206286947 \mathrm{e}-4)$

## Input interpretation:

$\frac{\frac{1}{2.39155248166 \times 10^{-6}} \times \frac{1}{9.5641535164 \times 10^{-7}} \times}{\frac{1}{7.5545989655 \times 10^{-8}} \times \frac{1}{3.2206286947 \times 10^{-4}}}$

## Result:

$1.7968899220884632555950165273920648039964203906477204 \ldots \times 10^{22}$
$1.796889922 \ldots * 10^{22}$
$[4096 /(((1 / 2.39155248166 \mathrm{e}-6) *(1 / 9.5641535164 \mathrm{e}-7) *(1 / 7.5545989655 \mathrm{e}-8) *(1$ / $3.2206286947 \mathrm{e}-4))$ )] ${ }^{\wedge} 1 / 4096$

Note that, if we insert 4096, either as a numerator, or as a root index, we obtain:

## Input interpretation:



## Result:

0.98957494535224...
$0.989574 \ldots$. result very near to the dilaton value $\mathbf{0 . 9 8 9 1 1 7 3 5 2 2 4 3}=\boldsymbol{\phi}$
$((((1 / 2.39155248166 \mathrm{e}-6) *(1 / 9.5641535164 \mathrm{e}-7) *(1 / 7.5545989655 \mathrm{e}-8) *(1 /$ $3.2206286947 \mathrm{e}-4)))) 5 /\left(\left(64^{\wedge} 2\right)^{\wedge} 5\right)-\left(64^{\wedge} 2+64 * 5+16\right)$

## Input interpretation:

$$
\begin{gathered}
\left(\frac{1}{2.39155248166 \times 10^{-6}} \times \frac{1}{9.5641535164 \times 10^{-7}} \times \frac{1}{7.5545989655 \times 10^{-8}} \times\right. \\
\left.\frac{1}{3.2206286947 \times 10^{-4}}\right) \times \frac{5}{\left(64^{2}\right)^{5}}-\left(64^{2}+64 \times 5+16\right)
\end{gathered}
$$

## Result:

73495.67828982482649822253539945441525705912723073940387622...
73495.6782898...

Thence, we have the following mathematical connection:

$$
\binom{\left(\frac{1}{2.39155248166 \times 10^{-6}} \times \frac{1}{9.5641535164 \times 10^{-7}} \times \frac{1}{7.5545989655 \times 10^{-8}} \times\right.}{\left.\frac{1}{3.2206286947 \times 10^{-4}}\right) \times \frac{5}{\left(64^{2}\right)^{5}}-\left(64^{2}+64 \times 5+16\right)}=73495.678 \Rightarrow
$$

$$
\begin{gathered}
=73490.8437525 \ldots \Rightarrow \\
\Rightarrow\left(A(r) \times \frac{1}{B(r)}\left(-\frac{1}{\phi(r)}\right) \times \frac{1}{e^{\Lambda(r)}}\right) \Rightarrow \\
\Rightarrow\left(-0.000029211892 \times \frac{1}{0.0003644621}\left(-\frac{1}{0.0005946833}\right) \times \frac{1}{0.00183393}\right)= \\
=73491.78832548118710549159572042220548025195726563413398700 \ldots \\
=73491.7883254 \ldots \Rightarrow \\
\left(J_{21} \leqslant\left.\left.\int_{-\infty}^{+\infty} \exp \left(-\left(\frac{t}{H}\right)^{2}\right)\right|_{\lambda \leqslant p^{1-\varepsilon}} \frac{a(\lambda)}{\sqrt{\lambda}} B(\lambda) \lambda^{-i(T+t)}\right|^{2} d t \leqslant\right. \\
\& H\left\{\left(\frac{4}{\varepsilon_{2} \log T}\right)^{2 r}(\log T)(\log X)^{-2 \beta}+\left(\varepsilon_{2}^{-2 r}(\log T)^{-2 r}+\varepsilon_{2}^{-r} h_{1}^{r}\left(\log T^{-r}\right) T^{-\varepsilon_{1}}\right\}\right) / \\
/(26 \times 4)^{2}-24=\left(\frac{7.9313976505275 \times 10^{8}}{(26 \times 4)^{2}-24}\right)=73493.30662 \ldots
\end{gathered}
$$

Mathematical connections with the boundary state corresponding to the NSNS-sector of N Dp-branes in the limit of $u \rightarrow \infty$, with the ratio concerning the general asymptotically flat solution of the equations of motion of the p-brane and with the Karatsuba's equation concerning the zeros of a special type of function connected with Dirichlet series.

From the results of $1024^{\text {th }}$ roots of the expressions:
0.992178440454249520310411311750776776068998591904671813514
0.987439348870893804562981265483323778329220689630847778127
0.986555961237011117594683147326554333473724037551432510022
0.984113361469563511529046508637472734079204162729013649674
we obtain the following mean:

## 1/4

$(0.992178440454249520310411311+0.98743934887089380456298126+0.98655596$ $12370111175946831+0.984113361469563511529046)$

## Input interpretation:

```
\frac{1}{4}}(0.992178440454249520310411311+0.98743934887089380456298126
    0.9865559612370111175946831 + 0.984113361469563511529046)
```


## Result:

0.98757177800792948849928041775
$0.987571778 \ldots$ result very near to the result of:
$\left(2.3915524816 * 10^{\wedge}-6\right)^{\wedge} 1 / 1024=0.98743934887087$

We note that, performing the following calculation on the results signed in red, we obtain:
$\left(\left(\left(\left(0.98743934887087 * 1 /(2.3915524816 \mathrm{e}-6)^{*} 1 / 2\right)\right)\right)\right)-4096^{*}($ golden ratio $)^{\wedge} 2+(1.65578)^{\wedge} 14$

Where there are $4096=64^{2}, \phi=$ golden ratio and the following Ramanujan's class invariant $Q=\left(G_{505} / G_{101 / 5}\right)^{3}=1164,2696$ i.e. $(1,65578)^{14}$

## Input interpretation:

$0.98743934887087 \times \frac{1}{2.3915524816 \times 10^{-6}} \times \frac{1}{2}-4096 \phi^{2}+1.65578^{14}$

## Result:

196883.9271503793665467874480555413832494353978358613100275
196883.92715... result very near to 196884 , that is a fundamental number of the following $\boldsymbol{j}$-invariant
$j(\tau)=q^{-1}+744+196884 q+21493760 q^{2}+864299970 q^{3}+20245856256 q^{4}+\cdots$
(In mathematics, Felix Klein's $\boldsymbol{j}$-invariant or $\boldsymbol{j}$ function, regarded as a function of a complex variable $\tau$, is a modular function of weight zero for $\operatorname{SL}(2, \mathbf{Z})$ defined on the upper half plane of complex numbers. Several remarkable properties of $j$ have to do with its $q$ expansion (Fourier series expansion), written as a Laurent series in terms of $q=e^{2 \pi i \tau}$ (the square of the nome), which begins:

$$
j(\tau)=q^{-1}+744+196884 q+21493760 q^{2}+864299970 q^{3}+20245856256 q^{4}+\cdots
$$

Note that $j$ has a simple pole at the cusp, so its $q$-expansion has no terms below $q^{-1}$. All the Fourier coefficients are integers, which results in several almost integers, notably Ramanujan's constant:

$$
e^{\pi \sqrt{163}} \approx 640320^{3}+744
$$

The asymptotic formula for the coefficient of $q^{n}$ is given by

$$
\frac{e^{4 \pi \sqrt{n}}}{\sqrt{ } 2 n^{3 / 4}}
$$

as can be proved by the Hardy-Littlewood circle method)

From the following calculation of the four above results, we obtain: 1/
( $0.992178440454249520310411311 * 1 / 0.98743934887089380456298126 * 1 / 0.98655$ $59612370111175946831 * 1 / 0.984113361469563511529046$ )

## Input interpretation:

$$
\left.\begin{array}{rl}
1 /(0.992178440454249520310411311
\end{array} \times \frac{1}{0.98743934887089380456298126} \times 1 \times \frac{1}{0.984113361469563511529046}\right) \quad .
$$

## Result:

0.966245528794624343760338481601039771812738767989917932463 .
$0.9662455287 \ldots$. result very near to the value of the following Rogers-Ramanujan continued fraction:

$$
\frac{\mathrm{e}^{-\frac{\pi}{5}}}{\sqrt{(\varphi-1) \sqrt{5}}-\varphi+1}=1-\frac{\mathrm{e}^{-\pi}}{1+\frac{\mathrm{e}^{-2 \pi}}{1+\frac{\mathrm{e}^{-3 \pi}}{1+\frac{\mathrm{e}^{-4 \pi}}{1+\ldots}}}} \approx 0.9568666373
$$

and also to the spectral index $\mathrm{n}_{\mathrm{s}}$ and to the mesonic Regge slope (see Appendix)

From the algebraic sum, we obtain:
$(0.98743934887089380456298126+0.9865559612370111175946831+0.9841133614$ 69563511529046-0.992178440454249520310411311)

## Input interpretation:

$0.98743934887089380456298126+0.9865559612370111175946831+$
$0.984113361469563511529046-0.992178440454249520310411311$

## Result:

### 1.965930231123218913376299049

$1.96593023 \ldots$ result practically near to the mean value $1.962 * 10^{19}$ of DM particle

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From:
$\left(\mathrm{Pi}^{\wedge} 7\right) / 11520-\left(\mathrm{Pi}^{*} \theta^{6} / 180\right)$, we obtain:
$\left(x^{\wedge} 6^{*} \mathrm{Pi} / 180\right)=\left(\mathrm{Pi}^{\wedge} 7\right) / 11520$

## Input:

$x^{6} \times \frac{\pi}{180}=\frac{\pi^{7}}{11520}$

Alternate form:
$\frac{\pi x^{6}}{180}-\frac{\pi^{7}}{11520}=0$

## Real solutions:

$x=-\frac{\pi}{2}$
$x=\frac{\pi}{2}$
$\theta^{6}=\left(-\frac{\pi}{2},+\frac{\pi}{2}\right)$

## Complex solutions:

$x=-\frac{1}{4} i(\sqrt{3}+-i) \pi$
$x=\frac{1}{4}(1-i \sqrt{3}) \pi$
$x=\frac{1}{4} i(\sqrt{3}+i) \pi$
$x=\frac{1}{4}(1+i \sqrt{3}) \pi$
Input:
$\left(\frac{\pi}{2}\right)^{6} \times \frac{\pi}{180}=\frac{\pi^{7}}{11520}$

Result:
True
Thence, we obtain:
$\left(\mathrm{Pi}^{\wedge} 7\right) / 11520$

## Input:

$\frac{\pi^{7}}{11520}$

## Decimal approximation:

0.262178231577846533638385980301392520131721569036059224197...
$0.2621782315778 \ldots$

## Property:

$\frac{\pi^{7}}{11520}$ is a transcendental number

Alternative representations:
$\frac{\pi^{7}}{11520}=\frac{\left(180^{\circ}\right)^{7}}{11520}$
$\frac{\pi^{7}}{11520}=\frac{(-i \log (-1))^{7}}{11520}$
$\frac{\pi^{7}}{11520}=\frac{\cos ^{-1}(-1)^{7}}{11520}$

Series representations:
$\frac{\pi^{7}}{11520}=\frac{64}{45}\left(\sum_{k=0}^{\infty} \frac{(-1)^{k}}{1+2 k}\right)^{7}$
$\frac{\pi^{7}}{11520}=\frac{64}{45}\left(\sum_{k=0}^{\infty} \frac{(-1)^{1+k} 1195^{-1-2 k}\left(5^{1+2 k}-4 \times 239^{1+2 k}\right)}{1+2 k}\right)^{7}$
$\frac{\pi^{7}}{11520}=\frac{\left(\sum_{k=0}^{\infty}\left(-\frac{1}{4}\right)^{k}\left(\frac{1}{1+2 k}+\frac{2}{1+4 k}+\frac{1}{3+4 k}\right)\right)^{7}}{11520}$

## Integral representations:

$\frac{\pi^{7}}{11520}=\frac{64}{45}\left(\int_{0}^{1} \sqrt{1-t^{2}} d t\right)^{7}$
$\frac{\pi^{7}}{11520}=\frac{1}{90}\left(\int_{0}^{\infty} \frac{1}{1+t^{2}} d t\right)^{7}$

$$
\frac{\pi^{7}}{11520}=\frac{1}{90}\left(\int_{0}^{1} \frac{1}{\sqrt{1-t^{2}}} d t\right)^{7}
$$

And:
$\left(\left(\left(\left(\mathrm{Pi}^{\wedge} 7\right) / 11520\right)\right)\right)^{\wedge} 1 / 128$

## Input:

$\sqrt[128]{\frac{\pi^{7}}{11520}}$

## Exact result:

$\frac{\pi^{7 / 128}}{\sqrt[16]{2} \sqrt[64]{3} \sqrt[128]{5}}$

## Decimal approximation:

0.989595669569276480646550081884615536979140924167165851018...
$0.9895956695692 \ldots$. result very near to the dilaton value $\mathbf{0 . 9 8 9 1 1 7 3 5 2 2 4 3}=\boldsymbol{\phi}$

## Property:

$\frac{\pi^{7 / 128}}{\sqrt[16]{2} \sqrt[64]{3} \sqrt[128]{5}}$ is a transcendental number

## All 128th roots of $\boldsymbol{\pi}^{\wedge} 7 / 11520$ :

$\frac{\pi^{7 / 128} e^{0}}{\sqrt[16]{2} \sqrt[64]{3} \sqrt[128]{5}} \approx 0.98960$ (real, principal root)
$\frac{\pi^{7 / 128} e^{(i \pi) / 64}}{\sqrt[16]{2} \sqrt[64]{3} \sqrt[128]{5}} \approx 0.98840+0.04856 i$
$\frac{\pi^{7 / 128} e^{(i \pi) / 32}}{\sqrt[16]{2} \sqrt[64]{3} \sqrt[128]{5}} \approx 0.98483+0.09700 i$
$\frac{\pi^{7 / 128} e^{(3 i \pi) / 64}}{\sqrt[16]{2} \sqrt[64]{3} \sqrt[128]{5}} \approx 0.97888+0.14520 i$

$$
\frac{\pi^{7 / 128} e^{(i \pi) / 16}}{\sqrt[16]{2} \sqrt[64]{3} \sqrt[128]{5}} \approx 0.97058+0.19306 i
$$

Alternative representations:

$$
\sqrt[128]{\frac{\pi^{7}}{11520}}=\sqrt[128]{\frac{\left(180^{\circ}\right)^{7}}{11520}}
$$

$\sqrt[128]{\frac{\pi^{7}}{11520}}=\sqrt[128]{\frac{(-i \log (-1))^{7}}{11520}}$

$$
\sqrt[128]{\frac{\pi^{7}}{11520}}=\sqrt[128]{\frac{\cos ^{-1}(-1)^{7}}{11520}}
$$

## Series representations:

$\sqrt[128]{\frac{\pi^{7}}{11520}}=\frac{2^{3 / 64}\left(\sum_{k=0}^{\infty} \frac{(-1)^{k}}{1+2 k}\right)^{7 / 128}}{\sqrt[64]{3} \sqrt[128]{5}}$
$\sqrt[128]{\frac{\pi^{7}}{11520}}=\frac{2^{3 / 64}\left(\sum_{k=0}^{\infty} \frac{(-1)^{1+k} 1195^{-1-2 k}\left(5^{1+2 k}-4 \times 239^{1+2 k}\right)}{1 / 128}\right)^{7 / 128}}{\sqrt[1+2]{3} \sqrt[128]{5}}$
$\sqrt[128]{\frac{\pi^{7}}{11520}}=\frac{\left(\sum_{k=0}^{\infty}\left(-\frac{1}{4}\right)^{k}\left(\frac{1}{1+2 k}+\frac{2}{1+4 k}+\frac{1}{3+4 k}\right)\right)^{7 / 128}}{\sqrt[16]{2} \sqrt[64]{3} \sqrt[128]{5}}$

## Integral representations:

$\sqrt[128]{\frac{\pi^{7}}{11520}}=\frac{\left(\int_{0}^{\infty} \frac{1}{1+t^{2}} d t\right)^{7 / 128}}{\sqrt[64]{3} \sqrt[128]{10}}$
$\sqrt[128]{\frac{\pi^{7}}{11520}}=\frac{\left(\int_{0}^{1} \frac{1}{\sqrt{1-t^{2}}} d t\right)^{7 / 128}}{\sqrt[64]{3} \sqrt[128]{10}}$
$\sqrt[128]{\frac{\pi^{7}}{11520}}=\frac{2^{3 / 64}\left(\int_{0}^{1} \sqrt{1-t^{2}} d t\right)^{7 / 128}}{\sqrt[64]{3} \sqrt[128]{5}}$

Now, we have:
36*1/(((Pi^7)/11520))

## Input:

$36 \times \frac{1}{\frac{\pi^{7}}{11520}}$

Result:
$\frac{414720}{\pi^{7}}$

## Decimal approximation:

137.3111710432404885012591457356723678236459462317279639474...
$137.311171 \ldots$ result near to the rest mass of Pion meson 139.57 and practically equal to the reciprocal of fine-structure constant 137.035...

## Property:

$\frac{414720}{\pi^{7}}$ is a transcendental number

## Alternative representations:

$\frac{36}{\frac{\pi^{7}}{11520}}=\frac{36}{\frac{\left(180^{\circ}\right)^{7}}{11520}}$
$\frac{36}{\frac{\pi^{7}}{11520}}=\frac{36}{\frac{(-i \log (-1))^{7}}{11520}}$
$\frac{36}{\frac{\pi^{7}}{11520}}=\frac{36}{\frac{\cos ^{-1}(-1)^{7}}{11520}}$

## Series representations:

$$
\begin{aligned}
& \frac{36}{\frac{\pi^{7}}{11520}}=\frac{405}{16\left(\sum_{k=0}^{\infty} \frac{(-1)^{k}}{1+2 k}\right)^{7}} \\
& \frac{36}{\frac{\pi^{7}}{11520}}=\frac{405}{16\left(\sum_{k=0}^{\infty} \frac{(-1)^{1+k} 1195^{-1-2 k}\left(5^{1+2 k}-4 \times 239^{1+2 k}\right)}{1+2 k}\right)^{7}} \\
& \frac{36}{\frac{\pi^{7}}{11520}}=\frac{414720}{\left(\sum_{k=0}^{\infty}\left(-\frac{1}{4}\right)^{k}\left(\frac{1}{1+2 k}+\frac{2}{1+4 k}+\frac{1}{3+4 k}\right)\right)^{7}}
\end{aligned}
$$

## Integral representations:

$$
\begin{aligned}
& \frac{36}{\frac{\pi^{7}}{11520}}=\frac{3240}{\left(\int_{0}^{\infty} \frac{1}{1+t^{2}} d t\right)^{7}} \\
& \frac{36}{\frac{\pi^{7}}{11520}}=\frac{3240}{\left(\int_{0}^{1} \frac{1}{\sqrt{1-t^{2}}} d t\right)^{7}} \\
& \frac{36}{\frac{\pi^{7}}{11520}}=\frac{405}{16\left(\int_{0}^{1} \sqrt{1-t^{2}} d t\right)^{7}}
\end{aligned}
$$

We note that:
$1 /\left(\left(\left(36^{*} 1 /\left(\left(\left(\operatorname{Pi}^{\wedge} 7\right) / 11520\right)\right)\right)\right)\right)^{\wedge} 1 / 1024$

## Input:

$\frac{1}{\sqrt[1024]{36 \times \frac{1}{\frac{\pi^{7}}{11520}}}}$

## Exact result:

$\frac{\pi^{7 / 1024}}{2^{5 / 512} \sqrt[256]{3} \sqrt[1024]{5}}$

## Decimal approximation:

$0.995204650134757443388135466900444429050754894465357320562 \ldots$
$0.99520465 \ldots$ result very near to the value of the following Rogers-Ramanujan continued fraction:
$\frac{\mathrm{e}^{-\frac{\pi}{\sqrt{5}}}}{\frac{\sqrt{5}}{1+\sqrt[5]{\sqrt{\varphi^{5} \sqrt[4]{5^{3}}}-1}}-\varphi+1}=1-\frac{\mathrm{e}^{-\pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-2 \pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-3 \pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-4 \pi \sqrt{5}}}{1+\ldots}}}} \approx 0.9991104684$
and to the dilaton value $\mathbf{0 . 9 8 9 1 1 7 3 5 2 2 4 3 = \boldsymbol { \phi }}$

## Property:

$\frac{\pi^{7 / 1024}}{2 \sqrt[5 / 512]{\sqrt[256]{3}} \sqrt[1024]{5}}$ is a transcendental number

## Alternative representations:


$\frac{1}{\sqrt[1024]{\frac{36}{\frac{\pi^{7}}{11520}}}}=\frac{1}{\sqrt[1024]{\frac{36}{\frac{\cos ^{-1}(-1)^{7}}{11520}}}}$
$\frac{1}{\sqrt[1024]{\frac{36}{\frac{\pi^{7}}{11520}}}}$
$=\frac{1}{1024} \sqrt{\frac{36}{\frac{(-i \log (-1))^{7}}{11520}}}$

## Series representations:

$\frac{1}{\sqrt[1024]{\frac{36}{\frac{\pi^{7}}{11520}}}}=\frac{\sqrt[256]{\frac{2}{3}}\left(\sum_{k=0}^{\infty} \frac{(-1)^{k}}{1+2 k}\right)^{7 / 1024}}{\sqrt[1024]{5}}$
$\frac{1}{\sqrt[1024]{\frac{36}{\frac{\pi^{7}}{11520}}}}=\frac{\sqrt[256]{\frac{2}{3}}\left(\sum_{k=0}^{\infty} \frac{(-1)^{1+k} 1195^{-1-2 k}\left(5^{\left.1+2 k-4 \times 239^{1+2 k}\right)}\right.}{1+2 k}\right)^{7 / 1024}}{\sqrt[1024]{5}}$
$\frac{1}{\sqrt[1024]{\sqrt{\frac{36}{1 \pi^{7}}}}}=\frac{\left(\sum_{k=0}^{\infty}\left(-\frac{1}{4}\right)^{k}\left(\frac{1}{1+2 k}+\frac{2}{1+4 k}+\frac{1}{3+4 k}\right)\right)^{7 / 1024}}{2^{5 / 512} \sqrt[256]{3} \sqrt[1024]{5}}$

## Integral representations:

$\frac{1}{\sqrt[1024]{\frac{36}{\frac{\pi^{7}}{11520}}}}=\frac{\sqrt[256]{\frac{2}{3}}\left(\int_{0}^{1} \sqrt{1-t^{2}} d t\right)^{7 / 1024}}{\sqrt[1024]{5}}$
$\frac{1}{\sqrt[1024]{\frac{36}{\frac{\pi^{7}}{11520}}}}=\frac{\left(\int_{0}^{\infty} \frac{1}{1+t^{2}} d t\right)^{7 / 1024}}{2^{3 / 1024} \sqrt[256]{3} \sqrt[1024]{5}}$
$\frac{1}{\sqrt[1024]{\frac{36}{\frac{\pi^{7}}{11520}}}}=\frac{\left(\int_{0}^{1} \frac{1}{\sqrt{1-t^{2}}} d t\right)^{7 / 1024}}{2^{3 / 1024} \sqrt[256]{3} \sqrt[1024]{5}}$
$1 / 16^{*} \log$ base $0.99520465\left(1 /\left(\left(\left(36^{*} 1 /\left(\left(\left(\mathrm{Pi}^{\wedge} 7\right) / 11520\right)\right)\right)\right)\right)\right)$

## Input interpretation:

$\frac{1}{16} \log _{0.99520465}\left(\frac{1}{36 \times \frac{1}{\frac{\pi^{7}}{11520}}}\right)$

## Result:

64.0000...

64

## Alternative representation:

$\frac{1}{16} \log _{0.995205}\left(\frac{1}{\frac{36}{\frac{\pi^{7}}{11520}}}\right)=\frac{\log \left(\frac{\frac{1}{36}}{\frac{\pi^{7}}{11520}}\right)}{16 \log (0.995205)}$

## Series representations:

$$
\begin{aligned}
& \frac{1}{16} \log _{0.095205}\left(\frac{1}{\frac{36}{\frac{\pi^{7}}{11520}}}\right)=-\frac{\sum_{k=1}^{\infty} \frac{(-1)^{k}\left(-1+\frac{\pi^{7}}{414720}\right)^{k}}{16 \log (0.995205)}}{1} \\
& \frac{1}{16} \log _{0.995205}\left(\frac{1}{\frac{36}{\frac{\pi^{7}}{11520}}}\right)= \\
& -13.0022 \log \left(\frac{\pi^{7}}{414720}\right)-0.0625 \log \left(\frac{\pi^{7}}{414720}\right) \sum_{k=0}^{\infty}(-0.00479535)^{k} G(k) \\
& \text { for }\left(G(0)=0 \text { and } \frac{(-1)^{k} k}{2(1+k)(2+k)}+G(k)=\sum_{j=1}^{k} \frac{(-1)^{1+j} G(-j+k)}{1+j}\right)
\end{aligned}
$$

And:
$21+\left[64 * 7 * 1 /\left(\left(\left(\mathrm{Pi}^{\wedge} 7\right) / 11520\right)\right)\right]$

## Input:

$21+64 \times 7 \times \frac{1}{\frac{\pi^{7}}{11520}}$

## Result:

$21+\frac{5160960}{\pi^{7}}$

## Decimal approximation:

1729.761239649214968015669369155033910694260664217059106901...
1729.761239649.....

This result is very near to the mass of candidate glueball $\mathrm{f}_{0}(1710)$ meson. Furthermore, 1728 occurs in the algebraic formula for the $j$-invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the GrossZagier theorem. The number 1728 is one less than the Hardy-Ramanujan number 1729

## Property:

$21+\frac{5160960}{\pi^{7}}$ is a transcendental number

## Alternate form:

$\frac{21\left(\pi^{7}+245760\right)}{\pi^{7}}$

## Alternative representations:

$21+\frac{64 \times 7}{\frac{\pi^{7}}{11520}}=21+\frac{448}{\frac{\left(180^{\circ} 7^{7}\right.}{11520}}$
$21+\frac{64 \times 7}{\frac{\pi^{7}}{11520}}=21+\frac{448}{\frac{(-i \log (-1))^{7}}{11520}}$
$21+\frac{64 \times 7}{\frac{\pi^{7}}{11520}}=21+\frac{448}{\frac{\cos ^{-1}(-1)^{7}}{11520}}$

## Series representations:

$$
\begin{aligned}
& 21+\frac{64 \times 7}{\frac{\pi^{7}}{11520}}=21+\frac{315}{\left(\sum_{k=0}^{\infty} \frac{(-1)^{k}}{1+2 k}\right)^{7}} \\
& 21+\frac{64 \times 7}{\frac{\pi^{7}}{11520}}=21+\frac{315}{\left(\sum_{k=0}^{\infty} \frac{(-1)^{1+k} 1195^{-1-2 k}\left(5^{1+2 k}-4 \times 239^{1+2 k}\right)}{1+2 k}\right)^{7}} \\
& 21+\frac{64 \times 7}{\frac{\pi^{7}}{11520}}=21+\frac{5160960}{\left(\sum_{k=0}^{\infty}\left(-\frac{1}{4}\right)^{k}\left(\frac{1}{1+2 k}+\frac{2}{1+4 k}+\frac{1}{3+4 k}\right)\right)^{7}}
\end{aligned}
$$

## Integral representations:

$$
\begin{aligned}
& 21+\frac{64 \times 7}{\frac{\pi^{7}}{11520}}=21+\frac{315}{\left(\int_{0}^{1} \sqrt{1-t^{2}} d t\right)^{7}} \\
& 21+\frac{64 \times 7}{\frac{\pi^{7}}{11520}}=21+\frac{40320}{\left(\int_{0}^{\infty} \frac{1}{1+t^{2}} d t\right)^{7}} \\
& 21+\frac{64 \times 7}{\frac{\pi^{7}}{11520}}=21+\frac{40320}{\left(\int_{0}^{1} \frac{1}{\sqrt{1-t^{2}}} d t\right)^{7}}
\end{aligned}
$$

Furthermore:
$2 \mathrm{Pi}^{*}\left(\mathrm{Pi}^{\wedge} 7\right) / 11520$

## Input:

$2 \pi \times \frac{\pi^{7}}{11520}$

## Result:

$\frac{\pi^{8}}{5760}$

## Decimal approximation:

$1.647314412512252431793155469428257950815482547159910189602 \ldots$
$1.6473144125122 \ldots \approx \zeta(2)=\frac{\pi^{2}}{6}=1.644934 \ldots$

## Property:

$\frac{\pi^{8}}{5760}$ is a transcendental number

## Alternative representations:

$\frac{(2 \pi) \pi^{7}}{11520}=\frac{360^{\circ}\left(180^{\circ}\right)^{7}}{11520}$
$\frac{(2 \pi) \pi^{7}}{11520}=-\frac{2 i \log (-1)(-i \log (-1))^{7}}{11520}$
$\frac{(2 \pi) \pi^{7}}{11520}=\frac{2 \cos ^{-1}(-1) \cos ^{-1}(-1)^{7}}{11520}$

## Series representations:

$\frac{(2 \pi) \pi^{7}}{11520}=\frac{512}{45}\left(\sum_{k=0}^{\infty} \frac{(-1)^{k}}{1+2 k}\right)^{8}$
$\frac{(2 \pi) \pi^{7}}{11520}=\frac{512}{45}\left(\sum_{k=0}^{\infty} \frac{(-1)^{k} 1195^{-1-2 k}\left(5^{1+2 k}-4 \times 239^{1+2 k}\right)}{1+2 k}\right)^{8}$
$\frac{(2 \pi) \pi^{7}}{11520}=\frac{\left(\sum_{k=0}^{\infty}\left(-\frac{1}{4}\right)^{k}\left(\frac{1}{1+2 k}+\frac{2}{1+4 k}+\frac{1}{3+4 k}\right)\right)^{8}}{5760}$

## Integral representations:

$\frac{(2 \pi) \pi^{7}}{11520}=\frac{2}{45}\left(\int_{0}^{\infty} \frac{1}{1+t^{2}} d t\right)^{8}$
$\frac{(2 \pi) \pi^{7}}{11520}=\frac{512}{45}\left(\int_{0}^{1} \sqrt{1-t^{2}} d t\right)^{8}$

$$
\frac{(2 \pi) \pi^{7}}{11520}=\frac{2}{45}\left(\int_{0}^{1} \frac{1}{\sqrt{1-t^{2}}} d t\right)^{8}
$$

We note that:
$\zeta(2)=\frac{\pi^{2}}{6}=1.644934 \ldots \approx \frac{\pi^{8}}{5768.33516}=1.647314 \ldots \cong 1.644934 \ldots$

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$71^{\wedge} 3-23^{\wedge} 3=588^{\wedge} 2$

## Input:

$71^{3}-23^{3}=588^{2}$

## Result:

True

## Left hand side:

$71^{3}-23^{3}=345744$
Right hand side:
$588^{2}=345744$
(71^3-23^3)/4-(4096*3)-588-71
$4096=64^{2}$

## Input:

$\frac{1}{4}\left(71^{3}-23^{3}\right)-4096 \times 3-588-71$
Result:
73489
73489

$1^{\wedge} 3+135^{\wedge} 3+138^{\wedge} 3=172^{\wedge} 3$

## Input:

$$
1^{3}+135^{3}+138^{3}=172^{3}
$$

## Result:

True

## Left hand side:

$1^{3}+135^{3}+138^{3}=5088448$

## Right hand side:

$172^{3}=5088448$
$\left(1^{\wedge} 3+135^{\wedge} 3+138^{\wedge} 3\right) / 64-4096-2048+128$
$4096=64^{2} ; 2048=64 * 8 * 4 ; 128=64 * 2$

## Input:

$\frac{1}{64}\left(1^{3}+135^{3}+138^{3}\right)-4096-2048+128$

## Result:

73491
73491

$23^{\wedge} 3+134^{\wedge} 3=95^{\wedge} 3+116^{\wedge} 3$

## Input:

$23^{3}+134^{3}=95^{3}+116^{3}$

## Result:

True

## Left hand side:

$23^{3}+134^{3}=2418271$

Right hand side:
$95^{3}+116^{3}=2418271$
$\left(23^{\wedge} 3+134 \wedge 3\right) / 32-4096+2048-32$
$4096=64^{2} ; 2048=64 * 8 * 4 ; 32=8 * 4$
Input:
$\frac{1}{32}\left(23^{3}+134^{3}\right)-4096+2048-32$

## Exact result:

$\frac{2351711}{32}$
Decimal form:
73490.96875
73490.96875

$19^{\wedge} 3+60^{\wedge} 3+69^{\wedge} 3=82^{\wedge} 3$

## Input:

$19^{3}+60^{3}+69^{3}=82^{3}$

## Result:

True

## Left hand side:

$19^{3}+60^{3}+69^{3}=551368$
Right hand side:
$82^{3}=551368$
$\left(19^{\wedge} 3+60^{\wedge} 3+69^{\wedge} 3\right) / 8+4096+512-32-8$
$4096=64^{2} ; 512=64 * 8 ; 32=8 * 4$

## Input:

$\frac{1}{8}\left(19^{3}+60^{3}+69^{3}\right)+4096+512-32-8$

## Result:

73489
73489

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$1+(1 / 4) \mathrm{x}+(3 / 8)^{\wedge} 2 \mathrm{x}^{\wedge} 2$

## Input:

$1+\frac{1}{4} x+\left(\frac{3}{8}\right)^{2} x^{2}$

## Result:

$\frac{9 x^{2}}{64}+\frac{x}{4}+1$
Plots:



## Geometric figure:

parabola

## Alternate forms:

$\frac{1}{64}\left(9 x^{2}+16 x+64\right)$
$\frac{1}{64} x(9 x+16)+1$
$\left(\frac{9 x}{64}+\frac{1}{4}\right) x+1$

## Complex roots:

$$
\begin{aligned}
& x \approx-0.8889-2.5142 i \\
& x \approx-0.8889+2.5142 i
\end{aligned}
$$

## Polynomial discriminant:

$\Delta=-\frac{1}{2}$
Properties as a real function:

## Domain

$\mathbf{R}$ (all real numbers)

## Range

$\left(y \in \mathbb{R}: y \geq \frac{8}{9}\right)$

Derivative:
$\frac{d}{d x}\left(1+\frac{x}{4}+\left(\frac{3}{8}\right)^{2} x^{2}\right)=\frac{1}{32}(9 x+8)$

Indefinite integral:
$\int\left(1+\frac{x}{4}+\frac{9 x^{2}}{64}\right) d x=\frac{3 x^{3}}{64}+\frac{x^{2}}{8}+x+$ constant

## Global minimum:

$\min \left\{1+\frac{x}{4}+\left(\frac{3}{8}\right)^{2} x^{2}\right\}=\frac{8}{9}$ at $x=-\frac{8}{9}$
$(-0.8889+2.5142 \mathrm{i}) * \mathrm{Pi} / 3$

## Input interpretation:

$(-0.8889+2.5142 i) \times \frac{\pi}{3}$

## Result:

- 0.930854... +
2.63286... $i$


## Polar coordinates:

```
r=2.79257 (radius), }0=109.47\mp@subsup{1}{}{\circ}\mathrm{ (angle)
```

2.79257

Alternative representations:
$\frac{1}{3}(-0.8889+2.5142 i) \pi=60^{\circ}(-0.8889+2.5142 i)$
$\frac{1}{3}(-0.8889+2.5142 i) \pi=-\frac{1}{3} i(-0.8889+2.5142 i) \log (-1)$
$\frac{1}{3}(-0.8889+2.5142 i) \pi=\frac{1}{3}(-0.8889+2.5142 i) \cos ^{-1}(-1)$

## Series representations:

$\frac{1}{3}(-0.8889+2.5142 i) \pi=3.35227(-0.353552+i) \sum_{k=0}^{\infty} \frac{(-1)^{k}}{1+2 k}$

$$
\begin{aligned}
& \frac{1}{3}(-0.8889+2.5142 i) \pi=1.67613(-0.353552+i)\left(-1+\sum_{k=1}^{\infty} \frac{2^{k}}{\binom{2 k}{k}}\right) \\
& \frac{1}{3}(-0.8889+2.5142 i) \pi=0.838067(-0.353552+i) \sum_{k=0}^{\infty} \frac{2^{-k}(-6+50 k)}{\binom{3 k}{k}}
\end{aligned}
$$

$\binom{n}{m}$ is the binomial coefficient

## Integral representations:

$\frac{1}{3}(-0.8889+2.5142 i) \pi=\int_{0}^{\infty} \frac{-0.5926+1.67613 i}{1+t^{2}} d t$
$\frac{1}{3}(-0.8889+2.5142 i) \pi=3.35227(-0.353552+i) \int_{0}^{1} \sqrt{1-t^{2}} d t$
$\frac{1}{3}(-0.8889+2.5142 i) \pi=\int_{0}^{\infty} \frac{(-0.5926+1.67613 i) \sin (t)}{t} d t$
$((((-0.8889+2.5142 \mathrm{i}) * \mathrm{Pi} / 3)))^{\wedge} 1 / 2$

## Input interpretation:

$$
\sqrt{(-0.8889+2.5142 i) \times \frac{\pi}{3}}
$$

## Result:

0.964811... +
1.36445... $i$

## Polar coordinates:

$r=1.6711$ (radius), $\theta=54.7356^{\circ}$ (angle)
1.6711

We note that 1.6711 is a result practically equal to the value of the formula:

$$
m_{p^{\prime}}=2 \times \frac{\eta}{R} m_{P}=1.6714213 \times 10^{-24} \mathrm{gm}
$$

that is the holographic proton mass (N. Haramein)
$1 /((((-0.8889+2.5142 \mathrm{i}) * \mathrm{Pi} / 3)))^{\wedge} 1 / 4096$

## Input interpretation:



## Result:

0.99974920... -
0.00046634590 .. . $i$

## Polar coordinates:

$r=0.999749$ (radius), $\theta=-0.0267264^{\circ}$ (angle)
0.999749 result practically equal to the value of the following Rogers-Ramanujan continued fraction:
$\frac{\mathrm{e}^{-\frac{\pi}{\sqrt{5}}}}{\frac{\sqrt{5}}{1+\sqrt[5]{\sqrt{\varphi^{5 \sqrt[4]{5^{3}}}}-1}}-\varphi+1}=1-\frac{\mathrm{e}^{-\pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-2 \pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-3 \pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-4 \pi \sqrt{5}}}{1+\ldots}}}} \approx 0.9991104684$

## Alternative representations:


$\frac{1}{\sqrt[4096]{\frac{1}{3}(-0.8889+2.5142 i) \pi}}=\frac{1}{\sqrt[4096]{\frac{1}{3}(-0.8889+2.5142 i) \cos ^{-1}(-1)}}$

Series representations:

$\binom{n}{m}$ is the binomial coefficient

## Integral representations:

$\frac{1}{\sqrt[4096]{\frac{1}{3}(-0.8889+2.5142 i) \pi}}=\frac{0.999874}{\sqrt[4096]{-0.353552+i \int_{0}^{\infty} \frac{1}{1+t^{2}} d t}}$

$\frac{1}{\sqrt[4096]{\frac{1}{3}(-0.8889+2.5142 i) \pi}}=\frac{0.999874}{\sqrt[4096]{-0.353552+i \int_{0}^{\infty} \frac{\sin (t)}{t} d t}}$
$-512-2048-1 / 3((((-0.8889+2.5142 \mathrm{i}) * \mathrm{Pi} / 3)))^{\wedge} 12$

## Input interpretation:

$-512-2048-\frac{1}{3}\left((-0.8889+2.5142 i) \times \frac{\pi}{3}\right)^{12}$

## Result:

41876.7... +
60390.8...

## Polar coordinates:

$$
r=73489.5 \text { (radius), } \quad \theta=55.2615^{\circ} \text { (angle) }
$$

73489.5

## Alternative representations:

$$
\begin{aligned}
& -512-2048-\frac{1}{3}\left(\frac{1}{3}(-0.8889+2.5142 i) \pi\right)^{12}=-2560-\frac{1}{3}\left(60^{\circ}(-0.8889+2.5142 i)\right)^{12} \\
& -512-2048-\frac{1}{3}\left(\frac{1}{3}(-0.8889+2.5142 i) \pi\right)^{12}= \\
& -2560-\frac{1}{3}\left(-\frac{1}{3} i(-0.8889+2.5142 i) \log (-1)\right)^{12} \\
& -512-2048-\frac{1}{3}\left(\frac{1}{3}(-0.8889+2.5142 i) \pi\right)^{12}= \\
& -2560-\frac{1}{3}\left(\frac{1}{3}(-0.8889+2.5142 i) \cos ^{-1}(-1)\right)^{12}
\end{aligned}
$$

## Series representations:

$$
\begin{aligned}
& -512-2048-\frac{1}{3}\left(\frac{1}{3}(-0.8889+2.5142 i) \pi\right)^{12}= \\
& -2560-671338 \cdot(0.353552-i)^{12}\left(\sum_{k=0}^{\infty} \frac{(-1)^{k}}{1+2 k}\right)^{12} \\
& -512-2048-\frac{1}{3}\left(\frac{1}{3}(-0.8889+2.5142 i) \pi\right)^{12}= \\
& -2560-0.0400149(0.353552-i)^{12}\left(\sum_{k=0}^{\infty} \frac{2^{-k}(-6+50 k)}{\binom{3 k}{k}}\right)^{12}
\end{aligned}
$$

$$
\begin{aligned}
& -512-2048-\frac{1}{3}\left(\frac{1}{3}(-0.8889+2.5142 i) \pi\right)^{12}= \\
& -2560-163.901(0.353552-i)^{12} \sqrt{3} 12\left(\sum_{k=0}^{\infty} \frac{\left(-\frac{1}{3}\right)^{k}}{1+2 k}\right)^{12}
\end{aligned}
$$

## Integral representations:

$$
\begin{aligned}
& -512-2048-\frac{1}{3}\left(\frac{1}{3}(-0.8889+2.5142 i) \pi\right)^{12}= \\
& -2560-163.901(0.353552-i)^{12}\left(\int_{0}^{\infty} \frac{1}{1+t^{2}} d t\right)^{12} \\
& -512-2048-\frac{1}{3}\left(\frac{1}{3}(-0.8889+2.5142 i) \pi\right)^{12}= \\
& -2560-671338 .(0.353552-i)^{12}\left(\int_{0}^{1} \sqrt{1-t^{2}} d t\right)^{12} \\
& -512-2048-\frac{1}{3}\left(\frac{1}{3}(-0.8889+2.5142 i) \pi\right)^{12}= \\
& -2560-163.901(0.353552-i)^{12}\left(\int_{0}^{\infty} \frac{\sin (t)}{t} d t\right)^{12}
\end{aligned}
$$

$(-0.8889+2.5142 \mathrm{i}) * \mathrm{Pi} / 6$

## Input interpretation:

$(-0.8889+2.5142 i) \times \frac{\pi}{6}$

## Result:

- 0.465427... +
1.31643... $i$


## Polar coordinates:

$$
r=1.39629 \text { (radius), } \quad \theta=109.471^{\circ} \text { (angle) }
$$

1.39629

## Alternative representations:

$\frac{1}{6}(-0.8889+2.5142 i) \pi=\frac{180}{6}{ }^{\circ}(-0.8889+2.5142 i)$

$$
\begin{aligned}
& \frac{1}{6}(-0.8889+2.5142 i) \pi=-\frac{1}{6} i((-0.8889+2.5142 i) \log (-1)) \\
& \frac{1}{6}(-0.8889+2.5142 i) \pi=\frac{1}{6}(-0.8889+2.5142 i) \cos ^{-1}(-1)
\end{aligned}
$$

## Series representations:

$$
\begin{aligned}
& \frac{1}{6}(-0.8889+2.5142 i) \pi=1.67613(-0.353552+i) \sum_{k=0}^{\infty} \frac{(-1)^{k}}{1+2 k} \\
& \frac{1}{6}(-0.8889+2.5142 i) \pi=0.838067(-0.353552+i)\left(-1+\sum_{k=1}^{\infty} \frac{2^{k}}{\binom{2 k}{k}}\right) \\
& \frac{1}{6}(-0.8889+2.5142 i) \pi=0.419033(-0.353552+i) \sum_{k=0}^{\infty} \frac{2^{-k}(-6+50 k)}{\binom{3 k}{k}}
\end{aligned}
$$

## Integral representations:

$\frac{1}{6}(-0.8889+2.5142 i) \pi=\int_{0}^{\infty} \frac{-0.2963+0.838067 i}{1+t^{2}} d t$

$$
\frac{1}{6}(-0.8889+2.5142 i) \pi=1.67613(-0.353552+i) \int_{0}^{1} \sqrt{1-t^{2}} d t
$$

$$
\frac{1}{6}(-0.8889+2.5142 i) \pi=\int_{0}^{\infty} \frac{(-0.2963+0.838067 i) \sin (t)}{t} d t
$$

$1 /((((-0.8889+2.5142 \mathrm{i}) * \mathrm{Pi} / 6)))^{\wedge} 1 / 1024$

## Input interpretation:

1
$\sqrt[1024]{(-0.8889+2.5142 i) \times \frac{\pi}{6}}$

## Result:

0.99967232... -
$0.0018652422 \ldots i$

## Polar coordinates:

$r=0.999674$ (radius), $\theta=-0.106905^{\circ}$ (angle)
0.999674 result practically equal to the value of the following Rogers-Ramanujan continued fraction:
$\frac{\mathrm{e}^{-\frac{\pi}{\sqrt{5}}}}{\frac{\sqrt{5}}{1+\sqrt[5]{\sqrt{\varphi^{5 \sqrt[4]{5^{3}}}-1}}-\varphi+1}=1-\frac{\mathrm{e}^{-\pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-2 \pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-3 \pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-4 \pi \sqrt{5}}}{1+\ldots}}}} \approx 0.9991104684 .10 .}$

## Alternative representations:

$\frac{1}{\sqrt[1024]{\frac{1}{6}(-0.8889+2.5142 i) \pi}}=\frac{1}{\sqrt[1024]{\frac{180}{6}{ }^{\circ}(-0.8889+2.5142 i)}}$

$\frac{1}{\sqrt[1024]{\frac{1}{6}(-0.8889+2.5142 i) \pi}}=\frac{1}{\sqrt[1024]{\frac{1}{6}(-0.8889+2.5142 i) \cos ^{-1}(-1)}}$

## Series representations:



$\sqrt[1024]{\frac{1}{6}(-0.8889+2.5142 i) \pi}$


## Integral representations:


$((((-0.8889+2.5142 \mathrm{i}) * \mathrm{Pi} / 6))))^{\wedge} 32 * 1.61803398-4096 * \mathrm{Pi}-276-320-384-89$

## Input interpretation:

$\left((-0.8889+2.5142 i) \times \frac{\pi}{6}\right)^{32} \times 1.61803398-4096 \pi-276-320-384-89$
$i$ is the imaginary unit

## Result:

- 22435.0... -
69983.1... $i$


## Polar coordinates:

$$
r=73491.2 \text { (radius), } \quad \theta=-107.775^{\circ} \text { (angle) }
$$

73491.2

## Alternative representations:

$$
\begin{aligned}
& \left(\frac{1}{6}(-0.8889+2.5142 i) \pi\right)^{32} 1.61803-4096 \pi-276-320-384-89= \\
& \quad-1069-737280^{\circ}+1.61803\left(\frac{180}{6}^{\circ}(-0.8889+2.5142 i)\right)^{32}
\end{aligned}
$$

$$
\begin{aligned}
& \left(\frac{1}{6}(-0.8889+2.5142 i) \pi\right)^{32} 1.61803-4096 \pi-276-320-384-89= \\
& \quad-1069+4096 i \log (-1)+1.61803\left(-\frac{1}{6} i((-0.8889+2.5142 i) \log (-1))\right)^{32}
\end{aligned}
$$

$$
\left(\frac{1}{6}(-0.8889+2.5142 i) \pi\right)^{32} 1.61803-4096 \pi-276-320-384-89=
$$

$$
-1069-4096 \cos ^{-1}(-1)+1.61803\left(\frac{1}{6}(-0.8889+2.5142 i) \cos ^{-1}(-1)\right)^{32}
$$

## Series representations:

$$
\begin{aligned}
& \left(\frac{1}{6}(-0.8889+2.5142 i) \pi\right)^{32} 1.61803-4096 \pi-276-320-384-89= \\
& \quad-1069-16384 \sum_{k=0}^{\infty} \frac{(-1)^{k}}{1+2 k}+2.43703 \times 10^{7}(0.353552-i)^{32}\left(\sum_{k=0}^{\infty} \frac{(-1)^{k}}{1+2 k}\right)^{32}
\end{aligned}
$$

$$
\left(\frac{1}{6}(-0.8889+2.5142 i) \pi\right)^{32} 1.61803-4096 \pi-276-320-384-89=
$$

$$
-1069-4096\left(-2+2 \sum_{k=1}^{\infty} \frac{2^{k}}{\binom{2 k}{k}}\right)+
$$

$$
2.03305 \times 10^{-25}(-0.8889+2.5142 i)^{32}\left(-2+2 \sum_{k=1}^{\infty} \frac{2^{k}}{\binom{2 k}{k}}\right)^{32}
$$

$$
\begin{aligned}
& \left(\frac{1}{6}(-0.8889+2.5142 i) \pi\right)^{32} 1.61803-4096 \pi-276-320-384-89= \\
& -1069-4096\left(x+2 \sum_{k=1}^{\infty} \frac{\sin (k x)}{k}\right)+2.03305 \times 10^{-25} \\
& \quad(-0.8889+2.5142 i)^{32}\left(x+2 \sum_{k=1}^{\infty} \frac{\sin (k x)}{k}\right)^{32} \text { for }(x \in \mathbb{R} \text { and } x>0)
\end{aligned}
$$

## Integral representations:

$$
\begin{aligned}
& \left(\frac{1}{6}(-0.8889+2.5142 i) \pi\right)^{32} 1.61803-4096 \pi-276-320-384-89= \\
& -1069-8192 \int_{0}^{\infty} \frac{1}{1+t^{2}} d t+0.00567416(0.353552-i)^{32}\left(\int_{0}^{\infty} \frac{1}{1+t^{2}} d t\right)^{32} \\
& \left(\frac{1}{6}(-0.8889+2.5142 i) \pi\right)^{32} 1.61803-4096 \pi-276-320-384-89= \\
& -1069-8192 \int_{0}^{\infty} \frac{\sin (t)}{t} d t+0.00567416(0.353552-i)^{32}\left(\int_{0}^{\infty} \frac{\sin (t)}{t} d t\right)^{32}
\end{aligned}
$$

$$
\begin{aligned}
& \left(\frac{1}{6}(-0.8889+2.5142 i) \pi\right)^{32} 1.61803-4096 \pi-276-320-384-89= \\
& \quad-1069-16384 \int_{0}^{1} \sqrt{1-t^{2}} d t+2.43703 \times 10^{7}(0.353552-i)^{32}\left(\int_{0}^{1} \sqrt{1-t^{2}} d t\right)^{32}
\end{aligned}
$$

Note that we have obtained various very similar results:
73489; 73491; 73490.96875; 73489; 73489.5; 73491.2
Performing the average of these values, we obtain:

$$
\begin{aligned}
& (73489+73491+73490.96875+73489+73489.5+73491.2) / 6= \\
& =73490.1114583 \ldots
\end{aligned}
$$

Thence, we have the following mathematical connection:

$$
\begin{aligned}
& \left(\begin{array}{l}
\frac{1}{6}(73489+73491+73490.96875+73489+73489.5+73491.2)
\end{array}\right)=73490.1114 \ldots \Rightarrow \\
& \Rightarrow-3927+2\left(\begin{array}{c}
13\binom{N \exp \left[\int d \hat{\sigma}\left(-\frac{1}{4 u^{2}} \mathrm{P}_{i} D \mathbf{P}_{i}\right)\right]|B p\rangle_{\mathrm{NS}}+}{\int\left[d \mathrm{X}^{\mu}\right] \exp \left\{\int d \hat{\sigma}\left(-\frac{1}{4 v^{2}} D \mathrm{X}^{\mu} D^{2} \mathrm{X}^{\mu}\right)\right\}\left|\mathrm{X}^{\mu}, \mathrm{X}^{i}=0\right\rangle_{\mathrm{NS}}}= \\
\\
\quad-3927+2 \sqrt[13]{2.2983717437 \times 10^{59}+2.0823329825883 \times 10^{59}} \\
\quad=73490.8437525 \ldots \Rightarrow
\end{array}\right.
\end{aligned}
$$

$$
\begin{gathered}
\Rightarrow\left(A(r) \times \frac{1}{B(r)}\left(-\frac{1}{\phi(r)}\right) \times \frac{1}{e^{\Lambda(r)}}\right) \Rightarrow \\
\Rightarrow\left(-0.000029211892 \times \frac{1}{0.0003644621}\left(-\frac{1}{0.0005946833}\right) \times \frac{1}{0.00183393}\right)= \\
=73491.78832548118710549159572042220548025195726563413398700 \ldots \\
=73491.7883254 \ldots \Rightarrow \\
\left(\begin{array}{l}
I_{21} \leqslant\left.\left.\int_{-\infty}^{+\infty} \exp \left(-\left(\frac{t}{H}\right)^{2}\right)\right|_{\lambda \leqslant p^{1-\varepsilon}} \sum_{1} \frac{a(\lambda)}{\sqrt{\lambda}} B(\lambda) \lambda^{-i(T+t)}\right|^{2} d t \leqslant \\
\left.\leqslant H\left\{\left(\frac{4}{\varepsilon_{2} \log T}\right)^{2 r}(\log T)(\log X)^{-2 \beta}+\left(\varepsilon_{2}^{-2 r}(\log T)^{-2 r}+\varepsilon_{2}^{-r} h_{1}^{r}(\log T)^{-r}\right) T^{-\varepsilon_{1}}\right\}\right) \\
\\
\\
/(26 \times 4)^{2}-24=\left(\frac{7.9313976505275 \times 10^{8}}{(26 \times 4)^{2}-24}\right)=73493.30662 \ldots
\end{array}\right)
\end{gathered}
$$

Mathematical connections with the boundary state corresponding to the NSNS-sector of N Dp-branes in the limit of $u \rightarrow \infty$, with the ratio concerning the general asymptotically flat solution of the equations of motion of the $p$-brane and with the Karatsuba's equation concerning the zeros of a special type of function connected with Dirichlet series.

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For $v=y ; u=z$, and $f^{6} / f^{6}=f^{12} / f^{12}=-1 \quad f^{18} / f^{18}=1$, we obtain:
$y-z=5^{\wedge} 5^{*} 11+75^{\wedge} 2^{*}-1 / x^{\wedge} 5+15^{\wedge} 2^{*}-1 / x^{\wedge} 6-1 / x^{\wedge} 7$

## Input:

$y-z=5^{5} \times 11+\frac{75^{2} \times(-1)}{x^{5}}+\frac{15^{2} \times(-1)}{x^{6}}-\frac{1}{x^{7}}$

Result:
$y-z=-\frac{1}{x^{7}}-\frac{225}{x^{6}}-\frac{5625}{x^{5}}+34375$
Alternate forms:
$\frac{1}{x^{7}}+\frac{225}{x^{6}}+\frac{5625}{x^{5}}+y-34375=z$
$y-z=\frac{34375 x^{7}-5625 x^{2}-225 x-1}{x^{7}}$
$y-z=\frac{25 x\left(25 x\left(55 x^{5}-9\right)-9\right)-1}{x^{7}}$
Solution:
$x \neq 0, \quad z=\frac{x^{7} y-34375 x^{7}+5625 x^{2}+225 x+1}{x^{7}}$

## Integer solutions:

$x=-1, \quad z=y-39776$
$x=1, \quad z=y-28524$

## Implicit derivatives:

$\frac{\partial x(y, z)}{\partial z}=-\frac{x^{8}}{7+1350 x+28125 x^{2}}$
$\frac{\partial x(y, z)}{\partial y}=\frac{x^{8}}{7+1350 x+28125 x^{2}}$
$\frac{\partial y(x, z)}{\partial z}=1$
$\frac{\partial y(x, z)}{\partial x}=\frac{7+1350 x+28125 x^{2}}{x^{8}}$
$\frac{\partial z(x, y)}{\partial y}=1$
$\frac{\partial z(x, y)}{\partial x}=-\frac{7+1350 x+28125 x^{2}}{x^{8}}$
$y-39776=\left(1+225 x+5625 x^{\wedge} 2-34375 x^{\wedge} 7+x^{\wedge} 7 y\right) / x^{\wedge} 7$
Input:
$y-39776=\frac{1+225 x+5625 x^{2}-34375 x^{7}+x^{7} y}{x^{7}}$

Alternate form assuming $x$ and $y$ are real:
$5401 x^{6}+5625 x+\frac{1}{x}+225=0$

## Alternate forms:

$y-39776=\frac{1}{x^{7}}+\frac{225}{x^{6}}+\frac{5625}{x^{5}}+y-34375$
$y-39776=\frac{225 x(25 x+1)+1}{x^{7}}+y-34375$

## Real solutions:

$x=-1$
$x \approx-0.0349071$
$x \approx-0.00509288$

## Complex solutions:

$$
\begin{aligned}
& x \approx-0.303495-0.958968 i \\
& x \approx-0.303495+0.958968 i \\
& x \approx 0.823495-0.592668 i \\
& x \approx 0.823495+0.592668 i
\end{aligned}
$$

## Implicit derivatives:

$$
\frac{\partial x(y)}{\partial y}=0
$$

For $\mathrm{x}=-1$

$$
y=39776+(1+225 *-1+5625-34375 *-1-y) /-1
$$

## Input:

$y=39776+-\frac{1}{1}(1+225 \times(-1)+5625-34375 \times(-1)-y)$

## Result:

True
$y-39776+(1+225 *-1+5625-34375 *-1-y) /-1=0$

## Input:

$y-39776+-\frac{1}{1}(1+225 \times(-1)+5625-34375 \times(-1)-y)=0$

## Result:

$2 y-79552=0$

## Root plot:



## Alternate form:

$2(y-39776)=0$

## Solution:

$y=39776$
$39776-0=5^{\wedge} 5^{*} 11+75^{\wedge} 2^{*}-1 /(-1)^{\wedge} 5+15^{\wedge} 2^{*}-1+1$

## Input:

$39776-0=5^{5} \times 11+\frac{75^{2} \times(-1)}{(-1)^{5}}+15^{2} \times(-1)+1$

## Result:

True

## Left hand side:

$39776-0=39776$

Right hand side:
$5^{5} \times 11+\frac{75^{2}(-1)}{(-1)^{5}}+15^{2}(-1)+1=39776$

Now, we have that:
$\left(\left(5^{\wedge} 5^{*} 11+75^{\wedge} 2^{*}-1 /(-1)^{\wedge} 5+15^{\wedge} 2^{*}-1+1\right)\right)^{*} 2-4096-2048+64+16+4$
Input:

$$
\left(5^{5} \times 11+\frac{75^{2} \times(-1)}{(-1)^{5}}+15^{2} \times(-1)+1\right) \times 2-4096-2048+64+16+4
$$

## Result:

73492
73492

Thence, we have the following mathematical connection:

$$
\begin{aligned}
& \left(\left(5^{5} \times 11+\frac{75^{2} \times(-1)}{(-1)^{5}}+15^{2} \times(-1)+1\right) \times 2-4096-2048+64+16+4\right)=73492 \Rightarrow \\
& \Rightarrow-3927+2\binom{13 \sqrt{N \exp \left[\int d \hat{\sigma}\left(-\frac{1}{4 u^{2}} \mathbf{P}_{i} D \mathbf{P}_{i}\right)\right]|B p\rangle_{\mathrm{NS}}+}}{\int\left[d \mathbf{X}^{\mu}\right] \exp \left\{\int d \hat{\sigma}\left(-\frac{1}{4 v^{2}} D \mathbf{X}^{\mu} D^{2} \mathbf{X}^{\mu}\right)\right\}\left|\mathbf{X}^{\mu}, \mathbf{X}^{i}=0\right\rangle_{\mathrm{NS}}}= \\
& -3927+2 \sqrt[13]{2.2983717437 \times 10^{59}+2.0823329825883 \times 10^{59}} \\
& =73490.8437525 \ldots \Rightarrow \\
& \Rightarrow\left(A(r) \times \frac{1}{B(r)}\left(-\frac{1}{\phi(r)}\right) \times \frac{1}{e^{\Lambda(r)}}\right) \Rightarrow \\
& \Rightarrow\left(-0.000029211892 \times \frac{1}{0.0003644621}\left(-\frac{1}{0.0005946833}\right) \times \frac{1}{0.00183393}\right)= \\
& =73491.78832548118710549159572042220548025195726563413398700 \ldots \\
& =73491.7883254 \ldots \Rightarrow \\
& \binom{I_{21} \leqslant \int_{-\infty}^{+\infty} \exp \left(-\left(\frac{t}{H}\right)^{2}\right)\left|\sum_{\lambda \leqslant P^{1-}-\varepsilon_{2}} \frac{a(\lambda)}{\sqrt{\lambda}} B(\lambda) \lambda^{-i(T+t)}\right|^{2} d t \ll}{\leqslant H\left\{\left(\frac{4}{\varepsilon_{2} \log T}\right)^{2 r}(\log T)(\log X)^{-2 \beta}+\left(\varepsilon_{2}^{-2 r}(\log T)^{-2 r}+\varepsilon_{2}^{-r} h_{1}^{r}(\log T)^{-r}\right) T^{-\varepsilon_{1}}\right\}} / \\
& /(26 \times 4)^{2}-24=\left(\frac{7.9313976505275 \times 10^{8}}{(26 \times 4)^{2}-24}\right)=73493.30662 \ldots
\end{aligned}
$$

Mathematical connections with the boundary state corresponding to the NSNS-sector of N Dp-branes in the limit of $u \rightarrow \infty$, with the ratio concerning the general asymptotically flat solution of the equations of motion of the p-brane and with the Karatsuba's equation concerning the zeros of a special type of function connected with Dirichlet series.

The above expression, can be calculated also as follows:
$y-z=5^{\wedge} 5^{*} 11+75^{\wedge} 2^{*} 1 / x^{\wedge} 5+15^{\wedge} 2^{*} 1 / x^{\wedge} 6-1 / x^{\wedge} 7$

## Input:

$y-z=5^{5} \times 11+75^{2} \times \frac{1}{x^{5}}+15^{2} \times \frac{1}{x^{6}}-\frac{1}{x^{7}}$

## Result:

$y-z=-\frac{1}{x^{7}}+\frac{225}{x^{6}}+\frac{5625}{x^{5}}+34375$

## Alternate forms:

$z=\frac{1}{x^{7}}-\frac{225}{x^{6}}-\frac{5625}{x^{5}}+y-34375$
$\frac{1}{x^{7}}+y=\frac{225}{x^{6}}+\frac{5625}{x^{5}}+z+34375$
$y-z=\frac{34375 x^{7}+5625 x^{2}+225 x-1}{x^{7}}$

## Solution:

$x \neq 0, \quad z=\frac{x^{7} y-34375 x^{7}-5625 x^{2}-225 x+1}{x^{7}}$

## Integer solutions:

$x=-1, \quad z=y-28976$
$x=1, \quad z=y-40224$

## Implicit derivatives:

$$
\begin{aligned}
& \frac{\partial x(y, z)}{\partial z}=\frac{x^{8}}{-7+1350 x+28125 x^{2}} \\
& \frac{\partial x(y, z)}{\partial y}=\frac{x^{8}}{7-1350 x-28125 x^{2}}
\end{aligned}
$$

$\frac{\partial y(x, z)}{\partial z}=1$
$\frac{\partial y(x, z)}{\partial x}=\frac{7-1350 x-28125 x^{2}}{x^{8}}$
$\frac{\partial z(x, y)}{\partial y}=1$
$\frac{\partial z(x, y)}{\partial x}=\frac{-7+1350 x+28125 x^{2}}{x^{8}}$
$y-40224=\left(1-225 x-5625 x^{\wedge} 2-34375 x^{\wedge} 7+x^{\wedge} 7 y\right) / x^{\wedge} 7$

## Input:

$y-40224=\frac{1-225 x-5625 x^{2}-34375 x^{7}+x^{7} y}{x^{7}}$

Alternate form assuming $x$ and $y$ are real:
$5849 x^{6}+\frac{1}{x}=5625 x+225$

## Alternate forms:

$y-40224=\frac{1}{x^{7}}-\frac{225}{x^{6}}-\frac{5625}{x^{5}}+y-34375$
$y-40224=\frac{1-225 x(25 x+1)}{x^{7}}+y-34375$
Alternate form assuming $x$ and $y$ are positive:
$5849 x^{7}+1=225 x(25 x+1)$

## Real solutions:

$x=1$
$x \approx-0.044037$
$x \approx 0.00403701$

## Complex solutions:

$x \approx-0.794535-0.583357 i$
$x \approx-0.794535+0.583357 i$
$x \approx 0.314535-0.94387 i$
$x \approx 0.314535+0.94387 i$

## Implicit derivatives:

$$
\frac{\partial x(y)}{\partial y}=0
$$

$\mathrm{y}-40224=-34375+(1-225(1+25))+\mathrm{y}$
Input:
$y-40224=-34375+(1-225(1+25))+y$

## Result:

True
$-34375+(1-225(1+25))+y=0$

## Input:

$-34375+(1-225(1+25))+y=0$

## Result:

$y-40224=0$
Root plot:
-40000 -20000

## Solution:

$y=40224$
$40224 * 2-(64 \wedge 2+64 * 4 * 8+64 * 8+64 * 4+8 * 4+16)$

## Input:

$40224 \times 2-\left(64^{2}+64 \times 4 \times 8+64 \times 8+64 \times 4+8 \times 4+16\right)$

## Result:

73488
73488

Now, we have that:


For $x=-1$ and $X=\left(\Psi^{2} / \Psi^{2}\right)$, we obtain:
$0=1-5^{*} \mathrm{X}$
$5 X=1$
$5 X-1=0$
$X=\frac{1}{5}$
$\mathrm{X}=\left(\Psi^{2} / \Psi^{2}\right)=1 / 5$
$\mathrm{v}=\mathrm{y} ; \mathrm{u}=\mathrm{z} ; \quad \mathrm{v}=40224 ; \mathrm{u}=0$
We have that:


$$
-40224-\left(1-5^{*} 1 / 5\right)^{*}\left(\left(11-20^{*} 1 / 5+25^{*}(1 / 5)^{\wedge} 2\right)\right)=-40224
$$

## Input:

$-40224-\left(1-5 \times \frac{1}{5}\right)\left(11-20 \times \frac{1}{5}+25\left(\frac{1}{5}\right)^{2}\right)=-40224$

## Result:

True
$-40224=-40224 ; \quad 40224=40224$

And:

$(((1+0-40224) / 25)))^{\wedge} 1 / 3$

## Input:

$\sqrt[3]{\frac{1}{25}(1+0-40224)}$

## Result:

$$
\frac{\sqrt[3]{-40223}}{5^{2 / 3}}
$$

## Decimal approximation:

5.85888294238292786529883089587725142144433920849672873689... + 10.1478829318058701834705486960572299586888687249430612018... i

## Polar coordinates:

```
r\approx11.7178 (radius), }0=6\mp@subsup{0}{}{\circ}\mathrm{ (angle)
```

11.7178 result very near to the black hole entropy 11.8458

## Alternate forms:

$\sqrt[3]{-201115}$
5
root of $25 x^{3}+40223$ near $x=5.85888+10.1479 i$
$\frac{\sqrt[3]{40223}}{2 \times 5^{2 / 3}}+\frac{i \sqrt{3} \sqrt[3]{40223}}{2 \times 5^{2 / 3}}$

$$
1 /(((1+0-40224) / 25)))^{\wedge} 1 / 3
$$

## Input:

1
$\sqrt[3]{\frac{1}{25}(1+0-40224)}$

## Result:

$-\frac{(-5)^{2 / 3}}{\sqrt[3]{40223}}$

## Decimal approximation:

0.04267025002181044979262887140046482427577369945595943074... -
$0.07390704100944269351090280626296223509316942160101431505 \ldots i$

## Polar coordinates:

$r \approx 0.0853405$ (radius), $\quad \theta=-60^{\circ}$ (angle)
0.0853405

Alternate forms:
$-\frac{(-201115)^{2 / 3}}{40223}$
$\left(\left((1 /(((1+0-40224) / 25)))^{\wedge} 1 / 3\right)\right)^{\wedge} 1 / 64$

## Input:

$\sqrt[64]{\sqrt[3]{\frac{1}{25}(1+0-40224)}}$

## Result:

$\sqrt[192]{-\frac{1}{40223}} \sqrt[96]{5}$

## Decimal approximation:

$0.9621464023344880154486574313176803411252001447397312689 \ldots+$
$0.01574448881057173225038021685401795511252820425883944368 \ldots i$

## Polar coordinates:

$$
r \approx 0.962275 \text { (radius), } \quad \theta \approx 0.9375^{\circ} \text { (angle) }
$$

0.962275 result very near to the value of the following Rogers-Ramanujan continued fraction:

$$
\frac{\mathrm{e}^{-\frac{\pi}{5}}}{\sqrt{(\varphi-1) \sqrt{5}}-\varphi+1}=1-\frac{\mathrm{e}^{-\pi}}{1+\frac{\mathrm{e}^{-2 \pi}}{1+\frac{\mathrm{e}^{-3 \pi}}{1+\frac{\mathrm{e}^{-4 \pi}}{1+\ldots}}}} \approx 0.9568666373
$$

and to the spectral index $\mathrm{n}_{\mathrm{s}}$ and to the mesonic Regge slope (see Appendix)

## Alternate forms:

$\frac{40223^{191 / 192} \sqrt[192]{-25}}{40223}$
$\frac{\sqrt[96]{5} \cos \left(\frac{\pi}{192}\right)}{\sqrt[i 92]{40223}}+\frac{i \sqrt[96]{5} \sin \left(\frac{\pi}{192}\right)}{\sqrt[192]{40223}}$

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For $\mathrm{x}=0.00403701$, we obtain:
$57+14 * 1 /(0.00403701)^{\wedge} 7+1 /(0.00403701)^{\wedge} 8-1$
Input interpretation:
$57+14 \times \frac{1}{0.00403701^{7}}+\frac{1}{0.00403701^{8}}-1$

## Result:

$1.4976087076988711276669815936609084297451154706750441 \ldots \times 10^{19}$
$1.4976087 \ldots * 10^{19}$
$289+126^{*} 1 /(0.00403701)^{\wedge} 7+19^{*} 1 /(0.00403701)^{\wedge} 8+1 /(0.00403701)^{\wedge} 9-1$

## Input interpretation:

$289+126 \times \frac{1}{0.00403701^{7}}+19 \times \frac{1}{0.00403701^{8}}+\frac{1}{0.00403701^{9}}-1$

## Result:

$3.7877827920479735372937110238941005416858226535497303 \ldots \times 10^{21}$
$3.787782792 \ldots * 10^{21}$
$3.78778279204797353 \times 10^{\wedge} 21 / 1.497608707698871 \times 10^{\wedge} 19$

## Input interpretation:

$\frac{3.78778279204797353 \times 10^{21}}{1.497608707698871 \times 10^{19}}$

## Result:

252.9220598528728105936171790617321567508409163378235206521
252.922059...
$\left(3.78778279204797353 \times 10^{\wedge} 21 / 1.497608707698871 \times 10^{\wedge} 19\right)^{\wedge} 1 / 11$
Input interpretation:
$\sqrt[1]{\frac{3.78778279204797353 \times 10^{21}}{1.497608707698871 \times 10^{19}}}$

## Result:

1.653687095030971...
1.653687.... is very near to the 14th root of the following Ramanujan's class invariant $Q=\left(G_{505} / G_{101 / 5}\right)^{3}=1164,2696$ i.e. 1,65578...
$1 /\left(\left(\left(3.78778279204797353 \times 10^{\wedge} 21 / 1.497608707698871 \times 10^{\wedge} 19\right)\right)\right)^{\wedge} 1 / 512$

## Input interpretation:



## Result:

0.989251384111376078...
$0.98925138 \ldots$ result very near to the dilaton value $\mathbf{0 . 9 8 9 1 1 7 3 5 2 2 4 3}=\boldsymbol{\phi}$

$57+2 * 7 \wedge 3 *(0.00403701)^{\wedge} 7+7 \wedge 4 *(0.00403701)^{\wedge} 8-1$

## Input interpretation:

$57+2 \times 7^{3} \times 0.00403701^{7}+7^{4} \times 0.00403701^{8}-1$

## Result:

56.00000000000001215727730954987175619516546307399143728263.

56
$289+18^{* 7 \wedge} 3^{*}(0.00403701)^{\wedge} 7+19 * 7 \wedge 4 *(0.00403701)^{\wedge} 8+7 \wedge 6 *(0.00403701)^{\wedge} 9$

## Input interpretation:

```
289+18\times7}\mp@subsup{7}{}{3}\times0.0040370\mp@subsup{1}{}{7}+19\times\mp@subsup{7}{}{4}\times0.0040370\mp@subsup{1}{}{8}+\mp@subsup{7}{}{6}\times0.0040370\mp@subsup{1}{}{9
```


## Result:

$289.0000000000001111428357713006231449530352660377074291756 \ldots$
289
((()1/2)((289+18*7^3*(0.00403701)^7+19*7^4*(0.00403701)^8+7^6*(0.00403701)^
$\left.\left.\left.\left.9))) /\left(\left(\left(57+2^{*} 7 \wedge 3 *(0.00403701)^{\wedge} 7+7 \wedge 4 *(0.00403701)^{\wedge} 8-1\right)\right)\right)\right)\right)\right)\right)^{\wedge} 1 / 2$

## Input interpretation:

$$
\sqrt{\frac{1}{2} \times \frac{289+18 \times 7^{3} \times 0.00403701^{7}+19 \times 7^{4} \times 0.00403701^{8}+7^{6} \times 0.00403701^{9}}{57+2 \times 7^{3} \times 0.00403701^{7}+7^{4} \times 0.00403701^{8}-1}}
$$

## Result:

1.60634901028921585018...
1.606349.... result very near to the elementary charge

In conclusion, we have that, from the multiplication of the two previous results, we obtain:
$1 / 10^{\wedge} 4\left(\left(\left(57+2 * 7 \wedge 3 *(0.00403701)^{\wedge} 7+7^{\wedge} 4^{*}(0.00403701)^{\wedge} 8-1\right)\right)\right)^{*}((($ $\left.\left.\left.289+18^{*} 7^{\wedge} 3^{*}(0.00403701)^{\wedge} 7+19^{*} 7^{\wedge} 4^{*}(0.00403701)^{\wedge} 8+7 \wedge 6^{*}(0.00403701)^{\wedge} 9\right)\right)\right)$
where $f=1 / 10^{4}$

## Input interpretation:

```
\(\frac{1}{10^{4}}\left(57+2 \times 7^{3} \times 0.00403701^{7}+7^{4} \times 0.00403701^{8}-1\right)\)
    \(\left(289+18 \times 7^{3} \times 0.00403701^{7}+19 \times 7^{4} \times 0.00403701^{8}+7^{6} \times 0.00403701^{9}\right)\)
```


## Result:

1.618400000000000973745194565274918485204823518738061318220 .
1.6184...

This result is a very good approximation to the value of the golden ratio 1,618033988749...
$\left[1 /\left(\left(\left((1 / 2)\left(\left(289+18^{*} 7 \wedge 3 *(0.00403701) \wedge 7+19 * 7 \wedge 4^{*}(0.00403701) \wedge 8+7 \wedge 6 *(0.0040370\right.\right.\right.\right.\right.\right.$ $\left.\left.\left.\left.\left.\left.\left.\left.1)^{\wedge} 9\right)\right)\right) /\left(\left(\left(57+2 * 7 \wedge 3 *(0.00403701)^{\wedge} 7+7 \wedge 4 *(0.00403701)^{\wedge} 8-1\right)\right)\right)\right)\right)\right)\right)^{\wedge} 1 / 2\right]^{\wedge} 1 / 32$

## Input interpretation:



## Result:

$0.9852977766887614314869 \ldots$
$0.985297776 \ldots$ result very near to the dilaton value $\mathbf{0 . 9 8 9 1 1 7 3 5 2 2 4 3}=\boldsymbol{\phi}$


## $3 u=7\left(v^{3}+5 \omega^{2}+7 v\right)+\left(v^{2}+7 v+7\right) \sqrt{4 v^{3}+21 v^{2}+2 v v}$

For $\mathrm{u}=\mathrm{v}=1$, we obtain:
$(((7(1+5+7)+(1+7+7) * \operatorname{sqrt}(4+21+28))))-2$

## Input:

$$
(7(1+5+7)+(1+7+7) \sqrt{4+21+28})-2
$$

## Result:

$89+15 \sqrt{53}$

## Decimal approximation:

198.2016483392077740664595373729054919066650452386471615756...
198.201648...

Minimal polynomial:
$x^{2}-178 x-4004$

Note that:
$289-56=233 ; \quad 198.201648-56=142.201648 ; \quad 233 / 142.201648=$
$=1.63851828215 \approx \zeta(2)=\frac{\pi^{2}}{6}=1.644934 \ldots$
We note also that:
$((1 /(1.63851828215)))^{\wedge} 1 / 512$

## Input interpretation:

$\sqrt[512]{\frac{1}{1.63851828215}}$

## Result:

0.999036026743384
$0.999036 \ldots$ result practically equal to the value of the following Rogers-Ramanujan continued fraction:
$\frac{\mathrm{e}^{-\frac{\pi}{\sqrt{5}}}}{\frac{\sqrt{5}}{1+\sqrt[5]{\sqrt{\varphi^{5 \sqrt[4]{5^{3}}}-1}}-\varphi+1}=1-\frac{\mathrm{e}^{-\pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-2 \pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-3 \pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-4 \pi \sqrt{5}}}{1+\ldots}}}} \approx 0.9991104684 .10 .}$

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$$
\begin{aligned}
\text { vi: \&f } \alpha & =p \cdot\left(\frac{2+p}{1+7 p}\right)^{3} \\
1-\alpha & =(1+p)\left(\frac{1-p}{1+4 p}\right)^{3} \text { \& } \quad 1-\beta=(1+p)^{3} \cdot \frac{1-p}{1+3 p}
\end{aligned}
$$

For $\mathrm{p}=2 ; \alpha=2((2+2) /(1+2 * 2))^{\wedge} 3=1.024 \quad \beta=2^{\wedge} 3^{*}(2+2) /(1+2 * 2)=6.4$
$1-\alpha=(1+2)((1-2) /(1+2 * 2))^{\wedge} 3=-0.024 \quad 1-\beta=(1+2)^{\wedge} 3^{*}((1-2) /(1+2 * 2))=-5.4$

$1-\left(\left(\left(6.4^{\wedge} 3(-0.024)^{\wedge} 3\right) /(1.024(1-6.4))\right)\right)^{\wedge} 1 / 8$

## Input:

$1-\sqrt[8]{\frac{6.4^{3}(-0.024)^{3}}{1.024(1-6.4)}}$

## Result:

0.6
0.6
$\left.\operatorname{sqrt}\left(\left(\left(\left(\left(1+\operatorname{sqrt}(1.024 * 6.4)+\operatorname{sqrt}\left(-0.024^{*}-5.4\right)\right)\right) / 2\right)\right)\right)\right)$

## Input:

$\sqrt{\frac{1}{2}(1+\sqrt{1.024 \times 6.4}+\sqrt{-0.024 \times(-5.4)})}$

## Result:

1.4
1.4

We have that:
(()(()(1-(((6.4^3)(-0.024)^3)/(1.024(1-1)
$\left.\left.\left.6.4))))^{\wedge} 1 / 8\right)\right)\right)^{*}\left(\left(\left(\operatorname{sqrt}\left(\left(\left(\left(\left(1+\operatorname{sqrt}\left(1.024^{*} 6.4\right)+\operatorname{sqrt}\left(-0.024^{*}-5.4\right)\right)\right) / 2\right)\right)\right)\right)\right)\right.$

## Input:

$$
\sqrt[16]{\left(1-\sqrt[8]{\frac{6.4^{3}(-0.024)^{3}}{1.024(1-6.4)}}\right) \sqrt{\frac{1}{2}(1+\sqrt{1.024 \times 6.4}+\sqrt{-0.024 \times(-5.4)})}}
$$

## Result:

0.9891621...
$0.9891621 \ldots$. result practically equal to the dilaton value $\mathbf{0 . 9 8 9 1 1 7 3 5 2 2 4 3}=\boldsymbol{\phi}$


For:
$\alpha=2((2+2) /(1+2 * 2))^{\wedge} 3=1.024 \quad \beta=2^{\wedge} 3 *(2+2) /(1+2 * 2)=6.4$
$1-\alpha=(1+2)((1-2) /(1+2 * 2))^{\wedge} 3=-0.024 \quad 1-\beta=(1+2)^{\wedge} 3 *((1-2) /(1+2 * 2))=-5.4$
we obtain:
$2 *\left(\left(\left(\left(1.024 * 6.4^{*}(-0.024) *(-5.4)\right)\right)\right)^{\wedge} 1 / 8\right.$

## Input:

$2 \sqrt[8]{1.024 \times 6.4 \times(-0.024) \times(-5.4)}$

## Result:

1.95959...
$1.95959 \ldots$ result practically near to the mean value $1.962 * 10^{19}$ of DM particle
$1 / 2 * 2\left(\left(\left(\left(1.024^{*} 6.4^{*}(-0.024) *(-5.4)\right)\right)\right)^{\wedge} 1 / 8\right.$

## Input:

$\frac{1}{2} \times 2 \sqrt[8]{1.024 \times 6.4 \times(-0.024) \times(-5.4)}$

## Result:

0.979796...
$0.979796 \ldots$ result near to the value of the following Rogers-Ramanujan continued fraction:
$\frac{\mathrm{e}^{-\frac{\pi}{\sqrt{5}}}}{\sqrt{5}}-\varphi+1 \quad 1-\frac{\mathrm{e}^{-\pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-2 \pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-3 \pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-4 \pi \sqrt{5}}}{1+\ldots}}}} \approx 0.9991104684$
and near to the dilaton value $\mathbf{0 . 9 8 9 1 1 7 3 5 2 2 4 3 = \boldsymbol { \phi }}$
$2 *((((-0.024) *(-5.4))))^{\wedge} 1 / 8$

## Input:

$2 \sqrt[8]{-0.024 \times(-5.4)}$

## Result:

1.549193.
1.549193...

And, inverting the formula, we obtain:
$1 /\left(\left(\left(2 *((((-0.024) *(-5.4))))^{\wedge} 1 / 8\right)\right)\right)$

## Input:

$\frac{1}{2 \sqrt[8]{-0.024 \times(-5.4)}}$

## Result:

0.6454972...
0.6454972...

And:
$\left(\left(\left(1 /\left(\left(\left(2^{*}((((-0.024) *(-5.4)))) \wedge 1 / 8\right)\right)\right)\right)\right)\right)^{\wedge}(1 /(24 / 2))$

## Input:

$\sqrt[24]{\frac{1}{2 \sqrt[8]{-0.024 \times(-5.4)}}}$

## Result:

0.96417944 ..
$0.96417944 \ldots$. result very near to the value of the following Rogers-Ramanujan continued fraction:

$$
\frac{\mathrm{e}^{-\frac{\pi}{5}}}{\sqrt{(\varphi-1) \sqrt{5}}-\varphi+1}=1-\frac{\mathrm{e}^{-\pi}}{1+\frac{\mathrm{e}^{-2 \pi}}{1+\frac{\mathrm{e}^{-3 \pi}}{1+\frac{\mathrm{e}^{-4 \pi}}{1+\ldots}}}} \approx 0.9568666373
$$

to the spectral index $\mathrm{n}_{\mathrm{s}}$ and to the mesonic Regge slope (see Appendix)
$2^{*}((((1.024) *(6.4))))^{\wedge} 1 / 8$

## Input:

$2 \sqrt[8]{1.024 \times 6.4}$

## Result:

2.529822...
2.529822... result very near to the inflaton (dilaton) mass 2.53
$\left.4 * \operatorname{sqrt}\left(\left(\left(\left(1 / 2\left(\left(\left(1+\operatorname{sqrt}\left(1.024^{*} 6.4\right)+\operatorname{sqrt}((-0.024)(-5.4))\right)\right)\right)\right)\right)\right)\right)\right)$

## Input:

$4 \sqrt{\frac{1}{2}(1+\sqrt{1.024 \times 6.4}+\sqrt{-0.024 \times(-5.4)})}$

## Result:

5.6
5.6

From the below four results obtained:
5.6; 2.529822; 1.549193; 1.95959

We have the following expressions:
$(5.6-2.529822+1.549193+1.95959)$

## Input interpretation:

$5.6-2.529822+1.549193+1.95959$

## Result:

6.578961
6.578961 result very near to the value of reduced Planck constant 6.58 without exponent

And:
$(5.6-2.529822+1.549193+1.95959) * 1 / 4$

## Input interpretation:

$(5.6-2.529822+1.549193+1.95959) \times \frac{1}{4}$

## Result:

1.64474025
$1.64474025 \approx \zeta(2)=\frac{\pi^{2}}{6}=1.644934 \ldots$

Multiplying the four results obtained, we have:
$(5.6 * 2.529822 * 1.549193 * 1.95959)$

## Input interpretation:

$5.6 \times 2.529822 \times 1.549193 \times 1.95959$

## Result:

43.007949046201244784
43.007949...
$(5.6 * 2.529822 * 1.549193 * 1.95959) * 1597+((4181+610+13))$
Where $1597,4181,610$ and 13 are Fibonacci numbers

## Input interpretation:

$(5.6 \times 2.529822 \times 1.549193 \times 1.95959) \times 1597+(4181+610+13)$

## Result:

73487.694626783387920048
73487.694626...

We note that, from the following formula concerning the '5th order' mock theta function psi_1(q). (OEIS - sequence A053261)
$\operatorname{sqrt}($ golden ratio $) * \exp \left(\mathrm{Pi}^{*} \operatorname{sqrt}(\mathrm{n} / 15)\right) /\left(2 * 5^{\wedge}(1 / 4) * \operatorname{sqrt}(\mathrm{n})\right)$
we obtain, for $\mathrm{n}=69 \quad[69=64+5=47+18+4$ (Lucas number) $]$
$\operatorname{sqrt}($ golden ratio $) * \exp \left(\mathrm{Pi}^{*} \operatorname{sqrt}(69 / 15)\right) /\left(2 * 5^{\wedge}(1 / 4) * \operatorname{sqrt}(69)\right)$

## Input:

$\sqrt{\phi} \times \frac{\exp \left(\pi \sqrt{\frac{60}{15}}\right)}{2 \sqrt[4]{5} \sqrt{69}}$

## Exact result:

$\frac{e^{\sqrt{23 / 5} \pi} \sqrt{\frac{\phi}{69}}}{2 \sqrt[4]{5}}$
Decimal approximation:
$43.20739184232318277413818553313812361467380250463695690932 \ldots$

## Property:

$\frac{e^{\sqrt{23 / 5} \pi} \sqrt{\frac{\phi}{69}}}{2 \sqrt[4]{5}}$ is a transcendental number

## Alternate forms:

$$
\begin{aligned}
& \frac{1}{2} \sqrt{\frac{1}{690}(5+\sqrt{5})} e^{\sqrt{23 / 5} \pi} \\
& \frac{\sqrt{\frac{1}{138}(1+\sqrt{5})} e^{\sqrt{23 / 5} \pi}}{2 \sqrt[4]{5}}
\end{aligned}
$$

## Series representations:

$\frac{\sqrt{\phi} \exp \left(\pi \sqrt{\frac{69}{15}}\right)}{2 \sqrt[4]{5} \sqrt{69}}=\frac{\exp \left(\pi \sqrt{z_{0}} \sum_{k=0}^{\infty} \frac{(-1)^{k}\left(-\frac{1}{2}\right)_{k}\left(\frac{23}{5}-z_{0}\right)^{k} z_{0}^{-k}}{k!}\right) \sum_{k=0}^{\infty} \frac{(-1)^{k}\left(-\frac{1}{2}\right)_{k}\left(\phi-z_{0}\right)^{k} z_{0}^{-k}}{k!}}{2 \sqrt[4]{5} \sum_{k=0}^{\infty} \frac{(-1)^{k}\left(-\frac{1}{2}\right)_{k}\left(60-z_{0} k^{k} z_{0}^{-k}\right.}{k!}}$
for $\operatorname{not}\left(\left(z_{0} \in \mathbb{R}\right.\right.$ and $\left.\left.-\infty<z_{0} \leq 0\right)\right)$

$$
\begin{aligned}
& \frac{\sqrt{\phi} \exp \left(\pi \sqrt{\frac{69}{15}}\right)}{2 \sqrt[4]{5} \sqrt{69}}= \\
& \left(\exp \left(i \pi\left[\frac{\arg (\phi-x)}{2 \pi}\right]\right) \exp \left(\pi \exp \left(i \pi \left\lvert\, \frac{\arg \left(\frac{23}{5}-x\right)}{2 \pi}\right.\right)\right] \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^{k}\left(\frac{23}{5}-x\right)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}\right) \\
& \left.\sum_{k=0}^{\infty} \frac{(-1)^{k}(\phi-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}\right) / \\
& \left(2 \sqrt[4]{5} \exp \left(i \pi\left[\frac{\arg (69-x)}{2 \pi}\right]\right) \sum_{k=0}^{\infty} \frac{(-1)^{k}(69-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}\right) \text { for }(x \in \mathbb{R} \text { and } x<0) \\
& \frac{\sqrt{\phi} \exp \left(\pi \sqrt{\frac{69}{15}}\right)}{2 \sqrt[4]{5} \sqrt{69}}= \\
& \left(\exp \left(\pi\left(\frac{1}{z_{0}}\right)^{1 / 2\left\lfloor\arg \left(\frac{23}{5}-z_{0}\right) /(2 \pi)\right\rfloor} z_{0}^{1 / 2\left(1+\left\lfloor\arg \left(\frac{23}{5}-z_{0}\right) /(2 \pi)\right]\right)} \sum_{k=0}^{\infty} \frac{(-1)^{k}\left(-\frac{1}{2}\right)_{k}\left(\frac{23}{5}-z_{0}\right)^{k} z_{0}^{k}}{k!}\right)\right. \\
& \left(\frac{1}{z_{0}}\right)^{-1 / 2\left\lfloor\arg \left(69-z_{0}\right) /(2 \pi)\right\rfloor+1 / 2\left\lfloor\arg \left(\phi-z_{0}\right) /(2 \pi)\right\rfloor} z_{0}^{-1 / 2\left\lfloor\arg \left(69-z_{0}\right) /(2 \pi)\right\rfloor+1 / 2\left\lfloor\arg \left(\phi-z_{0}\right) /(2 \pi)\right\rfloor} \\
& \left.\sum_{k=0}^{\infty} \frac{(-1)^{k}\left(-\frac{1}{2}\right)_{k}\left(\phi-z_{0}\right)^{k} z_{0}^{-k}}{k!}\right) /\left(2 \sqrt[4]{5} \sum_{k=0}^{\infty} \frac{(-1)^{k}\left(-\frac{1}{2}\right)_{k}\left(69-z_{0}\right)^{k} z_{0}^{k}}{k!}\right)
\end{aligned}
$$

$\left(\left(\left(\operatorname{sqrt}(\right.\right.\right.$ golden ratio $) * \exp \left(\mathrm{Pi}^{*} \operatorname{sqrt}(69 / 15)\right) /$
$\left.\left.\left.\left(2^{*} 5^{\wedge}(1 / 4) * \operatorname{sqrt}(69)\right)\right)\right)\right) * 1597+(((64 * 4+8) *(13+4)))$
Where 1597, 8 and 13 are Fibonacci numbers

## Input:

$\left(\sqrt{\phi} \times \frac{\exp \left(\pi \sqrt{\frac{69}{15}}\right)}{2 \sqrt[4]{5} \sqrt{69}}\right) \times 1597+(64 \times 4+8)(13+4)$

## Exact result:

$\frac{1597 e^{\sqrt{23 / 5} \pi} \sqrt{\frac{\phi}{69}}}{2 \sqrt[4]{5}}+4488$

## Decimal approximation:

73490.20477219012289029868229642158341263406259990522018419...
73490.2047721...

## Property:

$4488+\frac{1597 e^{\sqrt{23 / 5} \pi} \sqrt{\frac{\phi}{69}}}{2 \sqrt[4]{5}}$ is a transcendental number

## Alternate forms:

$4488+\frac{1597}{2} \sqrt{\frac{1}{690}(5+\sqrt{5})} e^{\sqrt{23 / 5} \pi}$
$4488+\frac{1597 \sqrt{\frac{1}{138}(1+\sqrt{5})} e^{\sqrt{23 / 5} \pi}}{2 \sqrt[4]{5}}$
$\frac{6193440+1597 \times 5^{3 / 4} \sqrt{138(1+\sqrt{5})} e^{\sqrt{23 / 5} \pi}}{1380}$

## Series representations:

$$
\begin{aligned}
& \frac{1597 \sqrt{\phi} \exp \left(\pi \sqrt{\frac{69}{15}}\right)}{2 \sqrt[4]{5} \sqrt{69}}+(64 \times 4+8)(13+4)= \\
& \left(44880 \sum_{k=0}^{\infty} \frac{(-1)^{k}\left(-\frac{1}{2}\right)_{k}\left(69-z_{0}\right)^{k} z_{0}^{-k}}{k!}+1597 \times 5^{3 / 4}\right. \\
& \left.\quad \exp \left(\pi \sqrt{z_{0}} \sum_{k=0}^{\infty} \frac{(-1)^{k}\left(-\frac{1}{2}\right)_{k}\left(\frac{23}{5}-z_{0}\right)^{k} z_{0}^{-k}}{k!}\right) \sum_{k=0}^{\infty} \frac{(-1)^{k}\left(-\frac{1}{2}\right)_{k}\left(\phi-z_{0}\right)^{k} z_{0}^{-k}}{k!}\right) / \\
& \left(10 \sum_{k=0}^{\infty} \frac{(-1)^{k}\left(-\frac{1}{2}\right)_{k}\left(69-z_{0}\right)^{k} z_{0}^{-k}}{k!}\right) \text { for not }\left(\left(z_{0} \in \mathbb{R} \text { and }-\infty<z_{0} \leq 0\right)\right)
\end{aligned}
$$

$$
\begin{aligned}
& \frac{1597 \sqrt{\phi} \exp \left(\pi \sqrt{\frac{69}{15}}\right)}{2 \sqrt[4]{5} \sqrt{69}}+(64 \times 4+8)(13+4)= \\
& \left(44880 \exp \left(i \pi\left\lfloor\frac{\arg (69-x)}{2 \pi}\right]\right) \sum_{k=0}^{\infty} \frac{(-1)^{k}(69-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}+\right. \\
& 1597 \times 5^{3 / 4} \exp \left(i \pi\left\lfloor\frac{\arg (\phi-x)}{2 \pi}\right\rfloor\right) \exp \left(\pi \exp \left(i \pi\left[\frac{\arg \left(\frac{23}{5}-x\right)}{2 \pi}\right]\right) \sqrt{x}\right. \\
& \left.\sum_{k=0}^{\infty} \frac{(-1)^{k}\left(\frac{23}{5}-x\right)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!} \sum_{k=0}^{\infty} \frac{(-1)^{k}(\phi-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}\right) / \\
& \left(10 \exp \left(i \pi\left[\frac{\arg (69-x)}{2 \pi}\right]\right) \sum_{k=0}^{\infty} \frac{(-1)^{k}(69-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}\right) \text { for }(x \in \mathbb{R} \text { and } x<0) \\
& \frac{1597 \sqrt{\phi} \exp \left(\pi \sqrt{\frac{69}{15}}\right)}{2 \sqrt[4]{5} \sqrt{69}}+(64 \times 4+8)(13+4)= \\
& \left(\left(\frac{1}{z_{0}}\right)^{-1 / 2\left\lfloor\arg \left(60-z_{0}\right) /(2 \pi)\right\rfloor} z_{0}^{-1 / 2\left\lfloor\arg \left(60-z_{0}\right) /(2 \pi)\right\rfloor}\right. \\
& \left(44880\left(\frac{1}{z_{0}}\right)^{1 / 2\left\lfloor\operatorname{agg}\left(60-z_{0}\right) /(2 \pi)\right\rfloor} z_{0}^{1 / 2\left\lfloor\arg \left(69-z_{0}\right) /(2 \pi)\right\rfloor} \sum_{k=0}^{\infty} \frac{(-1)^{k}\left(-\frac{1}{2}\right)_{k}\left(69-z_{0}\right)^{k} z_{0}^{-k}}{k!}+\right. \\
& 1597 \times 5^{3 / 4} \exp \left(\pi\left(\frac{1}{z_{0}}\right)^{1 / 2\left\lfloor\left.\arg \left(\frac{23}{5}-z_{0}\right) /(2 \pi) \right\rvert\,\right.} z_{0}^{1 / 2\left(1+\left\lfloor\left.\arg \left(\frac{23}{5}-z_{0}\right) /(2 \pi) \right\rvert\,\right)\right.}\right. \\
& \left.\sum_{k=0}^{\infty} \frac{(-1)^{k}\left(-\frac{1}{2}\right)_{k}\left(\frac{23}{5}-z_{0}\right)^{k} z_{0}^{-k}}{k!}\right)\left(\frac{1}{z_{0}}\right)^{1 / 2\left\lfloor\arg \left(\phi-z_{0}\right) /(2 \pi)\right\rfloor} z_{0}^{\left.1 / 2 \arg \left(\phi-z_{0}\right) /(2 \pi)\right\rfloor} \\
& \left.\left.\sum_{k=0}^{\infty} \frac{(-1)^{k}\left(-\frac{1}{2}\right)_{k}\left(\phi-z_{0}\right)^{k} z_{0}^{-k}}{k!}\right)\right) /\left(10 \sum_{k=0}^{\infty} \frac{(-1)^{k}\left(-\frac{1}{2}\right)_{k}\left(69-z_{0}\right)^{k} z_{0}^{-k}}{k!}\right)
\end{aligned}
$$

Thence, we have the following mathematical connection:

$$
((5.6 \times 2.529822 \times 1.549193 \times 1.95959) \times 1597+(4181+610+13))=73487.694626 \Rightarrow
$$

$$
\begin{aligned}
& \Rightarrow\left(\frac{1597 e^{\sqrt{23 / 5} \pi} \sqrt{\frac{\phi}{69}}}{2 \sqrt[4]{5}}+4488\right)=73490.2047 \Rightarrow \\
& \Rightarrow-3927+2\binom{13 \sqrt{N \exp \left[\int d \hat{\sigma}\left(-\frac{1}{4 u^{2}} \mathbf{P}_{i} D \mathbf{P}_{i}\right)\right]|B p\rangle_{\mathrm{NS}}+}}{\int\left[d \mathbf{X}^{\mu}\right] \exp \left\{\int d \hat{\sigma}\left(-\frac{1}{4 v^{2}} D \mathbf{X}^{\mu} D^{2} \mathbf{X}^{\mu}\right)\right\}\left|\mathbf{X}^{\mu}, \mathbf{X}^{i}=0\right\rangle_{\mathrm{NS}}}= \\
& -3927+2 \sqrt[13]{2.2983717437 \times 10^{59}+2.0823329825883 \times 10^{59}} \\
& =73490.8437525 \ldots \Rightarrow \\
& \Rightarrow\left(A(r) \times \frac{1}{B(r)}\left(-\frac{1}{\phi(r)}\right) \times \frac{1}{e^{\Lambda(r)}}\right) \Rightarrow \\
& \Rightarrow\left(-0.000029211892 \times \frac{1}{0.0003644621}\left(-\frac{1}{0.0005946833}\right) \times \frac{1}{0.00183393}\right)= \\
& =73491.78832548118710549159572042220548025195726563413398700 \ldots \\
& =73491.7883254 \ldots \Rightarrow
\end{aligned}
$$

$$
\begin{gathered}
\binom{I_{21} \leqslant \int_{-\infty}^{+\infty} \exp \left(-\left(\frac{t}{H}\right)^{2}\right)\left|\sum_{\lambda \leqslant P^{1-\varepsilon_{2}}} \frac{a(\lambda)}{\sqrt{\lambda}} B(\lambda) \lambda^{-i\left(T^{r}+t\right)}\right|^{2} d t \leqslant}{\leftrightarrow H\left\{\left(\frac{4}{\varepsilon_{2} \log T}\right)^{2 r}(\log T)(\log X)^{-2 \beta}+\left(\varepsilon_{2}^{-2 r}(\log T)^{-2 r}+\varepsilon_{2}^{-r} h_{1}^{r}(\log T)^{-r}\right) T^{-\varepsilon_{1}}\right\}} / \\
/(26 \times 4)^{2}-24=\left(\frac{7.9313976505275 \times 10^{8}}{(26 \times 4)^{2}-24}\right)=73493.30662 \ldots
\end{gathered}
$$

Mathematical connections with the boundary state corresponding to the NSNS-sector of N Dp-branes in the limit of $u \rightarrow \infty$, with the ratio concerning the general
asymptotically flat solution of the equations of motion of the p-brane and with the Karatsuba's equation concerning the zeros of a special type of function connected with Dirichlet series.

Now, we have that:
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for
$\alpha=2((2+2) /(1+2 * 2))^{\wedge} 3=1.024 \quad \beta=2^{\wedge} 3 *(2+2) /(1+2 * 2)=6.4$
$1-\alpha=(1+2)((1-2) /(1+2 * 2))^{\wedge} 3=-0.024 \quad 1-\beta=(1+2)^{\wedge} 3 *((1-2) /(1+2 * 2))=-5.4$
we obtain:
$1-2^{\wedge}(1 / 3)^{*}\left(\left(\left(\left(\left(6.4^{\wedge} 5(-5.4)^{\wedge} 5\right)\right) /((1.024(-0.024)))\right)\right)\right)^{\wedge} 1 / 24-4^{\wedge}(1 / 3)^{*}\left(\left(\left(\left(\left(6.4^{\wedge} 5(-\right.\right.\right.\right.\right.$
$\left.\left.\left.\left.\left.5.4)^{\wedge} 5\right)\right) /((1.024(-0.024)))\right)\right)\right)^{\wedge} 1 / 12$

## Input:

$1-\sqrt[3]{2} \sqrt[24]{\frac{6.4^{5}(-5.4)^{5}}{1.024 \times(-0.024)}}-\sqrt[3]{4} \sqrt[12]{\frac{6.4^{5}(-5.4)^{5}}{1.024 \times(-0.024)}}$

## Result:

-11.5355082897977464153536028054008545716237240205812907446...
$-11.5355082897977464153536 / \operatorname{sqrt}\left[1-3^{*}\left(\left(\left(16^{*} 1.024^{*} 6.4^{*}(-0.024)(-\right.\right.\right.\right.$
$\left.\left.5.4)))^{\wedge} 1 / 6\right)+\left(\left(\left(16^{*} 1.024^{*} 6.4^{*}(-0.024)(-5.4)\right)\right)^{\wedge} 1 / 3\right)\right]$

## Input interpretation:

11.5355082897977464153536
$\sqrt{1-3 \sqrt[6]{16 \times 1.024 \times 6.4 \times(-0.024) \times(-5.4)}+\sqrt[3]{16 \times 1.024 \times 6.4 \times(-0.024) \times(-5.4)}}$

## Result:

10.3260...

Polar coordinates:
$r=10.326$ (radius), $\theta=90^{\circ}$ (angle)
10.326

Now:

10.326*((((1+sqrt(1.024*6.4)+sqrt(-0.024*-5.4))))))/2

## Input interpretation:

$10.326\left(\frac{1}{2}(1+\sqrt{1.024 \times 6.4}+\sqrt{-0.024 \times(-5.4)})\right)$

## Result:

20.23896
20.23896

5/10.326*((((1+sqrt(1.024*6.4)+sqrt(-0.024*-5.4)))))/2
Input interpretation:
$\frac{5}{10.326}\left(\frac{1}{2}(1+\sqrt{1.024 \times 6.4}+\sqrt{-0.024 \times(-5.4)})\right)$

## Result:

$0.949060623668409839240751501065272128607398799147782297114 \ldots$

## Repeating decimal:

$0.949060623668409839240751501065272128607398799147782297114 \ldots$
(period 430)
$0.9490606236684 \ldots$... result very near to the value of the following RogersRamanujan continued fraction:

$$
\frac{\mathrm{e}^{-\frac{\pi}{5}}}{\sqrt{(\varphi-1) \sqrt{5}}-\varphi+1}=1-\frac{\mathrm{e}^{-\pi}}{1+\frac{\mathrm{e}^{-2 \pi}}{1+\frac{\mathrm{e}^{-3 \pi}}{1+\frac{\mathrm{e}^{-4 \pi}}{1+\ldots}}}} \approx 0.9568666373
$$

And to the inflaton value at the end of the inflation 0.9402 (see Appendix)

$$
1+4^{\wedge}(1 / 3)\left(\left(\left(\left((1.024)^{\wedge} 5^{*}(-0.024)^{\wedge} 5\right)\right)\right) /((6.4(-5.4)))\right)^{\wedge} 1 / 12
$$

## Input:

$$
1+\sqrt[3]{4} \sqrt[12]{\frac{1.024^{5}(-0.024)^{5}}{6.4 \times(-5.4)}}
$$

## Result:

1.252262010064803514388581600215084645961775120443318151338
1.2522620100648....
$\left(\left(\left(\left(1+4^{\wedge}(1 / 3)\left(\left(\left(\left((1.024)^{\wedge} 5^{*}(-0.024)^{\wedge} 5\right)\right)\right) /((6.4(-5.4)))\right)^{\wedge} 1 / 12\right)\right)\right)\right)-\left(30 / 10^{\wedge} 2+3 / 10^{\wedge} 3\right)$

## Input:

$\left(1+\sqrt[3]{4} \sqrt[12]{\frac{1.024^{5}(-0.024)^{5}}{6.4 \times(-5.4)}}\right)-\left(\frac{30}{10^{2}}+\frac{3}{10^{3}}\right)$

## Result:

$0.949262010064803514388581600215084645961775120443318151338 \ldots$
$0.9492620100648 \ldots$... result very near to the value of the following Rogers-Ramanujan continued fraction:

$$
\frac{\mathrm{e}^{-\frac{\pi}{5}}}{\sqrt{(\varphi-1) \sqrt{5}}-\varphi+1}=1-\frac{\mathrm{e}^{-\pi}}{1+\frac{\mathrm{e}^{-2 \pi}}{1+\frac{\mathrm{e}^{-3 \pi}}{1+\frac{\mathrm{e}^{-4 \pi}}{1+\ldots}}}} \approx 0.9568666373
$$

And to the inflaton value at the end of the inflation 0.9402 (see Appendix)
$1+1 /(5(1.2522620100648-0.9490606236684))$

## Input interpretation:

$1+\frac{1}{5(1.2522620100648-0.9490606236684)}$

## Result:

1.659627590681671959948709584976407464428121318352722534734...
1.65962759068..... is very near to the 14th root of the following Ramanujan's class invariant $Q=\left(G_{505} / G_{101 / 5}\right)^{3}=1164,2696$ i.e. $1,65578 \ldots$

And:
$(((1 /(5(1.2522620100648-0.9490606236684)))))^{\wedge} 1 / 8$

## Input interpretation:

$\sqrt[8]{\frac{1}{5(1.2522620100648-0.9490606236684)}}$

## Result:

0.9493193902436
$0.9493193902436 \ldots$. result very near to the value of the following Rogers-Ramanujan continued fraction:

$$
\frac{\mathrm{e}^{-\frac{\pi}{5}}}{\sqrt{(\varphi-1) \sqrt{5}}-\varphi+1}=1-\frac{\mathrm{e}^{-\pi}}{1+\frac{\mathrm{e}^{-2 \pi}}{1+\frac{\mathrm{e}^{-3 \pi}}{1+\frac{\mathrm{e}^{-4 \pi}}{1+\ldots}}}} \approx 0.9568666373
$$

And to the inflaton value at the end of the inflation 0.9402 (see Appendix)

## Ramanujan's mathematics applied to cosmology

From:

## Higgs-dilaton cosmology:

An inflation- dark-energy connection and forecasts for future galaxy surveys Santiago Casas, Martin Pauly, and Javier Rubio - arXiv:1712.04956v3 [astroph.CO] 21 Feb 2018

From

$$
\begin{equation*}
\Theta_{\mathrm{E}}=\frac{1-4 c-2 \sqrt{4 c^{2}-2 c-2 \kappa}}{1+8 \kappa} \tag{27}
\end{equation*}
$$

$$
|\kappa| \simeq\left|\kappa_{c}\right| \simeq 1 / 6
$$



We obtain, for $\mathrm{c}=0.0013$ and $\kappa=1 / 6$, we obtain:
$\left(\left(\left(1-4 * 0.0013-2 * \operatorname{sqrt}\left(4^{*} 0.0013 \wedge 2-2 * 0.0013-2 / 6\right)\right)\right)\right) /((1+8 / 6))$

## Input:

$\frac{1-4 \times 0.0013-2 \sqrt{4 \times 0.0013^{2}-2 \times 0.0013-\frac{2}{6}}}{1+\frac{8}{6}}$

## Result:

0.42634286... -
$0.49679291 \ldots i$

## Polar coordinates:

$r=0.654654$ (radius), $\theta=-49.3641^{\circ}$ (angle)
0.654654 result very near to the value of the following Rogers-Ramanujan continued fraction:

$$
\sqrt{\frac{\mathrm{e} \pi}{2}}=\sum_{n=0}^{\infty} \frac{1}{(2 n+1)!!}+\frac{1}{1+\frac{1}{1+\frac{2}{1+\frac{3}{1+\frac{4}{1+\ldots}}}}} \approx 2.0663656771
$$

$$
\sqrt{\frac{\mathrm{e} \pi}{2}} \operatorname{erfc}\left(\frac{\sqrt{2}}{2}\right) \approx 0.6556795424
$$

Note that: $1+0.654654=1.654654$;

## Continued fraction:

$$
1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{8+\frac{1}{1+\frac{1}{1+\frac{1}{2+\frac{1}{1+\frac{1}{1+\frac{1}{13+\frac{1}{5+\frac{1}{5+\frac{1}{2}}}}}}}}}}}}}
$$

Possible closed forms:
$1+\sqrt{\frac{3}{7}} \approx 1.6546536707$

From:

$$
\begin{equation*}
A_{s}=\frac{\lambda \sinh ^{2}\left(4 c N_{*}\right)}{1152 \pi^{2} \xi_{\mathrm{eff}}^{2} c^{2}} \tag{28}
\end{equation*}
$$

For $\mathrm{c}=0.0013 ; \mathrm{N}_{*}=60$ and $\xi_{\mathrm{eff}} / \sqrt{ } \lambda=50000$, we obtain:
$\left(\left(\left(\sinh ^{\wedge} 2\left(4^{*} 0.0013 * 60\right)\right)\right)\right) /\left(\left(\left(1152 * \operatorname{Pi}^{\wedge} 2^{*} 50000^{\wedge} 2^{*} 0.0013 \wedge 2\right)\right)\right)$

## Input:

$\frac{\sinh ^{2}(4 \times 0.0013 \times 60)}{1152 \pi^{2} \times 50000^{2} \times 0.0013^{2}}$

## Result:

$2.09304 \ldots \times 10^{-9}$
2.09304...* $10^{-9}$

## Alternative representations:

$\frac{\sinh ^{2}(4 \times 0.0013 \times 60)}{1152 \pi^{2} 50000^{2} \times 0.0013^{2}}=\frac{\left(\frac{1}{\operatorname{csch}(0.312)}\right)^{2}}{1152 \times 0.0013^{2} \times 50000^{2} \pi^{2}}$
$\frac{\sinh ^{2}(4 \times 0.0013 \times 60)}{1152 \pi^{2} 50000^{2} \times 0.0013^{2}}=\frac{\left(\frac{1}{2}\left(-\frac{1}{e^{0.312}}+e^{0.312}\right)\right)^{2}}{1152 \times 0.0013^{2} \times 50000^{2} \pi^{2}}$
$\frac{\sinh ^{2}(4 \times 0.0013 \times 60)}{1152 \pi^{2} 50000^{2} \times 0.0013^{2}}=\frac{\left(-\frac{i}{\csc (0.312 i)}\right)^{2}}{1152 \times 0.0013^{2} \times 50000^{2} \pi^{2}}$

## Series representations:

$\frac{\sinh ^{2}(4 \times 0.0013 \times 60)}{1152 \pi^{2} 50000^{2} \times 0.0013^{2}}=\frac{1.02728 \times 10^{-7} \sum_{k=1}^{\infty} \frac{e^{-0.94321 k}}{(2 k)!}}{\pi^{2}}$
$\frac{\sinh ^{2}(4 \times 0.0013 \times 60)}{1152 \pi^{2} 50000^{2} \times 0.0013^{2}}=\frac{8.21828 \times 10^{-7}\left(\sum_{k=0}^{\infty} I_{1+2 k}(0.312)\right)^{2}}{\pi^{2}}$
$\frac{\sinh ^{2}(4 \times 0.0013 \times 60)}{1152 \pi^{2} 50000^{2} \times 0.0013^{2}}=\frac{2.05457 \times 10^{-7}\left(\sum_{k=0}^{\infty} \frac{0.312^{1+2 k}}{(1+2 k)!}\right)^{2}}{\pi^{2}}$

And:
$\left[\left(\left(\left(\sinh \wedge 2\left(4^{*} 0.0013 * 60\right)\right)\right)\right) /\left(\left(\left(1152^{*} \mathrm{Pi}^{\wedge} 2^{*} 50000^{\wedge} 2^{*} 0.0013^{\wedge} 2\right)\right)\right)\right]^{\wedge} 1 /\left(64^{\wedge} 2\right)$

## Input:

$\sqrt[64]{\frac{\sinh ^{2}(4 \times 0.0013 \times 60)}{1152 \pi^{2} \times 50000^{2} \times 0.0013^{2}}}$

## Result:

0.995132818...
$0.995132818 \ldots$... result very near to the value of the following Rogers-Ramanujan continued fraction:
$\frac{\mathrm{e}^{-\frac{\pi}{\sqrt{5}}}}{\frac{\sqrt{5}}{1+\sqrt[5]{\sqrt{\varphi^{5 \sqrt[4]{5^{3}}}-1}}-\varphi+1}=1-\frac{\mathrm{e}^{-\pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-2 \pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-3 \pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-4 \pi \sqrt{5}}}{1+\ldots}}}} \approx 0.9991104684 .10 .}$

From:

$$
\begin{align*}
& n_{s}=1-8 c \operatorname{coth}\left(4 c N_{*}\right)  \tag{29}\\
& \alpha_{s}=-32 c^{2} \operatorname{csch}^{2}\left(4 c N_{*}\right) \tag{30}
\end{align*}
$$

We have:
$1-8 * 0.0013 \operatorname{coth}(4 * 0.0013 * 60)$

## Input:

$1-(8 \times 0.0013) \operatorname{coth}(4 \times 0.0013 \times 60)$

## Result:

0.9655920...
$0.9655920 \ldots$ result very near to the spectral index $n_{s}$ and to the value of the following Rogers-Ramanujan continued fraction:

$$
\frac{\mathrm{e}^{-\frac{\pi}{5}}}{\sqrt{(\varphi-1) \sqrt{5}}-\varphi+1}=1-\frac{\mathrm{e}^{-\pi}}{1+\frac{\mathrm{e}^{-2 \pi}}{1+\frac{\mathrm{e}^{-3 \pi}}{1+\frac{\mathrm{e}^{-4 \pi}}{1+\ldots}}}} \approx 0.9568666373
$$

## Alternative representations:

```
\(1-\operatorname{coth}(4 \times 0.0013 \times 60) 8 \times 0.0013=1-0.0104\left(1+\frac{2}{-1+e^{0.624}}\right)\)
\(1-\operatorname{coth}(4 \times 0.0013 \times 60) 8 \times 0.0013=1-0.0104 i \cot (0.312 i)\)
\(1-\operatorname{coth}(4 \times 0.0013 \times 60) 8 \times 0.0013=1+0.0104 i \cot (-0.312 i)\)
```


## Series representations:

$1-\operatorname{coth}(4 \times 0.0013 \times 60) 8 \times 0.0013=1.0104+0.0208 \sum_{k=1}^{\infty} q^{2 k}$ for $q=1.36615$
$1-\operatorname{coth}(4 \times 0.0013 \times 60) 8 \times 0.0013=0.966667-0.0064896 \sum_{k=1}^{\infty} \frac{1}{0.097344+k^{2} \pi^{2}}$
$1-\operatorname{coth}(4 \times 0.0013 \times 60) 8 \times 0.0013=1-0.0032448 \sum_{k=-\infty}^{\infty} \frac{1}{0.097344+k^{2} \pi^{2}}$

## Integral representation:

$1-\operatorname{coth}(4 \times 0.0013 \times 60) 8 \times 0.0013=1+0.0104 \int_{\frac{i \pi}{2}}^{0.312} \operatorname{csch}^{2}(t) d t$

If we put 0.9568666373 , that is the value of the above Rogers-Ramanujan continued fraction instead of 0.9655920 as solution of the above equation, we obtain another value of $\mathrm{N}^{*}$. Indeed:
$1-8 * 0.0013 \operatorname{coth}(4 * 0.0013 * x)=0.9568666373$

## Input interpretation:

$1-(8 \times 0.0013) \operatorname{coth}(4 \times 0.0013 x)=0.9568666373$

## Result:

$1-0.0104 \operatorname{coth}(0.0052 x)=0.956867$
Plot:


## Alternate forms:

$-0.0104(\operatorname{coth}(0.0052 x)-96.1538)=0.956867$
$1-\frac{0.0104 \cosh (0.0052 x)}{\sinh (0.0052 x)}=0.956867$
$-0.0104 \operatorname{csch}(0.0052 x)(\cosh (0.0052 x)-96.1538 \sinh (0.0052 x))=0.956867$

## Alternate form assuming $x$ is positive:

$\operatorname{coth}(0.0052 x)=4.14744$

## Alternate form assuming $x$ is real:

$\frac{0.0104 \sinh (0.0104 x)}{1-\cosh (0.0104 x)}+1=0.956867$

## Real solution:

$x \approx 47.2991$
47.2991

## Solution:

$x \approx(192.308 i)(3.14159 n+(-0.245955 i)), \quad n \in \mathbb{Z}$

We note that the result is different from the range of $\mathrm{N}_{*}$ that is $60-62$, also if 0.9655920 and 0.9568666373 are very near. This last value, i.e. the RogersRamanujan continued fraction, could provide a value more near to physical reality

Multiplying by $35=(34+29+7) / 2$ the following expression, we obtain:
$35((((47.2991 /(((1-8 * 0.0013 \operatorname{coth}(4 * 0.0013 * 47.2991))))))))$
Note that we have put 47.2991 also as numerator of the internal fraction
Input interpretation:
$35 \times \frac{47.2991}{1-(8 \times 0.0013) \operatorname{coth}(4 \times 0.0013 \times 47.2991)}$

## Result:

1730.093177891177196232409642840610813567050956273027300978...
1730.09317789...

This result is very near to the mass of candidate glueball $\mathrm{f}_{0}(1710)$ meson. Furthermore, 1728 occurs in the algebraic formula for the j-invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the GrossZagier theorem. The number 1728 is one less than the Hardy-Ramanujan number 1729

## Alternative representations:

$\frac{35 \times 47.2991}{1-(8 \times 0.0013) \operatorname{coth}(4 \times 0.0013 \times 47.2991)}=\frac{1655.47}{1-0.0104 i \cot (0.245955 i)}$
$\frac{35 \times 47.2991}{1-(8 \times 0.0013) \operatorname{coth}(4 \times 0.0013 \times 47.2991)}=\frac{1655.47}{1+0.0104 i \cot (-0.245955 i)}$
$\left.\frac{35 \times 47.2991}{1-(8 \times 0.0013) \operatorname{coth}(4 \times 0.0013 \times 47.2991)}=\frac{1655.47}{1-0.0104\left(1+\frac{2}{-1+e^{0.4919} 11}\right.}\right) \quad$

## Series representations:

$\frac{35 \times 47.2991}{1-(8 \times 0.0013) \operatorname{coth}(4 \times 0.0013 \times 47.2991)}=\frac{79589.8}{48.5769+\sum_{k=1}^{\infty} q^{2 k}}$ for $q=1.27884$
$\frac{35 \times 47.2991}{1-(8 \times 0.0013) \operatorname{coth}(4 \times 0.0013 \times 47.2991)}=-\frac{323595 .}{-187.205+\sum_{k=1}^{\infty} \frac{1}{0.060494+k^{2} \pi^{2}}}$
$\frac{35 \times 47.2991}{1-(8 \times 0.0013) \operatorname{coth}(4 \times 0.0013 \times 47.2991)}=\frac{1655.47}{1-0.00255794 \sum_{k=-\infty}^{\infty} \frac{1}{0.060494+k^{2} \pi^{2}}}$

We have that:
$-32 * 0.0013^{\wedge} 2 \operatorname{csch}^{\wedge} 2\left(4^{*} 0.0013^{*} 60\right)$

## Input:

$-32 \times 0.0013^{2} \operatorname{csch}^{2}(4 \times 0.0013 \times 60)$
$\operatorname{csch}(x)$ is the hyperbolic cosecant function

## Result:

-0.000537874...
$-0.000537874 \ldots$

## Alternative representations:

$-32 \times 0.0013^{2} \operatorname{csch}^{2}(4 \times 0.0013 \times 60)=-32 \times 0.0013^{2}(i \csc (0.312 i))^{2}$
$-32 \times 0.0013^{2} \operatorname{csch}^{2}(4 \times 0.0013 \times 60)=-32 \times 0.0013^{2}(-i \csc (-0.312 i))^{2}$
$-32 \times 0.0013^{2} \operatorname{csch}^{2}(4 \times 0.0013 \times 60)=-32 \times 0.0013^{2}\left(\frac{2 e^{0.312}}{-1+e^{0.624}}\right)^{2}$

## Series representations:

$-32 \times 0.0013^{2} \operatorname{csch}^{2}(4 \times 0.0013 \times 60)=-0.00005408 \sum_{k=-\infty}^{\infty} \frac{1}{(-0.312+i k \pi)^{2}}$
$-32 \times 0.0013^{2} \operatorname{csch}^{2}(4 \times 0.0013 \times 60)=-0.00005408 \sum_{k=-\infty}^{\infty} \frac{1}{(0.312+i k \pi)^{2}}$
$-32 \times 0.0013^{2} \operatorname{csch}^{2}(4 \times 0.0013 \times 60)=-0.00021632\left(\sum_{k=1}^{\infty} q^{-1+2 k}\right)^{2}$ for $q=1.36615$

From which:
$\left(\left(-\left(-32^{*} 0.0013^{\wedge} 2 \operatorname{csch}^{\wedge} 2\left(4^{*} 0.0013^{*} 60\right)\right)\right)\right)^{\wedge} 1 /\left(64^{\wedge} 2\right)$
Input:
$\sqrt[64]{2} \sqrt{-\left(-32 \times 0.0013^{2} \operatorname{csch}^{2}(4 \times 0.0013 \times 60)\right)}$
$\operatorname{csch}(x)$ is the hyperbolic cosecant function

## Result:

0.998163825 ..
$0.998163825 \ldots$ result very near to the value of the following Rogers-Ramanujan continued fraction:
$\frac{\mathrm{e}^{-\frac{\pi}{\sqrt{5}}}}{\frac{\sqrt{5}}{1+\sqrt[5]{\sqrt{\varphi^{5 \sqrt[4]{5^{3}}}-1}}-\varphi+1}=1-\frac{\mathrm{e}^{-\pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-2 \pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-3 \pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-4 \pi \sqrt{5}}}{1+\ldots}}}} \approx 0.9991104684 .10 .}$

From:

$$
\begin{equation*}
n_{s}=1-\frac{2}{N_{*}} X \operatorname{coth} X, \tag{43}
\end{equation*}
$$

with

$$
\begin{equation*}
X \equiv 4 c N_{*}=\frac{3 N_{*}(1+w)}{4 F\left(\Omega_{\mathrm{DE}}\right)} . \tag{44}
\end{equation*}
$$

We obtain:
4*0.0013*60

## Input:

$4 \times 0.0013 \times 60$

## Result:

0.312
0.312

And:
$1-(2 / 60 * 0.312 \operatorname{coth}(0.312))$

## Input:

$1-\frac{2}{60} \times 0.312 \operatorname{coth}(0.312)$
$\operatorname{coth}(x)$ is the hyperbolic cotangent function

## Result:

0.9655920...
$0.9655920 \ldots$ result very near to the spectral index $n_{s}$ and to the value of the following Rogers-Ramanujan continued fraction:

$$
\frac{\mathrm{e}^{-\frac{\pi}{5}}}{\sqrt{(\varphi-1) \sqrt{5}}-\varphi+1}=1-\frac{\mathrm{e}^{-\pi}}{1+\frac{\mathrm{e}^{-2 \pi}}{1+\frac{\mathrm{e}^{-3 \pi}}{1+\frac{\mathrm{e}^{-4 \pi}}{1+\ldots}}}} \approx 0.9568666373
$$

## Alternative representations:

$1-\frac{2}{60}(0.312 \operatorname{coth}(0.312))=1-\frac{1}{60} \times 0.624\left(1+\frac{2}{-1+e^{0.624}}\right)$
$1-\frac{2}{60}(0.312 \operatorname{coth}(0.312))=1-\frac{1}{60} \times 0.624 i \cot (0.312 i)$
$1-\frac{2}{60}(0.312 \operatorname{coth}(0.312))=1+\frac{1}{60} \times 0.624 i \cot (-0.312 i)$

## Series representations:

$1-\frac{2}{60}(0.312 \operatorname{coth}(0.312))=1.0104+0.0208 \sum_{k=1}^{\infty} q^{2 k}$ for $q=1.36615$
$1-\frac{2}{60}(0.312 \operatorname{coth}(0.312))=0.966667-0.0064896 \sum_{k=1}^{\infty} \frac{1}{0.097344+k^{2} \pi^{2}}$
$1-\frac{2}{60}(0.312 \operatorname{coth}(0.312))=1-0.0032448 \sum_{k=-\infty}^{\infty} \frac{1}{0.097344+k^{2} \pi^{2}}$

## Integral representation:

$1-\frac{2}{60}(0.312 \operatorname{coth}(0.312))=1+0.0104 \int_{\frac{i \pi}{2}}^{0.312} \operatorname{csch}^{2}(t) d t$

If we put 0.9568666373 as result of the above equation, we obtain a different value of X. Indeed:
$1-(2 / 60 * x \operatorname{coth}(x))=0.9568666373$

## Input interpretation:

$1-\frac{2}{60} x \operatorname{coth}(x)=0.9568666373$

## Result:

$1-\frac{1}{30} x \operatorname{coth}(x)=0.956867$

## Plot:



## Alternate forms:

$\frac{1}{30}(30-x \operatorname{coth}(x))=0.956867$
$1-\frac{x \cosh (x)}{30 \sinh (x)}=0.956867$
$-\frac{1}{30} \operatorname{csch}(x)(x \cosh (x)-30 \sinh (x))=0.956867$

## Alternate form assuming $x$ is positive:

$x \operatorname{coth}(x)=1.294$
Alternate form assuming $x$ is real:
$\frac{x \sinh (2 x)}{30(1-\cosh (2 x))}+1=0.956867$

## Solutions:

$x=-0.967266$
$x=0.967266$
0.967266 a result very different from the previous value of X . We note that:

## From:

The $\omega$ and $\omega_{3}$ trajectories were also fitted simultaneously. Here again the higher spin trajectory alone resulted in an optimal linear fit, with $\alpha^{\prime}=0.86 \mathrm{GeV}^{-2}$. The two fitted simultancously arc best fitted with a high mass, $m_{u / d}=340$, and high slope, $\alpha^{\prime}=1.09$ $\mathrm{GcV}^{-2}$. Excluding the ground state $\omega(782)$ from the fits climinates the need for a mass and the linear fit with $\alpha^{\prime}=0.97 \mathrm{GeV}^{-2}$ is then optimal. The mass of the ground state from the resulting fit is 950 MeV . This is odd, since we have no reason to expect the $\omega(782)$ to have an abnormally low mass, especially since it fits in perfectly with its trajectory in the ( $J, M^{2}$ ) plane.

$$
\begin{array}{c|c|c|c}
\omega / \omega_{3} & 5+3 & m_{u / d}=255-390 & 0.988-1.18 \\
\omega / \omega_{3} & 5+3 & m_{u / d}=240-345 & 0.937-1.000
\end{array}
$$

The average between the following value $(0.988+0.937) / 2$ is equal to 0.9625 , very near to the above indicated value $\alpha^{\prime}=0.97$ and to the result that we have obtained for X. Also here, can be that this last value, i.e. the Rogers-Ramanujan continued fraction, provides a value more real from physical point of view.

Now:
$1+w=\frac{16 \gamma^{2}}{3}$
$\gamma<1 /(2 \sqrt{2})$
$\gamma<0.3535 \ldots . \gamma=0.25 ; \quad 1+w=\left(16^{*} 0.25^{\wedge} 2\right) / 3=1 / 3$
From which we obtain $\mathrm{F}\left(\Omega_{\mathrm{DE}}\right)$ :
$0.312 * 4 \mathrm{x}=3 * 60 * 1 / 3$

## Input:

$0.312 \times 4 x=3 \times 60 \times \frac{1}{3}$
Result:
$1.248 x=60$
Plot:


## Alternate form:

$1.248 x-60=0$

Alternate form assuming x is real:
$1.248 x+0=60$

## Solution:

$x \approx 48.0769$
$48.0769=\mathrm{F}\left(\Omega_{\mathrm{DE}}\right)$

If:

$$
F\left(\Omega_{\mathrm{DE}}\right)=\left[\frac{1}{\sqrt{\Omega_{\mathrm{DE}}}}-\Delta \tanh ^{-1} \sqrt{\Omega_{\mathrm{DE}}}\right]^{2}
$$

and

$$
\Delta \equiv \frac{1-\Omega_{\mathrm{DE}}}{\Omega_{\mathrm{DE}}}
$$

we have that:
$48.0769=\left[1 / \mathrm{x}-(1-\mathrm{sqrt}(\mathrm{x})) / \mathrm{sqrt}(\mathrm{x})^{*} \tanh ^{\wedge}-1 \mathrm{x}\right]^{\wedge} 2$

## Input interpretation:

$48.0769=\left(\frac{1}{x}-\frac{1-\sqrt{x}}{\sqrt{x}} \tanh ^{-1}(x)\right)^{2}$
$\tanh ^{-1}(x)$ is the inverse hyperbolic tangent function

## Result:

$48.0769=\left(\frac{1}{x}-\frac{(1-\sqrt{x}) \tanh ^{-1}(x)}{\sqrt{x}}\right)^{2}$
Plot:


## Numerical solution:

$x \approx 0.139484062721383$.
0.1394840.....

Indeed:
[1/0.139484-(1-sqrt(0.139484))/sqrt(0.139484)*tanh^-1 0.139484]^2

## Input interpretation:

$\left(\frac{1}{0.139484}-\frac{1-\sqrt{0.139484}}{\sqrt{0.139484}} \tanh ^{-1}(0.139484)\right)^{2}$

## Result:

48.0769 .
48.0769...

Thence :

## Input interpretation:

$0.139484062721383^{2}$

## Result:

0.019455803753262706715885432689
0.019455803...

## Repeating decimal:

0.01945580375326270671588543268900
0.01945580375...
$\Omega_{\mathrm{DE}}=0.019455786256$
We obtain:
$(0.0194558037532627)^{\wedge} 1 / 4096$

## Input interpretation:

$\sqrt[4096]{0.0194558037532627}$

## Result:

0.9990386435859919748.
$0.9990386435859 \ldots$. result practically equal to the value of the following RogersRamanujan continued fraction:
$\frac{\mathrm{e}^{-\frac{\pi}{\sqrt{5}}}}{\frac{\sqrt{5}}{1+\sqrt[5]{\sqrt{\varphi^{5 \sqrt[4]{5^{3}}}}-1}}-\varphi+1}=1-\frac{\mathrm{e}^{-\pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-2 \pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-3 \pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-4 \pi \sqrt{5}}}{1+\ldots}}}} \approx 0.9991104684$

From $48.0769=\mathrm{F}\left(\Omega_{\mathrm{DE}}\right)$, we obtain, multiplying by 36 , the following interesting result:
$36^{*}\left[1 / 0.139484-(1-\operatorname{sqrt}(0.139484)) / \operatorname{sqrt}(0.139484) * \tanh ^{\wedge}-10.139484\right]^{\wedge} 2$

## Input interpretation:

$$
36\left(\frac{1}{0.139484}-\frac{1-\sqrt{0.139484}}{\sqrt{0.139484}} \tanh ^{-1}(0.139484)\right)^{2}
$$

## Result:

1730.770020787909535328594395065643391166319277625646442926 .
1730.7700207...

This result is very near to the mass of candidate glueball $\mathrm{f}_{0}(1710)$ meson. Furthermore, 1728 occurs in the algebraic formula for the j-invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the GrossZagier theorem. The number 1728 is one less than the Hardy-Ramanujan number 1729

## Alternative representations:

$$
\begin{aligned}
& 36\left(\frac{1}{0.139484}-\frac{\tanh ^{-1}(0.139484)(1-\sqrt{0.139484})}{\sqrt{0.139484}}\right)^{2}= \\
& 36\left(\frac{1}{0.139484}-\frac{\operatorname{sn}^{-1}(0.139484 \mid 1)(1-\sqrt{0.139484})}{\sqrt{0.139484}}\right)^{2} \\
& 36\left(\frac{1}{0.139484}-\frac{\tanh ^{-1}(0.139484)(1-\sqrt{0.139484})}{\sqrt{0.139484}}\right)^{2}= \\
& 36\left(\frac{1}{0.139484}-\frac{\operatorname{coth}^{-1}\left(\frac{1}{0.139484}\right)(1-\sqrt{0.139484})}{\sqrt{0.139484}}\right)^{2} \\
& 36\left(\frac{1}{0.139484}-\frac{\tanh ^{-1}(0.139484)(1-\sqrt{0.139484})}{\sqrt{0.139484}}\right)^{2}= \\
& 36\left(\frac{1}{0.139484}-\frac{(-\log (0.860516)+\log (1.13948))(1-\sqrt{0.139484})}{2 \sqrt{0.139484}}\right)^{2}
\end{aligned}
$$

## Series representations:

$$
\begin{aligned}
& 36\left(\frac{1}{0.139484}-\frac{\tanh ^{-1}(0.139484)(1-\sqrt{0.139484})}{\sqrt{0.139484}}\right)^{2}= \\
& 36\left(7.16928+\left(\sum_{k=0}^{\infty} \frac{0.139484^{1+2 k}}{1+2 k}\right)\left(1-\frac{1}{\sum_{k=0}^{\infty} \frac{(-1)^{k}(-0.860516)^{k}\left(-\frac{1}{2}\right)_{k}}{k!}}\right)\right)^{2} \\
& 36\left(\frac{1}{0.139484}-\frac{\tanh ^{-1}(0.139484)(1-\sqrt{0.139484})}{\sqrt{0.139484}}\right)^{2}=36(7.16928+ \\
& \left.\frac{\left(\log (1.13948)-\log (2)+\sum_{k=1}^{\infty} \frac{0.569742^{k}}{k}\right)\left(-1+\sum_{k=0}^{\infty} \frac{(-1)^{k}(-0.860516)^{k}\left(-\frac{1}{2}\right)_{k}}{k!}\right)}{2 \sum_{k=0}^{\infty} \frac{(-1)^{k}(-0.860516)^{k}\left(-\frac{1}{2}\right)_{k}}{k!}}\right)^{2} \\
& 36\left(\frac{1}{0.139484}-\frac{\tanh ^{-1}(0.139484)(1-\sqrt{0.139484})}{\sqrt{0.139484}}\right)^{2}= \\
& 36\left(7.16928-\left(\left(\log (1.13948)-\log (2)+\sum_{k=1}^{\infty} \frac{0.569742^{k}}{k}\right)\right.\right. \\
& \left(1-\exp \left(i \pi\left\lfloor\frac{\arg (0.139484-x)}{2 \pi}\right\rfloor\right) \sqrt{x}\right. \\
& \left.\left.\sum_{k=0}^{\infty} \frac{(-1)^{k}(0.139484-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}\right)\right) / \\
& \left(2 \exp \left(i \pi\left\lfloor\frac{\arg (0.139484-x)}{2 \pi}\right\rfloor\right) \sqrt{x}\right. \\
& \left.\left.\sum_{k=0}^{\infty} \frac{(-1)^{k}(0.139484-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}\right)\right)^{2} \text { for }(x \in \mathbb{R} \text { and } x<0)
\end{aligned}
$$

## Integral representations:

$36\left(\frac{1}{0.139484}-\frac{\tanh ^{-1}(0.139484)(1-\sqrt{0.139484})}{\sqrt{0.139484}}\right)^{2}=$
$36\left(7.16928+0.139484-\frac{0.139484}{\sqrt{0.139484}} \int_{0}^{1} \frac{1}{1-0.0194558 t^{2}} d t\right)^{2}$

$$
\begin{aligned}
& 36\left(\frac{1}{0.139484}-\frac{\tanh ^{-1}(0.139484)(1-\sqrt{0.139484})}{\sqrt{0.139484}}\right)^{2}= \\
& 36\left(7.16928-\frac{0.034871 i(-1+\sqrt{0.139484})}{\pi^{3 / 2} \sqrt{0.139484}}\right. \\
& \left.\int_{-i \infty+\gamma}^{i \infty+\gamma} e^{0.0196475 s} \Gamma\left(\frac{1}{2}-s\right) \Gamma(1-s) \Gamma(s)^{2} d s\right)^{2} \text { for } 0<\gamma<\frac{1}{2}
\end{aligned}
$$

From this result divided with the previous one very similar, ie 1730.0931..., we obtain the following very interesting expression:

1/(((((36*[1/0.139484-(1-sqrt(0.139484))/sqrt(0.139484)*tanh^-1 0.139484]^2)))
*1/((((35((((47.2991/(((1-8*0.0013 coth(4*0.0013*47.2991)))))))))))))))

## Input interpretation:

$$
\left(36\left(\frac{1}{0.139484}-\frac{1-\sqrt{0.139484}}{\sqrt{0.139484}} \tanh ^{-1}(0.139484)\right)^{2}\right) \times \frac{1}{35 \times \frac{47.2991}{1-(8 \times 0.0013) \operatorname{coth}(4 \times 0.0013 \times 47.2991)}}
$$

## Result:

$0.999608935393724802580084555829004238392945534965615462022 \ldots$
$0.999608935 \ldots$ result practically equal to the value of the following RogersRamanujan continued fraction:
$\frac{\mathrm{e}^{-\frac{\pi}{\sqrt{5}}}}{\frac{\sqrt{5}}{1+\sqrt[5]{\sqrt{\varphi^{5 \sqrt[4]{5^{3}}}}-1}}-\varphi+1}=1-\frac{\mathrm{e}^{-\pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-2 \pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-3 \pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-4 \pi \sqrt{5}}}{1+\ldots}}}} \approx 0.9991104684$

## Alternative representations:

$\frac{1}{\frac{36\left(\frac{1}{0.139484}-\frac{(1-\sqrt{0.139484}) \tanh ^{-1}(0.139484)}{\sqrt{0.139484}}\right)^{2}}{\frac{35 \times 47.2991}{1-(8 \times 0.0013) \operatorname{coth}(4 \times 0.0013 \times 47.2991)}}=\frac{1}{36\left(\frac{1}{0.139484}-\frac{\tanh ^{-1}(0.139484)(1-\sqrt{0.139484})}{\sqrt{0.139484}}\right)^{2}}}$
$\left.\frac{1}{\frac{36\left(\frac{1}{0.139484}-\frac{(1-\sqrt{0.139484}) \tanh ^{-1}(0.139484)}{\sqrt{0.139484}}\right)^{2}}{\frac{35 \times 47.2991}{1-(8 \times 0.0013) \operatorname{coth}(4 \times 0.0013 \times 47.2991)}}}=\frac{1}{36\left(\frac{1}{0.139484}-\frac{\tanh ^{-1}(0.139484)(1-\sqrt{0.139484})}{\sqrt{0.139484}}\right)^{2}}\right) \frac{\frac{1655.47}{1-0.0104\left(1+\frac{2}{\left.-1+e^{0.491911}\right)}\right.}}{}$


## Integral representation:

$$
\frac{1}{\frac{36\left(\frac{1}{0.139484}-\frac{(1-\sqrt{0.139484}) \tanh ^{-1}(0.139484)}{\sqrt{0.139484}}\right)^{2}}{\frac{35 \times 47.2991}{1-(8 \times 0.0013) \operatorname{coth}(4 \times 0.0013 \times 47.2991)}}}=
$$

From the eq. (28)

$$
A_{s}=\frac{\lambda \sinh ^{2}\left(4 c N_{*}\right)}{1152 \pi^{2} \xi_{\mathrm{eff}}^{2} c^{2}}
$$

that described the amplitude of the primordial spectrum of scalar perturbations, we obtain $\pi$ and $\zeta(2)$
$\operatorname{sqrt}\left(\left(\left(\left(\left(\left(\left(\left(\left(\left(\left(\sinh \wedge 2\left(4^{*} 0.0013^{*} 60\right)\right)\right)\right)\right) /\left(\left(\left(2.09304 \mathrm{e}-9 * 50000^{\wedge} 2^{*} 0.0013^{\wedge} 2\right)\right)\right)\right)\right)\right)\right.\right.\right.\right.$ * 1/1152))))))

Input interpretation:
$\sqrt{\frac{\sinh ^{2}(4 \times 0.0013 \times 60)}{2.09304 \times 10^{-9} \times 50000^{2} \times 0.0013^{2}} \times \frac{1}{1152}}$

## Result:

3.141589992664707710013184878441010454597412658806979785594...

### 3.14158999... $\approx \pi$

And:
1/6((((((((((((sinh^2(4*0.0013*60))))) /(((2.09304e-9*50000^2*0.0013^2))))))***) 1/1152))))))

## Input interpretation:

$\frac{1}{6}\left(\frac{\sinh ^{2}(4 \times 0.0013 \times 60)}{2.09304 \times 10^{-9} \times 50000^{2} \times 0.0013^{2}} \times \frac{1}{1152}\right)$

## Result:

$1.644931280335173040534525990677167048961947115957791868556 \ldots \approx \zeta(2)=\frac{\pi^{2}}{6}$
$=1.644934066848226436472415166646025189218949901206798437735$.

## Property:

$\frac{\pi^{2}}{6}$ is a transcendental number

## Alternative representations:

$$
\begin{aligned}
& \zeta(2)=\zeta(2,1) \\
& \zeta(2)=S_{1,1}(1)
\end{aligned}
$$

$\zeta(2)=-\frac{\mathrm{Li}_{2}(-1)}{\frac{1}{2}}$

## Integral representations:

$\zeta(2)=\frac{8}{3}\left(\int_{0}^{1} \sqrt{1-t^{2}} d t\right)^{2}$
$\zeta(2)=\frac{2}{3}\left(\int_{0}^{\infty} \frac{1}{1+t^{2}} d t\right)^{2}$
$\zeta(2)=\frac{2}{3}\left(\int_{0}^{1} \frac{1}{\sqrt{1-t^{2}}} d t\right)^{2}$

## From:

Eur. Phys. J. C (2019) 79:713 - https://doi.org/10.1140/epjc/s10052-019-7225-2-Regular Article - Theoretical Physics
Generalized dilaton-axion models of inflation, de Sitter vacua and spontaneous SUSY breaking in supergravity
Yermek Aldabergenov, Auttakit Chatrabhuti, Sergei V. Ketov

Table 1 The predictions for the inflationary parameters ( $\left.n_{s}, r\right)$, and the values of $\varphi$ at the horizon crossing $\left(\varphi_{i}\right)$ and at the end of inflation $\left(\varphi_{f}\right)$, in the case $3 \leq \alpha \leq \alpha_{*}$ with both signs of $\omega_{1}$. The $\alpha$ parameter is taken to be integer, except of the upper limit $\alpha_{*} \equiv(7+\sqrt{33}) / 2$

| $\alpha$ | 3 | 4 |  | 5 | 6 | - |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\operatorname{sgn}\left(\omega_{1}\right)$ | - | + | - | $+/-$ | + | - |  |
| $n_{s}$ | 0.9650 | 0.9649 | 0.9640 | 0.9639 | 0.9634 | 0.9637 | 0.9632 |
| $r$ | 0.0035 | 0.0010 | 0.0013 | 0.0007 | 0.0005 | 0.0004 | 0.0003 |
| $-\kappa \varphi_{i}$ | 5.3529 | 3.5542 | 3.9899 | 3.2657 | 3.0215 | 2.7427 | 2.5674 |
| $-\kappa \varphi_{f}$ | 0.9402 | 0.7426 | 0.8067 | 0.7163 | 0.6935 | 0.6488 | 0.6276 |

Table 2 The masses of inflaton, axion and gravitino, and the VEVs of $F$ - and $D$-fields derived from our models by fixing the amplitude $A_{5}$ according to PLANCK data - see Eq. (57). The value of $\left\langle F_{T}\right\rangle$ for a positive $\omega_{1}$ is not fixed by $A_{s}$

| $\alpha$ | 3 | 4 |  | 5 |  | 6 |  | 7 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\operatorname{sgn}\left(\omega_{1}\right)$ | - | + | - | + | - | - | - | - |
| $m_{\varphi}$ | 2.83 | 2.95 | 2.73 | 2.71 | 2.71 | 2.53 | 2.58 | 1.86 |
| $m_{t^{\prime}}$ | 0 | 0.93 | 1.73 | 2.02 | 2.02 | 4.97 | 2.01 | 1.56 |
| $m_{3 / 2}$ | $\geq 1.41$ | 2.80 | 0.86 | 2.56 | 0.64 | 3.91 | 0.49 | 0.29 |
| $\left\langle F_{T}\right\rangle$ | any | $\neq 0$ | 0 | $\neq 0$ | 0 | $\neq 0$ | 0 | 0 |
| $\langle D\rangle$ | 8.31 | 4.48 | 5.08 | 3.76 | 3.76 | 3.25 | 2.87 | 1.73 |$\} \times 10^{13} \mathrm{GeV}$

We take the following two values of axion mass: 0.93 and 1.73 . If we perform the following calculations, we obtain:
$(1 / 0.93+1 / 1.73)$

## Input: <br> $\frac{1}{0.93}+\frac{1}{1.73}$

## Result:

1.653303499285225930760146684069861395984834358878737025296...
$1.653303499285 \ldots .$. is very near to the 14 th root of the following Ramanujan's class invariant $Q=\left(G_{505} / G_{101 / 5}\right)^{3}=1164,2696$ i.e. $1,65578 \ldots$

And the inverse:
$1 /(1 / 0.93+1 / 1.73)$

## Input: <br> $\frac{1}{\frac{1}{0.93}+\frac{1}{1.73}}$

## Result:

0.604849624060150375939849624060150375939849624060150375939

## Repeating decimal:

$0.604 \overline{849624060150375939}$ (period 18)
0.604849624...

If we put, instead of 0.93 , the value of the Rogers-Ramanujan continued fraction,

$$
\frac{\mathrm{e}^{-\frac{\pi}{5}}}{\sqrt{(\varphi-1) \sqrt{5}}-\varphi+1}=1-\frac{\mathrm{e}^{-\pi}}{1+\frac{\mathrm{e}^{-2 \pi}}{1+\frac{\mathrm{e}^{-3 \pi}}{1+\frac{\mathrm{e}^{-4 \pi}}{1+\ldots}}}} \approx 0.9568666373
$$

we obtain:

Input interpretation:
$\frac{1}{0.9568666373}+\frac{1}{1.73}$

## Result:

1.623112398262680166441180693689879956488457189122659411750...
$1.62311239826 \ldots$ result that is a golden number
and the inverse:
1/(1/0.9568666373+1/1.73)
Input interpretation:
$\frac{1}{\frac{1}{0.9568666373}+\frac{1}{1.73}}$

## Result:

0.616100278126372044628610417559558567227887473981699434010...
0.616100278126372......
values that tend more and more towards the golden ratio and its conjugate.

Thence, we have also:
$(((1 /(1 / 0.9568666373+1 / 1.73))))^{\wedge} 1 / 8$

## Input interpretation:

$$
\sqrt[8]{\frac{1}{\frac{1}{0.9568666373}+\frac{1}{1.73}}}
$$

## Result:

0.9412531 ..
0.9412531 result very near to the value 0.9402 (see above Table I)

The inflaton masses are:

| $m_{\varphi}$ | 2.83 | 2.95 | 2.73 | 2.71 | 2.71 | 2.53 | 2.58 | 1.86 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

We have the following Rogers-Ramanujan continued fraction:

$$
\sqrt{\frac{\mathrm{e} \pi}{2}}=\sum_{n=0}^{\infty} \frac{1}{(2 n+1)!!}+\frac{1}{1+\frac{1}{1+\frac{2}{1+\frac{3}{1+\frac{4}{1+\ldots}}}}} \approx 2.0663656771
$$

And

$$
2 \int_{0}^{\infty} \frac{t^{2} d t}{\mathrm{e}^{\sqrt{3} t} \sinh t}=\frac{1}{1+\frac{1^{3}}{1+\frac{1^{3}}{3+\frac{2^{3}}{1+\frac{2^{3}}{5+\frac{3^{3}}{1+\frac{3^{3}}{7+\ldots}}}}}}} \approx 0.5269391135
$$

$$
4 \int_{0}^{\infty} \frac{t d t}{\mathrm{e}^{\sqrt{5} t} \cosh t}=\frac{1}{1+\frac{1^{2}}{1+\frac{1^{2}}{1+\frac{2^{2}}{1+\frac{2^{2}}{1+\frac{3^{2}}{1+\frac{3^{2}}{1+\ldots}}}}}}} \approx 0.5683000031
$$

We observe that: $2.0663656771+0.5683000031=2.6346656802$ and
$2.0663656771+0.5269391135=2.5933047906$, results very near to the above inflaton (dilaton) masses values $2.58-2.71$

From the following masses:

| $m_{\varphi}$ | 2.83 | 2.95 | 2.73 | 2.71 | 2.71 | 2.53 | 2.58 | 1.86 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

we obtain this average:
$(2.83+2.95+2.73+2.71+2.71+2.53+2.58+1.86) / 8$

## Input:

$\frac{1}{8}(2.83+2.95+2.73+2.71+2.71+2.53+2.58+1.86)$

## Result:

2.6125
2.6125

The effective value is multiplied by $10^{13} \mathrm{GeV}$
We have also:
$(1 /(2.6125))^{\wedge} 1 / 16$

## Input interpretation:

$\sqrt[16]{\frac{1}{2.6125}}$

## Result:

0.941746 .
$0.941746 . .$. result very near to 0.9402 (Table I)
Now, we have that, multiplying the average $2.6125 \mathrm{e}+13$ of the mass of inflaton (dilaton) by $9 \mathrm{e}+16$, inverting and performing the $1920^{\text {th }}(64 * 30)$ root, we obtain:
$\left(\left(1 /\left(2.6125 * 10^{\wedge} 13 * 9 \mathrm{e}+16\right)\right)\right)^{\wedge} 1 /(64 * 30)$

## Input interpretation:

$\sqrt[64 \times 30]{\frac{1}{2.6125 \times 10^{13} \times 9 \times 10^{16}}}$

## Result:

0.96423217 ..
$0.96423217 \ldots$ result very near to the spectral tilt $n_{s}=0.9649 \pm 0.0042$.

From the following masses (axions):

| $m_{t^{\prime}}$ | 0 | 0.93 | 1.73 | 2.02 | 2.02 | 4.97 | 2.01 | 1.56 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

we obtain the following average: 1.905
We note that, multiplying by 2 the following Rogers-Ramanujan continued fraction:

$$
\frac{\mathrm{e}^{-\frac{\pi}{5}}}{\sqrt{(\varphi-1) \sqrt{5}}-\varphi+1}=1-\frac{\mathrm{e}^{-\pi}}{1+\frac{\mathrm{e}^{-2 \pi}}{1+\frac{\mathrm{e}^{-3 \pi}}{1+\frac{\mathrm{e}^{-4 \pi}}{1+\ldots}}}} \approx 0.9568666373
$$

we obtain: 1.9137332746 , result very near to the above average and very near to the mean value $1.962 * 10^{19}$ of DM particle that has a Planck scale mass: $\mathrm{m} \approx 10^{19} \mathrm{GeV}$.

From:
Received: June 28, 2018 - Accepted: September 10, 2018 - Published: September 17, 2018 - Cosmological phase transitions in warped space: gravitational waves and collider signatures
Eugenio Megias, Germano Nardini and Mariano Quiros
We have:
$\ell=1,616252 \times 10^{-35} \mathrm{~m}$
$g^{e f f}=106,75$
$\mathrm{a}_{\mathrm{h}}(\mathrm{T}) \ll 1$

$$
\kappa=\left(8 \pi G_{\mathrm{N}}\right)^{1 / 2}=\frac{(8 \pi)^{1 / 2}}{M_{\mathrm{P}}}=\left(2.43 \times 10^{18} \mathrm{GeV}\right)^{-1}
$$

A parameter configuration leading to $T_{R}<T_{\mathcal{H}}$ is provided by scenario $\mathrm{D}_{1}$. In this case the dilaton and EW phase transitions happen simultaneously at $T=T_{n} \simeq 112 \mathrm{GeV}$, ending up with $T=T_{R}=133.7 \mathrm{GeV}<T_{\mathrm{EW}}$, so that both the radion and the Higgs acquire a VEV. Before and after the reheating, the bound of eq. (8.7) is fulfilled, and the condition of strong-enongh first order phase transition for FW haryogenesis is satisfied. ${ }^{22}$

It follows that $g^{\text {eff }}=g_{B}(T)+\frac{7}{8} g_{F}(T)=106.75$ at $172 \mathrm{GeV} \lesssim T \ll m_{G}$.

$$
\begin{aligned}
\alpha & \simeq \frac{E_{0}}{3\left(\pi^{4} \ell^{3} / \kappa^{2}\right) a_{h}\left(T_{n}\right) T_{n}^{4}}, \\
T_{i} & \approx\left(\frac{30 \kappa^{2} E_{0}}{90 \pi^{4} \ell^{3} a_{h}+\pi^{2} \kappa^{2} g_{d}^{\text {eff }}}\right)^{1 / 4}
\end{aligned}
$$

From this last expression, we obtain:
$0.591=\left[\left(\left(\left(\left(30^{*}\left(\left((2.43 \mathrm{e}+18)^{\wedge}-1\right)\right)^{\wedge} 2^{*} \mathrm{x}\right)\right)\right)\right) /\left(\left(\left(\left(\left(90 \mathrm{Pi}^{\wedge} 4^{*}(1.616252 \mathrm{e}-\right.\right.\right.\right.\right.\right.$
$\left.\left.\left.\left.\left.\left.35)^{\wedge} 3^{*} 1 / 12+\mathrm{Pi}^{\wedge} 2^{*}\left(\left((2.43 \mathrm{e}+18)^{\wedge}-1\right)\right)^{\wedge} 2^{*} 172\right)\right)\right)\right)\right)\right]^{\wedge} 1 / 4$

## Input interpretation:

$0.591=\sqrt[4]{\frac{30\left(\frac{1}{2.43 \times 10^{18}}\right)^{2} x}{90 \pi^{4}\left(1.616252 \times 10^{-35}\right)^{3} \times \frac{1}{12}+\pi^{2}\left(\frac{1}{2.43 \times 10^{18}}\right)^{2} \times 172}}$

## Result:

$0.591=0.364606 \sqrt[4]{x}$
Plot:


## Alternate form assuming x is positive:

$\sqrt[4]{x}=1.62093$

## Solution:

$x \approx 6.9033$
6.9033 GeV $=\mathrm{E}_{0}$
convert $6.9033 \mathrm{GeV} / \mathrm{k}_{\boldsymbol{B}}$ (gigaelectronvolts per Boltzmann constant) to degrees Celsius
$8.011 \times 10^{13}{ }^{\circ} \mathrm{C}$ (degrees Celsius)
$8.011 \times 10^{13} \mathrm{~K}$ (kelvins)

Indeed:
$\left[\left(\left(\left(\left(30^{*}\left(\left((2.43 \mathrm{e}+18)^{\wedge}-1\right)\right)^{\wedge} 2^{*} 6.9033\right)\right)\right)\right) /\left(\left(\left(\left(\left(90 \mathrm{Pi}^{\wedge} 4^{*}(1.616252 \mathrm{e}-\right.\right.\right.\right.\right.\right.$
$\left.\left.\left.\left.\left.\left.35)^{\wedge} 3^{*} 1 / 12+\mathrm{Pi}^{\wedge} 2^{*}\left(\left((2.43 \mathrm{e}+18)^{\wedge}-1\right)\right)^{\wedge} 2^{*} 172\right)\right)\right)\right)\right)\right]^{\wedge} 1 / 4$

## Input interpretation:

$\sqrt[4]{\frac{30\left(\frac{1}{2.43 \times 10^{18}}\right)^{2} \times 6.9033}{90 \pi^{4}\left(1.616252 \times 10^{-35}\right)^{3} \times \frac{1}{12}+\pi^{2}\left(\frac{1}{2.43 \times 10^{18}}\right)^{2} \times 172}}$

## Result:

0.591000...
0.591

Or/and:
$0.580=\left[\left(\left(\left(\left(30^{*}\left(\left((2.43 \mathrm{e}+18)^{\wedge}-1\right)\right)^{\wedge} 2^{*} \mathrm{x}\right)\right)\right)\right) /\left(\left(\left(\left(\left(90 \mathrm{Pi}^{\wedge} 4^{*}(1.616252 \mathrm{e}-\right.\right.\right.\right.\right.\right.$ $\left.\left.\left.\left.\left.\left.35)^{\wedge} 3 * 1 / 12+\operatorname{Pi}^{\wedge} 2 *\left(\left((2.43 \mathrm{e}+18)^{\wedge}-1\right)\right)^{\wedge} 2 * 106.75\right)\right)\right)\right)\right)\right]^{\wedge} 1 / 4$

## Input interpretation:

$0.58=\sqrt[4]{\frac{30\left(\frac{1}{2.43 \times 10^{18}}\right)^{2} x}{90 \pi^{4}\left(1.616252 \times 10^{-35}\right)^{3} \times \frac{1}{12}+\pi^{2}\left(\frac{1}{2.43 \times 10^{18}}\right)^{2} \times 106.75}}$

## Result:

$0.58=0.410784 \sqrt[4]{x}$

Plot:


## Alternate form assuming x is positive:

$\sqrt[4]{x}=1.41193$

## Solution:

## $x \approx 3.97428$

$3.97428 \mathrm{GeV}=\mathrm{E}_{0}$ another value of the vacuum energy

```
convert 3.97428 GeV/k}\mp@subsup{k}{B}{}\mathrm{ (gigaelectronvolts per Boltzmann constant)
    to degrees Celsius
4.612\times10 13 %}\textrm{C}\mathrm{ (degrees Celsius)
4.612\times10 13 K (kelvins)
```

Indeed:
$\left[\left(\left(\left(\left(30^{*}\left(\left((2.43 \mathrm{e}+18)^{\wedge}-1\right)\right)^{\wedge} 2 * 3.97428\right)\right)\right)\right) /\left(\left(\left(\left(\left(90 \mathrm{Pi}^{\wedge} 4^{*}(1.616252 \mathrm{e}-\right.\right.\right.\right.\right.\right.$ $\left.\left.\left.\left.\left.\left.35)^{\wedge} 3^{*} 1 / 12+\mathrm{Pi}^{\wedge} 2^{*}\left(\left((2.43 \mathrm{e}+18)^{\wedge}-1\right)\right)^{\wedge} 2 * 106.75\right)\right)\right)\right)\right)\right]^{\wedge} 1 / 4$

## Input interpretation:

$\sqrt[4]{\frac{30\left(\frac{1}{2.43 \times 10^{18}}\right)^{2} \times 3.97428}{90 \pi^{4}\left(1.616252 \times 10^{-35}\right)^{3} \times \frac{1}{12}+\pi^{2}\left(\frac{1}{2.43 \times 10^{18}}\right)^{2} \times 106.75}}$
Result:
0.580000...
0.580

From

$$
\alpha \simeq \frac{E_{0}}{3\left(\pi^{4} \ell^{3} / \kappa^{2}\right) a_{h}\left(T_{n}\right) T_{n}^{4}},
$$

we obtain:
$6.9033 /\left(\left(\left((3)\left(\left(\left(\left(\mathrm{Pi}^{\wedge} 4^{*}(1.616252 \mathrm{e}-35)^{\wedge} 3\right)\right) /\left(\left((2.43 \mathrm{e}+18)^{\wedge}-1\right)\right)^{\wedge} 2\right)\right)\right)\right)\right)$
$\left.\left.0.00766^{*} 112^{\wedge} 4\right)\right)$

## Input interpretation:

$\frac{6.9033}{\left(3 \times \frac{\pi^{4}\left(1.616252 \times 10^{-35}\right)^{3}}{\left(\frac{1}{2.43 \times 10^{18}}\right)^{2}}\right) \times 0.00766 \times 112^{4}}$

## Result:

$7.86132 \ldots \times 10^{59}$
7.86132 ... $* 10^{59}=\alpha$
and this another value of $\alpha$
$3.97428 /\left(\left(\left(\left(3\left(\left(\left(\left(\left(\mathrm{Pi}^{\wedge} 4 *(1.616252 \mathrm{e}-35)^{\wedge} 3\right)\right) /\left(\left((2.43 \mathrm{e}+18)^{\wedge}-1\right)\right)^{\wedge} 2\right)\right)\right)\right)\right) 0.002 * 112^{\wedge} 4\right)\right)$

## Input interpretation:

$\frac{3.97428}{\left(3 \times \frac{\pi^{4}\left(1.616252 \times 10^{-35}\right)^{3}}{\left(\frac{1}{2.43 \times 10^{18}}\right)^{2}}\right) \times 0.002 \times 112^{4}}$

## Result:

$1.73339 \ldots \times 10^{60}$

## Input interpretation:

$1.73339 \times 10^{60}=17.3339 \times 10^{59}$
$17.3339 * 10^{59}=\alpha$

From

$$
\begin{equation*}
F_{c}(T)=-\frac{\pi^{2}}{90} g_{c}^{\text {eff }} T^{4}, \tag{7.2}
\end{equation*}
$$

we obtain, dividing by $\mathrm{c}^{2}$, two masses:
$\left.\left(\left(\left(\left(-\mathrm{Pi}^{\wedge} 2\right) / 90\right) * 106.75^{*} 112^{\wedge} 4\right)\right)\right) /(9 \mathrm{e}+16)$

## Input interpretation:

$\frac{-\frac{\pi^{2}}{90} \times 106.75 \times 112^{4}}{9 \times 10^{16}}$

## Result:

$-2.04670 \ldots \times 10^{-8}$
$-2.04670 \ldots * 10^{-8}$
and:
$\left.\left(\left(\left(\left(-\mathrm{Pi}^{\wedge} 2\right) / 90\right) * 106.75^{*} 133.7 \wedge 4\right)\right)\right) /(9 \mathrm{e}+16)$

## Input interpretation:

$\frac{-\frac{\pi^{2}}{90} \times 106.75 \times 133.7^{4}}{9 \times 10^{16}}$

## Result:

$-4.15631 \ldots \times 10^{-8}$
$-4.15631 \ldots * 10^{-8}$

We note that:
$\left(\left(\left(\left(-\left(\left(\left(\left(\left(-\mathrm{Pi}^{\wedge} 2\right) / 90\right) * 106.75^{*} 112^{\wedge} 4\right)\right)\right) /(9 \mathrm{e}+16)\right)\right)\right)\right)^{\wedge} 1 /\left(4096^{*} 5\right)$

## Input interpretation:

$\sqrt[4096 \times 5]{-\frac{-\frac{\pi^{2}}{90} \times 106.75 \times 112^{4}}{9 \times 10^{16}}}$

## Result:

0.999135898...
0.999135898...

And:

$$
\left(\left(\left(\left(-\left(\left(\left(\left(-\mathrm{Pi}^{\wedge} 2\right) / 90\right)^{*} 106.75^{*} 133.7 \wedge 4\right)\right)\right) /(9 \mathrm{e}+16)\right)\right)\right)^{\wedge} 1 /\left(4096^{*} 5\right)
$$

## Input interpretation:

$\sqrt[4096 \times 5]{-\frac{-\frac{\pi^{2}}{90} \times 106.75 \times 133.7^{4}}{9 \times 10^{16}}}$

## Result:

0.999170459...
0.999170459...

Note that, the two results $0.999135898 \ldots$ and $0.999170459 \ldots$ are practically equals to the value of the following Rogers-Ramanujan continued fraction:
$\frac{\mathrm{e}^{-\frac{\pi}{\sqrt{5}}}}{\frac{\sqrt{5}}{1+\sqrt[5]{\sqrt{\varphi^{5} \sqrt[4]{5^{3}}}-1}}-\varphi+1}=1-\frac{\mathrm{e}^{-\pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-2 \pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-3 \pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-4 \pi \sqrt{5}}}{1+\ldots}}}} \approx 0.9991104684$

From the Table 3

| Scen. | $m_{\mathrm{rad}} / \mathrm{TeV}$ | $m_{G} / \mathrm{TeV}$ | $c_{\gamma}$ | $c_{g}$ | $c_{V}$ | $c_{\mathcal{H}}$ | $c_{f}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{~B}_{2}$ | 0.915 | 4.80 | 0.472 | 0.164 | 0.0649 | 0.259 | 0.259 |
| $\mathrm{~B}_{8}$ | 0.745 | 4.19 | 0.542 | 0.146 | 0.0744 | 0.298 | 0.298 |
| $\mathrm{C}_{1}$ | 0.890 | 3.08 | 0.532 | 0.179 | 0.0904 | 0.362 | 0.362 |
| $\mathrm{C}_{2}$ | 0.751 | 2.77 | 0.595 | 0.162 | 0.101 | 0.404 | 0.401 |
| $\mathrm{D}_{1}$ | 0.477 | 4.50 | 3.791 | 0.475 | 0.397 | 1.586 | 1.586 |
| $\mathrm{E}_{1}$ | 0.643 | 4.16 | 0.562 | 0.124 | 0.0746 | 0.298 | 0.298 |

Table 3. Masses of the radion and the $n=1$ graviton mode, and coupling coefficients of the radion interactions with the SM fields, for the scenario $\mathrm{B}_{2}, \mathrm{~B}_{8}, \mathrm{C}_{1}, \mathrm{C}_{2}, \mathrm{D}_{1}$ and $\mathrm{E}_{1}$.
we note that the mass of radion, for $B_{2}$ is equal to 0.915 , value that is a good approximation to the value of the following Rogers-Ramanujan continued fraction:

$$
\frac{\mathrm{e}^{-\frac{\pi}{5}}}{\sqrt{(\varphi-1) \sqrt{5}}-\varphi+1}=1-\frac{\mathrm{e}^{-\pi}}{1+\frac{\mathrm{e}^{-2 \pi}}{1+\frac{\mathrm{e}^{-3 \pi}}{1+\frac{\mathrm{e}^{-4 \pi}}{1+\ldots}}}} \approx 0.9568666373
$$

Now, we have that:

- Small back-reaction (class A)

$$
\begin{align*}
\gamma & =0.55 \ell^{3 / 2}, & v_{0} & =-9.35 \ell^{-3 / 2}, & v_{1} & =-6.79 \ell^{-3 / 2},
\end{align*} \quad \gamma_{1} \rightarrow \infty,
$$

- Large back-reaction (class B)

$$
\begin{align*}
& \gamma=0.1 \ell^{3 / 2}, \\
& v_{0}=-15 \ell^{-3 / 2}, \\
& v_{1}=-3.3 \ell^{-3 / 2}, \\
& \gamma_{1} \rightarrow \infty, \\
& \kappa^{2}=\frac{1}{4} \ell^{3}(N \simeq 18), \quad r_{S}=37.3 \ell, \quad\left\langle r_{1}\right\rangle=25.4 \ell \text {. } \tag{4.13}
\end{align*}
$$

- Large back-reaction $\xi^{8}$ larger $N$ (class C)

$$
\begin{align*}
\gamma & =0.1 \ell^{3 / 2}, & v_{0} & =-20 \ell^{-3 / 2}, & v_{1} & =0.7 \ell^{-3 / 2},
\end{align*} \quad \gamma_{1} \rightarrow \infty, ~(4)
$$

- Large back-reaction \& smaller $N$ (class D)

$$
\begin{align*}
\gamma & =0.1 \ell^{3 / 2}, & v_{0} & =2 \ell^{-3 / 2}, & v_{1} & =8.9 \ell^{-3 / 2},
\end{align*} \quad \gamma_{1} \rightarrow \infty
$$

- Finite $\gamma_{1}$ (class E)

$$
\begin{align*}
& \gamma=0.1 \ell^{3 / 2}, \quad v_{0}=-15 \ell^{-3 / 2}, \quad v_{1}=-2.6 \ell^{-3 / 2}, \quad \gamma_{1}=10 \ell^{-1}, \\
& \kappa^{2}=\frac{1}{4} \ell^{3}(N \simeq 18), \quad r_{S}=37.3 \ell, \quad\left\langle r_{1}\right\rangle=25.4 \ell . \tag{4.16}
\end{align*}
$$

We have:

For the warp factor $A-A_{0}+s A_{1}$, we can determine $A_{0}$ as

$$
\begin{equation*}
A_{0}(r)=\frac{r}{\ell}+\frac{\kappa^{2}}{3 \gamma}\left(\phi_{0}(r)-v_{0}\right)=\frac{r}{\ell}-\frac{\kappa^{2}}{3 \gamma^{2}} \log \left(1-\frac{r}{r_{S}}\right) . \tag{4.9}
\end{equation*}
$$

${ }^{7}$ The scale $\rho_{1}$ is $\mathcal{O}(\mathrm{TeV})$ for $\ell^{-1} \simeq M_{P}=2.4 \times 10^{18} \mathrm{GeV}$ and $A\left(r_{1}\right) \simeq 35$. In the numerical calculations we will work in units where $\ell=1$.

For

$$
\begin{array}{lll}
\gamma=0.1 \ell^{3 / 2}, & v_{0}=-15 \ell^{-3 / 2}, & v_{1}=-3.3 \ell^{-3 / 2}, \quad \gamma_{1} \rightarrow \infty \\
\kappa^{2}=\frac{1}{4} \ell^{3}(N \simeq 18), & r_{S}=37.3 \ell, & \left\langle r_{1}\right\rangle=25.4 \ell . \\
\ell=1,616252 \times 10^{-35} \mathrm{~m} & \\
& \frac{r}{\ell}-\frac{\kappa^{2}}{3 \gamma^{2}} \log \left(1-\frac{r}{r_{S}}\right)
\end{array}
$$

we obtain:
$1 /((1.616252 \mathrm{e}-35))))-1 / 4^{*}(((1.616252 \mathrm{e}-35)))^{\wedge} 3^{*} 1 /\left(3^{*}\left(\left(\left(\left(0.1^{*}(1.616252 \mathrm{e}-\right.\right.\right.\right.\right.$ $\left.\left.\left.\left.\left.35)^{\wedge}(1.5)\right)\right)\right)\right)\right)^{\wedge} 2 \ln (1-(25.4 / 37.3))$

## Input interpretation:

$25.4 \times \frac{1}{1.616252 \times 10^{-35}}-$

$$
\left(\frac{1}{4}\left(1.616252 \times 10^{-35}\right)^{3} \times \frac{1}{\left(3\left(0.1\left(1.616252 \times 10^{-35}\right)^{1.5}\right)\right)^{2}}\right) \log \left(1-\frac{25.4}{37.3}\right)
$$

$\log (x)$ is the natural logarithm

## Result:

$1.5715371117870233107213479086182105297497871273883798 \ldots \times 10^{36}$
$1.571537111787 \ldots * 10^{36}$
and, we obtain also:
$(((1 /((()(((25.4 * 1 /((1.616252 \mathrm{e}-35))))-1 / 4 *(((1.616252 \mathrm{e}-$
$\left.\left.\left.\left.\left.\left.\left.\left.35)))^{\wedge} 3 * 1 /\left(3^{*}((((0.1 *(1.616252 \mathrm{e}-35) \wedge(1.5)))))\right)^{\wedge} 2 \ln (1-(25.4 / 37.3))\right)\right)\right)\right)\right)\right)\right)\right)^{\wedge}(1 / 2048)$

## Input interpretation:

$$
\begin{aligned}
& \left(1 /\left(25.4 \times \frac{1}{1.616252 \times 10^{-35}}-\right.\right. \\
& \\
& \quad\left(\frac{1}{4}\left(1.616252 \times 10^{-35}\right)^{3} \times \frac{1}{\left(3\left(0.1\left(1.616252 \times 10^{-35}\right)^{1.5}\right)\right)^{2}}\right) \\
& \\
& \left.\left.\quad \log \left(1-\frac{25.4}{37.3}\right)\right)\right) \wedge(1 / 2048)
\end{aligned}
$$

## Result:

$0.960121098529740875383702751138442555799865933620178276080 \ldots$
$0.9601210985297 \ldots$. result very near to the value of the following Rogers-Ramanujan continued fraction:

$$
\frac{\mathrm{e}^{-\frac{\pi}{5}}}{\sqrt{(\varphi-1) \sqrt{5}}-\varphi+1}=1-\frac{\mathrm{e}^{-\pi}}{1+\frac{\mathrm{e}^{-2 \pi}}{1+\frac{\mathrm{e}^{-3 \pi}}{1+\frac{\mathrm{e}^{-4 \pi}}{1+\ldots}}}} \approx 0.9568666373
$$

Now, we have that:
presence of a strong first order phase transition. This is a consequence of the cooling in the initial (BH) phase, which also triggers a (very brief) inflationary stage just before the onset of the phase transition.

The energy density $\rho=F-T d F / d T$ in the two phases is given by

$$
\begin{align*}
& \rho_{d}=E_{0}+\frac{3 \pi^{4} \ell^{3}}{\kappa^{2}} a_{h} T^{4}+\frac{\pi^{2}}{30} g_{d}^{\mathrm{eff}} T^{4}  \tag{7.15}\\
& \rho_{c}=\frac{\pi^{2}}{30} g_{c}^{\mathrm{eff}} T^{4} . \tag{7.16}
\end{align*}
$$

$3.97428+3 * \operatorname{Pi}^{\wedge} 4 *\left(\left(((((1.616252 \mathrm{e}-35))))^{\wedge} 3^{*} 0.002 * 112^{\wedge} 4\right)\right) /\left(\left(\left(\left(\left((2.43 \mathrm{e}+18)^{\wedge}-\right.\right.\right.\right.\right.$ $\left.\left.\left.1))^{\wedge} 2\right)\right)\right)+\left(\left(\left(\mathrm{Pi}^{\wedge} 2^{*} 172^{*} 112^{\wedge} 4\right)\right)\right) / 30$

## Input interpretation:

$3.97428+3 \pi^{4} \times \frac{\left(1.616252 \times 10^{-35}\right)^{3} \times 0.002 \times 112^{4}}{\left(\frac{1}{2.43 \times 10^{18}}\right)^{2}}+\frac{1}{30}\left(\pi^{2} \times 172 \times 112^{4}\right)$

## Result:

$8.90387446834999 \ldots \times 10^{9}$
8.903874... * $10^{9}$
$\left(\left(\left(\left(\operatorname{Pi}^{\wedge} 2\right) * 106.75^{*} 112^{\wedge} 4\right)\right)\right) / 30$
Input interpretation:
$\frac{1}{30}\left(\pi^{2} \times 106.75 \times 112^{4}\right)$

## Result:

$5.52610 \ldots \times 10^{9}$
5.52610... * $10^{9}$

Alternative representations:
$\frac{1}{30} \pi^{2}\left(106.75 \times 112^{4}\right)=\frac{1}{30} \times 106.75 \times 112^{4}\left(180^{\circ}\right)^{2}$
$\frac{1}{30} \pi^{2}\left(106.75 \times 112^{4}\right)=\frac{1}{30} \times 106.75 \times 112^{4}(-i \log (-1))^{2}$
$\frac{1}{30} \pi^{2}\left(106.75 \times 112^{4}\right)=\frac{1}{30} \times 640.5 \times 112^{4} \zeta(2)$

Series representations:
$\frac{1}{30} \pi^{2}\left(106.75 \times 112^{4}\right)=8.95857 \times 10^{9}\left(\sum_{k=0}^{\infty} \frac{(-1)^{k}}{1+2 k}\right)^{2}$
$\frac{1}{30} \pi^{2}\left(106.75 \times 112^{4}\right)=2.23964 \times 10^{\circ}\left(-1+\sum_{k=1}^{\infty} \frac{2^{k}}{\binom{k}{k}}\right)^{2}$
$\frac{1}{30} \pi^{2}\left(106.75 \times 112^{4}\right)=5.59911 \times 10^{8}\left(\sum_{k=0}^{\infty} \frac{2^{-k}(-6+50 k)}{\binom{3 k}{k}}\right)^{2}$

## Integral representations:

$\frac{1}{30} \pi^{2}\left(106.75 \times 112^{4}\right)=2.23964 \times 10^{\circ}\left(\int_{0}^{\infty} \frac{1}{1+t^{2}} d t\right)^{2}$

$$
\begin{aligned}
& \frac{1}{30} \pi^{2}\left(106.75 \times 112^{4}\right)=8.95857 \times 10^{9}\left(\int_{0}^{1} \sqrt{1-t^{2}} d t\right)^{2} \\
& \frac{1}{30} \pi^{2}\left(106.75 \times 112^{4}\right)=2.23964 \times 10^{9}\left(\int_{0}^{\infty} \frac{\sin (t)}{t} d t\right)^{2}
\end{aligned}
$$

Now, from the ratio between the two above results concerning the density, we obtain:
$\left(\left(\left(\left(\left(3.97428+3 * \mathrm{Pi}^{\wedge} 4 *(((((1.616252 \mathrm{e}-35)))))^{\wedge} 3^{*} 0.002^{*} 112^{\wedge} 4\right)\right) /\left(\left(\left(\left(\left((2.43 \mathrm{e}+18)^{\wedge}-\right.\right.\right.\right.\right.\right.\right.\right.$ $\left.\left.\left.\left.\left.\left.\left.\left.1))^{\wedge} 2\right)\right)\right)^{+}\left(\left(\left(\operatorname{Pi} 2^{*} 172 * 112^{\wedge} 4\right)\right)\right) / 30\right)\right)\right)\right)\right)$ * $1 /\left[\left(\left(\left((\operatorname{Pi} \wedge 2)^{*} 106.75^{*} 112^{\wedge} 4\right)\right)\right) / 30\right]$

## Input interpretation:

$$
\left(\begin{array}{l}
\left.3.97428+3 \pi^{4} \times \frac{\left(1.616252 \times 10^{-35}\right)^{3} \times 0.002 \times 112^{4}}{\left(\frac{1}{2.43 \times 10^{18}}\right)^{2}}+\frac{1}{30}\left(\pi^{2} \times 172 \times 112^{4}\right)\right) \times \\
\frac{1}{\frac{1}{30}\left(\pi^{2} \times 106.75 \times 112^{4}\right)}
\end{array}\right.
$$

## Result:

1.611241218517778813440124825329474753441482670191318098917...
$1.6112412185 \ldots$ result that is a good approximation to the golden ratio

Now, from the hypothetical dilaton mass -2.04670... * $10^{-8}$ and inserting this value in the Hawking radiation calculator, we obtain:

Mass $=-2.046700 \mathrm{e}-8$
Radius $=-3.039046 \mathrm{e}-35$
Temperature $=-5.996009 \mathrm{e}+30$
Entropy $=-4.825040$
From the Ramanujan-Nardelli mock formula, we have:
sqrt[[[[1//(((((((4*1.962364415e+19)/(5*0.0864055^2)))*1/(-2.046700e-8)* sqrt[[-$\left.\left.\left(\left(\left((-5.996009 \mathrm{e}+30) * 4 * \mathrm{Pi} *(-3.039046 \mathrm{e}-35)^{\wedge} 3-(-3.039046 \mathrm{e}-35)^{\wedge} 2\right)\right)\right)\right)\right) /$ ((6.67* $\left.\left.\left.\left.10^{\wedge}-11\right)\right)\right]\right]$ ]]]

## Input interpretation:

$$
\left.\begin{array}{l}
\sqrt{ }\left(1 /\left(\frac{4 \times 1.962364415 \times 10^{19}}{5 \times 0.0864055^{2}}\left(-\frac{1}{2.046700 \times 10^{-8}}\right)\right.\right. \\
\left.\sqrt{-\frac{-5.996009 \times 10^{30} \times 4 \pi\left(-3.039046 \times 10^{-35}\right)^{3}-\left(-3.039046 \times 10^{-35}\right)^{2}}{6.67 \times 10^{-11}}}\right)
\end{array}\right)
$$

## Result:

1.618249138019705193058637242823571021209210251498133405186...
1.618249138...i

## Polar coordinates:

$r=1.61825$ (radius), $\theta=90^{\circ}$ (angle)

And:
1/sqrt[[[[[1/(((((((4*1.962364415e+19)/(5*0.0864055^2)))*1/(-2.046700e-8)* sqrt[[-$\left.\left.\left(\left(\left((-5.996009 \mathrm{e}+30) * 4 * \mathrm{Pi}^{*}(-3.039046 \mathrm{e}-35)^{\wedge} 3-(-3.039046 \mathrm{e}-35)^{\wedge} 2\right)\right)\right)\right)\right) /\left(\left(6.67 * 10^{\wedge}-\right.\right.$ 11))]]]]]

## Input interpretation:

$$
\begin{aligned}
& 1 /\left(\sqrt { } \left(1 /\left(\frac{4 \times 1.962364415 \times 10^{19}}{5 \times 0.0864055^{2}}\left(-\frac{1}{2.046700 \times 10^{-8}}\right)\right.\right.\right. \\
& \sqrt{ }\left(-\frac{1}{6.67 \times 10^{-11}}\left(-5.996009 \times 10^{30} \times 4 \pi\left(-3.039046 \times 10^{-35}\right)^{3}-\right.\right. \\
& \left.\left.\left.\left.\left.\left(-3.039046 \times 10^{-35}\right)^{2}\right)\right)\right)\right)\right)
\end{aligned}
$$

## Result:

- 0.617952... i
-0.617952...i
Polar coordinates:
$r=0.617952$ (radius), $\theta=-90^{\circ}$ (angle)

Practically the values obtained, very near to the golden ratio and his conjugate, are imaginary. Further we note that, dividing the two results, we have:
(1.618249138019705193058637242823571021209210251498133 i) / (-
0.61795181996742898316724180900023935130532671541476 i)

## Input interpretation:

$1.618249138019705193058637242823571021209210251498133 i$
$0.61795181996742898316724180900023935130532671541476 i$

## Result:

-2.61873027270151886736291489794135914768425940438548034971...
$-2.61873027 \ldots$ result that is very near to the square of the golden ratio with minus sign.

Then, multiplying by $i^{2}$, dividing the value about equal to the golden ratio and the corresponding reciprocal and performing the square root, we obtain:
sqrt(i^2(1.618249138019705193058637242823571021209210251498133 i) / (0.61795181996742898316724180900023935130532671541476 i))

## Input interpretation:

$$
\sqrt{i^{2}\left(-\frac{1.618249138019705193058637242823571021209210251498133 i}{0.61795181996742898316724180900023935130532671541476 i}\right)}
$$

## Result:

1.6182491380197051930586372428235710212092102514981...
$1.618249138 \ldots$ a result practically about equal to the golden ratio

Now, we have that for

$$
\begin{aligned}
& \mathrm{m}=10.326 ; \alpha=2((2+2) /(1+2 * 2))^{\wedge} 3=1.024 \quad \beta=2^{\wedge} 3 *(2+2) /(1+2 * 2)=6.4 \\
& 1-\alpha=(1+2)((1-2) /(1+2 * 2))^{\wedge} 3=-0.024 \quad 1-\beta=(1+2)^{\wedge} 3^{*}((1-2) /(1+2 * 2))=-5.4
\end{aligned}
$$

we obtain:

```
\sqrt{2}{\alpha(1-\beta)}+\sqrt{4}{\beta(1-\alpha)}=\sqrt{4}{4}\sqrt{24}{\alphaa(1-\alpha)(1-\beta)}
```

$$
4^{\wedge}(1 / 3)^{*}\left(\left(\left(\left(1.024^{*} 6.4(-0.024)(-5.4)\right)\right)^{\wedge} 1 / 24\right.\right.
$$

## Input:

$\sqrt[3]{4} \sqrt[24]{1.024 \times 6.4 \times(-0.024) \times(-5.4)}$

## Result:

$1.576637562905021964928635001344279037261094502770738445866 \ldots$
1.5766375629...

And:
$1+1 /\left(\left(\left(\left(4^{\wedge}(1 / 3) *\left(\left(\left(\left(1.024^{*} 6.4(-0.024)(-5.4)\right)\right)\right)\right)^{\wedge} 1 / 24\right)\right)\right)\right)$

## Input:

$1+\frac{1}{\sqrt[3]{4} \sqrt[24]{1.024 \times 6.4 \times(-0.024) \times(-5.4)}}$

## Result:

1.634261...
$1.634261 \ldots \approx \zeta(2)=\frac{\pi^{2}}{6}=1.644934 \ldots$
$\left.\left.\left(\left(\left(\left(1 /\left(\left(\left(\left(4^{\wedge}(1 / 3) *(((1.024 * 6.4(-0.024)(-5.4))))\right)^{\wedge} 1 / 24\right)\right)\right)\right)\right)\right)\right)\right)\right)^{\wedge} 1 / 64$

## Input:

$\sqrt[64]{\sqrt[3]{4} \sqrt[24]{1.024 \times 6.4 \times(-0.024) \times(-5.4)}}$

## Result:

0.992911269...
0.992911269 .
result very near to the value of the following Rogers-Ramanujan continued fraction:
$\frac{\mathrm{e}^{-\frac{\pi}{\sqrt{5}}}}{\frac{\sqrt{5}}{1+\sqrt[5]{\sqrt{\varphi^{5} \sqrt[4]{5^{3}}}-1}}-\varphi+1}=1-\frac{\mathrm{e}^{-\pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-2 \pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-3 \pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-4 \pi \sqrt{5}}}{1+\ldots}}} \approx 0.9991104684 .1 \text {, }}$
and to the dilaton value $\mathbf{0 . 9 8 9 1 1 7 3 5 2 2 4 3}=\boldsymbol{\phi}$

Now, we have that:

$\left(\left((-5.4)^{\wedge} 7 /(-0.024)\right)\right)^{\wedge} 1 / 8+\left(\left(6.4^{\wedge} 7 / 1.024\right)\right)^{\wedge} 1 / 8+2\left(\left(\left(\left(6.4^{\wedge} 7 *(-5.4)^{\wedge} 7\right)\right)\right) /(((1.024)(-\right.$ $0.024))))^{\wedge} 1 / 24$

## Input:

$\sqrt[8]{-\frac{(-5.4)^{7}}{0.024}}+\sqrt[8]{\frac{6.4^{7}}{1.024}}+2 \sqrt[24]{\frac{6.4^{7}(-5.4)^{7}}{1.024 \times(-0.024)}}$

## Result:

18.5901...
18.5901...
$\left(\left(\left(-0.024^{\wedge} 7 /(-5.4)\right)\right)^{\wedge} 1 / 8+\left(\left(1.024^{\wedge} 7 / 6.4\right)\right)^{\wedge} 1 / 8+2\left(\left(\left(\left(1.024^{\wedge} 7^{*}(-0.024)^{\wedge} 7\right)\right)\right) /(((6.4)(-\right.\right.$ $5.4))))^{\wedge} 1 / 24$

## Input:

$\sqrt[8]{\frac{-0.024^{7}}{-5.4}}+\sqrt[8]{\frac{1.024^{7}}{6.4}}+2 \sqrt[24]{\frac{1.024^{7}(-0.024)^{7}}{6.4 \times(-5.4)}}$

## Result:

1.42598...
1.42598...

We obtain also:
$\left(\left(\left(\left(\left(1 / 18.5901\left(\left(\left(\left(\left(\left(\left(-0.024^{\wedge} 7 /(-5.4)\right)\right)\right)^{\wedge} 1 / 8+\left(\left(1.024^{\wedge} 7 / 6.4\right)\right)^{\wedge} 1 / 8+2\left(\left(\left(\left(1.024^{\wedge} 7^{*}(-\right.\right.\right.\right.\right.\right.\right.\right.\right.\right.\right.\right.\right.$ $\left.\left.\left.\left.\left.\left.\left.\left.\left.\left.\left.\left.\left.\left.0.024)^{\wedge} 7\right)\right)\right) /(((6.4)(-5.4)))\right)^{\wedge} 1 / 24\right)\right)\right)\right)\right)\right)\right)\right)\right)\right)^{\wedge} 1 / 256$

Input interpretation:
$\sqrt[256]{\frac{1}{18.5901}\left(\sqrt[8]{\frac{-0.024^{7}}{-5.4}}+\sqrt[8]{\frac{1.024^{7}}{6.4}}+2 \sqrt[24]{\frac{1.024^{7}(-0.024)^{7}}{6.4 \times(-5.4)}}\right), ~}$

## Result:

0.99001977...
$0.99001977 \ldots$. result very near to the value of the following Rogers-Ramanujan continued fraction:
$\frac{\mathrm{e}^{-\frac{\pi}{\sqrt{5}}}}{\frac{\sqrt{5}}{1+\sqrt[5]{\sqrt{\varphi^{5 \sqrt[4]{5^{3}}}}-1}}-\varphi+1}=1-\frac{\mathrm{e}^{-\pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-2 \pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-3 \pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-4 \pi \sqrt{5}}}{1+\ldots}}}} \approx 0.9991104684$
and to the dilaton value $\mathbf{0 . 9 8 9 1 1 7 3 5 2 2 4 3}=\boldsymbol{\phi}$

And:
$\left(\left(\left(\left(\left(1 / 18.5901\left(\left(\left(\left(\left(\left(\left(-0.024^{\wedge} 7 /(-5.4)\right)\right)\right)^{\wedge} 1 / 8+\left(\left(1.024^{\wedge} 7 / 6.4\right)\right)^{\wedge} 1 / 8+2\left(\left(\left(\left(1.024^{\wedge} 7^{*}(-\right.\right.\right.\right.\right.\right.\right.\right.\right.\right.\right.\right.\right.$ $\left.\left.\left.\left.\left.\left.\left.\left.\left.\left.\left.\left.\left.\left.0.024)^{\wedge} 7\right)\right)\right) /(((6.4)(-5.4)))\right)^{\wedge} 1 / 24\right)\right)\right)\right)\right)\right)\right)\right)\right)\right)^{\wedge} 1 / 48$

Input interpretation:
$\sqrt[48]{\frac{1}{18.5901}}\left(\sqrt[8]{\frac{-0.024^{7}}{-5.4}}+\sqrt[8]{\frac{1.024^{7}}{6.4}}+2 \sqrt[24]{\frac{1.024^{7}(-0.024)^{7}}{6.4 \times(-5.4)}}\right)$

## Result:

$0.947910419044673998026989135739103499438017025774530098451 \ldots$
$0.9479104190446 \ldots$ result very near to the value of the following RogersRamanujan continued fraction:

$$
\frac{\mathrm{e}^{-\frac{\pi}{5}}}{\sqrt{(\varphi-1) \sqrt{5}}-\varphi+1}=1-\frac{\mathrm{e}^{-\pi}}{1+\frac{\mathrm{e}^{-2 \pi}}{1+\frac{\mathrm{e}^{-3 \pi}}{1+\frac{\mathrm{e}^{-4 \pi}}{1+\ldots}}}} \approx 0.9568666373
$$

Now, we have that:

$\alpha=2\left((2+2) /\left(1+2^{*} 2\right)\right)^{\wedge} 3=1.024 \quad \beta=2^{\wedge} 3^{*}(2+2) /(1+2 * 2)=6.4$
$1-\alpha=(1+2)((1-2) /(1+2 * 2))^{\wedge} 3=-0.024 \quad 1-\beta=(1+2)^{\wedge} 3 *((1-2) /(1+2 * 2))=-5.4$
$\left.(1.024 / 6.4)^{\wedge} 1 / 4+(((-0.024) /(-5.4)))^{\wedge} 1 / 4+\left(\left(\left(\left(\left(1.024^{*}(-0.024)\right)\right) /\left(6.4^{*}(-5.4)\right)\right)^{\wedge} 1 / 4\right)\right)\right)-$ $2^{*}\left(\left(\left(\left(\left(1.024^{*}(-0.024)\right) /\left(6.4^{*}(-5.4)\right)\right)^{\wedge} 1 / 8\right)\right)\right)^{*}\left(1+(1.024 / 6.4)^{\wedge} 1 / 8+(((-0.024) /(-\right.$ 5.4)) $\left.)^{\wedge} 1 / 8\right)$ )

## Input:

$$
\begin{aligned}
& \sqrt[4]{\frac{1.024}{6.4}}+\sqrt[4]{\frac{-0.024}{-5.4}}+\sqrt[4]{\frac{1.024 \times(-0.024)}{6.4 \times(-5.4)}}- \\
& 2 \sqrt[8]{\frac{1.024 \times(-0.024)}{6.4 \times(-5.4)}}\left(1+\sqrt[8]{\frac{1.024}{6.4}}+\sqrt[8]{\frac{-0.024}{-5.4}}\right)
\end{aligned}
$$

## Result:

```
-0.80767123749212493469212082989238224653083927608658642345\ldots.
-0.807671237492....
```

And:
$-2^{*}\left(\left(\left(\left(()\left((1.024 / 6.4)^{\wedge} 1 / 4+(((-0.024) /(-5.4)))^{\wedge} 1 / 4+\left(\left(\left(\left(\left(1.024^{*}(-0.024)\right)\right) /\left(6.4^{*}(-\right.\right.\right.\right.\right.\right.\right.\right.\right.$ $\left.\left.\left.5.4)))^{\wedge} 1 / 4\right)\right)\right)-2^{*}\left(\left(\left(\left(\left(1.024^{*}(-0.024)\right) /\left(6.4^{*}(-5.4)\right)\right)^{\wedge} 1 / 8\right)\right)\right)^{*}\left(1+(1.024 / 6.4)^{\wedge} 1 / 8+(((-\right.$ $\left.\left.\left.0.024)((-5.4)))^{\wedge} 1 / 8\right)\right)\right)$ )) )) ))

## Input:

$$
\begin{aligned}
-2\left(\sqrt[4]{\frac{1.024}{6.4}}+\sqrt[4]{\frac{-0.024}{-5.4}}+\sqrt[4]{\frac{1.024 \times(-0.024)}{6.4 \times(-5.4)}}-\right. \\
\left.\quad 2 \sqrt[8]{\frac{1.024 \times(-0.024)}{6.4 \times(-5.4)}}\left(1+\sqrt[8]{\frac{1.024}{6.4}}+\sqrt[8]{\frac{-0.024}{-5.4}}\right)\right)
\end{aligned}
$$

## Result:

$1.615342474984249869384241659784764493061678552173172846908 \ldots$
1.61534247498....

This result is a good approximation to the value of the golden ratio 1,618033988749
$\left(\left(\left(\left(()\left(\left((1.024 / 6.4)^{\wedge} 1 / 4+(((-0.024) /(-5.4)))\right)^{\wedge} 1 / 4+\left(\left(\left(\left(\left(1.024^{*}(-0.024)\right)\right) /\left(6.4^{*}(-\right.\right.\right.\right.\right.\right.\right.\right.\right.$
$\left.\left.\left.5.4)))^{\wedge} 1 / 4\right)\right)\right)-2^{*}\left(\left(\left(\left(\left(1.024^{*}(-0.024)\right) /\left(6.4^{*}(-5.4)\right)\right)^{\wedge} 1 / 8\right)\right)\right)^{*}\left(1+(1.024 / 6.4)^{\wedge} 1 / 8+(((-\right.$ $\left.\left.\left.\left.\left.\left.\left.\left.\left.0.024)(-5.4)))^{\wedge} 1 / 8\right)\right)\right)\right)\right)\right)\right)\right)\right)^{\wedge} 1 / 5$

## Input:

$$
\begin{aligned}
& \left(\sqrt[4]{\frac{1.024}{6.4}}+\sqrt[4]{\frac{-0.024}{-5.4}}+\sqrt[4]{\frac{1.024 \times(-0.024)}{6.4 \times(-5.4)}}-\right. \\
& \left.28 \sqrt[8]{\frac{1.024 \times(-0.024)}{6.4 \times(-5.4)}}\left(1+\sqrt[8]{\frac{1.024}{6.4}}+\sqrt[8]{\frac{-0.024}{-5.4}}\right)\right) \wedge(1 / 5)
\end{aligned}
$$

## Result:

0.775184... +
0.563204...

## Polar coordinates:

$r=0.95818$ (radius), $\theta=36^{\circ}$ (angle)
0.95818 result very near to the spectral index $\mathrm{n}_{\mathrm{s}}$ and to the mesonic Regge slope (see Appendix) and to the inflaton value at the end of the inflation 0.9402

Now, we have that:

## VII - here $\sqrt{\alpha \beta}+\sqrt{G \alpha)(1-\alpha)}+20 \sqrt[4]{\alpha 0(1-\alpha)(1-\alpha)}$ 

$1-\mathrm{sqrt}(1.024 * 6.4)+\operatorname{sqrt}((-0.024)(-5.4))+20(((1.024 * 6.4(-0.024)(-$
$5.4))))^{\wedge} 1 / 4+8 * \operatorname{sqrt}(2)^{*}\left(\left(\left(1.024^{*} 6.4(-0.024)(-5.4)\right)\right)\right)^{\wedge} 1 / 8^{*}\left(\left(\left((1.024 * 6.4)^{\wedge} 1 / 4+(-\right.\right.\right.$ $\left.\left.0.024^{*}-5.4\right)^{\wedge} 1 / 4\right)$ ))

## Input:

$$
\begin{aligned}
& 1-\sqrt{1.024 \times 6.4}+\sqrt{-0.024 \times(-5.4)}+20 \sqrt[4]{1.024 \times 6.4 \times(-0.024) \times(-5.4)}+ \\
& \quad 8 \sqrt{2} \sqrt[8]{1.024 \times 6.4 \times(-0.024) \times(-5.4)}(\sqrt[4]{1.024 \times 6.4}+\sqrt[4]{-0.024 \times(-5.4)})
\end{aligned}
$$

## Result:

$42.38727537056979229286644448840268292655469797365015924302 \ldots$
42.387275370569...
$((()((1-\mathrm{sqrt}(1.024 * 6.4)+\operatorname{sqrt}((-0.024)(-5.4))+20(((1.024 * 6.4(-0.024)(-$
$5.4))))^{\wedge} 1 / 4+8 * \operatorname{sqrt}(2)^{*}(((1.024 * 6.4(-0.024)(-5.4))))^{\wedge} 1 / 8 *\left(\left(\left((1.024 * 6.4)^{\wedge} 1 / 4+(-\right.\right.\right.$ $\left.\left.\left.\left.\left.\left.\left.\left.\left.\left.0.024^{*}-5.4\right)^{\wedge} 1 / 4\right)\right)\right)\right)\right)\right)\right)\right)\right)^{\wedge} 3-(4096-1729+17 \wedge 2+8)$

Where $17^{2}=289=322-29-4$ that are Lucas numbers and 1729 is the HardyRamanujan number

## Input:

$$
\begin{aligned}
& (1-\sqrt{1.024 \times 6.4}+\sqrt{-0.024 \times(-5.4)}+ \\
& \quad 20 \sqrt[4]{1.024 \times 6.4 \times(-0.024) \times(-5.4)}+8 \sqrt{2} \sqrt[8]{1.024 \times 6.4 \times(-0.024) \times(-5.4)} \\
& \quad(\sqrt[4]{1.024 \times 6.4}+\sqrt[4]{-0.024 \times(-5.4)}))^{3}-\left(4096-1729+17^{2}+8\right)
\end{aligned}
$$

## Result:

73492.4...
73492.4...

Thence, we have the following mathematical connections:

$$
\binom{I_{21} \ll \int_{-\infty}^{+\infty} \exp \left(-\left(\frac{t}{H}\right)^{2}\right)\left|\sum_{\lambda \leqslant P^{1-e_{2}}} \frac{a(\lambda)}{\sqrt{\lambda}} B(\lambda) \lambda^{-i(T+t)}\right|^{2} d t \ll}{<H\left\{\left(\frac{4}{\varepsilon_{2} \log T}\right)^{2 r}(\log T)(\log X)^{-2 \beta}+\left(\varepsilon_{2}^{-2 r}(\log T)^{-2 r}+\varepsilon_{2}^{-r} h_{1}^{r}(\log T)^{-r}\right) T^{-\varepsilon_{1}}\right\}},
$$

$$
/(26 \times 4)^{2}-24=\left(\frac{7.9313976505275 \times 10^{8}}{(26 \times 4)^{2}-24}\right)=73493.30662 \ldots
$$

$$
\begin{aligned}
& -3927+2 \sqrt[13]{2.2983717437 \times 10^{59}+2.0823329825883 \times 10^{59}} \\
& =73490.8437525 \ldots \Rightarrow \\
& \Rightarrow\left(A(r) \times \frac{1}{B(r)}\left(-\frac{1}{\phi(r)}\right) \times \frac{1}{e^{\Lambda(r)}}\right) \Rightarrow \\
& \Rightarrow\left(-0.000029211892 \times \frac{1}{0.0003644621}\left(-\frac{1}{0.0005946833}\right) \times \frac{1}{0.00183393}\right)= \\
& =73491.78832548118710549159572042220548025195726563413398700 \ldots \\
& =73491.7883254 \ldots \Rightarrow
\end{aligned}
$$

Mathematical connections with the boundary state corresponding to the NSNS-sector of N Dp-branes in the limit of $\mathrm{u} \rightarrow \infty$, with the ratio concerning the general asymptotically flat solution of the equations of motion of the p-brane and with the Karatsuba's equation concerning the zeros of a special type of function connected with Dirichlet series.
$((((() 1-\mathrm{sqrt}(1.024 * 6.4)+\operatorname{sqrt}((-0.024)(-5.4))+20(((1.024 * 6.4(-0.024)(-$
$5.4))))^{\wedge} 1 / 4+8 * \operatorname{sqrt}(2)^{*}(((1.024 * 6.4(-0.024)(-5.4))))^{\wedge} 1 / 8 *\left(\left(\left((1.024 * 6.4)^{\wedge} 1 / 4+(-\right.\right.\right.$ $\left.\left.\left.\left.\left.\left.\left.\left.\left.0.024^{*}-5.4\right)^{\wedge} 1 / 4\right)\right)()\right)\right)\right)\right)\right)\right)^{\wedge} 2-\left(34^{*} 2\right)$

Where 34 and 2 are Fibonacci numbers

## Input:

$$
\begin{aligned}
& (1-\sqrt{1.024 \times 6.4}+\sqrt{-0.024 \times(-5.4)}+ \\
& \quad 20 \sqrt[4]{1.024 \times 6.4 \times(-0.024) \times(-5.4)}+8 \sqrt{2} \sqrt[8]{1.024 \times 6.4 \times(-0.024) \times(-5.4)} \\
& (\sqrt[4]{1.024 \times 6.4}+\sqrt[4]{-0.024 \times(-5.4)}))^{2}-34 \times 2
\end{aligned}
$$

## Result:

1728.68...
1728.68...

This result is very near to the mass of candidate glueball $\mathrm{f}_{0}(1710)$ meson. Furthermore, 1728 occurs in the algebraic formula for the $j$-invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the GrossZagier theorem. The number 1728 is one less than the Hardy-Ramanujan number 1729
$\operatorname{Pi}(((()(1-\mathrm{sqrt}(1.024 * 6.4)+\operatorname{sqrt}((-0.024)(-5.4))+20(((1.024 * 6.4(-0.024)(-$
$5.4))))^{\wedge} 1 / 4+8 * \operatorname{sqrt}(2)^{*}(((1.024 * 6.4(-0.024)(-5.4))))^{\wedge} 1 / 8 *\left(\left(\left((1.024 * 6.4)^{\wedge} 1 / 4+(-\right.\right.\right.$ $\left.\left.\left.\left.\left.\left.0.024^{*}-5.4\right)^{\wedge} 1 / 4\right)\right)\right)\right)\right)$ )) )) +1

Input:

$$
\begin{gathered}
\pi(1-\sqrt{1.024 \times 6.4}+\sqrt{-0.024 \times(-5.4)}+20 \sqrt[4]{1.024 \times 6.4 \times(-0.024) \times(-5.4)}+8 \sqrt{2} \\
\sqrt[8]{1.024 \times 6.4 \times(-0.024) \times(-5.4)}(\sqrt[4]{1.024 \times 6.4}+\sqrt[4]{-0.024 \times(-5.4)}))+1
\end{gathered}
$$

## Result:

134.164...
134.164... result very near to the rest mass of Pion meson 134.9766

## Series representations:

$$
\begin{aligned}
& \pi(1-\sqrt{1.024 \times 6.4}+\sqrt{-0.024(-5.4)}+ \\
& \left.\quad \begin{array}{r}
20 \sqrt[4]{1.024 \times 6.4(-0.024)(-5.4)}+8 \sqrt{2} \sqrt[8]{1.024 \times 6.4(-0.024)(-5.4)} \\
(\sqrt[4]{1.024 \times 6.4}+\sqrt[4]{-0.024(-5.4)}))+1
\end{array}\right)+1+20.2 \pi+
\end{aligned} \quad \begin{aligned}
& \sum_{k=0}^{\infty} \frac{(-1)^{k} \pi\left(-\frac{1}{2}\right)_{k} \sqrt{z_{0}\left(\left(0.1296-z_{0}\right)^{k}+17.2444\left(2-z_{0}\right)^{k}-\left(6.5536-z_{0}\right)^{k}\right) z_{0}^{-k}}}{k!} \\
& \text { for } \operatorname{not}\left(\left(z_{0} \in \mathbb{R} \text { and }-\infty<z_{0} \leq 0\right)\right)
\end{aligned}
$$

$$
\begin{array}{r}
\pi(1-\sqrt{1.024 \times 6.4}+\sqrt{-0.024(-5.4)}+20 \sqrt[4]{1.024 \times 6.4(-0.024)(-5.4)}+ \\
8 \sqrt{2} \sqrt[8]{1.024 \times 6.4(-0.024)(-5.4)}(\sqrt[4]{1.024 \times 6.4}+\sqrt[4]{-0.024(-5.4)}))+ \\
1=1+20.2 \pi+\sum_{k=0}^{\infty} \frac{1}{k!}(-1)^{k} \pi x^{-k}\left((0.1296-x)^{k} \exp \left(i \pi \left\lvert\, \frac{\arg (0.1296-x)}{2 \pi}\right.\right]\right)+ \\
\left.17.2444(2-x)^{k} \exp \left(i \pi \left\lvert\, \frac{\arg (2-x)}{2 \pi}\right.\right]\right)-(6.5536-x)^{k} \\
\left.\quad \exp \left(i \pi\left[\frac{\arg (6.5536-x)}{2 \pi}\right]\right)\right)\left(-\frac{1}{2}\right)_{k} \sqrt{x} \text { for }(x \in \mathbb{R} \text { and } x<0) \\
\pi(1-\sqrt{1.024 \times 6.4}+\sqrt{-0.024(-5.4)}+20 \sqrt[4]{1.024 \times 6.4(-0.024)(-5.4)}+ \\
8 \sqrt{2} \sqrt[8]{1.024 \times 6.4(-0.024)(-5.4)}(\sqrt[4]{1.024 \times 6.4}+\sqrt[4]{-0.024(-5.4)}))+ \\
1=1+ \\
20.2 \pi+\sum_{k=0}^{\infty}\left(\frac{1}{k!}(-1)^{k} \pi\left(-\frac{1}{2}\right)_{k}\left(0.1296-z_{0}\right)^{k}\right. \\
\left(\frac{1}{z_{0}}\right)^{1 / 2\left\lfloor\arg \left(0.1296-z_{0}\right) /(2 \pi)\right\rfloor} z_{0}^{-k+1 / 2\left(1+\left\lfloor\arg \left(0.1296-z_{0}\right) /(2 \pi)\right\rfloor\right)}+ \\
17.2444(-1)^{k} \pi\left(-\frac{1}{2}\right)_{k}\left(2-z_{0}\right)^{k}\left(\frac{1}{z_{0}}\right)^{1 / 2\left\lfloor\arg \left(2-z_{0}\right) /(2 \pi)\right\rfloor} z_{0}^{-k+1 / 2\left(1+\left\lfloor\arg \left(2-z_{0}\right) /(2 \pi)\right\rfloor\right)} \\
\quad \\
\frac{1}{k!}(-1)^{1+k} \pi\left(-\frac{1}{2}\right)_{k}\left(6.5536-z_{0}\right)^{k} \\
\left(\frac{1}{z_{0}}\right)^{1 / 2\left\lfloor\arg \left(6.5536-z_{0}\right) /(2 \pi)\right\rfloor} z_{0}^{-k+1 / 2\left(1+\left\lfloor\arg \left(6.5536-z_{0}\right) /(2 \pi)\right\rfloor\right)}+
\end{array}
$$

$\operatorname{Pi}(((((1-\mathrm{sqrt}(1.024 * 6.4)+\mathrm{sqrt}((-0.024)(-5.4))+20(((1.024 * 6.4(-0.024))(-$
$5.4))))^{\wedge} 1 / 4+8 * \operatorname{sqrt}(2)^{*}\left(\left(\left(1.024^{*} 6.4(-0.024)(-5.4)\right)\right)\right)^{\wedge} 1 / 8^{*}\left(\left(\left(\left(1.024^{*} 6.4\right)^{\wedge} 1 / 4+(-\right.\right.\right.$ $\left.\left.\left.0.024^{*}-5.4\right)^{\wedge} 1 / 4\right)\right)$ )) )) )) ) +4

Where 4 is a Lucas number

## Input:

$$
\begin{gathered}
\pi(1-\sqrt{1.024 \times 6.4}+\sqrt{-0.024 \times(-5.4)}+20 \sqrt[4]{1.024 \times 6.4 \times(-0.024) \times(-5.4)}+8 \sqrt{2} \\
\sqrt[8]{1.024 \times 6.4 \times(-0.024) \times(-5.4)}(\sqrt[4]{1.024 \times 6.4}+\sqrt[4]{-0.024 \times(-5.4)}))+4
\end{gathered}
$$

## Result:

137.164...
137.164... result very near to the mean of the rest masses of two Pion mesons 134.9766 and 139.57 that is 137.2733 and to the inverse of fine-structure constant 137,035

## Series representations:

$$
\begin{aligned}
& \pi(1-\sqrt{1.024 \times 6.4}+\sqrt{-0.024(-5.4)}+ \\
& \quad \begin{array}{r}
20 \sqrt[4]{1.024 \times 6.4(-0.024)(-5.4)}+8 \sqrt{2} \sqrt[8]{1.024 \times 6.4(-0.024)(-5.4)} \\
(\sqrt[4]{1.024 \times 6.4}+\sqrt[4]{-0.024(-5.4)}))+4=4+20.2 \pi+
\end{array} \\
& \quad \sum_{k=0}^{\infty} \frac{(-1)^{k} \pi\left(-\frac{1}{2}\right)_{k} \sqrt{z_{0}\left(\left(0.1296-z_{0}\right)^{k}+17.2444\left(2-z_{0}\right)^{k}-\left(6.5536-z_{0}\right)^{k}\right) z_{0}^{-k}}}{k!} \\
& \text { for } \operatorname{not}\left(\left(z_{0} \in \mathbb{R} \text { and }-\infty<z_{0} \leq 0\right)\right)
\end{aligned}
$$

$$
\begin{gathered}
\pi(1-\sqrt{1.024 \times 6.4}+\sqrt{-0.024(-5.4)}+20 \sqrt[4]{1.024 \times 6.4(-0.024)(-5.4)}+ \\
8 \sqrt{2} \sqrt[8]{1.024 \times 6.4(-0.024)(-5.4)}(\sqrt[4]{1.024 \times 6.4}+\sqrt[4]{-0.024(-5.4)}))+ \\
4=4+20.2 \pi+\sum_{k=0}^{\infty} \frac{1}{k!}(-1)^{k} \pi x^{-k}\left((0.1296-x)^{k} \exp \left(i \pi \left\lvert\, \frac{\arg (0.1296-x)}{2 \pi}\right.\right]\right)+ \\
\left.17.2444(2-x)^{k} \exp \left(i \pi \left\lvert\, \frac{\arg (2-x)}{2 \pi}\right.\right\rfloor\right)-(6.5536-x)^{k} \\
\exp \left(i \pi\left\lfloor\frac{\arg (6.5536-x)}{2 \pi}\right]\right)\left(-\frac{1}{2}\right)_{k} \sqrt{x} \text { for }(x \in \mathbb{R} \text { and } x<0)
\end{gathered}
$$

$$
\begin{aligned}
& \pi(1-\sqrt{1.024 \times 6.4}+\sqrt{-0.024(-5.4)}+20 \sqrt[4]{1.024 \times 6.4(-0.024)(-5.4)}+ \\
& 8 \sqrt{2} \sqrt[8]{1.024 \times 6.4(-0.024)(-5.4)}(\sqrt[4]{1.024 \times 6.4}+\sqrt[4]{-0.024(-5.4)}))+ \\
& 4=4+20.2 \pi+\sum_{k=0}^{\infty} \frac{1}{k!}(-1)^{k} \pi\left(-\frac{1}{2}\right)_{k} z_{0}^{1 / 2-k} \\
& \left(\left(0.1296-z_{0}\right)^{k}\left(\frac{1}{z_{0}}\right)^{1 / 2\left\lfloor\arg \left(0.1296-z_{0}\right) /(2 \pi)\right\rfloor} z_{z_{0} / 2\left\lfloor\arg \left(0.1296-z_{0}\right) /(2 \pi)\right\rfloor}^{1}+\right. \\
& 17.2444\left(2-z_{0}\right)^{k}\left(\frac{1}{z_{0}}\right)^{1 / 2\left\lfloor\arg \left(2-z_{0}\right) /(2 \pi)\right\rfloor} z_{0}^{1 / 2\left\lfloor\arg \left(2-z_{0}\right) /(2 \pi)\right\rfloor}- \\
& \left.\left(6.5536-z_{0}\right)^{k}\left(\left(\frac{1}{z_{0}}\right)^{1 / 2\left\lfloor\arg \left(6.5536-z_{0}\right) /(2 \pi)\right\rfloor} z_{0}^{1 / 2\left\lfloor\arg \left(6.5536-z_{0}\right) /(2 \pi)\right\rfloor}\right)\right)
\end{aligned}
$$

## X1 degree. $\sqrt{\text { ( } \beta}+\sqrt{(1-\alpha)(1-a)}+68 \sqrt{\text { axi- }(1)(1-a)}$

 $+16 \sqrt{y} \sqrt{\operatorname{s}(1-\alpha)}(\sqrt[3]{क n}+\sqrt[3]{(1-x)(1-\infty)})$
$\alpha=2((2+2) /(1+2 * 2))^{\wedge} 3=1.024 \quad \beta=2^{\wedge} 3 *(2+2) /(1+2 * 2)=6.4$
$1-\alpha=(1+2)((1-2) /(1+2 * 2))^{\wedge} 3=-0.024 \quad 1-\beta=(1+2)^{\wedge} 3 *((1-2) /(1+2 * 2))=-5.4$
$\operatorname{sqrt}(1.024 * 6.4)+\operatorname{sqrt}\left(-0.024^{*}-5.4\right)+68^{*}\left(1.024^{*} 6.4^{*}-0.024^{*}-\right.$
$5.4)^{\wedge} 1 / 4+16 *\left(1.024 * 6.4 *-0.024^{*}-5.4\right)^{\wedge} 1 / 12 *\left(\left(\left(\left(1.024^{*} 6.4\right)^{\wedge} 1 / 3+\left(-0.024^{*}-\right.\right.\right.\right.$
$\left.\left.\left.5.4)^{\wedge} 1 / 3\right)\right)\right)+48^{*}\left(1.024^{*} 6.4^{*}-0.024^{*}-5.4\right)^{\wedge} 1 / 6^{*}\left(\left(\left((1.024 * 6.4)^{\wedge} 1 / 6+\left(-0.024^{*}-\right.\right.\right.\right.$ $\left.5.4)^{\wedge} 1 / 6\right)$ ))
$16 *\left(1.024^{*} 6.4^{*}-0.024^{*}-5.4\right)^{\wedge} 1 / 12 *\left(\left(\left(\left(1.024^{*} 6.4\right)^{\wedge} 1 / 3+\left(-0.024^{*}-\right.\right.\right.\right.$
$\left.\left.\left.5.4)^{\wedge} 1 / 3\right)\right)\right)+48^{*}\left(1.024^{*} 6.4^{*}-0.024^{*}-5.4\right)^{\wedge} 1 / 6^{*}\left(\left(\left((1.024 * 6.4)^{\wedge} 1 / 6+\left(-0.024^{*}-\right.\right.\right.\right.$ $\left.5.4)^{\wedge} 1 / 6\right)$ )

## Input:

```
\(16 \sqrt[12]{1.024 \times 6.4 \times(-0.024) \times(-5.4)}(\sqrt[3]{1.024 \times 6.4}+\sqrt[3]{-0.024 \times(-5.4)})+\)
    \(48 \sqrt[6]{1.024 \times 6.4 \times(-0.024) \times(-5.4)}(\sqrt[6]{1.024 \times 6.4}+\sqrt[6]{-0.024 \times(-5.4)})\)
```


## Result:

$134.6543982 \ldots$... result very near to the rest mass of Pion meson 134.9766

```
sqrt(1.024*6.4)+sqrt(-0.024*-5.4)+68*(1.024*6.4*-0.024*-
5.4)^1/4+134.65439822445221899679646313495888823864870247559167
```


## Input interpretation:

```
\(\sqrt{1.024 \times 6.4}+\sqrt{-0.024 \times(-5.4)}+68 \sqrt[4]{1.024 \times 6.4 \times(-0.024) \times(-5.4)}+\)
    134.65439822445221899679646313495888823864870247559167
```


## Result:

Final result:
202.85439822445221899679646313495888823864870247559167
202.8543982.....

377(((()sqrt(1.024*6.4)+sqrt(-0.024*-5.4)+68*(1.024*6.4*-0.024*-
$\left.\left.\left.\left.5.4)^{\wedge} 1 / 4+134.6543982244522189\right)\right)\right)\right)$ )-(2048+1024-64-24)
Where 377 is a Fibonacci number

## Input interpretation:

```
\(377(\sqrt{1.024 \times 6.4}+\sqrt{-0.024 \times(-5.4)}+68 \sqrt[4]{1.024 \times 6.4 \times(-0.024) \times(-5.4)}+\)
    \(134.6543982244522189)-(2048+1024-64-24)\)
```


## Result:

73492.1081306184865253
73492.10813....

Thence, we have the following mathematical connections:

$$
\binom{377(\sqrt{1.024 \times 6.4}+\sqrt{-0.024 \times(-5.4)}+68 \sqrt[4]{1.024 \times 6.4 \times(-0.024) \times(-5.4)}+}{134.6543982244522189)-(2048+1024-64-24)}=73492.108 \Rightarrow
$$

$$
\begin{aligned}
& \Rightarrow-3927+2\left(\begin{array}{l}
13\binom{N \exp \left[\int d \hat{\sigma}\left(-\frac{1}{4 u^{2}} P_{i} D \mathbf{P}_{i}\right)\right]|B p\rangle_{\mathrm{NS}}+}{\int\left[d \mathrm{X}^{\mu}\right] \exp \left\{\int d \hat{\sigma}\left(-\frac{1}{4 v^{2}} D \mathrm{X}^{\mu} D^{2} \mathrm{X}^{\mu}\right)\right\}\left|\mathrm{X}^{\mu}, \mathrm{X}^{i}=0\right\rangle_{\mathrm{NS}}}= \\
\\
-3927+2 \sqrt[13]{2.2983717437 \times 10^{59}+2.0823329825883 \times 10^{59}} \\
=73490.8437525 \ldots \Rightarrow \\
\Rightarrow\left(A(r) \times \frac{1}{B(r)}\left(-\frac{1}{\phi(r)}\right) \times \frac{1}{e^{\Lambda(r)}}\right) \Rightarrow \\
\Rightarrow\left(-0.000029211892 \times \frac{1}{0.0003644621}\left(-\frac{1}{0.0005946833}\right) \times \frac{1}{0.00183393}\right)= \\
=73491.78832548118710549159572042220548025195726563413398700 \ldots
\end{array}\right. \\
& =73491.7883254 \ldots \Rightarrow
\end{aligned}
$$

$$
\binom{I_{21} \leqslant \int_{-\infty}^{+\infty} \exp \left(-\left(\frac{t}{H}\right)^{2}\right)\left|\sum_{\lambda \leqslant P^{1-\varepsilon_{2}}} \frac{a(\lambda)}{\sqrt{\lambda}} B(\lambda) \lambda^{-i\left(T^{r}+t\right)}\right|^{2} d t \leqslant}{\leqslant H\left\{\left(\frac{4}{\varepsilon_{2} \log T}\right)^{2 r}(\log T)(\log X)^{-2 \beta}+\left(\varepsilon_{2}^{-2 r}(\log T)^{-2 r}+\varepsilon_{2}^{-r} h_{1}^{r}(\log T)^{-r}\right) T^{-\varepsilon_{1}}\right\}} /, ~\left(\frac{7.9313976505275 \times 10^{8}}{(26 \times 4)^{2}-24}\right)=73493.30662 \ldots .
$$

Mathematical connections with the boundary state corresponding to the NSNS-sector of N Dp-branes in the limit of $u \rightarrow \infty$, with the ratio concerning the general asymptotically flat solution of the equations of motion of the p-brane and with the Karatsuba's equation concerning the zeros of a special type of function connected with Dirichlet series.

Now, we have that:

$$
\begin{aligned}
& \text { F. } \frac{1-\sqrt{1-t^{2} 4}}{2}=e^{-\pi \sqrt{29}} \text {. The } \\
& t^{74}+9 t^{20}+5 t^{16}-2 t^{12}-5 t^{8}+9 t^{4}-1=0 \\
& \quad \frac{t^{6}+t^{2}}{1-t^{4}}=\sqrt{\frac{\sqrt{29}-5}{2}} \\
& \quad \frac{t^{3}+t \sqrt{\sqrt{29}-2}}{1+t^{-} \sqrt{\sqrt{29}+2}}=\sqrt[4]{\frac{\sqrt{29}-8}{2}} \\
& \text { if } \sqrt[4]{1-t^{8}}=t\left(1+u^{2}\right) \text {. Them } u^{3}+u=\sqrt{2} .
\end{aligned}
$$

$$
F \cdot \frac{1-\sqrt{1-\frac{1}{64}}{ }^{24}}{2}=e^{-71 \sqrt{79}} \text { then }
$$

$$
t^{5}-t^{4}+t^{3}-2 t^{2}+3 t-1=0
$$

$$
\begin{aligned}
& t^{5}-t^{4}+t^{3}-2 t^{2}+3 t-1-0 \\
& F 1-\frac{\sqrt{1-84}}{2}=e^{4} \\
& 4 \sqrt{47} \text {, the }
\end{aligned}
$$

$$
t^{5}+2 t^{4}+2 t^{3}+t^{2}-1=0
$$

We have the following interesting expressions:
$\exp (-\mathrm{Pi} * \operatorname{sqrt}(29)) * \operatorname{sqrt}(((((\operatorname{sqrt}(29)-5)) / 2))) *(((((\operatorname{sqrt}(29)-$
$5)) / 2)))^{\wedge} 1 / 4 *(\operatorname{sqrt}(2))^{*} 1 /(\exp (-\mathrm{Pi} * \mathrm{sqrt}(79))) * \exp (-\mathrm{Pi} * \operatorname{sqrt}(47))$

## Input:

$$
\exp (-\pi \sqrt{29}) \sqrt{\frac{1}{2}(\sqrt{29}-5)} \sqrt[4]{\frac{1}{2}(\sqrt{29}-5)} \sqrt{2} \times \frac{1}{\exp (-\pi \sqrt{79})} \exp (-\pi \sqrt{47})
$$

## Exact result:

$\frac{(\sqrt{29}-5)^{3 / 4} e^{-\sqrt{29}} \pi-\sqrt{47} \pi+\sqrt{79} \pi}{\sqrt[4]{2}}$

## Decimal approximation:

0.000010958098248039814630288664252483569745480054423680146
0.000010958098248.....

## Property:

$\frac{(-5+\sqrt{29})^{3 / 4} e^{-\sqrt{29} \pi-\sqrt{47} \pi+\sqrt{79} \pi}}{\sqrt[4]{2}}$ is a transcendental number

## Alternate form:

$\frac{\sqrt{2} e^{-\sqrt{29} \pi-\sqrt{47} \pi+\sqrt{79} \pi}}{\sqrt[4]{70+13 \sqrt{29}}}$

## Series representations:

$$
\left.\begin{array}{l}
\frac{\left(\exp (-\pi \sqrt{29}) \sqrt{\frac{1}{2}(\sqrt{29}-5)}\right) \sqrt[4]{\frac{1}{2}(\sqrt{29}-5)}(\sqrt{2} \exp (-\pi \sqrt{47}))}{\exp (-\pi \sqrt{79})}= \\
\exp \left(-\pi \sqrt{z_{0}} \sum_{k=0}^{\infty} \frac{(-1)^{k}\left(-\frac{1}{2}\right)_{k}\left(29-z_{0}\right)^{k} z_{0}^{-k}}{k!}\right) \\
\left.{\sqrt{z_{0}}}^{2} \sqrt[4]{x_{0}} \sum_{k=0}^{\infty} \frac{(-1)^{k}\left(-\frac{1}{2}\right)_{k}\left(47-z_{0}\right)^{k} z_{0}^{-k}}{k!}\right) \\
\left.\sum_{k_{1}=0}^{\infty} \sum_{k_{2}=0}^{\infty} \frac{\left.(-1)^{k_{1}+k_{2}} 2^{2_{0}^{-k_{2}}\left(-\frac{1}{2}\right)_{k_{1}}\left(-\frac{1}{2}\right)_{k_{2}}(-5+\sqrt{29}}-2 z_{0}\right)^{k_{2}}\left(2-z_{0}\right)^{k_{1}} z_{0}^{-k_{1}-k_{2}}}{k_{1}!k_{2}!}\right) \\
/\left(\sqrt[4]{2} \exp \left(-\pi \sqrt{z_{0}} \sum_{k=0}^{\infty} \frac{(-1)^{k}\left(-\frac{1}{2}\right)_{k}\left(79-z_{0}\right)^{k} z_{0}^{-k}}{k!}\right)\right.
\end{array}\right)
$$

$$
\begin{aligned}
& \frac{\left(\exp (-\pi \sqrt{29}) \sqrt{\frac{1}{2}(\sqrt{29}-5)}\right) \sqrt[4]{\frac{1}{2}(\sqrt{29}-5)}(\sqrt{2} \exp (-\pi \sqrt{47}))}{\exp (-\pi \sqrt{79})}= \\
& \left(\exp \left(i \pi\left\lfloor\frac{\arg (2-x)}{2 \pi}\right\rfloor\right) \exp \left(i \pi\left\lfloor\frac{\arg \left(\frac{1}{2}(-5-2 x+\sqrt{29})\right)}{2 \pi}\right]\right)\right. \\
& \exp \left(-\pi \exp \left(i \pi\left\lfloor\frac{\arg (29-x)}{2 \pi}\right\rfloor\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^{k}(29-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}\right) \\
& \exp \left(-\pi \exp \left(i \pi\left\lfloor\frac{\arg (47-x)}{2 \pi}\right\rfloor\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^{k}(47-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}\right) \\
& \sqrt{x}^{2} \sqrt[4]{-5+\exp \left(i \pi\left[\frac{\arg (29-x)}{2 \pi}\right]\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^{k}(29-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}} \\
& \left.\sum_{k_{1}=0}^{\infty} \sum_{k_{2}=0}^{\infty} \frac{(-1)^{k_{1}+k_{2}} 2^{-k_{2}}(2-x)^{k_{1}} x^{-k_{1}-k_{2}}\left(-\frac{1}{2}\right)_{k_{1}}\left(-\frac{1}{2}\right)_{k_{2}}(-5-2 x+\sqrt{29})^{k_{2}}}{k_{1}!k_{2}!}\right) / \\
& \left(\sqrt[4]{2} \exp \left(-\pi \exp \left(i \pi\left\lfloor\frac{\arg (79-x)}{2 \pi}\right\rfloor\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^{k}(79-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}\right)\right)
\end{aligned}
$$

## for ( $x \in \mathbb{R}$ and $x<0$ )

$$
\begin{aligned}
& \frac{\left(\exp (-\pi \sqrt{29}) \sqrt{\frac{1}{2}(\sqrt{29}-5)}\right) \sqrt[4]{\frac{1}{2}(\sqrt{29}-5)}(\sqrt{2} \exp (-\pi \sqrt{47}))}{\exp (-\pi \sqrt{79})}= \\
& \left(\exp \left(i \pi\left[\frac{\arg (2-x)}{2 \pi}\right]\right) \exp \left(i \pi\left[\frac{\arg \left(-x+\frac{1}{2}(-5+\sqrt{29})\right)}{2 \pi}\right]\right)\right. \\
& \exp \left(-\pi \exp \left(i \pi\left[\frac{\arg (29-x)}{2 \pi}\right]\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^{k}(29-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}\right) \\
& \quad \exp \left(-\pi \exp \left(i \pi\left[\frac{\arg (47-x)}{2 \pi}\right]\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^{k}(47-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}\right) \\
& \sqrt{x}^{2} \sqrt[4]{-5+\exp \left(i \pi\left[\frac{\arg (29-x)}{2 \pi}\right]\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^{k}(29-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}} \\
& \left.\sum_{k_{1}=0}^{\infty} \sum_{k_{2}=0}^{\infty} \frac{(-1)^{k_{1}+k_{2}}(2-x)^{k_{1}} x^{-k_{1}-k_{2}}\left(-\frac{1}{2}\right)_{k_{1}}\left(-\frac{1}{2}\right)_{k_{2}}\left(-x+\frac{1}{2}(-5+\sqrt{29})\right)^{k_{2}}}{k_{1}!k_{2}!}\right) / \\
& \left(\sqrt[4]{2} \exp \left(-\pi \exp \left(i \pi\left\lfloor\frac{\arg (79-x)}{2 \pi}\right]\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^{k}(79-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}\right)\right)
\end{aligned}
$$

for $(x \in \mathbb{R}$ and $x<0$ )
$\left(\left(1 / \exp \left(-\mathrm{Pi}^{*} \operatorname{sqrt}(29)\right)\right)\right) * \operatorname{sqrt}(((((\operatorname{sqrt}(29)-5)) / 2))) *(((((\operatorname{sqrt}(29)-$
$5)) / 2)))^{\wedge} 1 / 4 *(\operatorname{sqrt}(2))^{*}\left(\exp \left(-\mathrm{Pi}^{*} \operatorname{sqrt}(79)\right)\right) * 1 /\left(\left(\left(\exp \left(-\mathrm{Pi}^{*} \operatorname{sqrt}(47)\right)\right)\right)\right)$

## Input:

$$
\frac{1}{\exp (-\pi \sqrt{29})} \sqrt{\frac{1}{2}(\sqrt{29}-5)} \sqrt[4]{\frac{1}{2}(\sqrt{29}-5)} \sqrt{2} \exp (-\pi \sqrt{79}) \times \frac{1}{\exp (-\pi \sqrt{47})}
$$

## Exact result:



## Decimal approximation:

15424.80597391886041466350273291144812882808136437211734803...
15424.80597....

## Property:

$\frac{(-5+\sqrt{29})^{3 / 4} e^{\sqrt{29}} \pi+\sqrt{47} \pi-\sqrt{79} \pi}{\sqrt[4]{2}}$ is a transcendental number

## Alternate form:

$\frac{\sqrt{2} e^{\sqrt{29} \pi+\sqrt{47} \pi-\sqrt{79} \pi}}{\sqrt[4]{70+13 \sqrt{29}}}$

## Series representations:

$$
\begin{aligned}
& \frac{\left(\sqrt{\frac{1}{2}(\sqrt{29}-5)} \sqrt[4]{\frac{1}{2}(\sqrt{29}-5)}\right) \sqrt{2} \exp (-\pi \sqrt{79})}{\exp (-\pi \sqrt{29}) \exp (-\pi \sqrt{47})}= \\
& \left(\exp \left(-\pi \sqrt{z_{0}} \sum_{k=0}^{\infty} \frac{(-1)^{k}\left(-\frac{1}{2}\right)_{k}\left(79-z_{0}\right)^{k} z_{0}^{-k}}{k!}\right)\right. \\
& \left.{\sqrt{z_{0}}}^{2} \sqrt[4]{4}_{-5+\sqrt{z_{0}} \sum_{k=0}^{\infty} \frac{(-1)^{k}\left(-\frac{1}{2}\right)_{k}\left(29-z_{0}\right)^{k} z_{0}^{-k}}{k!}}^{k!}\right) \\
& \left.\sum_{k_{1}=0}^{\infty} \sum_{k_{2}=0}^{\infty} \frac{(-1)^{k_{1}+k_{2}} 2^{-k_{2}}\left(-\frac{1}{2}\right)_{k_{1}}\left(-\frac{1}{2}\right)_{k_{2}}\left(-5+\sqrt{29}-2 z_{0}\right)^{k_{2}}\left(2-z_{0}\right)^{k_{1}} z_{0}^{-k_{1}-k_{2}}}{k_{1}!k_{2}!}\right) \\
& /\left(\sqrt[4]{2} \exp \left(-\pi \sqrt{z_{0}} \sum_{k=0}^{\infty} \frac{(-1)^{k}\left(-\frac{1}{2}\right)_{k}\left(29-z_{0}\right)^{k} z_{0}^{-k}}{k!}\right)\right. \\
& \left.\exp \left(-\pi \sqrt{z_{0}} \sum_{k=0}^{\infty} \frac{(-1)^{k}\left(-\frac{1}{2}\right)_{k}\left(47-z_{0}\right)^{k} z_{0}^{-k}}{k!}\right)\right)
\end{aligned}
$$

for $\operatorname{not}\left(\left(z_{0} \in \mathbb{R}\right.\right.$ and $\left.\left.-\infty<z_{0} \leq 0\right)\right)$

$$
\frac{\left(\sqrt{\frac{1}{2}(\sqrt{29}-5)} \sqrt[4]{\frac{1}{2}(\sqrt{29}-5)}\right) \sqrt{2} \exp (-\pi \sqrt{79})}{\exp (-\pi \sqrt{29}) \exp (-\pi \sqrt{47})}=
$$

$$
\left(\exp \left(i \pi\left\lfloor\frac{\arg (2-x)}{2 \pi}\right\rfloor\right) \exp \left(i \pi\left\lfloor\frac{\arg \left(\frac{1}{2}(-5-2 x+\sqrt{29})\right)}{2 \pi}\right]\right)\right.
$$

$$
\exp \left(-\pi \exp \left(i \pi\left[\frac{\arg (79-x)}{2 \pi}\right]\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^{k}(79-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}\right)
$$

$$
\sqrt{x}^{2} \sqrt[4]{-5+\exp \left(i \pi\left[\frac{\arg (29-x)}{2 \pi}\right]\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^{k}(29-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}}
$$

$$
\left.\sum_{k_{1}=0}^{\infty} \sum_{k_{2}=0}^{\infty} \frac{(-1)^{k_{1}+k_{2}} 2^{-k_{2}}(2-x)^{k_{1}} x^{-k_{1}-k_{2}}\left(-\frac{1}{2}\right)_{k_{1}}\left(-\frac{1}{2}\right)_{k_{2}}(-5-2 x+\sqrt{29})^{k_{2}}}{k_{1}!k_{2}!}\right) /
$$

$$
\left(\sqrt[4]{2} \exp \left(-\pi \exp \left(i \pi\left[\frac{\arg (29-x)}{2 \pi}\right\rfloor\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^{k}(29-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}\right)\right.
$$

$$
\left.\exp \left(-\pi \exp \left(i \pi\left\lfloor\frac{\arg (47-x)}{2 \pi}\right\rfloor\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^{k}(47-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}\right)\right) \text { for }(x \in
$$

[^2]\[

$$
\begin{aligned}
& \frac{\left(\sqrt{\frac{1}{2}(\sqrt{29}-5)} \sqrt[4]{\frac{1}{2}(\sqrt{29}-5)}\right) \sqrt{2} \exp (-\pi \sqrt{79})}{\exp (-\pi \sqrt{29}) \exp (-\pi \sqrt{47})}= \\
& \left(\exp \left(i \pi\left[\left.\frac{\arg (2-x)}{2 \pi} \right\rvert\,\right) \exp \left(i \pi \left\lvert\, \frac{\arg \left(-x+\frac{1}{2}(-5+\sqrt{29})\right)}{2 \pi}\right.\right]\right)\right. \\
& \quad \exp \left(-\pi \exp \left(i \pi\left[\frac{\arg (79-x)}{2 \pi}\right]\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^{k}(79-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}\right) \\
& \sqrt{x}^{2} \sqrt[4]{-5+\exp \left(i \pi\left[\frac{\arg (29-x)}{2 \pi}\right]\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^{k}(29-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}} \\
& \left.\sum_{k_{1}=0}^{\infty} \sum_{k_{2}=0}^{\infty} \frac{(-1)^{k_{1}+k_{2}}(2-x)^{k_{1}} x^{-k_{1}-k_{2}}\left(-\frac{1}{2}\right)_{k_{1}}\left(-\frac{1}{2}\right)_{k_{2}}\left(-x+\frac{1}{2}(-5+\sqrt{29})\right)^{k_{2}}}{k_{1}!k_{2}!}\right) / \\
& \left(\sqrt[4]{2} \exp \left(-\pi \exp \left(i \pi\left[\frac{\arg (29-x)}{2 \pi}\right]\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^{k}(29-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}\right)\right. \\
& \left.\exp \left(-\pi \exp \left(i \pi\left\lfloor\frac{\arg (47-x)}{2 \pi}\right]\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^{k}(47-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}\right)\right) \text { for }(x \in
\end{aligned}
$$
\]

$\mathbb{R}$ and $x<0$ )
Or:
$1 /\left(\left(\left(\left(\left(\exp \left(-\mathrm{Pi}^{*} \mathrm{sqrt}(29)\right) * \operatorname{sqrt}(((((\operatorname{sqrt}(29)-5)) / 2))) *(((((\operatorname{sqrt}(29)-\right.\right.\right.\right.\right.$
$\left.\left.\left.\left.\left.5)) / 2)))^{\wedge} 1 / 4 *(\operatorname{sqrt}(2)) * 1 /\left(\exp \left(-\mathrm{Pi}^{*} \operatorname{sqrt}(79)\right)\right) * \exp \left(-\mathrm{Pi}^{*} \operatorname{sqrt}(47)\right)\right)\right)\right)\right)\right)$

## Input:

1
$\exp (-\pi \sqrt{29}) \sqrt{\frac{1}{2}(\sqrt{29}-5)} \sqrt[4]{\frac{1}{2}(\sqrt{29}-5)} \sqrt{2} \times \frac{1}{\exp (-\pi \sqrt{70})} \exp (-\pi \sqrt{47})$

## Exact result:

$\frac{\sqrt[4]{2} e^{\sqrt{29} \pi+\sqrt{47} \pi-\sqrt{79} \pi}}{(\sqrt{29}-5)^{3 / 4}}$
Decimal approximation:
91256.71055001537962192684759646752167309120530505483189508...
91256.7105....

## Property:

$\frac{\sqrt[4]{2} e^{\sqrt{29}} \pi+\sqrt{47} \pi-\sqrt{79} \pi}{(-5+\sqrt{29})^{3 / 4}}$ is a transcendental number

## Alternate form:

$\sqrt[4]{\frac{35}{2}+\frac{13 \sqrt{29}}{4}} e^{\sqrt{29} \pi+\sqrt{47} \pi-\sqrt{79} \pi}$

## Series representations:

$$
\begin{aligned}
& \frac{1}{\left(\frac{\left.\exp (-\pi \sqrt{29}) \sqrt{\frac{1}{2}(\sqrt{29}-5)}\right) \sqrt[4]{\frac{1}{2}(\sqrt{29}-5)}(\sqrt{2} \exp (-\pi \sqrt{47}))}{\exp (-\pi \sqrt{79})}\right.}= \\
& \left(\sqrt[4]{2} \exp \left(-\pi \sqrt{z_{0}} \sum_{k=0}^{\infty} \frac{(-1)^{k}\left(-\frac{1}{2}\right)_{k}\left(79-z_{0}\right)^{k} z_{0}^{-k}}{k!}\right)\right) / \\
& \left(\exp \left(-\pi \sqrt{z_{0}} \sum_{k=0}^{\infty} \frac{(-1)^{k}\left(-\frac{1}{2}\right)_{k}\left(29-z_{0}\right)^{k} z_{0}^{-k}}{k!}\right)\right. \\
& \left.\exp \left(-\pi \sqrt{z_{0}} \sum_{k=0}^{\infty} \frac{(-1)^{k}\left(-\frac{1}{2}\right)_{k}\left(47-z_{0}\right)^{k} z_{0}^{k}}{k!}\right){\sqrt{z_{0}}}^{2}\right) \\
& \left(\sum_{k=0}^{\infty} \frac{\left(-\frac{1}{2}\right)^{k}\left(-\frac{1}{2}\right)_{k}\left(-5+\sqrt{29}-2 z_{0}\right)^{k} z_{0}^{-k}}{k!}\right)\left(\sum_{k=0}^{\infty} \frac{(-1)^{k}\left(-\frac{1}{2}\right)_{k}\left(2-z_{0}\right)^{k} z_{0}^{k}}{k!}\right) \\
& \sqrt[4]{\left.-5+\sqrt{z_{0}} \sum_{k=0}^{\infty} \frac{(-1)^{k}\left(-\frac{1}{2}\right)_{k}\left(29-z_{0}\right)^{k} z_{0}^{-k}}{k!}\right)}
\end{aligned}
$$

for $\operatorname{not}\left(\left(z_{0} \in \mathbb{R}\right.\right.$ and $\left.\left.-\infty<z_{0} \leq 0\right)\right)$

$$
\begin{aligned}
& \frac{1}{\frac{\left(\exp (-\pi \sqrt{29}) \sqrt{\frac{1}{2}(\sqrt{29}-5)} \sqrt[4]{\frac{1}{2}(\sqrt{29}-5)}(\sqrt{2} \exp (-\pi \sqrt{47}))\right.}{\exp (-\pi \sqrt{79})}}= \\
& \left(\sqrt[4]{2} \exp \left(-\pi \exp \left(i \pi\left\lfloor\frac{\arg (79-x)}{2 \pi}\right\rfloor\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^{k}(79-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}\right)\right) / \\
& \left(\exp \left(i \pi\left[\frac{\arg (2-x)}{2 \pi}\right]\right) \exp \left(i \pi\left[\frac{\arg \left(\frac{1}{2}(-5-2 x+\sqrt{29})\right)}{2 \pi}\right]\right)\right. \\
& \exp \left(-\pi \exp \left(i \pi\left\lfloor\frac{\arg (29-x)}{2 \pi}\right\rfloor\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^{k}(29-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}\right) \\
& \exp \left(-\pi \exp \left(i \pi\left\lfloor\frac{\arg (47-x)}{2 \pi}\right\rfloor\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^{k}(47-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}\right) \\
& \sqrt{x}^{2}\left(\sum_{k=0}^{\infty} \frac{(-1)^{k}(2-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}\right) \\
& \sqrt[4]{-5+\exp \left(i \pi\left[\frac{\arg (29-x)}{2 \pi}\right\rfloor\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^{k}(29-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}} \\
& \left.\sum_{k=0}^{\infty} \frac{\left(-\frac{1}{2}\right)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}(-5-2 x+\sqrt{29})^{k}}{k!}\right) \text { for }(x \in \mathbb{R} \text { and } x<0)
\end{aligned}
$$

$$
\begin{aligned}
& \frac{1}{\frac{\left(\exp (-\pi \sqrt{29}) \sqrt{\frac{1}{2}(\sqrt{29}-5)}\right) \sqrt[4]{\frac{1}{2}(\sqrt{29}-5)}(\sqrt{2} \exp (-\pi \sqrt{47}))}{\exp (-\pi \sqrt{79})}}= \\
& \left(\sqrt[4]{2} \exp \left(-\pi \exp \left(i \pi\left\lfloor\frac{\arg (79-x)}{2 \pi}\right\rfloor\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^{k}(79-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}\right)\right) / \\
& \left(\exp \left(i \pi\left[\frac{\arg (2-x)}{2 \pi}\right\rfloor\right) \exp \left(i \pi\left[\frac{\arg \left(-x+\frac{1}{2}(-5+\sqrt{29})\right)}{2 \pi}\right]\right)\right. \\
& \exp \left(-\pi \exp \left(i \pi\left\lfloor\frac{\arg (29-x)}{2 \pi}\right\rfloor\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^{k}(29-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}\right) \\
& \exp \left(-\pi \exp \left(i \pi\left\lfloor\frac{\arg (47-x)}{2 \pi}\right\rfloor\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^{k}(47-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}\right) \\
& \sqrt{x}^{2}\left(\sum_{k=0}^{\infty} \frac{(-1)^{k}(2-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}\right) \\
& \sqrt[4]{-5+\exp \left(i \pi\left[\frac{\arg (29-x)}{2 \pi}\right\rfloor\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^{k}(29-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}} \\
& \left.\sum_{k=0}^{\infty} \frac{(-1)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}\left(-x+\frac{1}{2}(-5+\sqrt{29})\right)^{k}}{k!}\right) \text { for }(x \in \mathbb{R} \text { and } x<0)
\end{aligned}
$$

Or:
$1 /\left(\left(\left(\left(\left(\exp \left(-\mathrm{Pi}^{*} \operatorname{sqrt}(29)\right) * \operatorname{sqrt}(((((\operatorname{sqrt}(29)-5)) / 2))){ }^{*}(((((\operatorname{sqrt}(29)-\right.\right.\right.\right.\right.$
$\left.\left.\left.\left.\left.5)) / 2)))^{\wedge} 1 / 4 *(\operatorname{sqrt}(2)) * \exp \left(-\mathrm{Pi}^{*} \operatorname{sqrt}(79)\right) * \exp \left(-\mathrm{Pi}^{*} \mathrm{sqrt}(47)\right)\right)\right)\right)\right)\right)$

## Input:

$\exp (-\pi \sqrt{29}) \sqrt{\frac{1}{2}(\sqrt{29}-5)} \sqrt[4]{\frac{1}{2}(\sqrt{29}-5)} \sqrt{2} \exp (-\pi \sqrt{79}) \exp (-\pi \sqrt{47})$

## Exact result:

$\frac{\sqrt[4]{2} e^{\sqrt{29}} \pi+\sqrt{47} \pi+\sqrt{79} \pi}{(\sqrt{29}-5)^{3 / 4}}$

## Decimal approximation:

$1.6366257984354820364561326031128794782879798624822973 \ldots \times 10^{29}$
$1.6366257984 \ldots * 10^{29}$

## Property:

$\frac{\sqrt[4]{2} e^{\sqrt{29}} \pi+\sqrt{47} \pi+\sqrt{79} \pi}{(-5+\sqrt{29})^{3 / 4}}$ is a transcendental number

## Alternate form:

$\sqrt[4]{\frac{35}{2}+\frac{13 \sqrt{29}}{4}} e^{\sqrt{29} \pi+\sqrt{47} \pi+\sqrt{79} \pi}$

## Series representations:

$$
\begin{aligned}
& \frac{1}{\exp (-\pi \sqrt{29}) \sqrt{\frac{1}{2}(\sqrt{29}-5)} \sqrt[4]{\frac{1}{2}(\sqrt{29}-5)} \sqrt{2} \exp (-\pi \sqrt{79}) \exp (-\pi \sqrt{47})}= \\
& (\sqrt[4]{2}) /\left(\exp \left(-\pi \sqrt{z_{0}} \sum_{k=0}^{\infty} \frac{(-1)^{k}\left(-\frac{1}{2}\right)_{k}\left(29-z_{0}\right)^{k} z_{0}^{k}}{k!}\right)\right. \\
& \quad \exp \left(-\pi \sqrt{z_{0}} \sum_{k=0}^{\infty} \frac{(-1)^{k}\left(-\frac{1}{2}\right)_{k}\left(47-z_{0}\right)^{k} z_{0}^{-k}}{k!}\right) \\
& \quad \exp \left(-\pi \sqrt{z_{0}} \sum_{k=0}^{\infty} \frac{(-1)^{k}\left(-\frac{1}{2}\right)_{k}\left(79-z_{0}\right)^{k} z_{0}^{-k}}{k!}\right){\sqrt{z_{0}}}^{2} \\
& \left(\sum_{k=0}^{\infty} \frac{\left(-\frac{1}{2}\right)^{k}\left(-\frac{1}{2}\right)_{k}\left(-5+\sqrt{29}-2 z_{0}\right)^{k} z_{0}^{-k}}{k!}\right)\left(\sum_{k=0}^{\infty} \frac{(-1)^{k}\left(-\frac{1}{2}\right)_{k}\left(2-z_{0}\right)^{k} z_{0}^{-k}}{k!}\right) \\
& \sqrt[4]{\left.-5+\sqrt{z_{0}} \sum_{k=0}^{\infty} \frac{(-1)^{k}\left(-\frac{1}{2}\right)_{k}\left(29-z_{0}\right)^{k} z_{0}^{k}}{k!}\right)}
\end{aligned}
$$

for $\operatorname{not}\left(\left(z_{0} \in \mathbb{R}\right.\right.$ and $\left.\left.-\infty<z_{0} \leq 0\right)\right)$

$$
\begin{aligned}
& \exp (-\pi \sqrt{29}) \sqrt{\frac{1}{2}(\sqrt{29}-5)} \sqrt[4]{\frac{1}{2}(\sqrt{29}-5)} \sqrt{2} \exp (-\pi \sqrt{79}) \exp (-\pi \sqrt{47}) \\
&(\sqrt[4]{2}) /\left(\operatorname { e x p } \left(i \pi\left[\frac{\arg (2-x)}{2 \pi} f\right) \exp \left(i \pi\left[\frac{\arg \left(\frac{1}{2}(-5-2 x+\sqrt{29})\right)}{2 \pi}\right]\right)\right.\right. \\
& \exp \left(-\pi \exp \left(i \pi\left[\frac{\arg (29-x)}{2 \pi}\right]\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^{k}(29-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}\right) \\
& \exp \left(-\pi \exp \left(i \pi\left[\frac{\arg (47-x)}{2 \pi}\right]\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^{k}(47-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}\right) \\
& \exp \left(-\pi \exp \left(i \pi\left[\frac{\arg (79-x)}{2 \pi}\right]\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^{k}(79-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}\right) \\
& \sqrt{x}^{2}\left(\sum_{k=0}^{\infty} \frac{(-1)^{k}(2-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}\right) \\
& \sqrt[4]{-5+\exp \left(i \pi\left[\frac{\arg (29-x)}{2 \pi}\right]\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^{k}(29-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}} \\
&\left.\sum_{k=0}^{\infty} \frac{\left(-\frac{1}{2}\right)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}(-5-2 x+\sqrt{29})^{k}}{k!}\right) \text { for }(x \in \mathbb{R} \text { and } x<0)
\end{aligned}
$$

$$
\begin{aligned}
& \exp (-\pi \sqrt{29}) \sqrt{\frac{1}{2}(\sqrt{29}-5)} \sqrt[4]{\frac{1}{2}(\sqrt{29}-5)} \sqrt{2} \exp (-\pi \sqrt{79}) \exp (-\pi \sqrt{47}) \\
&(\sqrt[4]{2}) /\left(\exp \left(i \pi\left[\frac{\arg (2-x)}{2 \pi}\right]\right) \exp \left(i \pi\left[\frac{\arg \left(-x+\frac{1}{2}(-5+\sqrt{29})\right)}{2 \pi}\right]\right)\right. \\
& \exp \left(-\pi \exp \left(i \pi\left[\frac{\arg (29-x)}{2 \pi}\right]\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^{k}(29-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}\right) \\
& \exp \left(-\pi \exp \left(i \pi\left[\frac{\arg (47-x)}{2 \pi}\right]\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^{k}(47-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}\right) \\
& \exp \left(-\pi \exp \left(i \pi\left[\frac{\arg (79-x)}{2 \pi}\right]\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^{k}(79-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}\right) \\
& \sqrt{x}^{2}\left(\sum_{k=0}^{\infty} \frac{(-1)^{k}(2-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}\right) \\
& \sqrt[4]{-5+\exp \left(i \pi\left[\frac{\arg (29-x)}{2 \pi}\right]\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^{k}(29-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}} \\
&\left.\sum_{k=0}^{\infty} \frac{(-1)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}\left(-x+\frac{1}{2}(-5+\sqrt{29})\right)^{k}}{k!}\right) \text { for }(x \in \mathbb{R} \text { and } x<0)
\end{aligned}
$$

Now, we have that:
$(((((\exp (-\mathrm{Pi} * \mathrm{sqrt}(29)) * \operatorname{sqrt}(((((\operatorname{sqrt}(29)-5)) / 2))) *(((((\operatorname{sqrt}(29)-$
5))/2)) ) $\left.\left.\left.\left.\left.\left.\left.\left.\left.\left.\wedge 1 / 4 *(\operatorname{sqrt}(2)) * \exp \left(-\mathrm{Pi}^{*} \operatorname{sqrt}(79)\right) * \exp \left(-\mathrm{Pi}^{*} \operatorname{sqrt}(47)\right)\right)\right)\right)\right)\right)\right)\right)\right)\right)\right)^{\wedge} 1 / 4096$

## Input:

$$
\sqrt[4096]{\exp (-\pi \sqrt{29}) \sqrt{\frac{1}{2}(\sqrt{29}-5)} \sqrt[4]{\frac{1}{2}(\sqrt{29}-5)} \sqrt{2} \exp (-\pi \sqrt{79}) \exp (-\pi \sqrt{47})}
$$

## Exact result:

$\frac{(\sqrt{29}-5)^{3 / 16384} \exp (-(\sqrt{29} \pi) / 4096-(\sqrt{47} \pi) / 4096-(\sqrt{79} \pi) / 4096)}{\sqrt[16384]{2}}$

## Decimal approximation:

### 0.983711363264398896645805536424239641142801225764713657841

$0.98371136326 \ldots$...esult near to the value of the following Rogers-Ramanujan continued fraction:
$\frac{\mathrm{e}^{-\frac{\pi}{\sqrt{5}}}}{\frac{\sqrt{5}}{1+\sqrt[5]{\sqrt{\varphi^{5 \sqrt[4]{5^{3}}}}-1}}-\varphi+1}=1-\frac{\mathrm{e}^{-\pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-2 \pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-3 \pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-4 \pi \sqrt{5}}}{1+\ldots}}}} \approx 0.9991104684$
and very near to the dilaton value $\mathbf{0 . 9 8 9 1 1 7 3 5 2 2 4 3 = \boldsymbol { \phi }}$

## Property:

$\frac{(-5+\sqrt{29})^{3 / 16384} e^{-(\sqrt{29} \pi) / 4096-(\sqrt{47} \pi) / 4096-(\sqrt{79} \pi) / 4096}}{16384} \sqrt{2}$ is a transcendental number
Alternate form:
$\frac{(\sqrt{29}-5)^{3 / 16384} e-((\sqrt{29}+\sqrt{47}+\sqrt{79}) \pi) / 4096}{16 \sqrt[38]{2}}$

All 4096th roots of $\left((\operatorname{sqrt}(29)-5)^{\wedge}(3 / 4) \mathrm{e}^{\wedge}(-\mathrm{sqrt}(29) \pi-\operatorname{sqrt}(47) \pi-\operatorname{sqrt}(79)\right.$ $\pi)$ )/ $\mathbf{2}^{\wedge(1 / 4): ~}$

- Polar form

$$
\begin{aligned}
& \frac{(\sqrt{29}-5)^{3 / 16384} e^{0} \exp (-(\sqrt{29} \pi) / 4096-(\sqrt{47} \pi) / 4096-(\sqrt{79} \pi) / 4096)}{16 \sqrt[384]{2}} \\
& \approx 0.983711 \text { (real. principal root) } \\
& \frac{(\sqrt{29}-5)^{3 / 16384} e^{(i \pi) / 2048} \exp (-(\sqrt{29} \pi) / 4096-(\sqrt{47} \pi) / 4096-(\sqrt{79} \pi) / 4096)}{16384} \sqrt{2} \\
& \approx 0.983710+0.0015090 i
\end{aligned}
$$

$$
\begin{aligned}
& \frac{(\sqrt{29}-5)^{3 / 16384} e^{(i \pi) / 1024} \exp (-(\sqrt{29} \pi) / 4096-(\sqrt{47} \pi) / 4096-(\sqrt{79} \pi) / 4096)}{16384} \sqrt{2} \\
& \approx 0.983707+0.0030180 i \\
& \frac{(\sqrt{29}-5)^{3 / 16384} e^{(3 i \pi) / 2048} \exp (-(\sqrt{29} \pi) / 4096-(\sqrt{47} \pi) / 4096-(\sqrt{79} \pi) / 4096)}{16384} \sqrt{2} \\
& \approx 0.983701+0.0045270 i \\
& \frac{(\sqrt{29}-5)^{3 / 16384} e^{(i \pi) / 512} \exp (-(\sqrt{29} \pi) / 4096-(\sqrt{47} \pi) / 4096-(\sqrt{79} \pi) / 4096)}{16 \sqrt[384]{2}} \\
& \approx 0.983693+0.006036 i \quad
\end{aligned}
$$

## Series representations:

$$
\begin{aligned}
& \sqrt[4096]{\exp (-\pi \sqrt{29}) \sqrt{\frac{1}{2}(\sqrt{29}-5)} \sqrt[4]{\frac{1}{2}(\sqrt{29}-5)} \sqrt{2} \exp (-\pi \sqrt{79}) \exp (-\pi \sqrt{47})} \\
& =\frac{1}{\sqrt[16384]{2}}\left(\left(\exp \left(-\pi \sqrt{z_{0}} \sum_{k=0}^{\infty} \frac{(-1)^{k}\left(-\frac{1}{2}\right)_{k}\left(29-z_{0}\right)^{k} z_{0}^{-k}}{k!}\right)\right.\right. \\
& \exp \left(-\pi \sqrt{z_{0}} \sum_{k=0}^{\infty} \frac{(-1)^{k}\left(-\frac{1}{2}\right)_{k}\left(47-z_{0}\right)^{k} z_{0}^{-k}}{k!}\right) \\
& \exp \left(-\pi \sqrt{z_{0}} \sum_{k=0}^{\infty} \frac{(-1)^{k}\left(-\frac{1}{2}\right)_{k}\left(79-z_{0}\right)^{k} z_{0}^{k}}{k!}\right){\sqrt{z_{0}}}^{2} \\
& \sqrt[4]{-5+\sqrt{z_{0}} \sum_{k=0}^{\infty} \frac{(-1)^{k}\left(-\frac{1}{2}\right)_{k}\left(29-z_{0}\right)^{k} z_{0}^{k}}{k!} \sum_{k_{1}=0}^{\infty} \sum_{k_{2}=0}^{\infty}} \\
& \left.\frac{(-1)^{k_{1}+k_{2}} 2^{-k_{2}}\left(-\frac{1}{2}\right)_{k_{1}}\left(-\frac{1}{2}\right)_{k_{2}}\left(-5+\sqrt{29}-2 z_{0}\right)^{k_{2}}\left(2-z_{0}\right)^{k_{1}} z_{0}^{-k_{1}-k_{2}}}{k_{1}!k_{2}!}\right) \\
& \left.{ }^{\wedge}(1 / 4096)\right) \text { for } \operatorname{not}\left(\left(z_{0} \in \mathbb{R} \text { and }-\infty<z_{0} \leq 0\right)\right)
\end{aligned}
$$

$$
\begin{aligned}
& \sqrt[4096]{\exp (-\pi \sqrt{29}) \sqrt{\frac{1}{2}(\sqrt{29}-5)} \sqrt[4]{\frac{1}{2}(\sqrt{29}-5)} \sqrt{2} \exp (-\pi \sqrt{79}) \exp (-\pi \sqrt{47})} \\
& =\frac{1}{\sqrt[16384]{2}}\left(\left(\exp \left(i \pi\left[\frac{\arg (2-x)}{2 \pi}\right]\right) \exp \left(i \pi\left[\frac{\arg \left(\frac{1}{2}(-5-2 x+\sqrt{29})\right)}{2 \pi}\right]\right)\right.\right. \\
& \exp \left(-\pi \exp \left(i \pi\left[\frac{\arg (29-x)}{2 \pi}\right\rfloor\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^{k}(29-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}\right) \\
& \exp \left(-\pi \exp \left(i \pi\left\lfloor\frac{\arg (47-x)}{2 \pi}\right\rfloor\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^{k}(47-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}\right) \\
& \exp \left(-\pi \exp \left(i \pi\left\lfloor\frac{\arg (79-x)}{2 \pi}\right\rfloor\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^{k}(79-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}\right) \\
& \sqrt{x}^{2} \sqrt[4]{-5+\exp \left(i \pi\left\lfloor\frac{\arg (29-x)}{2 \pi}\right\rfloor\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^{k}(29-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}} \\
& \sum_{k_{1}=0}^{\infty} \sum_{k_{2}=0}^{\infty} \\
& \left.\frac{(-1)^{k_{1}+k_{2}} 2^{-k_{2}}(2-x)^{k_{1}} x^{-k_{1}-k_{2}}\left(-\frac{1}{2}\right)_{k_{1}}\left(-\frac{1}{2}\right)_{k_{2}}(-5-2 x+\sqrt{29})^{k_{2}}}{k_{1}!k_{2}!}\right) \\
& \wedge(1 / 4096)) \text { for }(x \in \mathbb{R} \text { and } x<0)
\end{aligned}
$$

$$
\begin{aligned}
& \sqrt[4096]{\exp (-\pi \sqrt{29}) \sqrt{\frac{1}{2}(\sqrt{29}-5)} \sqrt[4]{\frac{1}{2}(\sqrt{29}-5)} \sqrt{2} \exp (-\pi \sqrt{79}) \exp (-\pi \sqrt{47})} \\
& =\frac{1}{\sqrt[16884]{2}}\left(\left(\exp \left(i \pi\left\lfloor\frac{\arg (2-x)}{2 \pi}\right\rfloor\right) \exp \left(i \pi\left[\frac{\arg \left(-x+\frac{1}{2}(-5+\sqrt{29})\right)}{2 \pi}\right]\right)\right.\right. \\
& \exp \left(-\pi \exp \left(i \pi\left[\frac{\arg (29-x)}{2 \pi}\right\rfloor\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^{k}(29-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}\right) \\
& \exp \left(-\pi \exp \left(i \pi\left\lfloor\frac{\arg (47-x)}{2 \pi}\right\rfloor\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^{k}(47-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}\right) \\
& \exp \left(-\pi \exp \left(i \pi\left\lfloor\frac{\arg (79-x)}{2 \pi}\right\rfloor\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^{k}(79-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}\right) \\
& \sqrt{x}^{2} \sqrt[4]{-5+\exp \left(i \pi\left[\frac{\arg (29-x)}{2 \pi}\right]\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^{k}(29-x)^{k} x^{-k}\left(-\frac{1}{2}\right)_{k}}{k!}} \\
& \sum_{k_{1}=0}^{\infty} \sum_{k_{2}=0}^{\infty} \frac{(-1)^{k_{1}+k_{2}}(2-x)^{k_{1}} x^{-k_{1}-k_{2}}\left(-\frac{1}{2}\right)_{k_{1}}\left(-\frac{1}{2}\right)_{k_{2}}\left(-x+\frac{1}{2}(-5+\sqrt{29})\right)^{k_{2}}}{k_{1}!k_{2}!} \\
& \left.\int \wedge(1 / 4096)\right) \text { for }(x \in \mathbb{R} \text { and } x<0)
\end{aligned}
$$

## Integral representation:

$(1+z)^{a}=\frac{\int_{-i \infty+\gamma}^{i \infty+\gamma} \frac{\Gamma(s) \Gamma(-a-s)}{z^{s}} d s}{(2 \pi i) \Gamma(-a)}$ for $(0<\gamma<-\operatorname{Re}(a)$ and $|\arg (z)|<\pi)$
$\Gamma(x)$ is the gamma function

We observe that:
[log base $0.98371136326439889\left(\left(\left(\left(\right.\right.\right.\right.$ exp $(-\mathrm{Pi} * \operatorname{sqrt}(29)){ }^{*} \operatorname{sqrt}(((((\operatorname{sqrt}(29)-$ $5)) / 2)))^{*}(((((\operatorname{sqrt}(29)-5)) / 2)))^{\wedge} 1 / 4 *(\operatorname{sqrt}(2))^{*} \exp (-\operatorname{Pi} * \operatorname{sqrt}(79)) * \exp (-$ Pi*sqrt(47))))))) $]^{\wedge} 1 / 2$

## Input interpretation:



## Result:

63.99999999999999...
$63.99999 \ldots .=64$

## Alternative representation:

$$
\begin{aligned}
& \sqrt{\log _{0.983711}\left(\exp (-\pi \sqrt{29}) \sqrt{\frac{1}{2}(\sqrt{29}-5)}\right.} \\
& \left.\sqrt[4]{\frac{1}{2}(\sqrt{29}-5)} \sqrt{2} \exp (-\pi \sqrt{79}) \exp (-\pi \sqrt{47})\right)= \\
& \sqrt{\left(\frac{1}{\log (0.983711)} \log (\exp (-\pi \sqrt{29}) \exp (-\pi \sqrt{47}) \exp (-\pi \sqrt{79})\right.} \\
& \left.\left.\sqrt[4]{\frac{1}{2}(-5+\sqrt{29})} \sqrt{2} \sqrt{\frac{1}{2}(-5+\sqrt{29})}\right)\right)
\end{aligned}
$$

## Series representations:

$$
\begin{aligned}
& \sqrt{\log _{0.983711}\left(\exp (-\pi \sqrt{29}) \sqrt{\frac{1}{2}(\sqrt{29}-5)}\right.} \\
& \left.\sqrt[4]{\frac{1}{2}(\sqrt{29}-5)} \sqrt{2} \exp (-\pi \sqrt{79}) \exp (-\pi \sqrt{47})\right)= \\
& \exp \left(i \pi \left(\frac { 1 } { 2 \pi } \operatorname { a r g } \left(-x+\log _{0.983711}\left(\frac{1}{\sqrt[4]{2}} \exp (-\pi \sqrt{29}) \exp (-\pi \sqrt{47}) \exp (-\pi \sqrt{79})\right.\right.\right.\right. \\
& \left.\left.\left.\left.\sqrt{2} \sqrt[4]{-5}+\sqrt{29} \sqrt{\frac{1}{2}(-5+\sqrt{29})}\right)\right)\right]\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{1}{k!}(-1)^{k} x^{-k} \\
& \left.\left.\left.\left.\sqrt[4]{-5+\sqrt{29}} \sqrt{\frac{1}{2}(-5+\sqrt{29})}\right)\right)\right)^{k}\left(-\frac{1}{2}\right)\right)_{k} \text { for }(x \in \mathbb{R} \text { and } x<0)
\end{aligned}
$$

$$
\begin{aligned}
& \sqrt{\log _{0.983711}\left(\exp (-\pi \sqrt{29}) \sqrt{\frac{1}{2}(\sqrt{29}-5)}\right.} \\
& \left.\sqrt[4]{\frac{1}{2}(\sqrt{29}-5)} \sqrt{2} \exp (-\pi \sqrt{79}) \exp (-\pi \sqrt{47})\right)= \\
& \left(\frac{1}{z_{0}}\right)^{1 / 2} \left\lvert\, \arg \left(\log _{0.983711}\left(\frac{\left.\left.\exp (-\pi \sqrt{29}) \exp (-\pi \sqrt{47}) \exp (-\pi \sqrt{79}) \sqrt{2} \sqrt[4]{-5+\sqrt{29}} \sqrt{\frac{1}{2}(-5+\sqrt{29})}\right)-z_{0}\right) /(2 \pi) \mid}{\sqrt[4]{2}}\right)\right.\right. \\
& z_{0}^{1 / 2}\left(1+\arg \left(\left.\log _{0.983711}\left(\frac{\left.\exp (-\pi \sqrt{29}) \exp (-\pi \sqrt{47}) \exp (-\pi \sqrt{79}) \sqrt{2} \sqrt[4]{-5+\sqrt{29}} \sqrt{\frac{1}{2}(-5+\sqrt{29})}\right)-z_{0}}{\sqrt[4]{2}}\right) /(2 \pi) \right\rvert\,\right)\right. \\
& \sum_{k=0}^{\infty} \frac{1}{k!}(-1)^{k}\left(-\frac{1}{2}\right)_{k} \\
& \left(\operatorname { l o g } _ { 0 . 9 8 3 7 1 1 } \left(\frac{1}{\sqrt[4]{2}} \exp (-\pi \sqrt{29}) \exp (-\pi \sqrt{47}) \exp (-\pi \sqrt{79})\right.\right. \\
& \left.\left.\sqrt{2} \sqrt[4]{-5+\sqrt{29}} \sqrt{\frac{1}{2}(-5+\sqrt{29})}\right)-z_{0}\right)^{k} z_{0}^{-k}
\end{aligned}
$$

## Appendix

| Scen. | $\lambda_{1}$ | $\ell^{-1} / M_{P}$ | $m_{\text {rad }} / m_{G}$ | $\rho_{1} / \mathrm{LeV}$ | $m_{\text {rad }} / \mathrm{LeV}$ | $\langle\mu\rangle / \mathrm{LeV}$ | $\mu_{0} /\langle\mu\rangle$ | $T_{c} /\langle\mu\rangle$ | $T_{r} /\langle\mu\rangle$ |
| :---: | ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\Lambda_{1}$ | 1.250 | 0.501 | 0.0645 | 0.758 | 0.1998 | 0.750 |  | 0.305 |  |
| $\mathrm{~B}_{1}$ | -3.000 | 0.554 | 0.1969 | 1.085 | 1.018 | 0.828 | 0.9995 | 0.903 | 0.609 |
| $\mathrm{~B}_{2}$ | -2.583 | 0.554 | 0.1905 | 1.007 | 0.915 | 0.767 | 0.989 | 0.825 | 0.428 |
| $\mathrm{~B}_{3}$ | -2.500 | 0.551 | 0.1888 | 0.989 | 0.890 | 0.752 | 0.971 | 0.806 | 0.367 |
| $\mathrm{~B}_{4}$ | -2.438 | 0.554 | 0.1874 | 0.973 | 0.870 | 0.741 | 0.937 | 0.790 | 0.297 |
| $\mathrm{~B}_{5}$ | -2.375 | 0.554 | 0.1859 | 0.957 | 0.849 | 0.728 | 0.982 | 0.774 | 0.193 |
| $\mathrm{~B}_{6}$ | -2.292 | 0.554 | 0.1836 | 0.934 | 0.818 | 0.710 | 0.971 | 0.750 | 0.149 |
| $\mathrm{~B}_{8}$ | 2.208 | 0.554 | 0.1809 | 0.908 | 0.784 | 0.690 | 0.949 | 0.724 | 0.0990 |
| $\mathrm{~B}_{8}$ | -2.125 | 0.554 | 0.1776 | 0.879 | 0.745 | 0.667 | 0.890 | 0.694 | 0.0388 |
| $\mathrm{~B}_{9}$ | -2.096 | 0.554 | 0.1763 | 0.8675 | 0.7303 | 0.6585 | 0.827 | 0.682 | 0.0122 |
| $\mathrm{~B}_{10}$ | -2.092 | 0.554 | 0.1761 | 0.8658 | 0.7281 | 0.6572 | 0.808 | 0.680 | 0.0073 |
| $\mathrm{~B}_{11}$ | -2.090 | 0.554 | 0.1760 | 0.8650 | 0.7270 | 0.6565 | 0.793 | 0.679 | 0.0039 |
| $\mathrm{C}_{1}$ | -3.125 | 0.377 | 0.289 | 0.554 | 0.890 | 0.378 | 0.989 | 1.123 | 0.601 |
| $\mathrm{C}_{2}$ | -2.604 | 0.377 | 0.271 | 0.496 | 0.751 | 0.336 | 0.937 | 0.976 | 0.098 |
| $\mathrm{D}_{1}$ | -3.462 | 1.49 | 0.106 | 0.468 | 0.477 | 0.250 | 0.9996 | 1.007 | 0.445 |
| $\mathrm{~F}_{1}$ | -2.429 | 0.554 | 0.155 | 0.877 | 0.643 | 0.667 | 0.895 | 0.694 | 0.142 |

Table 1. List of benchmark scenarios defined by the classes in eqs. (4.12)-(4.16) and the input values of $\lambda_{1}$ (second column). The outputs obtained in each scenario are presented from the third column on. The foreground red [blue] color on the value of $\lambda_{1}$ indicates that the corresponding phase transition is driven by $O(3)[O(4)]$ symmetric bounce solutions. In scenario $\mathrm{A}_{1}$ there is no phase transition.

| Scen. | $T_{i} /\langle\mu\rangle$ | $N_{e}$ | $T_{R} /\langle\mu\rangle$ | $T_{R} / \mathrm{GeV}$ | $\alpha$ | $\log _{10}\left(\beta / H_{\star}\right)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{B}_{1}$ | 0.663 | 0.09 | 1.272 | 1053 | 1.60 | 2.36 |
| $\mathrm{~B}_{2}$ | 0.605 | 0.35 | 1.071 | 821.8 | 4.61 | 1.99 |
| $\mathrm{~B}_{3}$ | 0.591 | 0.48 | 1.024 | 770.4 | 7.86 | 1.79 |
| $\mathrm{~B}_{4}$ | 0.580 | 0.67 | 0.986 | 730.6 | 17.1 | 1.48 |
| $\mathrm{~B}_{5}$ | 0.568 | 1.08 | 0.953 | 694.0 | 90.1 | 1.97 |
| $\mathrm{~B}_{6}$ | 0.551 | 1.31 | 0.921 | 654.2 | 228 | 1.86 |
| $\mathrm{~B}_{7}$ | 0.531 | 1.68 | 0.887 | 612.0 | 1047 | 1.67 |
| $\mathrm{~B}_{8}$ | 0.509 | 2.57 | 0.849 | 566.4 | $4.0 \cdot 10^{4}$ | 1.23 |
| $\mathrm{~B}_{9}$ | 0.5004 | 3.71 | 0.834 | 549.3 | $4.1 \cdot 10^{6}$ | 0.64 |
| $\mathrm{~B}_{10}$ | 0.4991 | 4.22 | 0.832 | 546.8 | $3.3 \cdot 10^{7}$ | 0.34 |
| $\mathrm{~B}_{11}$ | 0.4985 | 4.86 | 0.831 | 545.6 | $4.5 \cdot 10^{8}$ | -0.32 |
| $\mathrm{C}_{1}$ | 0.828 | 0.32 | 1.531 | 578.4 | 4.3 | 2.03 |
| $\mathrm{C}_{2}$ | 0.718 | 1.99 | 1.239 | 416.2 | $5.0 \cdot 10^{3}$ | 1.45 |
| $\mathrm{D}_{1}$ | - | - | 0.535 | 133.7 | 5.0 | 1.05 |
| $\mathrm{E}_{1}$ | 0.509 | 1.28 | 0.850 | 567.2 | 203 | 1.89 |

Table 2. Some physical parameters for the cases $B_{i}, C_{i}, D$ and $E$ considered in the text.

Table of connection between the physical and mathematical constants and the very closed approximations to the dilaton value.

## Table 1

| Elementary charge $=1.602176$ | $1 /(1,602176)^{1 / 64}=0,992662013$ |
| :--- | :--- |
| Golden ratio $=1.61803398$ | $1 /(1,61803398)^{1 / 64}=0,992509261$ |
| $\zeta(2)=1.644934$ | $1 /(1,644934)^{1 / 64}=0,99253592$ |
| $\sqrt[14]{Q=\left(G_{505} / G_{101 / 5}\right)^{3}}=1.65578$ | $1 /(1,65578)^{1 / 64}=0,992151706$ |
| Proton mass $=1.672621$ | $1 /(1,672621)^{1 / 64}=0,991994840$ |
| Neutron mass $=1.674927$ | $1 /(1,674927)^{1 / 64}=0,991973486$ |

## From:

## Rotating strings confronting PDG mesons

Jacob Sonnenschein and Dorin Weissman - arXiv:1402.5603v1 [hep-ph] 23 Feb 2014
$c c$. The $\Psi$ trajectory: The left side of figure (15) depicts the $\Psi$ trajectory. Here we use the states $J / \Psi(1 S)(3097) 1^{--}, \chi_{c 1}(1 P)(3510) 1^{++}$, and $\Psi(3770) 1^{--}$. Since no $J=3$ state has been observed, we use three states with $J=1$, but with increasing orbital angular momentum $(L=0,1,2)$ and do the fit to $L$ instead of $J$. To give an idea of the shifts in mass involved, the $J^{P C}=2^{++}$state $\chi_{c 2}$ has a mass of 3556 MeV , and the $J^{P C}=3^{--}$state is expected to lie $30-60 \mathrm{MeV}$ above the $\Psi(3770)$ [23].

The best linear fit is

$$
\alpha^{\prime}=0.418, a=-4.04
$$

with $\chi_{l}^{2}=3.41 \times 10^{-4}$, but the optimal fit is far from the linear, with endpoint masses in the range of the constituent $c$ quark mass:

$$
m_{c}=1500, \alpha^{\prime}=0.979, a=-0.09
$$

with $\chi_{m}^{2}=5 \times 10^{-7}\left(\chi_{m}^{2} / \chi_{l}^{2}=0.002\right)$. Aside from the improvement in $\chi^{2}$, by adding the mass we also get a value for the slope (and to a lesser extent, the intercept) that is much closer to that obtained in fits for the light meson trajectories.
where $\alpha^{\prime}$ is the Regge slope (string tension)

We know also that:

$$
\begin{array}{c|c|c}
\omega|6| m_{u / d}=0-60 & 0.910-0.918 \\
\omega / \omega_{3}|5+3| m_{u / d}=255-390 & 0.988-1.18 \\
\omega / \omega_{3}|5+3| m_{u / d}=240-345 & 0.937-1.000
\end{array}
$$

The average of the various Regge slope of Omega mesons are:
$1 / 7 *(0.979+0.910+0.918+0.988+0.937+1.18+1)=0.987428571$
result very near to the value of dilaton and to the solution $0.987516007 \ldots$ of the above expression.

From:
Astronomy \& Astrophysics manuscript no. ms c ESO 2019 - September 24, 2019 Planck 2018 results. VI. Cosmological parameters

The primordial fluctuations are consistent with Gaussian purely adiabatic scalar perturbations characterized by a power spectrum with a spectral index $n_{s}=0.965 \pm$ 0.004, consistent with the predictions of slow-roll, single-field, inflation.
from:
Modular equations and approximations to $\boldsymbol{\pi}$ - Srinivasa Ramanujan
Quarterly Journal of Mathematics, XLV, 1914, 350-372
We have that:

Hence

$$
\begin{array}{rlrl}
64 g_{22}^{24} & =e^{\pi \sqrt{22}} \quad 24 \quad 276 e^{-\pi \sqrt{22}} & \cdots \\
64 g_{22}^{-24} & = & & 4096 e^{-\pi \sqrt{22}}+\cdots,
\end{array}
$$

so that

$$
64\left(g_{22}^{24}+g_{22}^{-24}\right)-e^{\pi \sqrt{22}}-24+4372 e^{-\pi \sqrt{22}}+\cdots-64\left\{(1+\sqrt{2})^{12}+(1-\sqrt{2})^{12}\right\}
$$

Hence

$$
e^{\pi \sqrt{22}}=2508951.9982 \ldots
$$

Again

$$
\begin{array}{cc}
G_{37}=(6+\sqrt{37})^{\frac{1}{\tau}} \\
64 G_{37}^{24}= & e^{\pi \sqrt{37}}+24+276 e^{-\pi \sqrt{37}}+\cdots \\
64 G_{37}^{-24}= & 1096 e^{-\pi \sqrt{37}}-\cdots,
\end{array}
$$

so that

$$
64\left(G_{37}^{24}+G_{37}^{24}\right)=e^{\pi \sqrt{37}}+24+4372 e^{\pi \sqrt{37}}-\cdots=64\left\{(6+\sqrt{37})^{6}+(6-\sqrt{37})^{6}\right\} .
$$

Hence

$$
e^{\pi \sqrt{37}}=199148647.999978
$$

Similarly, from

$$
g_{58}-\sqrt{\left(\frac{5+\sqrt{29}}{2}\right)}
$$

we obtain

$$
64\left(g_{58}^{24} \mid g_{58}^{-24}\right)=e^{\pi \sqrt{58}} \quad 24\left|4372 e^{-\pi \sqrt{58}}\right| \cdots=64\left\{\left.\left(\frac{5+\sqrt{29}}{2}\right)^{12} \right\rvert\,\left(\frac{5-\sqrt{29}}{2}\right)^{12}\right\} .
$$

Нене

$$
e^{\pi \sqrt{58}}=24591257751.99990982 \ldots
$$

## From:

## An Update on Brane Supersymmetry Breaking

J. Mourad and A. Sagnotti - arXiv:1711.11494v1 [hep-th] 30 Nov 2017

From the following vacuum equations:

$$
\begin{aligned}
& T e^{\gamma_{E} \phi}=-\frac{\beta_{E}^{(p)} h^{2}}{\gamma_{E}} e^{-2(8-p) C+2 \beta_{E}^{(p)} \phi} \\
& 16 k^{\prime} e^{2 C}=\frac{h^{2}\left(p+1-\frac{2 \beta_{E}^{(p)}}{\gamma_{E}}\right) e^{-2(8-p) C+2 \beta_{E}^{(p)} \phi}}{(7-p)} \\
&\left(A^{\prime}\right)^{2}-k e^{-2 A}+\frac{h^{2}}{16(p+1)}\left(7-p+\frac{2 \beta_{E}^{(p)}}{\gamma_{E}}\right) e^{-2(8-p) C+2 \beta_{E}^{(p)} \phi}
\end{aligned}
$$

we have obtained, from the results almost equals of the equations, putting
$4096 e^{-\pi \sqrt{18}}$ instead of

$$
e^{-2(8-p) C+2 \beta_{E}^{(p)} \phi}
$$

a new possible mathematical connection between the two exponentials. Thence, also the values concerning $p, C, \beta_{E}$ and $\phi$ correspond to the exponents of $e$ (i.e. of exp). Thence we obtain for $\mathrm{p}=5$ and $\beta_{E}=1 / 2$ :

$$
e^{-6 C+\phi}=4096 e^{-\pi \sqrt{18}}
$$

Therefore, with respect to the exponentials of the vacuum equations, the Ramanujan's exponential has a coefficient of 4096 which is equal to $64^{2}$, while $-6 \mathrm{C}+\phi$ is equal to $\pi \sqrt{18}$. From this it follows that it is possible to establish mathematically, the dilaton value.

For
$\exp \left(\left(-\mathrm{Pi}^{*} \operatorname{sqrt}(18)\right)\right.$ we obtain:

## Input:

$\exp (-\pi \sqrt{18})$

## Exact result:

$e^{-3 \sqrt{2} \pi}$

## Decimal approximation:

$1.6272016226072509292942156739117979541838581136954016 \ldots \times 10^{-6}$
$1.6272016 \ldots * 10^{-6}$

## Property:

$e^{-3 \sqrt{2} \pi}$ is a transcendental number

## Series representations:

$e^{-\pi \sqrt{18}}=e^{-\pi \sqrt{17} \sum_{k=0}^{\infty} 17^{-k}\binom{1 / 2}{k}}$
$e^{-\pi \sqrt{18}}=\exp \left(-\pi \sqrt{17} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{17}\right)^{k}\left(-\frac{1}{2}\right)_{k}}{k!}\right)$
$e^{-\pi \sqrt{18}}=\exp \left(-\frac{\pi \sum_{j=0}^{\infty} \text { Res }_{s=-\frac{1}{2}+j} 17^{-s} \Gamma\left(-\frac{1}{2}-s\right) \Gamma(s)}{2 \sqrt{\pi}}\right)$

Now, we have the following calculations:

$$
\begin{gathered}
e^{-6 C+\phi}=4096 e^{-\pi \sqrt{18}} \\
e^{-\pi \sqrt{18}}=1.6272016 \ldots * 10^{-6}
\end{gathered}
$$

from which:

$$
\begin{gathered}
\frac{1}{4096} e^{-6 C+\phi}=1.6272016 \ldots * 10^{-6} \\
0.000244140625 e^{-6 C+\phi}=e^{-\pi \sqrt{18}}=1.6272016 \ldots * 10^{-6}
\end{gathered}
$$

Now:

$$
\ln \left(e^{-\pi \sqrt{18}}\right)=-13.328648814475=-\pi \sqrt{18}
$$

And:

## $\left(1.6272016 * 10^{\wedge}-6\right) * 1 /(0.000244140625)$

## Input interpretation:

$$
\frac{1.6272016}{10^{6}} \times \frac{1}{0.000244140625}
$$

## Result:

0.0066650177536
0.006665017...

Thence:

$$
0.000244140625 e^{-6 C+\phi}=e^{-\pi \sqrt{18}}
$$

Dividing both sides by 0.000244140625 , we obtain:

$$
\begin{aligned}
& \frac{0.000244140625}{0.000244140625} e^{-6 C+\phi}=\frac{1}{0.000244140625} e^{-\pi \sqrt{18}} \\
& e^{-6 C+\phi}=0.0066650177536
\end{aligned}
$$

$\left(\left(\left(\left(\exp \left(\left(-\mathrm{Pi}^{*} \operatorname{sqrt}(18)\right)\right)\right)\right)\right)\right) * 1 / 0.000244140625$
Input interpretation:
$\exp (-\pi \sqrt{18}) \times \frac{1}{0.000244140625}$

## Result:

0.00666501785...
$0.00666501785 \ldots$

## Series representations:

$$
\begin{aligned}
& \frac{\exp (-\pi \sqrt{18})}{0.000244141}=4096 \exp \left(-\pi \sqrt{17} \sum_{k=0}^{\infty} 17^{-k}\binom{\frac{1}{2}}{k}\right) \\
& \frac{\exp (-\pi \sqrt{18})}{0.000244141}=4096 \exp \left(-\pi \sqrt{17} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{17}\right)^{k}\left(-\frac{1}{2}\right)_{k}}{k!}\right) \\
& \frac{\exp (-\pi \sqrt{18})}{0.000244141}=4096 \exp \left(-\frac{\pi \sum_{j=0}^{\infty} \text { Res }_{s=-\frac{1}{2}+j} 17^{-s} \Gamma\left(-\frac{1}{2}-s\right) \Gamma(s)}{2 \sqrt{\pi}}\right)
\end{aligned}
$$

Now:

$$
\begin{aligned}
& e^{-6 C+\phi}=0.0066650177536 \\
& \exp (-\pi \sqrt{18}) \times \frac{1}{0.000244140625}= \\
& e^{-\pi \sqrt{18}} \times \frac{1}{0.000244140625} \\
& =0.00666501785 \ldots
\end{aligned}
$$

From:
$\ln (0.00666501784619)$

## Input interpretation:

$\log (0.00666501784619)$

## Result:

-5.010882647757...
$-5.010882647757 \ldots$

## Alternative representations:

```
log(0.006665017846190000) = log(a) 知a(0.006665017846190000)
```

$\log (0.006665017846190000)=-\mathrm{Li}_{1}(0.993334982153810000)$

## Series representations:

$$
\begin{gathered}
\log (0.006665017846190000)=-\sum_{k=1}^{\infty} \frac{(-1)^{k}(-0.993334982153810000)^{k}}{k} \\
\log (0.006665017846190000)=2 i \pi\left[\frac{\arg (0.006665017846190000-x)}{2 \pi}\right]+ \\
\log (x)-\sum_{k=1}^{\infty} \frac{(-1)^{k}(0.006665017846190000-x)^{k} x^{-k}}{k} \text { for } x<0
\end{gathered}
$$

$$
\log (0.006665017846190000)=\left\lfloor\frac{\arg \left(0.006665017846190000-z_{0}\right)}{2 \pi}\right\rfloor \log \left(\frac{1}{z_{0}}\right)+
$$

$$
\log \left(z_{0}\right)+\left\lfloor\frac{\arg \left(0.006665017846190000-z_{0}\right)}{2 \pi}\right\rfloor \log \left(z_{0}\right)-
$$

$$
\sum_{k=1}^{\infty} \frac{(-1)^{k}\left(0.006665017846190000-z_{0}\right)^{k} z_{0}^{-k}}{k}
$$

## Integral representation:

$\log (0.006665017846190000)=\int_{1}^{0.006665017846190000} \frac{1}{t} d t$

In conclusion:

$$
-6 C+\phi=-5.010882647757 \ldots
$$

and for $\mathrm{C}=1$, we obtain:
$\phi=-5.010882647757+6=\mathbf{0 . 9 8 9 1 1 7 3 5 2 2 4 3}=\boldsymbol{\phi}$

Note that the values of $\mathrm{n}_{\mathrm{s}}$ (spectral index) 0.965 , of the average of the Omega mesons Regge slope 0.987428571 and of the dilaton 0.989117352243 , are also connected to the following two Rogers-Ramanujan continued fractions:

$$
\frac{\mathrm{e}^{-\frac{\pi}{5}}}{\sqrt{(\varphi-1) \sqrt{5}}-\varphi+1}=1-\frac{\mathrm{e}^{-\pi}}{1+\frac{\mathrm{e}^{-2 \pi}}{1+\frac{\mathrm{e}^{-3 \pi}}{1+\frac{\mathrm{e}^{-4 \pi}}{1+\ldots}}}} \approx 0.9568666373
$$

$$
\frac{\mathrm{e}^{-\frac{\pi}{\sqrt{5}}}}{\frac{\sqrt{5}}{1+\sqrt[5]{\sqrt{\varphi^{5 \sqrt[4]{5^{3}}}-1}}}-\varphi+1}=1-\frac{\mathrm{e}^{-\pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-2 \pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-3 \pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-4 \pi \sqrt{5}}}{1+\ldots}}}} \approx 0.9991104684
$$

## (http://www.bitman.name/math/article/102/109/)

Also performing the $512^{\text {th }}$ root of the inverse value of the Pion meson rest mass 139.57, we obtain:
$((1 /(139.57)))^{\wedge} 1 / 512$

## Input interpretation:

$\sqrt[512]{\frac{1}{139.57}}$

## Result:

$0.990400732708644027550973755713301415460732796178555551684 \ldots$
$0.99040073 \ldots$. result very near to the dilaton value $\mathbf{0 . 9 8 9 1 1 7 3 5 2 2 4 3}=\boldsymbol{\phi}$ and to the value of the following Rogers-Ramanujan continued fraction:
$\frac{\mathrm{e}^{-\frac{\pi}{\sqrt{5}}}}{\frac{\sqrt{5}}{1+\sqrt[5]{\sqrt{\varphi^{5 \sqrt[4]{5^{3}}}}-1}}-\varphi+1}=1-\frac{\mathrm{e}^{-\pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-2 \pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-3 \pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-4 \pi \sqrt{5}}}{1+\ldots}}}} \approx 0.9991104684$

## From:

Eur. Phys. J. C (2019) 79:713 - https://doi.org/10.1140/epjc/s10052-019-7225-2-Regular Article - Theoretical Physics Generalized dilaton-axion models of inflation, de Sitter vacua and spontaneous SUSY breaking in supergravity
Yermek Aldabergenov, Auttakit Chatrabhuti, Sergei V. Ketov

Table 1 The predictions for the inflationary parameters $\left(n_{s}, r\right)$, and the values of $\varphi$ at the horizon crossing $\left(\varphi_{i}\right)$ and at the end of inflation $\left(\varphi_{f}\right)$, in the case $3 \leq \alpha \leq \alpha_{*}$ with both signs of $\omega_{1}$. The $\alpha$ parameter is taken to be integer, except of the upper limit $\alpha_{*} \equiv(7+\sqrt{33}) / 2$

| $\alpha$ | 3 | 4 |  | 5 | 6 | $\alpha_{*}$ |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\operatorname{sgn}\left(\omega_{1}\right)$ | - | + | - | $+/-$ | + | - |  |
| $n_{s}$ | 0.9650 | 0.9649 | 0.9640 | 0.9639 | 0.9634 | 0.9637 | 0.9632 |
| $r$ | 0.0035 | 0.0010 | 0.0013 | 0.0007 | 0.0005 | 0.0004 | 0.0003 |
| $-\kappa \varphi_{i}$ | 5.3529 | 3.5542 | 3.9899 | 3.2657 | 3.0215 | 2.7427 | 2.5674 |
| $-\kappa \varphi_{f}$ | 0.9402 | 0.7426 | 0.8067 | 0.7163 | 0.6935 | 0.6488 | 0.6276 |

## Acknowledgments

I would like to thank Prof. George E. Andrews Evan Pugh Professor of Mathematics at Pennsylvania State University for his availability and kindness towards me

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Ramanujan's Lost Notebook: Part IV, George E. Andrews, Bruce C. Berndt (Springer, 2013, ISBN 978-1-4614-4080-2)

# Manuscript Book 2 - Srinivasa Ramanujan <br> MANUSCRIPT BOOK 2 <br> OF <br> SRINIVASA RAMANUIAN 

Manuscript Book 3-Srinivasa Ramanujan

MANUSCRIPT BOOK $\$$
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[^1]:    https://blogs.royalsociety.org/history-of-science/2014/02/17/movie-maths/

[^2]:    $\mathbb{R}$ and $x<0$ )

