
#### Abstract

A possible Theory of Mathematical Connections between various Ramanujan's formulas and the equations of Inflationary Cosmology and the Standard Model concerning the scalar field $\phi$, the Inflaton mass, the Higgs boson mass and the Pion meson $\pi^{ \pm}$mass. II


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https://www.britannica.com/biography/Srinivasa-Ramanujan https://biografieonline.it/foto-enrico-fermi

[^0]
## Proposal and discussion

We calculate the $4096^{\text {th }}\left(4096=64^{2}\right)$ root of the value of scalar field and from it, we obtain 64

Inflationary Cosmology: Exploring the Universe from the Smallest to the Largest Scales

where $\phi$ is the scalar field.
Thence, we obtain:

$$
\sqrt[4096]{\frac{1}{\phi}}=0.98877237 ; \sqrt{\log _{0.98877237}\left(\frac{1}{\phi}\right)}=64 ; 64^{2}=4096
$$

Now, we calculate the $4096^{\text {th }}$ root of the value of inflaton mass and from it we obtain, also here, 64

## Generalized dilaton-axion models of inflation, de Sitter vacua and spontaneous SLSY breaking in supergravity

Table 2 The masses of inflaton, axion and gravitino, and the VEVs of $F$ - and $D$-fields derived from our models by fixing the amplitude $A_{s}$ according to PLANCK data - see Eq. (57). The value of $\left\langle F_{T}\right\rangle$ for a positive $\omega_{1}$ is not fixed by $A_{s}$

| $\alpha$ | 3 | 4 |  | 5 |  | 6 |  | 7 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\operatorname{sgn}\left(\omega_{1}\right)$ | - | + | - | + | - | + | - | - |
| $m_{\varphi}$ | 2.83 | 2.95 | 2.73 | 2.71 | 2.71 | 2.53 | 2.58 | 1.86 |
| $m_{t^{\prime}}$ | 0 | 0.93 | 1.73 | 2.02 | 2.02 | 4.97 | 2.01 | 1.56 |
| $m_{3 / 2}$ | $\geq 1.41$ | 2.80 | 0.86 | 2.56 | 0.64 | 3.91 | 0.49 | 0.29 |
| $\left\langle F_{T}\right\rangle$ | any | $\neq 0$ | 0 | $\neq 0$ | 0 | $\neq 0$ | 0 | 0 |
| $\langle D\rangle$ | 8.31 | 4.48 | 5.08 | 3.76 | 3.76 | 3.25 | 2.87 | 1.73 |$\} \times 10^{13} \mathrm{GeV}$

$m_{0}=2.542-2.33 * 10^{13} \mathrm{GeV}$ with an average of $2.636 * 10^{13} \mathrm{GeV}$

$$
\begin{gathered}
\sqrt[4096]{\frac{1}{2.83 \times 10^{13}}}=0.992466536725379764 \ldots \\
\sqrt{\log _{0.99246653}\left(\frac{1}{2.83 \times 10^{13}}\right)}=64.0000 \ldots \\
64^{2}=4096
\end{gathered}
$$

where $m_{\varphi}$ is the inflaton mass.
Thence we obtain:

$$
\sqrt[4096]{\frac{1}{m_{\varphi}}}=0.99246653 ; \sqrt{\log _{0.99246653}\left(\frac{1}{m_{\varphi}}\right)}=64 ; \quad 64^{2}=4096
$$

We have the following mathematical connections:

$$
\begin{gathered}
\sqrt{\log _{0.98877237}\left(\frac{1}{1.2175 \times 10^{20}}\right)}=64 ; \quad \sqrt{\log _{0.99246653}\left(\frac{1}{2.83 \times 10^{13}}\right)}=64 \\
\sqrt{\log _{0.98877237}\left(\frac{1}{1.2175 \times 10^{20}}\right)}=\sqrt{\log _{0.99246653}\left(\frac{1}{2.83 \times 10^{13}}\right)}=64
\end{gathered}
$$

## From Ramanujan collected papers

## Modular equations and approximations to $\pi$

$$
g_{22}=\sqrt{(1+\sqrt{2})} .
$$

Hence

$$
\begin{array}{rlr}
64 g_{22}^{24} & = & e^{\pi \sqrt{22}}-24+276 e^{-\pi \sqrt{22}}-\cdots \\
64 g_{22}^{-24} & = & 4096 e^{-\pi \sqrt{22}}+\cdots,
\end{array}
$$

so that

$$
64\left(g_{22}^{24}+g_{22}^{-24}\right)=e^{\pi \sqrt{22}}-24+4372 e^{-\pi \sqrt{22}}+\cdots=64\left\{(1+\sqrt{2})^{12}+(1-\sqrt{2})^{12}\right\}
$$

Hence

$$
e^{\pi \sqrt{22}}=2508951.9982 \ldots
$$

Again

$$
\begin{array}{cc}
G_{37}=(6+\sqrt{37})^{\frac{1}{4}} \\
64 G_{37}^{24}= & e^{\pi \sqrt{37}}+24+276 e^{-\pi \sqrt{37}}+\cdots, \\
64 G_{37}^{-24}= & 4096 e^{-\pi \sqrt{37}}-\cdots,
\end{array}
$$

so that

$$
64\left(G_{37}^{24}+G_{37}^{-24}\right)=e^{\pi \sqrt{37}}+24+4372 e^{-\pi \sqrt{37}}-\cdots=64\left\{(6+\sqrt{37})^{6}+(6-\sqrt{37})^{6}\right\}
$$

Hence

$$
e^{\pi \sqrt{37}}=199148647.999978 \ldots
$$

Similarly, from

$$
g_{58}=\sqrt{\left(\frac{5+\sqrt{29}}{2}\right)}
$$

we obtain
$64\left(g_{58}^{24}+g_{58}^{-24}\right)=e^{\pi \sqrt{58}}-24+4372 e^{-\pi \sqrt{58}}+\cdots=64\left\{\left(\frac{5+\sqrt{29}}{2}\right)^{12}+\left(\frac{5-\sqrt{29}}{2}\right)^{12}\right\}$.
Hence

$$
e^{\pi \sqrt{58}}=24591257751.99999982 \ldots
$$

From the following expression (see above part of paper), we obtain:

$$
e^{\pi \sqrt{37}}+24+4372 e^{-\pi \sqrt{37}}-\cdots=64\left\{(6+\sqrt{37})^{6}+(6-\sqrt{37})^{6}\right\}
$$

$\left(\left(\left(\exp \left(\mathrm{Pi}^{*}\right.\right.\right.\right.$ sqrt37 $)+24+(4096+276) \exp -(\mathrm{Pi} *$ sqrt37 $\left.\left.\left.)\right)\right) /\left(\left(\left((6+\text { sqrt37 })^{\wedge} 6+(6-\text { sqrt37 })^{\wedge} 6\right)\right)\right)\right)$

$$
\begin{aligned}
& \frac{\exp (\pi \sqrt{37})+24+(4096+276) \exp (-(\pi \sqrt{37}))}{(6+\sqrt{37})^{6}+(6-\sqrt{37})^{6}}=\frac{24+4372 e^{-\sqrt{37} \pi}+e^{\sqrt{37} \pi}}{(6-\sqrt{37})^{6}+(6+\sqrt{37})^{6}}= \\
& =\frac{24+4372 e^{-\sqrt{37} \pi}+e^{\sqrt{37} \pi}}{(6-\sqrt{37})^{6}+(6+\sqrt{37})^{6}} \text { is a transcendental number }=
\end{aligned}
$$

$$
=64.00000000000000000077996590154140877656204274015527898430 \ldots
$$

From which:

$$
\begin{aligned}
& \left(((\exp (\mathbf{P i} * \mathbf{s q r t} \mathbf{3 7})+\mathbf{2 4}+(\mathbf{x}+\mathbf{2 7 6}) \exp -(\mathbf{P i} * \mathbf{s q r t 3 7}))) /\left(\left(\left((\mathbf{6}+\mathbf{s q r t 3} \mathbf{3})^{\wedge} \mathbf{6}+(\mathbf{6}-\mathbf{s q r t 3 7})^{\wedge} \mathbf{6}\right)\right)\right)\right. \\
& =\mathbf{6 4} \\
& \\
& \frac{\exp (\pi \sqrt{37})+24+(x+276) \exp (-(\pi \sqrt{37}))}{(6+\sqrt{37})^{6}+(6-\sqrt{37})^{6}}=64
\end{aligned}
$$

## Exact result:

$$
\frac{e^{-\sqrt{37} \pi}(x+276)+e^{\sqrt{37} \pi}+24}{(6-\sqrt{37})^{6}+(6+\sqrt{37})^{6}}=64
$$

## Alternate forms:

$$
\begin{aligned}
& \frac{e^{-\sqrt{37} \pi}(x+276)}{3111698}+\frac{e^{\sqrt{37} \pi}}{3111698}+\frac{12}{1555849}=64 \\
& \frac{e^{-\sqrt{37} \pi\left(x+e^{2 \sqrt{37} \pi}+24 e^{\sqrt{37} \pi}+276\right)}}{3111698}=64 \\
& \frac{e^{-\sqrt{37} \pi} x}{(6-\sqrt{37})^{6}+(6+\sqrt{37})^{6}}+\frac{e^{\sqrt{37} \pi}}{(6-\sqrt{37})^{6}+(6+\sqrt{37})^{6}}+ \\
& \frac{276 e^{-\sqrt{37} \pi}}{(6-\sqrt{37})^{6}+(6+\sqrt{37})^{6}}+\frac{24}{(6-\sqrt{37})^{6}+(6+\sqrt{37})^{6}}-64=0 \\
& x=-276+199148648 e^{\sqrt{37} \pi}-e^{2 \sqrt{37} \pi} \\
& x \approx 4096.0
\end{aligned}
$$

## Higgs Boson


$\underline{\text { http://therealmrscience.net/exactly-what-does-the-higgs-boson-do.html }}$

From the above values of scalar field $\phi$, and of the inflaton mass $m_{\varphi}$, we obtain results that are in the range of the Higgs boson mass:

$$
2 \sqrt{\log _{0.98877237}\left(\frac{1}{1.2175 \times 10^{20}}\right)}-\pi+\frac{1}{\phi}
$$

125.476...
and

$$
2 \sqrt{\log _{0.99246653}\left(\frac{1}{2.83 \times 10^{13}}\right)}-\pi+\frac{1}{\phi}
$$

125.476...

## Pion mesons

https://www.sciencephoto.com/media/476068/view/meson-octet-diagram


Meson octet. Diagram organising mesons into an octet according to their charge and strangeness. Particles along the same diagonal line share the same charge; positive $(+1)$, neutral (0), or negative ( -1 ). Particles along the same horizontal line share the same strangeness. Strangeness is a quantum property that is conserved in strong and
electromagnetic interactions, between particles, but not in weak interactions. Mesons are made up of one quark and one antiquark. Particles with a strangeness of +1 , such as the kaons (blue and red) in the top line, contain one strange antiquark. Particles with a strangeness of 0 , such as the pion mesons (green) and eta meson (yellow) in the middle line, contain no strange quarks. Particles with a strangeness of -1 , such as the antiparticle kaons (pink) in the bottom line, contain one strange quark

The $\pi^{ \pm}$mesons have a mass of $139.6 \mathrm{MeV} / \mathrm{c}^{2}$ and a mean lifetime of $2.6033 \times 10^{-8} \mathrm{~s}$. They decay due to the weak interaction. The primary decay mode of a pion, with a branching fraction of 0.999877 , is a leptonic decay into a muon and a muon neutrino:

$$
\begin{aligned}
& \pi^{+}-\mu^{+}+v_{\mu} \\
& \pi^{-} \rightarrow \mu^{-}+\bar{v}_{\mu}
\end{aligned}
$$

The second most common decay mode of a pion, with a branching fraction of 0.000123 , is also a leptonic decay into an electron and the corresponding electron antineutrino. This "electronic mode" was discovered at CERN in 1958: ${ }^{[6]}$

$$
\begin{aligned}
& \pi^{+}-\mathrm{e}^{+}+\mathrm{v}_{\mathrm{e}} \\
& \pi^{-}-\mathrm{e}^{-+}+\bar{v}_{\mathrm{e}}
\end{aligned}
$$

Pion

| Types | 3 |
| :--- | :--- |
| Mass | $\pi^{ \pm}:$ |
|  | $139.57018(35) \mathrm{MeV} / \mathrm{c}^{2}$ |
|  | $\pi^{0}:$ |
|  | $134.9766(6) \mathrm{MeV} / \mathrm{c}^{2}$ |


| Composition | $\pi^{+}: u \bar{d}$ |
| :--- | :--- |
|  | $\pi^{0}: \bar{u}$ or d $\bar{d}$ |
|  | $\pi^{-}: d \bar{u}$ |$|$| Statistics | Bosonic |
| :--- | :--- |
| Interactions | Strong, Weak, <br> Electromagnetic and <br> Gravity |
|  | $\pi^{+}, \pi^{0}$, and $\pi^{-}$ |
| Symbol | Hideki Yukawa (1935) |
| Theorized | César Lattes, |
| Discovered | Giuseppə Occhialini |
|  | (1947) and Cecil <br> Powell |
|  |  |

From the above values of scalar field $\phi$, and the inflaton mass $m_{\varphi}$, we obtain also the value of Pion meson $\pi^{ \pm}=139.57018 \mathrm{MeV} / \mathrm{c}^{2}$

$$
2 \sqrt{\log _{0.98877237}\left(\frac{1}{1.2175 \times 10^{20}}\right)}+11+\frac{1}{\phi}
$$

139.618...
and

$$
2 \sqrt{\log _{0.99246653}\left(\frac{1}{2.83 \times 10^{13}}\right)}+11+\frac{1}{\phi}
$$

### 139.618...

The $\pi^{ \pm}$mesons have a mass of $139.6 \mathrm{MeV} / c^{2}$ and a mean lifetime of $2.6033 \times 10^{-8} \mathrm{~s}$. They decay due to the weak interaction. The primary decay mode of a pion, with a branching fraction of 0.999877 , is a leptonic decay into a muon and a muon neutrino.

Note that the value 0.999877 is very closed to the following Rogers-Ramanujan continued fraction (http://www.bitman.name/math/article/102/109)):

$$
\frac{\mathrm{e}^{-\frac{\pi}{\sqrt{5}}}}{\frac{\sqrt{5}}{1+\sqrt[5]{\sqrt{\varphi^{5} \sqrt[4]{5^{3}}}-1}}-\varphi+1}=1-\frac{\mathrm{e}^{-\pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-2 \pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-3 \pi \sqrt{5}}}{1+\frac{\mathrm{e}^{-4 \pi \sqrt{5}}}{1+\ldots}}}} \approx 0.9991104684
$$

We observe that also the results of $4096^{\text {th }}$ root of the values of scalar field $\phi$, and the inflaton mass $m_{\varphi}$ :

$$
\sqrt[4096]{\frac{1}{\phi}}=0.98877237 ; \quad \sqrt[4096]{\frac{1}{m_{\varphi}}}=0.99246653
$$

are very closed to the above continued fraction.

Furthermore, from the results concerning the scalar field $\phi$ (0.98877237, $1.2175 \mathrm{e}+20)$, and the inflaton $\operatorname{mass} m_{\varphi}(0.99246653,2.83 \mathrm{e}+13)$, we obtain, performing the $10^{\text {th }}$ root:
$((((2 \operatorname{sqrt}(((\log \text { base } 0.98877237((1 / 1.2175 \mathrm{e}+20)))))-\mathrm{Pi}))))^{\wedge} 1 / 10$

## Input interpretation:

$\sqrt[10]{2 \sqrt{\log _{0.98877237}\left(\frac{1}{1.2175 \times 10^{20}}\right)}-\pi}$

## Result:

1.620472942364990195996419034511458317811826267744760835367...

And:
$1 / 10^{\wedge} 27\left[(47+4) / 10^{\wedge} 3+((((2 \operatorname{sqrt}(((\log\right.$ base $0.98877237((1 / 1.2175 \mathrm{e}+20)))))-$ Pi)))) $\left.{ }^{\wedge} 1 / 10\right]$
where 47 and 4 are Lucas numbers

$$
\frac{1}{10^{27}}\left(\frac{47+4}{10^{3}}+\sqrt[10]{2 \sqrt{\log _{0.98877237}\left(\frac{1}{1.2175 \times 10^{20}}\right)}-\pi}\right)
$$

## Result:

$1.671473 \ldots \times 10^{-27}$
$1.671473 \ldots * 10^{-27}$ result practically equal to the proton mass

We have also:
$((((2 \text { sqrt }(((\log \text { base } 0.99246653((1 / 2.83 \mathrm{e}+13)))))-\mathrm{Pi}))))^{\wedge} 1 / 10$
$\sqrt[10]{2 \sqrt{\log _{0.99246653}\left(\frac{1}{2.83 \times 10^{13}}\right)}-\pi}$

## Result:

1.620472850161415439289586204886587162444405282709701447326...

And:
$1 / 10^{\wedge} 27\left[(47+4) / 10^{\wedge} 3+((((2 \operatorname{sqrt}(((\log\right.$ base $0.99246653((1 / 2.83 \mathrm{e}+13)))))-$ Pi)) )) $\left.{ }^{\wedge} 1 / 10\right]$
$\frac{1}{10^{27}}\left(\frac{47+4}{10^{3}}+\sqrt[10]{2 \sqrt{\log _{0.99246653}\left(\frac{1}{2.83 \times 10^{13}}\right)}-\pi}\right)$

## Result:

$1.671473 \ldots \times 10^{-27}$
$1.671473 \ldots * 10^{-27}$ result that is practically equal to the proton mass as the previous

## Trascendental numbers

From the paper of S. Ramanujan "Modular equations and approximations to $\pi$ "
have the following expression:

$$
\frac{3}{\pi}=1-24\left(\frac{1}{e^{2 \pi}-1}+\frac{2}{e^{4 \pi}-1}+\frac{3}{e^{6 \pi}-1}+\cdots\right)
$$

$1-24\left[\left(1 /\left(\mathrm{e}^{\wedge}(2 \mathrm{Pi})-1\right)\right)+\left(2 /\left(\mathrm{e}^{\wedge}(4 \mathrm{Pi})-1\right)\right)+\left(3 /\left(\mathrm{e}^{\wedge}(6 \mathrm{Pi})-1\right)\right)\right]$
$1-24\left(\frac{1}{e^{2 \pi}-1}+\frac{2}{e^{4 \pi}-1}+\frac{3}{e^{6 \pi}-1}\right)$

## Decimal approximation:

$0.954929659721612900604724361833045671977574376370221277342 \ldots$
$0.954929659 \ldots$

## Property:

$1-24\left(\frac{1}{-1+e^{2 \pi}}+\frac{2}{-1+e^{4 \pi}}+\frac{3}{-1+e^{6 \pi}}\right)$ is a transcendental number

## Series representations:

$$
\begin{aligned}
& 1-24\left(\frac{1}{e^{2 \pi}-1}+\frac{2}{e^{4 \pi}-1}+\frac{3}{e^{6 \pi}-1}\right)= \\
& 1-\frac{24}{-1+e^{8} \sum_{k=0}^{\infty}(-1)^{k} /(1+2 k)}-\frac{48}{-1+e^{16 \sum_{k=0}^{\infty}(-1)^{k} /(1+2 k)}}-\frac{72}{-1+e^{24 \sum_{k=0}^{\infty}(-1)^{k} /(1+2 k)}} \\
& 1-24\left(\frac{1}{e^{2 \pi}-1}+\frac{2}{e^{4 \pi}-1}+\frac{3}{e^{6 \pi}-1}\right)=1-\frac{24}{-1+\left(\sum_{k=0}^{\infty} \frac{1}{k!}\right)^{8} \sum_{k=0}^{\infty}(-1)^{k} /(1+2 k)}- \\
& \frac{48}{-1+\left(\sum_{k=0}^{\infty} \frac{1}{k!}\right)^{16 \sum_{k=0}^{\infty}(-1)^{k} /(1+2 k)}-\frac{-1+\left(\sum_{k=0}^{\infty} \frac{1}{k!}\right)^{24} \sum_{k=0}^{\infty}(-1)^{k} /(1+2 k)}{-1}}
\end{aligned}
$$

$$
\begin{aligned}
& 1-24\left(\frac{1}{e^{2 \pi}-1}+\frac{2}{e^{4 \pi}-1}+\frac{3}{e^{6 \pi}-1}\right)=1-\frac{24}{-1+\left(\frac{1}{\sum_{k=0}^{\infty} \frac{(-1)^{k}}{k!}}\right)^{8} \sum_{k=0}^{\infty}(-1)^{k} /(1+2 k)}- \\
&-1+\left(\frac{1}{\sum_{k=0}^{\infty} \frac{(-1)^{k}}{k!}}\right)^{16 \sum_{k=0}^{\infty}(-1)^{k} /(1+2 k)}-\frac{-1+\left(\frac{1}{\sum_{k=0}^{\infty} \frac{(-1)^{k}}{k!}}\right)^{24} \sum_{k=0}^{\infty}(-1)^{k} /(1+2 k)}{}
\end{aligned}
$$

## Integral representations:

$$
\begin{aligned}
& 1-24\left(\frac{1}{e^{2 \pi}-1}+\frac{2}{e^{4 \pi}-1}+\frac{3}{e^{6 \pi}-1}\right)= \\
& 1-\frac{48}{-1+e^{4} \int_{0}^{\infty} 1 /\left(1+t^{2}\right) d t}-\frac{72}{-1+e^{8} \int_{0}^{\infty} 1 /\left(1+t^{2}\right) d t}-\frac{72}{-1+e^{12} \int_{0}^{\infty} 1 /\left(1+t^{2}\right) d t} \\
& 1-24\left(\frac{1}{e^{2 \pi}-1}+\frac{2}{e^{4 \pi}-1}+\frac{3}{e^{6 \pi}-1}\right)= \\
& 1-\frac{48}{-1+e^{4} \int_{0}^{\infty} \sin (t) / t d t}-\frac{-1+e^{8} \int_{0}^{\infty} \sin (t) / t d t}{-\frac{1}{2}}-1+e^{12 \int_{0}^{\infty} \sin (t) / t d t} \\
& 1-24\left(\frac{1}{e^{2 \pi}-1}+\frac{2}{e^{4 \pi}-1}+\frac{3}{e^{6 \pi}-1}\right)= \\
& 1-\frac{48}{-1+e^{8} \int_{0}^{1} \sqrt{1-t^{2}} d t}-\frac{-1+e^{16} \int_{0}^{1} \sqrt{1-t^{2}} d t}{-1+e^{24} \int_{0}^{1} \sqrt{1-t^{2}} d t}
\end{aligned}
$$

Note that the value of the following Rogers-Ramanujan continued fraction is practically equal to the result of the previous expression. Indeed:

$$
\left(\frac{\mathrm{e}^{-\frac{\pi}{5}}}{\sqrt{(\varphi-1) \sqrt{5}}-\varphi+1}=1-\frac{\mathrm{e}^{-\pi}}{1+\frac{\mathrm{e}^{-2 \pi}}{1+\frac{\mathrm{e}^{-3 \pi}}{1+\frac{\mathrm{e}^{-4 \pi}}{1+\ldots}}}} \approx 0.9568666373\right)
$$

$\cong\left(1-24\left(\frac{1}{e^{2 \pi}-1}+\frac{2}{e^{4 \pi}-1}+\frac{3}{e^{6 \pi}-1}\right)\right)=0.954929659 \ldots$

We know that:

$$
\begin{array}{r|c|c}
\omega|6| m_{u / d}=0-60 & 0.910-0.918 \\
\omega / \omega_{3}|5+3| m_{u / d}=255-390 & 0.988-1.18 \\
\omega / \omega_{3}|5+3| m_{u / d}=240-345 & 0.937-1.000
\end{array}
$$

that are the various Regge slope of Omega mesons

From the paper:

## Generalized dilaton-axion models of inflation, de Sitter vacua and spontaneous SUSY breaking in supergravity

Table 1 The predictions for the inflationary parameters ( $n_{s}, r$ ), and the values of $\varphi$ at the horizon crossing $\left(\varphi_{i}\right)$ and at the end of inflation $\left(\varphi_{f}\right)$, in the case $3 \leq \alpha \leq \alpha_{*}$ with both signs of $\omega_{1}$. The $\alpha$ parameter is taken to be integer, except of the upper limit $\alpha_{*} \equiv(7+\sqrt{33}) / 2$

| $\alpha$ | 3 | 4 |  | 5 | 6 | $\alpha_{*}$ |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\operatorname{sgn}\left(\omega_{1}\right)$ | - | + | - | $+/-$ | + | - | - |
| $n_{s}$ | 0.9650 | 0.9649 | 0.9640 | 0.9639 | 0.9634 | 0.9637 | 0.9632 |
| $r$ | 0.0035 | 0.0010 | 0.0013 | 0.0007 | 0.0005 | 0.0004 | 0.0003 |
| $-\kappa \varphi_{i}$ | 5.3529 | 3.5542 | 3.9899 | 3.2657 | 3.0215 | 2.7427 | 2.5674 |
| $-\kappa \varphi_{f}$ | 0.9402 | 0.7426 | 0.8067 | 0.7163 | 0.6935 | 0.6488 | 0.6276 |

We note that the value of inflationary parameter $n_{s}$ (spectral index) for $\alpha=3$ is equal to 0.9650 and that the range of Regge slope of the following Omega meson is:
$\omega / \omega_{3}|5+3| m_{u / d}=240-345 \mid 0.937-1.000$
the values $0.954929659 \ldots$ and 0.9568666373 are very near to the above Regge slope, to the spectral index $\mathrm{n}_{\mathrm{s}}$ and to the dilaton value $0.989117352243=\phi$

We observe that 0.954929659 has the following property:
$1-24\left(\frac{1}{-1+e^{2 \pi}}+\frac{2}{-1+e^{4 \pi}}+\frac{3}{-1+e^{6 \pi}}\right)$ is a transcendental number
$=0.9549296597216129$ the result is a transcendental number

We have also that, performing the $128^{\text {th }}$ root, we obtain:
$\left(\left(\left(\left(1-24\left[\left(1 /\left(\mathrm{e}^{\wedge}(2 \mathrm{Pi})-1\right)\right)+\left(2 /\left(\mathrm{e}^{\wedge}(4 \mathrm{Pi})-1\right)\right)+\left(3 /\left(\mathrm{e}^{\wedge}(6 \mathrm{Pi})-1\right)\right)\right]\right)\right)\right)\right)^{\wedge} 1 / 128$

## Input:

$\sqrt[128]{1-24\left(\frac{1}{e^{2 \pi}-1}+\frac{2}{e^{4 \pi}-1}+\frac{3}{e^{6 \pi}-1}\right)}$

## Decimal approximation:

$0.999639771179582593534832998563472389939029398477483191618 \ldots$
$0.9996397711 \ldots$ is also a transcendental number
This result is connected to the primary decay mode of a pion, with a branching fraction of 0.999877 , that is a leptonic decay into a muon and a muon neutrino.

## Property:

$\sqrt[128]{1-24\left(\frac{1}{-1+e^{2 \pi}}+\frac{2}{-1+e^{4 \pi}}+\frac{3}{-1+e^{6 \pi}}\right)}$ is a transcendental number

## Series representations:

$$
\begin{aligned}
& \sqrt[128]{1-24\left(\frac{1}{e^{2 \pi}-1}+\frac{2}{e^{4 \pi}-1}+\frac{3}{e^{6 \pi}-1}\right)}= \\
& \left(1-24\left(\frac{1}{-1+e^{8 \sum_{k=0}^{\infty}(-1)^{k} /(1+2 k)}+\frac{3}{-1+e^{16 \sum_{k=0}^{\infty}(-1)^{k} /(1+2 k)}}+} \begin{array}{c}
\left.\frac{3}{\left.-1+e^{24 \sum_{k=0}^{\infty}(-1)^{k} /(1+2 k)}\right)}\right) \wedge(1 / 128)
\end{array}\right.\right.
\end{aligned}
$$

$\sqrt[128]{1-24\left(\frac{1}{e^{2 \pi}-1}+\frac{2}{e^{4 \pi}-1}+\frac{3}{e^{6 \pi}-1}\right)=}$

$$
\sqrt[128]{1-24\left(\frac{1}{-1+\left(\sum_{k=0}^{\infty} \frac{1}{k!}\right)^{2 \pi}}+\frac{2}{-1+\left(\sum_{k=0}^{\infty} \frac{1}{k!}\right)^{4 \pi}}+\frac{3}{-1+\left(\sum_{k=0}^{\infty} \frac{1}{k!}\right)^{6 \pi}}\right)}
$$

$\sqrt[128]{1-24\left(\frac{1}{e^{2 \pi}-1}+\frac{2}{e^{4 \pi}-1}+\frac{3}{e^{6 \pi}-1}\right)}=$

$$
\sqrt[128]{1-24\left(\frac{1}{-1+\left(\frac{1}{\sum_{k=0}^{\infty} \frac{(-1)^{k}}{k!}}\right)^{2 \pi}}+\frac{2}{-1+\left(\frac{1}{\sum_{k=0}^{\infty} \frac{(-1)^{k}}{k!}}\right)^{4 \pi}}+\frac{3}{-1+\left(\frac{1}{\sum_{k=0}^{\infty} \frac{(-1)^{k}}{k!}}\right)^{6 \pi}}\right)}
$$

## Integral representations:

$$
\begin{aligned}
& \sqrt[128]{1-24\left(\frac{1}{e^{2 \pi}-1}+\frac{2}{e^{4 \pi}-1}+\frac{3}{e^{6 \pi}-1}\right)}= \\
& \sqrt[128]{1-24\left(\frac{1}{-1+e^{4} \int_{0}^{\infty} 1 /\left(1+t^{2}\right) d t}+\frac{2}{-1+e^{8} \int_{0}^{\infty} 1 /\left(1+t^{2}\right) d t}+\frac{3}{-1+e^{12} \int_{0}^{\infty} 1 /\left(1+t^{2}\right) d t}\right)} \\
& \sqrt[128]{1-24\left(\frac{1}{e^{2 \pi}-1}+\frac{2}{e^{4 \pi}-1}+\frac{3}{e^{6 \pi}-1}\right)}= \\
& \sqrt\left[1-24\left(\frac{1}{-1+e^{4} \int_{0}^{\infty \sin (t) / t d t}}+\frac{2}{-1+e^{8} \int_{0}^{\infty \sin (t) / t d t}}+\frac{3}{\left.-1+e^{12} \int_{0}^{\infty \sin (t) / t d t}\right)}\right]{ }\right.
\end{aligned}
$$

$\sqrt[128]{1-24\left(\frac{1}{e^{2 \pi}-1}+\frac{2}{e^{4 \pi}-1}+\frac{3}{e^{6 \pi}-1}\right)}=$

$$
\sqrt[128]{1-24\left(\frac{1}{-1+e^{8} \int_{0}^{1} \sqrt{1-t^{2}} d t}+\frac{2}{-1+e^{16} \int_{0}^{1 \sqrt{1-t^{2}} d t}}+\frac{3}{-1+e^{24} \int_{0}^{1} \sqrt{1-t^{2}} d t}\right)}
$$

Performing:
$\log$ base $0.999639771179\left(\left(\left(\left(1-24\left[\left(1 /\left(\mathrm{e}^{\wedge}(2 \mathrm{Pi})-1\right)\right)+\left(2 /\left(\mathrm{e}^{\wedge}(4 \mathrm{Pi})-1\right)\right)+\left(3 /\left(\mathrm{e}^{\wedge}(6 \mathrm{Pi})-\right.\right.\right.\right.\right.\right.\right.$ 1))])))) $-\mathrm{Pi}+1 /$ golden ratio
we obtain:

## Input interpretation:

$\log _{0.099639771170}\left(1-24\left(\frac{1}{e^{2 \pi}-1}+\frac{2}{e^{4 \pi}-1}+\frac{3}{e^{6 \pi}-1}\right)\right)-\pi+\frac{1}{\phi}$
$\log _{b}(x)$ is the base- $b$ logarithm

## Result:

125.476441...
125.476441.... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for $\mathrm{T}=0$ and to the Higgs boson mass 125.18

## Series representations:

$\log _{0.0996397711790000}\left(1-24\left(\frac{1}{e^{2 \pi}-1}+\frac{2}{e^{4 \pi}-1}+\frac{3}{e^{6 \pi}-1}\right)\right)-\pi+\frac{1}{\phi}=$
$\frac{1}{\phi}-\pi-\frac{\sum_{k=1}^{\infty} \frac{\left(-24 k^{k}\left(\frac{1}{1-e^{2 \pi}}-\frac{2}{-1+e^{4 \pi}}-\frac{3}{\left.-1+e^{6 \pi}\right)^{k}}\right.\right.}{k}}{\log (0.9996397711790000)}$
$\log _{0.0996397711790000}\left(1-24\left(\frac{1}{e^{2 \pi}-1}+\frac{2}{e^{4 \pi}-1}+\frac{3}{e^{6 \pi}-1}\right)\right)-\pi+\frac{1}{\phi}=$

$$
\begin{aligned}
& \frac{1.000000000000}{\phi}-1.000000000000 \pi+ \\
& \log \left(1-24\left(\frac{1}{-1+e^{2 \pi}}+\frac{2}{-1+e^{4 \pi}}+\frac{3}{-1+e^{6 \pi}}\right)\right) \\
& \quad\left(-2775.513305165-1.000000000000 \sum_{k=0}^{\infty}(-0.0003602288210000)^{k} G(k)\right) \\
& \text { for }\left(G(0)=0 \text { and } G(k)=\frac{(-1)^{1+k} k}{2(1+k)(2+k)}+\sum_{j=1}^{k} \frac{(-1)^{1+j} G(-j+k)}{1+j}\right)
\end{aligned}
$$

And:
$\log$ base $0.999639771179\left(\left(\left(\left(1-24\left[\left(1 /\left(\mathrm{e}^{\wedge}(2 \mathrm{Pi})-1\right)\right)+\left(2 /\left(\mathrm{e}^{\wedge}(4 \mathrm{Pi})-1\right)\right)+\left(3 /\left(\mathrm{e}^{\wedge}(6 \mathrm{Pi})-\right.\right.\right.\right.\right.\right.\right.$ 1)) $])$ ))) $+11+1 /$ golden ratio
where 11 is a Lucas number

## Input interpretation:

$$
\log _{0.099639771179}\left(1-24\left(\frac{1}{e^{2 \pi}-1}+\frac{2}{e^{4 \pi}-1}+\frac{3}{e^{6 \pi}-1}\right)\right)+11+\frac{1}{\phi}
$$

## Result:

139.618034...
139.618034.... result practically equal to the rest mass of Pion meson 139.57

## Series representations:

$\log _{0.0996397711790000}\left(1-24\left(\frac{1}{e^{2 \pi}-1}+\frac{2}{e^{4 \pi}-1}+\frac{3}{e^{6 \pi}-1}\right)\right)+11+\frac{1}{\phi}=$

$$
11+\frac{1}{\phi}-\frac{\sum_{k=1}^{\infty} \frac{(-24)^{k}\left(\frac{1}{1-e^{2 \pi}}-\frac{2}{-1+e^{4 \pi}}-\frac{3}{-1+e^{6 \pi}}\right)^{k}}{k}}{\log (0.9996397711790000)}
$$

$$
\begin{aligned}
& \log _{0.0996397711790000}\left(1-24\left(\frac{1}{e^{2 \pi}-1}+\frac{2}{e^{4 \pi}-1}+\frac{3}{e^{6 \pi}-1}\right)\right)+11+\frac{1}{\phi}= \\
& 11.00000000000+\frac{1.000000000000}{\phi}+ \\
& \quad \log \left(1-24\left(\frac{1}{-1+e^{2 \pi}}+\frac{2}{-1+e^{4 \pi}}+\frac{3}{-1+e^{6 \pi}}\right)\right) \\
& \quad\left(-2775.513305165-1.000000000000 \sum_{k=0}^{\infty}(-0.0003602288210000)^{k} G(k)\right) \\
& \text { for }\left(G(0)=0 \text { and } G(k)=\frac{(-1)^{1+k} k}{2(1+k)(2+k)}+\sum_{j=1}^{k} \frac{(-1)^{1+j} G(-j+k)}{1+j}\right)
\end{aligned}
$$

In conclusion, we have shown a possible theoretical connection between some parameters of inflationary cosmology, of particle masses (Higgs boson and Pion meson $\pi \pm$ ) and some fundamental equations of Ramanujan's mathematics.

Further, we note that $\pi, \phi, 1 / \phi$ and 11 , that is a Lucas number (often in developing Ramanujan's equations we use Fibonacci and Lucas numbers), play a fundamental role in the development, and therefore, in the final results of Ramanujan's equations. This fact can be explained by admitting that $\pi, \phi, 1 / \phi$ and 11 , and other numbers connected with Fibonacci and Lucas sequences, are not only mathematical constants and / or simple numbers, but "data", which inserted in the right place, and in the most various possible and always logical combinations, lead precisely to the solutions discussed so far: masses of particles and other physical and cosmological parameters.


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