Analogies of genetic and chemical code. Supplement 1

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Abstract

In the original work, for which this is a Supplement, I presented analogies of the genetic and chemical code (Rakočević 2018b, in relation to the source work from 1991). (Further: instead of "Rakočević" I use the abbreviation "MMR".) There I gave three Tables of the Periodic System of the Elements (PSE) in which I dealt with the problem of stable and unstable elements; in the sense that an unstable element is one that possesses at least one primordially unstable isotope, while elements that do not possess such isotopes are stable. I have shown that for the number of stable and the number of unstable elements there are strict regularities and a strict law; the same law that is valid for the association of codons to more complex and to less complex amino acids in the genetic code. I have not dealt with the question of the number of stable and the number of unstable isotopes, what I do now in this Supplement. [An expanded version of the original paper whose Supplement this is: OSF Preprint DOI 10.31219/osf.io/mxecj]

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Of the three PSE Tables I gave in a previous original paper (MMR, 2018b), for which this is a Supplement, only one contains the number of natural isotopes. It is a Table with six columns, in an arrangement of 1:2:3, in the form of *monads-diads-triads*, with one, two and three columns, respectively (Table 2 in: MMR, 2018b, p. 295).¹ In this Supplement, however, for elements up to the limit of stability/instability (up to Polonium, inclusive it) (Table 1) the number of both, stable and unstable isotopes is indicated: in front of the sign "+" the number of stable, and after the sign is given number of unstable isotopes (corresponding to the notation in: MMR, 2018b, Survey 1, p. 294). Only stable isotopes in stable elements are marked with color, which we are dealing with in this research: red in *diads*, blue in *triads* and green in *monads*; the same colors are also used to mark the groups to which the elements belong in the classical PSE Table with short and/or long periods (with groups, in total: I to XIV).

¹ "This six groups PSE one can compare with the first Mendeleev's Table of PSE, with 6 groups, March 13, 1869, in: (Kedrov, 1977, p. 128-129, photocopy II); also in: (Mendeleev, 1869, reprinted in 1970)" (MMR, 2018b, p. 294). [*Additional note*: The first Table of Mendeleev was with 6 columns, as given in the cited references, and the last Table with 14 columns, as explained in the Preliminaries of MMR, 2018b. This cannot be without being indicative from several aspects, especially from the aspect of questioning for the quantities "6" and "14", for their chemical meaning. As far as I am concerned, if it were not so with Mendeleev, there would be neither this work of mine nor the works from 2018-2020 on the PSE with 6 groups and 14 columns and vice versa, listed in References.] (Cf. Footnote 10)

It makes no sense to deal with determining the number of isotopes in unstable elements (either stable or unstable isotopes), at least for now, because it is more difficult experimentally to determine the demarcation limit of stability/instability in the isotopy of unstable elements. The reason more for this impossibility could be even deeper; the same one that S. Hawking and L. Mlodinow state in the third standpoint on the possibility / impossibility of the existence of a unified theory of the Universe – Heisenberg's Uncertainty principle. [It can be expected that future researches will provide an answer to this question as well (Hawking, Mlodinow, 2005, Chapter 11th)]. However, these are questions for future research, and for the current present only the question of determining the trend of agreement of experimental results and models presented in the original paper whose Supplement is this, as well as of the findings we present in this Supplement is important (Display 1).

[*Display* 1. "In IUPAC document – IUPAC Project 2007–038-3–200, "Development of an isotopic periodic table for the educational community" (October 1, 2013 www.ciaaw.org), for Europium was indicated the state (2+0), which means that both its isotopes are stable. However, in "New interactive, electronic version of the IUPAC Periodic Table of the Elements and Isotopes" it is modified so that now it is Eu (1+1) because Eu-151 is unstable isotope and Eu-153 is stable isotope, as it is in our system in Survey 1." (Footnote 8 in: MMR, 2018b, p. 296.) (Cf. Box 1).]

As can be seen from Table 1, the number of stable isotopes in stable elements, in diads-triads-monads (in that order) is such a number that it does not indicate chaoticity² but strict regularity: it corresponds to a series of natural numbers "20-30-50-80-130", which (series) strictly corresponds to the Fibonacci sequence "2–3–5–8–13". The fact that regularities are in the question, is also indicated by the sum of number which denote groups in the Table of short and/or long periods, in the positions of stable elements (Table 2).

The arithmetical arrangement given in Table 2 is generated as follows. First, the nine "ordinary" decades of the decimal number system are added to the nine corresponding modular ones: the first to the first, the second to the second, and so on. The members of the set of "ordinary" decades are then added to the obtained sums again, but in the reverse order. Then two more operations are performed, as described in the legend of Table 2. The final result is the last column with three subcolumns. The first result in that column is: 199 - 90 = 109. And that is the result we get as the final result of adding the "number of groups" in monads, diads and triads of Table 1: 90 for monads and diads and 109 for triads, which in total is 199 (a total of six columns minus three "inner" columns equals three "outer" columns).

 $^{^{2}}$ Chaoticity would inevitably have to occur if it were the case that PSE has 18 groups, as it is in "current science", and not 14, which I insist on, and for which I give evidence. In other words, the appearance of such strict regularities confirms the accuracy of all three of our PSE Tables. Confirmation more is the distribution of stable isotopes in stable elements within the classical PSE arrangement (of course, with 14 groups) as we will show in next step (Table 3).

All these results follow, provided that the PSE contains 14 groups and not 18; that the lanthanides are distributed in each group per one, and not all 14 in the third group; that hydrogen is not in the first but only in the seventh group, as a neighbor of helium which is in the eighth group; as well as that noble gases in the calculation of the sum of the number of groups are taken as members of the eighth group, although they are at the same time a zeroth group, from the aspect of their non-reactivity (cf. Footnote 6). The result for the "group number" as we have seen is such that it strictly corresponds to a specifically generated arrangement from a series of natural numbers (Table 2).³

Box 1. The excerpt from: MMR, 2018b, p. 296

2.3. Experimental limits and an obvious trend

Having in mind the fact that the stability/instability of isotopes is *experimentally established*, it must be said that the presented 100-percent-agreement between the real state (number of stable and primordially unstable isotopes) and the models, presented in Survey 2a and 3a (in relation to Survey 3b), must be taken (and considered) only *as a trend*, which should serve for further researches in both directions: for checking experimental results, and for checking the agreement of experimental results with the theoretical models.

In support of the mentioned above, there are some examples in the current state of affairs (which may possibly spoil the above 100-percent-agreement). In relevant literature one can see that potentially three of ten isotopes of tin are radioactive, but have not been observed to decay. One of these three actually has been identified as Sn-124, and in IUPAC sources is indicated its half-life decay a little larger than 1×10^{17} years. In addition, one of the seven (stable) isotopes of Gadolinium (Gd-152) we take to be unstable with a half-life decay of 1.08×10^{14} years, while the isotope (Gd-160) with a half-life decay larger than 1.3×10^{21} remained in a stable status. Overall, we marked the isotopic state of Gadolinium (6 + 1). These are only two our interventions in relation to the IUPAC document which are, as follows from the above, also consistent with the understanding of isotopy in current science.⁸

³ The testing the consistency (balance) with a sequence of natural numbers through the ordinal number of chemical elements in PSE does not make sense, because any result to be obtained would inevitably be less obvious than immediate obviousness: one hundred percent consistency of the ordinal number of chemical elements with the series of natural numbers stems from the fact that the atom of the first element (hydrogen) contains one proton, the second two, the third three and so on.

The fact that the "chemical code"⁴, through the sum of the number of groups in the PSE, holds a connection with the series of natural numbers, speaks us of a possible unity, and not only of an analogy of these two main natural codes.⁵

In the next research step, we calculate the number of stable isotopes in the classical PSE Table (with 14 groups), according to the distribution of elements as given in the original paper (MMR, 2018b, Survey 1, p. 294). This new result, presented in Table 3, might be seen "strange" and surprising at the first glance: The number of isotopes in the upper and lower areas, then on the first diagonal (red) and the second diagonal (blue) is such that it corresponds to the sequence of even numbers: 62, 64, 66, 68. On the other hand, one might ask where did Boolean spaces⁶ come from here now, and even more – where did the division of even and odd numbers come from, both times into two classes? However, as far as we are concerned, referring to our previous results (the appearance of a four-membered sequence from a series of even natural numbers, in relation to the Fibonacci sequence of numbers) such a result can be expected. The reason for this expectation lies in the fact that we have already found an analog four-member sequence of even natural numbers, in relation to the Fibonacci sequence, just in GC (MMR, 2011b: Table 9 in relation to Table 10 and Figure 5 in relation to Figure 6). [The said Table 9 is here Table A1, and Table 10 as Table A2.]⁷

The arrangement in Table 3, corresponding to PSE groups consists of two systems, the first (above) and the second (below). The first system starts with a lower rank subsystem (L) and continues with a higher rank subsystem (H). In the second system (below) it is the other way around (Display 2).

[*Display* 2. The numbers (vertices) in n-dimensional Boolean cube, B^n (B^n), are divided into lower and higher rank numbers as follows. In lower-ranking spaces, the numbers are in this order: 0–4, 1–5 (000–100 and 001–101), and so on. In higher-ranking spaces, the numbers are in this order: 2–6, 3–7 (010–110 and 011–111, and so on. In the

⁴ "A natural code is such an essence that can be represented by an appropriate mathematical expression, which contains a sequence from the series of natural numbers within itself. From this follows that both are natural codes, the Genetic code as well as the Periodic system of chemical elements (PSE)" (MMR, 2017b, in Abstract).

 $^{^{5}}$ "In determination of the genetic code, except two inherent alphabets – 20 amino acids and four amino bases (two pyrimidines & two purines) – is involved still one 'hidden alphabet', a series of natural numbers, with all its regularities and laws" (MMR, 2011a, p.4).

⁶ "In a previous work (MMR, 1991) we proposed a hypothesis that the PSE of the short period groups corresponds to the Boolean cube as well as the PSE of the long period groups corresponds to the Boolean hypercube; the role of the 16th group in such a case (in a cyclic ordering) plays either zeroth group or the first group "(MMR, 2018b, p. 292).

⁷ The two tables and two figures we cite here concern the determination of the genetic code by the golden mean on the binary code tree. However, as this is a binary tree in direct correspondence with the Farey tree which is determined by the Fibonacci sequence, the analogy is complete (MMR, 1998, Figure 1 in relation to Figure 2). The manner how the four-membered sequence of even numbers (quartets) appears in the genetic code is shown here in Table A2 in relation to Table A1.

upper area there are 7+11=18 of stable chemical elements, and in the lower area 6+12 = 18. The group number above is 27+62 = 89 and below 30 + 80 = 110. The number of stable elements in odd groups is: 7 + 6 = 13, while the number of stable elements in even groups is 11 + 12 = 23; exactly as stated in the original paper (MMR, 2018b, Survey 3a, p. 296); and exactly (13-23) as we find in the starting position of a specific arithmetic-chemical system contained in the Genetic Code (MMR, 2020, Table 2, p. 14/6).]

By comparing Table 1 (where the relationships in PSE with 6 columns are given) and Table 3 (where the relationships in PSE with 14 columns are given) we see that the result of the distinction of the number of groups into two areas, from result 90/109 passed to result 89/110; therefore with the smallest possible change by ± 1 . [In search of the possible meaning of the choice of quantity 89/109, we wonder whether there may be a correspondence with the properties of these numbers, presented in Tables B1 and B2.] By comparing these two tables (Table 1 and Table 3), we also find an unusual inversion. In Table 1 we have that the number of groups corresponds to *the decades sequences* of the decimal number system. In contrary, in Table 3 everything is the other way around: the number of isotopes does not correspond to Fibonacci sequences but to *the quartets sequences* of the decimal number system, and the group number corresponds to Fibonacci sequences in a specific way – via Fibonacci "triangles" (result 89/110 in the last column of Table 3 compared with the same result in the third row of Table 4).

The arithmetic arrangement given in Table 4 is generated as follows. The necessary and sufficient condition for the first possible validity of the Fibonacci law is to have (in a series) the first two natural numbers. The first two natural numbers in Boolean spaces are (0,1) [*Display* 3]. By applying the Fibonacci law over them, a zeroth Fibonacci "triangle" (Fibonacci triplet) is obtained and all other as in the order indicated in the Table 4. As we can see, in the third step of a specific logical square, we find the numbers (spatial points in Boolean space) that correspond to the "Group number" for LH (89) and HL (110) of PSE, as indicated in last column of Table 3. [Table 5 is one step further in relation to Table 4, and in Tables 6, 7 and 8 the details of the relationships in the last two columns of Table 5 are presented.]

[*Display* 3: In Boolean cube B \land 3 "below" are the first four numbers from a series of even natural numbers (0,2,4,6), while "above" are the first four numbers from a series of odd natural numbers (1,3,5,7). And otherwise, when in my works on natural codes I talk about a series of natural numbers, I mean numbers in Boolean spaces, which are not really numbers in the arithmetic sense but are points in space. Hence the possible correspondence with both the points of atoms in the space of molecules and the points of chemical elements in the space of the Periodic System – both times, when with 6 and/or

with 14 columns. Hence the unfounded criticism directed at many chemists, over the decades, that they allegedly practiced numerology.]⁸

The validity of the "Neighborhood law" (Tables 4 and 5) is necessary for the origin of these two results (89 and 100): the double value of the second member of any Fibonacci triangle is equal to the sum of the third member of that triangle and the third member of the previous one. [Examples: 3 + 3 = 6 and 5 + 1 = 6; or: 13 + 13 = 26 and 21 + 5 = 26.] In order for the law to apply to the zeroth Fibonacci triangle, it is necessary the existence of the space of negative Fibonacci triangles (Table 5 in relation to Table 6).

In Tables 7 and 8 we find correspondence with 2-bit, 4-bit and 6-bit binary trees: the numbers marked in red represent one third (1/3) of the corresponding binary tree: 0-3 for the 2-bit binary tree (with 4 one-word words); 0-15 for the 4-bit binary tree (with 16 two-letter words) and 0-63 for the 6-bit binary tree (with 64 three-letter words), as found in the genetic code. No other binary tree fits this regularity. [Note: One third of the binary tree represents a half of the harmonic mean of the whole of binary tree and its half.]

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Once again, we return to the analysis of the relationship between the two sequences: sequences 62-64-66-68 in the chemical code and sequences 48-50-52-54 in the genetic code (Surveys 1-3). Given the fact that such four-member (quartet) sequences exist in natural codes, it makes sense to test the whole series of such sequences, starting from the first sequence (2-4-6-8).⁹ We are first interested in the demarcation line between that initial sequence and the sequence valid for the chemical code: 2-4-6-8 versus 62-64-66-68 (Survey 1, in relation to Survey 3); in a parallel step, we analyze the relationship of two sequences: of chemical-code and of genetic-code. As we can see, the distance between the members of the two code sequences is 14; the distance between the first and the chemical code sequence is 60; the distance between the chemical-code sequence and the last sequence in the set of two-digit numbers is 30 (Survey 2, in relation to Survey 3). Knowing that the key quantities that Mendeleev dealt with were actually these tow

⁸ Andrea I. Woody, *Department of Philosophy, University of Washington, Seattle*: "There were likely significant differences of opinion about the appropriateness of ... predictions, which could appear overly speculative and thus not properly empiricist. Indeed, reticence is not hard to imagine given the surface similarities between various codifications of periodicity in the 1860s and 1870s and numerical relations suggested in earlier decades that had been ridiculed as pieces of Pythagorean numerology. More generally, there were likely relevant differences in interests and intellectual style among the individuals involved and across the communities they inhabited" (Woody, 2014) (Cf. Footnote 10).

⁹ Of course, all the time we are talking about sequences of even numbers within a series of natural numbers. When it comes to GC, we know that this sequence has a real meaning: it is a pattern in which 20 AAs are splitting down into four types of diversity (MMR, 2011b, Figure 2, p. 822).

quantities (6 and 14)¹⁰ we can conclude that it must have something to do with each other; so, as shown in Survey 4.

On the left side of Survey 4 we have the relationships among the first quartet sequence (2-4-6-8) and the chemical code sequence (62-64-66-68), and then with the genetic code sequence (48-50-52-54). On the right side in relation to the first possible quartet sequence (2-4-6-8), two sequences are placed; the sequence (42-44-46-48) which refers to the number of atoms in 20 amino acid molecules, in their 20 "heads" (amino acid functional group: $20 \times 9 = 180$), and the sequence of the genetic code, that we have already considered so far (48-50-52-54) and concerns the number of atoms in 20 amino acid molecules, this time in their "bodies", that is, their side chains (Display 4).

[*Display 4*: Whenever a question is asked for a given number whether it can be displayed in the form of a quartet sequence, it should be divided by four, andt this implies an integer as the result of that division. In the case of 20 amino acid "heads" ($20 \times 9 = 180$), dividing by 4 gives 45. Therefore, the two inner members of the quartet sequence must be 44 and 46, and the two outer 42 and 48. Up to the quartet sequence for the number of atoms in 20 side chains we came, however, by further research, starting from the results of V. Sukhodolets' (Table A1 in relation to Table A2).]

As a result of summation, on the right side of Survey 4 the following quantities are obtained: 204, number of atoms in 20 side chains of AAs (half: 102); 180, number of atoms in 20 "heads"; a total of 384, which number is also found in Platon's Timaeus (Platon, 1970), within one of the sequences of the series 2^n (n = 0, 1, 2, 4, 8...); that is, at the very beginning of the geometric progression with quotient 2, when their harmonic and arithmetic mean are inserted between numbers 1 and 2, and then the appropriate calculations are performed (MMR, 2011b, Tab. A.2, p. 839). On the left side (below), a new sequence is given in two lines: 72–74–76–78, which also represents the chemical code sequence created by adding 20 monoisotopic elements to the already discussed sequence 62-64-66-68. The complete result for the number of isotopes (and group number) in the monoisotopic elements, that follows from Table 1, is given at the bottom

¹⁰ The first Table he made and distributed to the world's key chemists had 6 columns (Mendeleev, 1969, reprinted in 1970; Kedrov, 1977, p. 128: photocopy II), and the last one he compiled near the end of his life had 14 columns (cf. MMR, 2018b, in Preliminaries) (Footnote 1). It must be admitted here that Mendeleev, in addition to his other predictions, also predicted that PSE must exist in form with 6 columns as well as with 14 columns. This is especially important today when we know that his allegedly erroneous calculations in the manuscript Table of short periods (recorded result 37 instead of 27 and 77 instead of 67) (Kedrov, 1977, p. 128, photocopy X) are not errors but dealing with quantities that will be much later detected in the genetic code (MMR, 2008: Tab. 3, p. 4; 2009: Table A.1, p. 21; 2017c: pp. 61-62 and footnote 34). [Andrea I. Woody, *Department of Philosophy, University of Washington, Seattle*: "In its nineteenth century formulation, the periodic law expresses the empirical generalization that trends in various chemical and physical properties of the elements tend to follow a single repeating pattern with respect to increasing atomic weight. According to historical lore, the validity of the law was demonstrated originally by a series of remarkable predictions made by the discoverer, the now immortal Dmitri Mendeleev.") (Woody, 2014) (Cf. Footnote 8).]

of the Survey 4.¹¹ The outcome for the total number of isotopes in all stable isotopes of all stable elements is 150. The double value of that number (according to the sequence 72-74-76-78) is 300. However, this number also represents a single value of the sum of the number of PSE groups in which (groups) stable elements are placed (36 + 20 = 56).¹²

The quantity of "300" for me has been a "missing link" within one specific "logical square" for years: [(0) 204, (1) 220, (2) 284, (3) 300] (Table A8). On one diagonal of that square is the first pair of friendly numbers (220–284), and on the other diagonal: 204 as the number of atoms within 20 amino acid side chains; and the number 300, as discussed herein, is the "group number" and twice the number of stable isotopes, and, finally, as the difference of the number of nucleons and the number of atoms in the GC (Table 9).¹³

Prediction. From the presented "logical square" [(0) 204, (1) 220, (2) 284, (3) 300] (Table A8) and from all other research results mentioned in this Supplement, and having in mind the fact that the entire universe is built of the same chemical elements, the presented "logical square" itself must be universal. Wherever in the universe there is a planet with the same physico-chemical conditions that exist on planet Earth, or near to being the same, there is the same kind of terrestrial life, or near to being the same.

Explanation of Prediction. Terrestrial life testifies to us that its origin, duration and survival are directly conditioned by the existence of the first possible non-metallic "island" of chemical elements in the Periodic Table, in an arrangement determined by the immediate neighborhood (by the said "Neighborhood island"). The first possible non-

¹¹ Monoisotopic elements are considered as stable elements, with one stable isotope each, without primordially unstable isotopes. The only exception is Bismuth: "IUPAC Periodic Table of the Elements and Isotopes" (Google, 9.07.2020): "Radioactive isotope having a relatively long half-life $(2.0 \times 10^{19} \text{ years})$ and a characteristic terrestrial isotopic composition that contributes significantly and reproducibly to the determination of the standard atomic weight of the element in normal materials." From this statement of IUPAC, however, it follows that Bismuth is a stable monoisotopic element. As far as I am concerned, here too I was in a situation to assess the significance of the experimental result, in the same way as I did in the original work for Tin and Gadolinium (Box 1).

¹² The number 36 as the square of number 6 (the first perfect number) to be togethwr with number 56 as a double value of the number 28 (second perfect number). [Possible correspondence with the unique arithmetical arrangement is indicated in Table B3.] We found the same logic for the relationships of the number of atoms in nucleotide bases: [U 12, C 13, (14), A 15, G 16] versus the number of atoms in nucleotides: [UMP 34, CMP 35, (36), AMP 37, GMP 38] (MMR, 1997b, pp. 62-63; www.rakocevcode.rs), which all together point to the validity of the principles of similarity and self-similarity within the unity of two codes - chemical and genetic ones. (Cf. MMR, 1997a, in relation to Tab. 2 in MMR, 2019b; cf. also last column in Table 9 in this Supplement)

¹³ The said three meanings of quantity "300", as the sum of the numbers of groups in PSE in which there are stable elements; as double values of number of stable isotopes; and as differences in the number of nucleons and the number of atoms (Table 9), leads us to the conclusion that Nature mixes here "chalk and cheese" ("lime and cheese"), and at the same time attributes to codons both the meaning of "material" (amino acid molecules) and the meaning of events (start and/or stop in protein biosynthesis). I have no other explanation for all this than the one with which I ended one of my previous papers, and it comes down to the stand point that these facts again "appealed to Aristotle and to his idea of unity of form and essence" (MMR, 2004, p. 233]

metal in PSE, going from left to right (from metals to non-metals) is carbon, followed by neighbor to neighbor: nitrogen, next to it oxygen, in a diagonal neighborhood with hydrogen in the seventh group, and a vertical neighborhood with sulfur, analogous to the neighborhood of nitrogen to phosphorus.

Concluding remark. In this Supplement, I have dealt only with the "Standard Genetic Code" in relation to the chemical code, to that part of it which refers to stable chemical elements. I have not dealt with other genetic codes, of which there are quite a number today. This is because I have repeatedly pointed out in my works that these genetic codes represent only deviations from the standard, within the given degree of freedom. In a way, here we have, *mutatis mutandis*, an analogy with the chemical code, in the following sense: in the chemical code there are strict determinations and balances only for stable elements and their stable isotopes, and in the genetic code strict determinations and balances exist only within the standard genetic code, while all others have a high degree of freedom in deviations and exceptions. This applies both to the assignment of codons to amino acids as well as to the expansion of the set of canonical amino acids within GC.

In the case of codons assignment to amino acids, deviations from standard GC, in terms of exceptions are almost a well-known fact (MMR, 2018a, Box 2, p. 41). In the case of including of 21st and 22nd AAs, the problem is almost unresolved. As for me, in this regard, at least I gave a hint where "iacet lepus" (MMR, 2011b, Fig. 11, p. 835; here: Table A7). For the 21st amino acid, Selenocysteine, the place can be found, in the area marked as "less variant" AAs, where Cysteine is already found (Table A7); and for the 22nd amino acid, Pyrrolysine, it is the area of the "more variant" AAs, where Lysine is already located. In both cases, there is the space for possible other "variant" AAs, but in all such cases the balances we have presented here no longer apply: then there is a relatively high degree of freedom in deviations on the scene.¹⁴

In conclusion, I can only repeat what I concluded in one of the previous works: "The presented facts confirm the hypothesis ... that genetic code is a specific image of a specific mirror image. On the other hand, these facts also confirm the hypothesis of V. Shcherbak (1994) that the genetic code contains an analogy with quantum physics. All this goes in support of our hypothesis (Rakočević, 2004) that the genetic code, from the aspect of completeness of the system of its constituents (amino acid and nucleotide constituents), was still prebiotic complete – 20 protein amino acids and four nucleotide molecules in RNA." And, let me add, that after the results presented in this Supplement, I think that it makes no sense to talk only about the analogies of the genetic and chemical

¹⁴ I presented the basic essence of deviant genetic codes in one of the previous papers (MMR, 2018a, Box 2, p. 41). However, that was not enough for the reviewer of my next paper, but he asked me to write again (MMR, 2020, Appendix). It turns out that whatever the author writes, he must rewrite in the next paper, because the reviewer does not have time to read what has been written before.

code, but also about their unity; the unity determined by "The Spontaneous Intelligent Design", which follows from the PSE, understood as "The Chemical Code", as it is elaborated in this Supplement.¹⁵

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¹⁵ MMR, 2018a, Box 4, p. 43: "With insight into the results ... one is forced to propose a hypothesis (for further researches) that here, there really is a kind of intelligent design; not the original intelligent design, dealing with the question – intelligent design or evolution ..., which is rightly criticized. ... Here, there could be such an intelligent design, which we could call 'Spontaneous Intelligent Design' (SPID) that is consistent with that design which was presented by F. Castro-Chavez (2010, p. 718) and is also in accordance with Darwinism."

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Academia.edu:

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$\begin{array}{c ccccccccccccccccccccccccccccccccccc$				Ŧ				т			TF	UADS II				ш				Π			М	ONADS	
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	1	1	н	(2+0)	VII	2	He	(2+0)	VIII	3	Li	(2+0)	I	4	Be	(1)	п	5	в	(2+0)	ш	6	С	(2+0)	IV
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	2	7	Ν	(2+0)	V	8	0	(3+0)	VI	9	F	(1)	VII	10	Ne	(3+0)	VIII	11	Na	(1)	Ι	12	Mg	(3+0)	п
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	3	13	Al	(1)	III	14	Si	(3+0)	IV	15	Р	(1)	V	16	s	(4+0)	VI	17	C1	(2+0)	VII	18	Ar	(3+0)	VIII
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	4	19	Κ	(2+1)	Ι	20	Ca	(5+1)	п	21	Sc	(1)	III	22	Ti	(5+0)	IV	23	v	(1+1)	V	24	\mathbf{Cr}	(4+0)	VI
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	5	25	Mn	(1)	VII	26	Fe	(4+0)	VIII	27	Co	(1)	IX	28	Ni	(5+0)	Х	29	Cu	(2+0)	I	30	Zn	(5+0)	п
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	6	31	Ga	(2+0)	III	32	Ge	(4+1)	IV	33	As	(1)	v	34	Se	(5+1)	VI	35	\mathbf{Br}	(2+0)	VII	36	Kr	(6+0)	VIII
	7	37	Rb	(1+1)	Ι	38	\mathbf{Sr}	(4+0)	п	39	Υ	(1)	III	40	Zr	(4+l)	IV	41	Nb	(1)	V	42	Mo	(6+1)	VI
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	8	43	Te	(0)	VII	44	Ru	(7+0)	VIII	45	Rh	(1)	IX	46	Pd	(6+0)	х	47	Ag	(2+0)	Ι	48	Cd	(6+2)	п
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	9	49	In	(1+1)	ш	50	Sn	(9+1)	IV	51	Sb	(2+0)	v	52	Te	(6+2)	VI	53	Ι	(1)	VII	54	Xe	(8+1)	VIII
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	10	55	Cs	(1)	Ι	56	Ba	(6+1)	II	57	La	(l+l)	III	58	Ce	(4+0)	IV	59	\mathbf{Pr}	(1)	V	60	Nd	(5+2)	VI
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	11	61	\mathbf{Pm}	(0)	VII	62	Sm	(5+2)	VIII	63	Eu	(1+1)	IX	64	Gd	(6+1)	х	65	ТЪ	(1)	XI	66	Dy	(7+0)	XII
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	12	67	Ho	(1)	XIII	68	Er	(6+0)	XIV	69	Tm	(1)	Ι	70	ΥЪ	(7+0)	п	71	Lu	(1+1)	Ш	72	Hf	(5+1)	IV
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	13	73	Ta	(2+0)	V	74	W	(4+1)	VI	75	Re	(1+1)	VII	76	Os	(6+1)	VIII	77	Ir	(2+0)	IX	78	Pt	(5+1)	x
Isotope number 08 36 06 38 12 30 $(D \ 20 + M \ 30 = DM \ 50) \ (DM \ 50 + T \ 80 = DMT \ 130) \ [20, 30, 50, 80, 130]$ $[DM \ (109 - 019)] + T \ 109 = DMT \ 199$ $[DM \ (109 - 019)] + T \ 109 = DMT \ 199$ $[Outer: 3 \ columns \ \rightarrow DM \ 90 + T \ 109 \leftarrow Inner: 3 \ columns] \rightarrow 199 \ [199 - 90 = 109]$ $[199 - 90 = 109]$	14	79	Au	(1)	I	80	Hg	(7+0)	II	81	Tl	(2+0)	ш	82	РЬ	(4+0)	IV	83	Bi	(1)	v	84	Po	(0)	VI
number 00 30 00 30 12 30 $(D \ 20 + M \ 30 = DM \ 50) \ (DM \ 50 + T \ 80 = DMT \ 130) \ [20, 30, 50, 80, 130]$ $[DM \ (109 - 019)] + T \ 109 = DMT \ 199$ [Outer: 3 columns $\rightarrow DM \ 90 + T \ 109 \leftarrow Inner: 3 \ columns] \rightarrow 199 \ [199 - 90 = 109]$	Iso	tope		08				26				06				29				12				20	
$(D \ 20 + M \ 30 = DM \ 50) \ (DM \ 50 + T \ 80 = DMT \ 130) \ [20, 30, 50, 80, 130]$ $[DM \ (109 - 019)] + T \ 109 = DMT \ 199$ [Outer: 3 columns $\rightarrow DM \ 90 + T \ 109 \leftarrow Inner: 3 \ columns] \rightarrow 199 \ [199 - 90 = 109]$	nur	nber		00				30				00				30				12				30	
$(D \ 20 + M \ 30 = DM \ 50) \ (DM \ 50 + T \ 80 = DMT \ 130) \ [20, 30, 50, 80, 130]$ $[DM \ (109 - 019)] + T \ 109 = DMT \ 199$ [Outer: 3 columns $\rightarrow DM \ 90 + T \ 109 \leftarrow Inner: 3 \ columns] \rightarrow 199 \ [199 - 90 = 109]$								-		-		_			-										
[DM (109 - 019)] + T 109 = DMT 199 [Outer: 3 columns $\rightarrow DM 90 + T 109 \leftarrow Inner: 3 columns] \rightarrow 199 [199 - 90 = 109]$								(D 20 -	+ M 30	= D.	M 50) (DM :	50 +	T 80	= DI	MT 130) [20, 3	30, 5	0, 80	, 130]					
[Outer: 3 columns \rightarrow DM 90 + T 109 \leftarrow Inner: 3 columns] \rightarrow 199 [199 - 90 = 109]	[DM (109 – 019)] + T 109 = DMT 199																								
	$[\text{Outer: 3 columns} \rightarrow \text{DM 90} + \text{T 109} \leftarrow \text{Inner: 3 columns}] \rightarrow 199 [199 - 90 = 109]$																								
Group number 20 52 9 48 28 42	Gro	Troup number 20							52				9				48				28				42
		10up millioci 20																							

Table 1. Periodic system of chemical elements with 6 groups

Legend to Table 1: This Table is the same one we gave in the original paper (MMR, 2018b, Table 2, p. 295). The only difference is that here the elements are given up to the limit of stability/ instability (up to Polonium); and the isotopes are given distinctly: stable plus primordially unstable. In the lower part of Table (area without elements: AWE) there is an overview of the results of summation of the number of stable isotopes in stable elements – in monads, diads and triads (upper two rows in AWE). The sums of the number of groups in which these elements are located (middle row and bottom two rows in AWE) are also given. The result for the number of isotopes is such that it represents a correspondence with a sequence of Fibonacci numbers. The result for the sum of the number of groups ("Group number") corresponds to the result in one specific arithmetic system (Table 2).

\downarrow	\downarrow		\downarrow		î		\downarrow	î	Î	
10	19	\rightarrow	29	+	<u>90</u>	\rightarrow	119	199	- 90 =	109
20	29	\rightarrow	49	+	80	\rightarrow	129	189	- 80 =	109
30	39	\rightarrow	69	+	70	\rightarrow	139	179	- 70 =	109
40	49	\rightarrow	89	+	60	\rightarrow	149	169	- 60 =	109
50	59	\rightarrow	109	+	50	\rightarrow	159	159	- 50 =	109
60	69	\rightarrow	129	+	40	\rightarrow	169	149	- 40 =	109
70	79	\rightarrow	149	+	30	\rightarrow	179	139	- 30 =	109
80	89	\rightarrow	169	+	20	\rightarrow	189	129	- 20 =	109
90	99	\rightarrow	189	+	10	\rightarrow	<u>199</u>	119	-10=	109

Table 2. An arithmetical arrangement, specific and significant for natural coding

Legend to Table 2: The first column shows the first nine decades of the decimal number system, while the second column contains the first nine modular decades (by module 9). In the third column is their sum. Then, the first column is repeated in the opposite direction (the first column after the "+" sign). The third column plus the fourth column give the fifth column. The sixth column consists of three subcolumns: the first represents the inverted fifth column, and the second subcolumn represents the fourth column. The third subcolumn represents the difference between the first and second subcolumn. The first result thus obtained in sixth column corresponds one hundred percent to the result of the number of groups in Table 1. [Note: The change of direction in the columns is analogous to the change of the direction of the column with amino acid molecules in: (MMR, 2019a, Table 2, p. 14, in relation to Figure 4, p. 22).]

G	EN	GN	IN		G	EN	GN	IN					
Ι	3	03	6			5	10	26					
V	3	15	6		VI	3	18	11	Lower / Higher				
IX	1	09	2		Х	2	20	11	Rank (LH)				
XIII	0	0	0		XIV	1	14	06					
	(7)	27	14			(11)	62	54	89 / 68				
G	EN	GN	IN		G	EN	GN	IN					
	3	09	6		IV	5	20	18					
VII	3	21	6		VIII	6	48	25	Higher / Lower				
XI	0	0	0		XII	. 1	12	07	rank (HL)				
	(6)	30	12			(12)	80	50	110 / 62				
[EN:	[EN: 7 + 6 = 13) & (11 + 12 = 23)] (IN: 62. 64, 66, 68) [GN: (90-1) + (109 + 1) = 199]												

Table 3. The PSE group arrangement within LH and HL Boolean spaces

Legend to Table 3: The meaning of the labels is as follows: G – the group in PSE; EN – number of chemical elements in the given group; GN – "Group number" (1 x 3 = 3; 5 x 3 = 15; 9 x 1 = 9 etc.); IN – number of stable isotopes ("Isotope number"). The explanation of relationships in the text.

0	0 0	1 1	1	2	\rightarrow	3	
1	2 2	3 3	5	8	\rightarrow	13	06
2	8 8	13 13	21	34	\rightarrow	55	26
3	34 34	55 55	89	144	\rightarrow	233	110
4	144 144 	233 233	377	610	\rightarrow	987	466

Table 4. Fibonacci "triangles" (I)

Explanation in the text.

0	0 0	-1 -1	-1	-2	\rightarrow	-3		
0	0 0	1 1	1	2	\rightarrow	3	02	
1	2 2	3 <mark>3</mark>	5	8	\rightarrow	13	06	08
2	8 8	13 13	21	34	\rightarrow	55	26	32
3	34 34	55 55	89	144	\rightarrow	233	110	136
4	144 144	233 233	377	610	\rightarrow	987	466	576
5	610 610	987 987	1597	2584	\rightarrow	4181	1974	2440

 Table 5. Fibonacci "triangles" (II)

Legend to Table 5: Everything is the same as in the previous Table (Table 4), except that the zeroth triangle from the area of negative Fibonacci triangles is added here at the beginning.

 Table 6. The "hidden" Fibonacci sequence (I)

8	32	136	576	2440	
1 x 8	4 x 8	17 x 8	72 x 8	305 x 8	
1	4	17	72	305	
	3 (13	55	233	
	3 (5, 8) 1	3 (21, 34)	55 (89, 144)	233	

Legend to Table 6: The "hiding" of some members of the Fibonacci sequence over the multiples of number 8 corresponds to the "hiding" of number 50 for the number of isotopes in monads-diads-triads in Table 1: it does not appear as the quantity of any of the three possible entities but as the sum of monads and diads. (Cf. the generation of the first and the second Fibonacci triangle within Table 4, highlighted in red color.)



 Table 7. The "hidden" Fibonacci sequence (II)

Legend to Table 7: Further more detailed of the relationships shown in the previous Table 6.

1	1	2	\rightarrow	4	1
					(1, 2)
5	1	6	\rightarrow	12	3
					(5, 8)
21	5	26	\rightarrow	52	13
					(21, 34)
89	21	110	\rightarrow	220	55
					(89, 144)
377	89	466	\rightarrow	932	233
					(377, 610)
1597	377	1974	\rightarrow	3948	98 7

Table 8. The "hidden" Fibonacci sequence (III)

Legend to Table 8: Further detailing the relationships shown in the previous Table 7. (Notice that the number 220 is the first friendly number.)

				0		
F91	S31		Y ₁₀₇	C ₄₇		1443
L ₅₇	0.01		1 107	W ₁₃₀		x 6
L ₅₇	P ₄₁		H ₈₁	R ₁₀₀		8658
-			Q/2	<u> </u>		
157	T ₄₅		IN58	S31		7770
IVI75			K 72	R 100		0888
V ₄₃	A ₁₅		D59 E73	G ₀₁		8658
380	132		522	409	\rightarrow	1443
	-					
2F14			<u></u>	2C05		0006
2L13	$4S_{05}$		2Y ₁₅	1W ₁₈		0028
10			ว⊔			0496
4L ₁₃	4P ₀₈		2011 2Q11	4R17		<u>8128</u> 8658
3I ₁₃	4.7		2N ₀₈	2S ₀₅		
1M ₁₁	4108		2K ₁₅	2R ₁₇		0111 (7)
4V ₁₀	4A ₀₄		2D ₀₇ 2E ₁₀	4G ₀₁		1000 (8)
196	100		154	144	\rightarrow	594
	61 x 9 = {	549 +	594 =	= 1143		
	1	44	43 – 1143	3 = 300		

Table 9. The entity "independence" of atoms and nucleons in GCT

Legend to Table 9: Genetic Code Table with 23 amino acid molecules (above) and 61 amino acid molecules (below). In the first case, the index indicates the number of nucleons in the side chain of amino acid, and in the second case, the number of atoms. To the right are the calculations, with the indicated relations with the sum of the first four perfect numbers and the Boolean hypercube. The difference between the two systems ("chalk" and "cheese") is 300, which is the vertices "3" (in binary number system: 11) of the logical square given in Table A10.



Survey 1. Relations among specific four-member sequences of even natural numbers (I)

Legend to Survey 1: The sequence 62-64-66-68 corresponds to the number of stable isotopes in Table 3; the sequence 48-50-52-54 corresponds to the number of atoms in the amino acid molecules in GC, as shown herein in Table A2 with green color; finally, the sequence 2-4-6-8 corresponds to the number of AAs in the four amino acid types of diversity, as we presented in: MMR, 2011b, Table 8, p. 830. The correspondence with the first and second perfect numbers (6 & 28) is immediately obvious. [*Note 1*: The difference between the quartets is indicated only at the first member in both sequences (for example: 62 - 02 = 60, etc.); the difference between the sum of each of the two central members is given at the end, between the dashed lines and the two arrows (for example: 130 - 10 = 120, etc. *Note 2*: On the perfect and friendly numbers as determinants of GC see in: MMR, 2019a, Survey B2 and Footnote 15.]



Survey 2. Relations among specific four-member sequences of even natural numbers (II)

Legend to Survey 2: Everything is the same as in Survey 1, except that here the direction of the sequences is downwards, starting from the sequence 62-64-66-68 to the last in the set of two-digit natural numbers. As can be seen, the correspondence with the first and second perfect number is immediately obvious here as well.



Survey 3. Relations among specific four-member sequences of even natural numbers (III)

Legend to Survey 3: Examining the relationship of the sequence 48-50-52.54 in the genetic code and the sequence 62-64-66-68 in the chemical code, as well as in Survey 1. The only difference is that there is the direction of growth of the sequences upwards, and here downwards. As can be seen, the correspondence with the first and second perfect number is immediately obvious here as well. [About perfect and friendly numbers see in: MMR, 2018a: Footnote 10, p. 38; 2019a: Footnote 15, p. 38, then pp. 22, 23, 34, 35.]

Survey 4. Quantity relations in chemical and genetic code

02	04	06	08		02	04	06	08		
60	60	60	60		40	40	40	40	\rightarrow	60 + 40 = 100
62	64	66	68		42	44	46	48	\rightarrow	62 - 42 = 20
14	14	14	14		06	06	06	06	\rightarrow	14 & 06
48	50	52	54		48	50	52	54		(a) (a) (a)
				İ						60 = 50 + 10 40 = 50 - 10
	64 + 6	6 = 130		ĺ	· · ·	50 + 5	52 = 102		1	40 - 50 - 10
74 72	1 + 76 = 2 + 78 =	= 150 : 150 (<mark>30</mark>	0)			42+44+40 48+50+52	6+48 = 18 2+54 = 20	0 4		180 204 384
Monois	otopic el	lements:	$IN \rightarrow I$ $GN \rightarrow$	D (10 D (5)+1) + 1 1+6) +	T (10-1) = 2 T (50-6) =	20 101; [101	+ 199 =	300]	

Legend to Survey 4: A detailed explanation is given in the text. However, I would like to draw the attention to the quantity "384", which will be in a (possible) relation with the same quantity in Table B4; also to the quantity "20" which appears as the key quantity in the determination of one specific arithmetical arrangement in Table B5. Finally, the appearance of the quantity "100" in the presented way, conditioned the search for the arithmetical arrangement in the next Survey 5, which includes the quantity "130", the number of stable isotopes in 36 stable chemical elements.

Survey 5. Relations within a set of specific three-digit natural numbers

$130 + 102 = (1 \times 144) + 130 + 158 = (2 \times 144) + 102 + 158 = (2 \times 130)$	88 00
130 = 144 - 14 (144 = 12	2 x 12)
100 - 10 = 090	45 x 2
111 - 11 = 100	50 x 2
122 - 12 = 110	55 x 2
133 - 13 = 120	60 x 2
$144 - 14 = 130 \ (5^{\text{th}}/6^{\text{th}})$	65 x 2
155 - 15 = 140	70 x 2
166 - 16 = 150	75 x 2
177 - 17 = 160	80 x 2
188 - 18 = 170	85 x 2
199 - 19 = 180	90 x 2

Legend to Survey 5: The upper part shows the relations between the quantities found in Survey 3. Number 102 as half of 204 atoms in the 20 canonical AAs, in their side chains. Number 130 as the number of stable isotopes in 36 stable elements. The number 158 is the corresponding quantity in sequence 76-78-80-82, corresponding to both coding sequences (48-50-52-54 in GC and 62-64-66-68 in CC), as shown in Survey 3. The lower part shows all three-digit numbers, which in the first position (going from left to right) have the number "1", and in the second and third positions the numbers from "00" to "99". In the specific relation with numbers 10-19, the number 130 (which represents the number of stable isotopes) is the only one that is in the relation of similarity and self-similarity with numbers 5 and 6, with their order 5th and 6th from top to bottom and from bottom to top, respectively. The uniqueness of the numbers 5 and 6 is that they are only two adjacent numbers whose squares differ by 11 within the Periodic System of Numbers, in the decimal number system (MMR, 2019a, Figure A1; here: Table A4). Half of the number 130 (65) also corresponds to the said similarity and self-similarity.

10	12	14	16	·	42	44	46	48					
14	14	14	14		14	14	14	14					
24	26	28	30		56	58	60	62					
34	38	42	46		98	102	106	110					
-	→		\downarrow		Î	-	→						
			50	(144)	94								
			54	(144)	90								
			58	(144)	86								
			62	(144)	82								
			66	(144)	78								
			70	\rightarrow	74								
(34	(34 + 110 = 144), (38 + 106 = 144), (42 + 102 = 144), (46 + 98 = 144)												

Survey 6. Specific Arithmetical Natural-Code Sequences, SANCS (I)

Legend to Survey 6: The path from the first two-digit number, and its counterpart, created by increasing by Mendeleev's quantity "14", to the first members of the quartet sequence GC and quartet sequence CC, removed from the first and last row in Survey 3. Quantity "144" appears whose appearance corresponds to his appearance in the previous Survey 5 (red color).

Survey 7. Specific Arithmetical Natural-Code Sequences, SANCS (II)

						_	_	_							
48	50	52	54		56	58	60	62	64	66	68		70	72	
14	14	14	14		14	14	14	14	14	14	14		14	14	
62	64	66	68		70	72	74	76	78	80	82		84	86	
110	114	118	122		126	130	134	138	142	146	150		154	158	
	(110 +	150 =	130 x 2	2), (1	14 + 14	46 = 13	30 x 2)	, (118 -	+ 142 =	= 130 x	2), (12	2+1	138 = 13	30 x 2)	
	[48	+ 76 =	124] [(48 +	82 = 1	130),	(50 + 8	0 = 13	0), (52	+ 78 =	130), ((54 +	76 = 1	30)]	

Legend to Survey 7: The continuation of the path started in previous Survey 6, reveals a symmetrical position of quantity 130. Here, for the chemical code the middle member is selected, but in GC the middle member is not selected (Table A3 in relation to Table A4. [Tables A5 and A6 show how Table A3 is formed, in connection to Table 4.]

(1)	$1 \times 1 = 1$ 1+2 = 3	(2 x 2)	(10)	
(2)	$2 \times 2 = 4$ 2 + 3 = 5	(3 x 3)	(9)	
(3)	$3 \times 3 = 9$ 3 + 4 = 7	(4 x 4)	(8)	
(4)	<mark>4 x 4</mark> = 16 4 + 5 = 9	(5 x 5)	(7)	
(5)	$\frac{5 \times 5}{5 + 6} = 25$ 5 + 6 = 11	(6 x 6)	(6)	5 th / 6 th
(6)	<mark>6 x 6</mark> = 36 6 + 7 = 13	(7 x 7)	(5)	6 th / 5 th
(7)	7 x 7 = 49 7 + 8 = 15	(8 x 8)	(4)	
(8)	<mark>8 x 8</mark> = 64 8 + 9 = 17	(9 x 9)	(3)	
(9)	<mark>9 x 9</mark> = 81 8 + 9 = 17	(9 x 9)	(2)	
(10)	10 x 10 = 100 10 + 11 = 21	(11 x 11)	(1)	

Survey 8. Relations between square of a given number and its sums with the follower

Legend to Survey 8: In the sixth row we find the relations of the number 6 (the first perfect number) and its successor, the number 7, which boils down to 36:13, which corresponds to the number of stable chemical elements (36) and the number of their stable isotopes (130), as shown in Table 1. In addition, the specific relationship of the squares of numbers 5 and 6 and their position in the given arithmetic system is shown, which is the realization of the principle of self-similarity. [On the validity of the principle of self-similarity in GC see in: MMR, 2004, Section 7.1, p. 231.]

Additional materials

Table A1. The Sukhodolets' system of amino acidsin a 4 x 5 arrangement.

The number	The number of H atoms (in brackets) and nucleons							
G (01) 01	A (03) 15	S (03) 31	D (03)	59	C (03) 47	(13)	153	
N (04) 58	P (05) 41	T (05) 45	E(05)	73	H (05) 81	(24)	298	(59 /58)
Q (06) 72	V (07) 43	F (07) 91	M (07)	75	Y (07)107	(34)	388	569 /686
W (08)130	R (10) 100	K (10) 72	I (09)	57	L (09) 57	(46)	416	
56	9 as neutron	number an	d 686 as	pro	oton number	r!		
56	9 – 59 = 627	-117						
686 - 58 = 628								

Legend to Table A1: "The Sukhodolets' system of amino acids in a 4 x 5 arrangement (Sukhodolets, 1985): the system of 4 x 5 AAs. The shadow space: AAs with even number of hydrogen atoms (4, 6, 8, 10); the non-shadow space: AAs with odd number of hydrogen atoms (1, 3, 7, 9, 11). In brackets: number of hydrogen atoms and out of brackets the number of nucleons. Nucleon number through a specific "simulation": 569 within two outer rows, as the number of neutrons, 569, in all 20 AAs – within their side chains; and 686 nucleons within two inner rows, as the number of protons, 686, in all 20 AAs – within their side chains. ... Within 20 side chains of amino acid molecules there are 569 neutrons as well as 569 non-hydrogen protons. Within 20 side chains of amino acid molecules there are 117 hydrogen protons, what means 117 hydrogen atoms at the same time (117 = 59 + 58)" (MMR, 2011b, Table 7, p. 830). (*Additional Note*: In the original Sukhodolets' article, the number of nucleons is given in the whole amino acid molecule, but here only in the side chain.)

out	in	out	in
G (01)	N (08)	G (01)	S (05)
W (18)	Q(11)	A (04)	T (08)
A (04)	S (05)	L (13)	I (13)
C (05)	D (07)	V (10)	D (07)
P (08)	T (08)	P (08)	E (10)
H(11)	E(10)	R (17)	K (15)
V (10)	F (14)	Y (15)	F (14)
Y (15)	M (11)	W (18)	Q (11)
R (17)	K (15)	H (11)	N (08)
L (13)	I (13)	C (05)	M (11)
O 40 E 62	50 52	48 54	50 52
102	102	102	102

Table A2. Atom number within 20 side chains of AAs as a quartet of even numbers

Legend to Table A2: "Atom number within 20 side chains of AAs as a quartet of even numbers. The outer/inner amino acid pairs which follow from ...Table A1. On the left: the original order as in Table A1; on the right: the chemical order of AAs as it is explained in Section 3.3" (MMR, 2011b, Table 9, p. 830). [*Additional Note 1*: The chemical order of AAs in the two right columns represents our view of arranging the two left Sukhodolets' columns according to the chemical similarity of amino acid molecules: to have the best possible chemical "alignment" according to chemical similarity in both readings – vertical and horizontal; examples of good chemical agreement: GA, AL, LV, VP, YW, WH; LI, RK, YF, CM; examples of less good agreement: PR, HC; GS, VD etc. *Additional Note 2*: Chemical similarity is not as well arranged here as it was in the arrangement: MMR, 2019a, Tab. 2, p. 14; because there AAs were viewed as free, independent of GC, and here is their order conditioned by the previous order of AAs determined by the number of hydrogen atoms in amino acid molecules. *Additional Note 3*: The sequence 48-50-52-54 is given also in Eq. 5 in (MMR, 2011b, p. 829).]



Table A3. The natural order of protein amino acids

Legend to Table A3: The order of protein amino acids corresponding to the diagonal in the Periodic System of Numbers (Table A4): "The structure of amino acid molecules. The simplest amino acid is glycine (G) whose side chain is only one atom of hydrogen. It is followed by alanine (A) whose side chain is only one CH₃ group, which is the smallest hydrocarbon group. There are total of 16 amino acids of alanine stereochemical type ... with one CH₂ group, each between the "body" and the "head". The glycine type contains glycine (G) only; valine type contains valine and isoleucine (V, I). The last stereochemical type is proline type with proline (P) which represents the inversion of valine in the sense that the "triangle" of three CH₂ groups for the "head" is not bound by the basis, therefore not only with one but with two CH₂ groups (Popov, 1989; Rakočević & Jokić, 1996). Light tones [(G, P, V, I) (32 atoms)] & [(A, L, S, D, F) (43 atoms)]: invariant AAs; most dark tones [(K, R, W, H) (61 atoms]: most variant AAs; less dark tones [(T, E, M, C, Q, N, Y) (68 atoms)]: less variant AAs. Notice a further possibility for splitting: 1. two aliphatic AAs [(K, R) (32 atoms)], 2. two aromatic AAs [(W, H) (29 atoms)], 3. chalcogene AAs plus aromatic hydroxide derivative [(MC, TY) (39 atoms), and 4. dicarboxylic

amino acid plus two amides [(E, QN) (29 atoms). A specific calculation: less variant AAs, all aliphatic but one (Y), plus two more variant (aromatic: W, H), equals 68 + 29 = 97 atoms; invariant AAs, all aliphatic but one (F) plus two more variant (aliphatic: K, R), equals 75 + 32 = 107 atoms; if so, then: 107 - 97 = 10; 107 + 97 = 204 ..." [*Additional Note*: Generating the arrangement of AAs follows from the natural order of AAs given in Tables A5 and A6. The logic of classifications and distinctions, given by shading, is explained in Table A7.]

(-2)											-22
(-1)	-21	-20	-19	-18	-17	-16	-15	-14	-13	-12	-11
(0)	-10	-09	-08	-07	-06	-05	-04	-03	-02	-01	00
(1)	01	02	03	04	05	06	07	08	09	10	11
(2)	12	13	14	15	,∕ 16 -	17	-18	19	20	21	22
(3)	23	24	25	26 ´	27	28	29	30	31	32	33
(4)	34	35	36	37	38	39	40	41	42	43	44
(5)	45	46	47	48	49	50	<u>51</u>	52	53	54	55
(6)	56	57	58	59	60	61	62	63	64	65	66
(7)	67	68	69	70	71	72	73	74	75	76	77
(8)	78	79	80	81	82	83	84	85	86	87	88
(9)	89	90	91	92	93	94	95	96	97	98	99
(A)	A0	A1	A2	A3	A4	A5	A6	A7	A8	A9	AA
(B)	B1	B2	B3	B4	B5	B 6	B7	B8	B9	BA	BB

Table A4. The periodic system of numbers (PSN) in decimal number System

Legend to Table A4: Periodic System of numbers in decimal number system as in MMR, 2011b, Tab. 4, p. 826 and in MMR, 2019a, Table A1, p. 28.



Table A5. The atom number within 8 pairs of alaninestereochemical type of AAs.

Legend to Table A5: The excerpt from original text in MMR, 2011b, Section 2, Table 2.1, p. 823): "The atom number within 8 pairs of alanine stereochemical type of AAs. On the full line, as well as on the dotted one, there are 86 atoms; the differences 8 and 9 (9 - 8 = 1) express "the minimum change relation among the amino acids" (Swanson, 1984, p 191). The order follows from the atom number hierarchy ..." [*Additional Note*: Amino acids are read here according to the Gray code model, that is, following the edges of Boolean logic square: STLA, DEMC, etc. and so as we find them in Table 3. On the other hand, in the order of AAs according to chemical similarity (MMR, 2019a, Tab. 2 in relation to Tab. 3), AAs go through the diagonals of the logical square.]

Table A6 (on the left): The atom number within four pairs of non-alanine sterepchemical types of AAs



Table A7 (on the right): The variability of AAs with respect to their polarity

Legend to Table A6: "The atom number within four pairs of non-alanine types of AAs. The two lines have 32 atoms each. The number of amino acids must be doubled through the pairs G-G and P-P; the amino acid order comes from the atom number hierarchy" (MMR, 2011b, Tab. 2.2, p. 823).

Legend to Table A7: "The variability of AAs with respect to their polarity ..." (MMR, 2011b, Fig. 11, p. 835) (See below: Explanation of Table A7.)

Explanation of Table A7 (The excerpt from original text in: MMR, 2011b, Section 4.3, p. 834): "Now the question what is the meaning of the concepts (notions) of "invariant" or "variant". It is easy to understand why, for example, the glycine and alanine are invariant molecules; a molecule (G) with the smallest possible non-hydrocarbon side chain, and a molecule (A) with the smallest possible hydrocarbon side chain. But, it is harder to understand why valine with a propyl group as its side chain is also invariant if there is (in the nature) simpler ethyl group. The explanation is contained in Table A3. There we see the sense, meaning and meaningfulness logic of selection: after the first possible case of non-hydrocarbonicity come possible cases of hydrocarbonicity; then the first possible case of openness, then of half-cyclicity, cyclicity and branching (hence the meaning of four stereochemical types of AAs). In such a selection it has to be so as it is (and so must be anywhere in the universe). If, however, could be possible second, third etc. cases, then the invariant AAs outlined here would not be invariant. Hence it makes sense to talk not only about more or less variant, but also of more or less invariant (Table A7). The arrangement in Table A7 shows that the splitting

of AAs into two classes – variant and invariant – is not only a formality¹⁶, or just a matter of chemical structure of molecules, but also the matter of amino acid functions (polarity). In column "more" (more variant and more invariant) there are six AAs, two polar (KR) and four semi-polar (GP and HW).¹⁷ In column "less" (less variant and less invariant) there are 14 AAs, seven polar and seven non-polar. If, however, do not look at the number of molecules than at the number of atomic associations then they are seven polar and six non-polar. [The AAs leucine (L) and isoleucine (I) are one and the same atom association through the structural isomery.] Altogether, the amino acid molecule pattern expressed in A7 appears to be 4-9-6, what means: 4 semi-polar (G,P,H,W), 9 polar (K,R,T,S,D,E,Q,N,Y) and 6 non-polar (A,V,IL,C,M,F).^{*18}

¹⁶ [Footnote 16 in source paper]: The matter of formality/ non-formality is also the atom number pattern: (60 + 10), 66, (78 - 10) in relation to the pattern which follows from the golden mean determination: 60, 66, 78 as it is presented in (MMR, 1998)

¹⁷ [Footnote 17 in source paper]: Lysine (K) and arginine (R) are polar in both parameters: hydropathy and cloister energy. On the other hand glycine (G) and triptophan (W) are polar in hydropathy and non-polar in cloister energy. The histidine (H) is polar in hydropathy, but neutral in cloister energy. The P is special case: it is polar from the aspect of hydropathy, and non-polar from the aspect of polar requirement (Woese et al., 1966; Konopel'chenko and Rumer, 1975; Rakočević and Jokić, 1996, Survey 1).

¹⁸ [Footnote 18 in source paper]: As a noteworthy is the fact that the pattern 4-9-6 corresponds to the third perfect number 496.

00	02	04	06	08	10	12
11	13	15	17	19	21	23
22	24	26	28	30	32	34
11	16	21	26	31	36	41
00	05	10	15	20	25	30
44	60	76	92	108	124	140
	12	14	16	18	20	22
	23	25	27	29	31	33
	34	36	38	40	42	44
	41	46	51	56	61	66
	30	35	40	45	50	55
	140	156	172	188	204	220
	22	24	26	28	30 \	/32
	33	35	37	39	41 \	/ 43
	44	46	48	50	52	54
	66	71	76	81	86 /	\ 91
	55	60	65	70	75 /	\ 80
	220	236	252	268	284	300
	32	34	36	38	40	42
	43	45	47	49	51	53
	54	56	58	60	62	64
	91	96	101	106	111	116
	80	85	90	95	100	105
	300	316	332	348	364	380

Table A8. The source of mirror symmetry withinProtein Amino Acid System (PAAS)

Legend to Table A8. "The arrangement represents the Table of Distinct 2-5 Adding (TDA) with starting column 00-11-22-11-00 which follows from PSN (Periodic system of numbers: Table A4) in decimal number system by overlapping the real sequence of doubled the first possible triangle in Boolean space (0-1-2) with its mirror image through compression and superposition at the point "22"). In the 10th step we have a realization of the sequence (20-31-42-61-50), the same with the number of atoms in five AAs classes (20, 31, 42, 61, 50) as it is here presented: all five results in the 10th step are mirror image of the first step."

	[72 (78 – 6)] [12 x 6]				
<u>G (01)</u>	A (04)	N (08)	D (07)	\rightarrow	20	
V (10) I (13)	<u>P (08)</u> L (13)	S (05) C (05)	T (08) M (11)	\rightarrow \rightarrow	31 42	
K (15) Q (11)	R (17) E (10)	F (14) W (18)	<u>Y (15)</u> H (11)	\rightarrow \rightarrow	61 50	
51-1	51+1	51-1	51+1			
[132 (2 x 66)] [22 x 6]						

Table A9. The order of five quartets of protein amino acidsfollowing from Table A8

Legend to Table A9: "This Table follows from Table A8 and PSN (Table A4), from a doubled starting triangle from the top of the last column; triangle switched with its mirror image and superimposed: $(00-11-22/22-11-00 \rightarrow 00-11-22-11-00 \dots)$ " (MMR, 2019a, Table 3).

Table A10. The determinations on the six-bit binary tree



Legend to Table A10: The Table follows from (MMR, 1997b, Figure 7, p. 60): "The determination of the series of the numbers 0-63. When we look closely into the structure of the sequence 0-63 of the series of the natural numbers we come to the obvious and self-evident explanation of the reason why the genetic code must be six-bit code, no matter if it is the manifestation in the form of the Gray Code model (Swanson, 1984, p 188), or it is in the form of the Binary tree (Rakočević, 1998, p 284). There must be 8 codons, *i.e.* amino acid classes. The structure of the sequence 0-63 is strictly determined by third perfect number (496) and the sum consisted of the first pair of the friendly numbers (220+284). Along with this, the specific Boolean square is being made and it is the restrictive factor, in a sense that it is not possible to 'go on' any further – not ahead, not back: (0) 220+284=504; (1) 156+348=504; (2) 92+412=504; (3) 28+476=504. The key distinctions within the genetic code are obviously self-evident: entity 64 as a series of continuity (correspondent with 64 codons); entity 20 from a difference 496 - 476 = 20 (correspondent with 20 amino acids) (496, the third perfect number) *etc.*" (*Additional Note*: The Table was republished in: MMR, 2019a, p. 35.)

Backup materials

Backup materials contain information about facts that are, or could (perhaps?) be in a relationship, that is, in correspondence with the chemical and/or genetic code.

Table B1. The uniqueness of numbers 89



Table B2. The uniqueness of number 109

The reciprocal of 109 is also based on the Fibonacci series, forwards and backwards

Here's another curiousity involving the number 109, discovered and contributed (10/20/2003) by Rick Toews.

1/109 is a repeating decimal fraction with 108 characters:

.009174311926605504587155963302752293577981651376146788 990825688073394495412844036697247706422018348623<mark>853211</mark>

You can see the beginning of the Fibonacci sequence in the LAST 6 digits of the decimal equivalent of 1/109, appearing in REVERSE order starting from the END of the decimal. (i.e., 0,1,1,2,3,5, 8 appears as ...853211)

https://www.goldennumber.net/89-and-109/

28	92	156	220	284	348	412	476	
144	96	48			48	96	144	504
172	188	204	220	284	300	316	332	x 16
200	280	360	440	568	648	728	808	8064
(200+80	8 = 504	x 2) + (2	280+728	= 504 x	2)	→ 504 x	8	
44	60	76	92	108	124	140	156	8658
304	304	304	304	304	304	304	304	8064
348	364	380	396	412	428	444	460	
392	424	456	488	520	552	584	616	594
(392+61	6 = 504	x 2) + (4	124+584	= 504 x	2)	→ 504 x	8	

Table B3. The arithmetical source of atom numberin 61 amino acids (within their side chains)

Legend to Table B3: The table follows from the merging of two arithmetic arrangements, presented in Table A8 and A10, respectively. The total sum of the numbers in front of and behind the logical square: [(0) 204, (1) 220, (2) 284, (3) 300] is 8064, which is 594 less than the sum of the first four perfect numbers, and that is exactly the number of atoms in 61 amino acid molecules (cf. Table 9). The following regularity can be noticed here. There are four quantities left and right (including two members of the first friendly pair of numbers (220-284). The distances left and right of the friendly pair are: 64 in the first and 16 in the second row. Number 4 corresponds to 2-bit, number 16 4-bit and number 64 6-bit binary tree. That is analogous to the situation we have in Tables 7 and 8.

Table B4. The arithmetical source of atom	number
in 20 amino acids (within their whole mo	lecules)

48	96	144
48	96	144
\downarrow	\downarrow	\downarrow
96	192	288
	x 2	
	↓ 384	
	384	

Legend to Tab. B4: The result follows from the differences between first two rows in Tab. B3.



Table B5. The arithmetical source of the number of stable chemical elements

Legend to Tab. B5: Number of stable elements with a unique position in a unique arithmetic system: a. ordinal number; b. a sequence of even natural numbers generated in Boolean spaces; c. squares of numbers from column "b"; d. numbers in column "c" increased by 20; e. halves of the numbers in column "d"; f. differences every two numbers in column "e". The sum of the stable and unstable elements is given in the far right column: a total of 81 up to the stability / instability limit in PSE, up to Polonium. The idea of the hypothesis of the existence of a logical square within a unique arithmetic arrangement is indicated in green. Notice that the connection with the arithmetic arrangement in Table B3 is established via the limit number 172: here it is the last number, and there it is the first.