

Abstract

The formula found by Hans de Vries for the fine structure constant is very elegant and accurate but there exists no explanation for it. In this paper, I try to give an interpretation. It is also shown why we have an electromagnetic field and why we have the value for the fine structure constant.

The Hans de Vries formular :

$$\alpha = \Gamma^2 \cdot e^{-\frac{\pi^2}{2}}$$

where $\Gamma = 1 + \frac{\alpha}{(2\pi)^0} (1 + \frac{\alpha}{(2\pi)^1} (1 + \frac{\alpha}{(2\pi)^2} (1 + \dots$

Someone can proof that the HdV formular is identical to

$$\alpha = \left[\sum_{n=0}^{\infty} \frac{\alpha^n}{(2\pi)^{\binom{n}{2}}} \right]^2 \cdot e^{-\frac{\pi^2}{2}}$$

then

$$\sqrt{\alpha} = \sum_{n=0}^{\infty} \frac{\alpha^n}{(2\pi)^{\binom{n}{2}}} \cdot e^{-\frac{\pi^2}{4}} = \left(1 + 1 \cdot \frac{\alpha}{(2\pi)^0} + 1 \cdot \frac{\alpha}{(2\pi)^0} \cdot \frac{\alpha}{(2\pi)^1} + 1 \cdot \frac{\alpha}{(2\pi)^0} \cdot \frac{\alpha}{(2\pi)^1} \cdot \frac{\alpha}{(2\pi)^2} + \dots \right) \cdot e^{-\frac{\pi^2}{4}}$$

The challenge now is to interpret this formular.

The factor $e^{-\frac{\pi^2}{4}}$ looks like the expectation value of the wrapped normal distribution which is

$$\langle z \rangle = e^{i\mu - \frac{\sigma^2}{2}} = e^{-\frac{\pi^2}{4}} \quad \text{for } \mu = 0 \text{ and } \sigma = \frac{\pi}{\sqrt{2}}$$

see https://en.wikipedia.org/wiki/Wrapped_normal_distribution

And the factor

$$\left(1 + 1 \cdot \frac{\alpha}{(2\pi)^0} + 1 \cdot \frac{\alpha}{(2\pi)^0} \cdot \frac{\alpha}{(2\pi)^1} + 1 \cdot \frac{\alpha}{(2\pi)^0} \cdot \frac{\alpha}{(2\pi)^1} \cdot \frac{\alpha}{(2\pi)^2} + \dots \right)$$

looks like the series of conditional probabilities.

more concrete (details see https://en.wikipedia.org/wiki/Conditional_probability)

$$\sqrt{\alpha} = \sum_{n=1}^{\infty} P(A_1 \cap \dots \cap A_n) = \left(1 + 1 \cdot \frac{\alpha}{(2\pi)^0} + 1 \cdot \frac{\alpha}{(2\pi)^0} \cdot \frac{\alpha}{(2\pi)^1} + 1 \cdot \frac{\alpha}{(2\pi)^0} \cdot \frac{\alpha}{(2\pi)^1} \cdot \frac{\alpha}{(2\pi)^2} + \dots \right) \cdot e^{-\frac{\pi^2}{4}}$$

with

$$P(A_1 \cap \dots \cap A_n) = P(A_1) \cdot P(A_2|A_1) \cdot P(A_3|A_1 \cap A_2) \dots P(A_n|A_1 \cap \dots \cap A_{n-1}) = \frac{\alpha^{n-1}}{(2\pi)^{\binom{n-1}{2}}} \cdot e^{-\frac{\pi^2}{4}}$$

$$e^{-\frac{\pi^2}{4}} \quad \frac{\alpha}{(2\pi)^0} \quad \frac{\alpha}{(2\pi)^1} \quad \frac{\alpha}{(2\pi)^{n-2}}$$

the denominator of $\frac{\alpha}{(2\pi)^i}$ looks like the i -dimensional 'volume' of a torus therefore

the factors $\frac{1}{(2\pi)^i}$ can be seen as normalization factors.

Now if we understand what is A_1, A_2, A_3, \dots then we understand the HdV formular.

And furthermore we understand why we have an electrical charge.

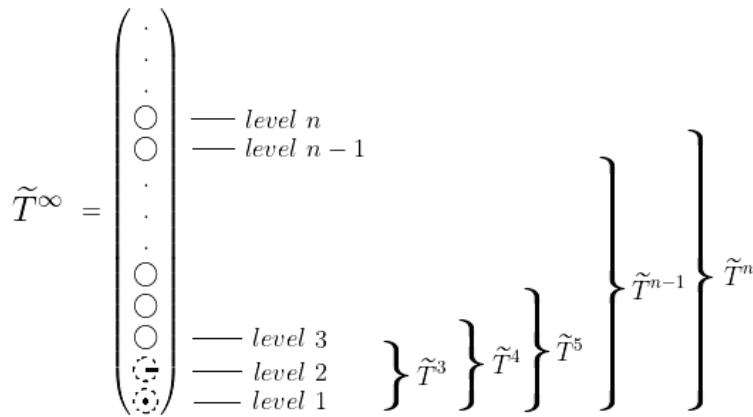
Normally a n -dimensional torus is defined as $T^n := S^1 \times \dots \times S^1 = (S^1)^n$

But in our formular we have two denominators which have the dimension of a point and a line.

Therefore we define the torus as

$$\tilde{T}^n := \{0\} \times [0, 1] \times S^1 \times \dots \times S^1 = \{0\} \times [0, 1] \times (S^1)^{n-2}$$

The infinit torus \tilde{T}^∞ then can be seen as infinit ladder.



With this geometrical picture we can explain our probability sum.

$P(\text{absorbing or emitting a photon}) = P(\pm\gamma) = \sqrt{\alpha}$ is given by the different levels of the \tilde{T}^∞ .

A photon is emitted when we climb down from one level to the prior level.

or is absorbed when we climb up on the torusladder one step from one level to the next

Our events A_1, A_2, \dots are then

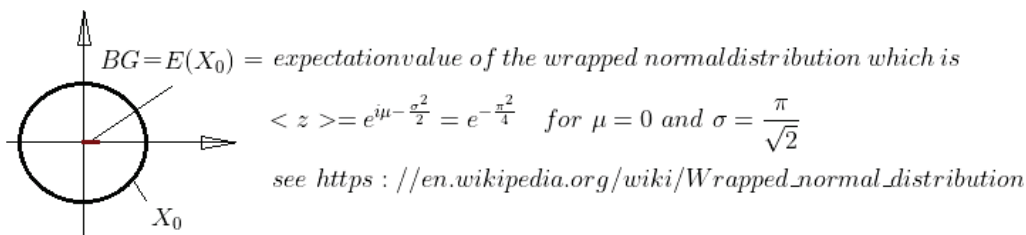
$A_1 \dots$ absorbing a photon by climbing up to level 1 from vacuum or emitting a photon by climbing down from level 1 to vacuum.

$A_2 \dots$ absorbing a photon by climbing up to level 2 from level 1 or emitting a photon by climbing down from level 2 to level 1.

and so on.

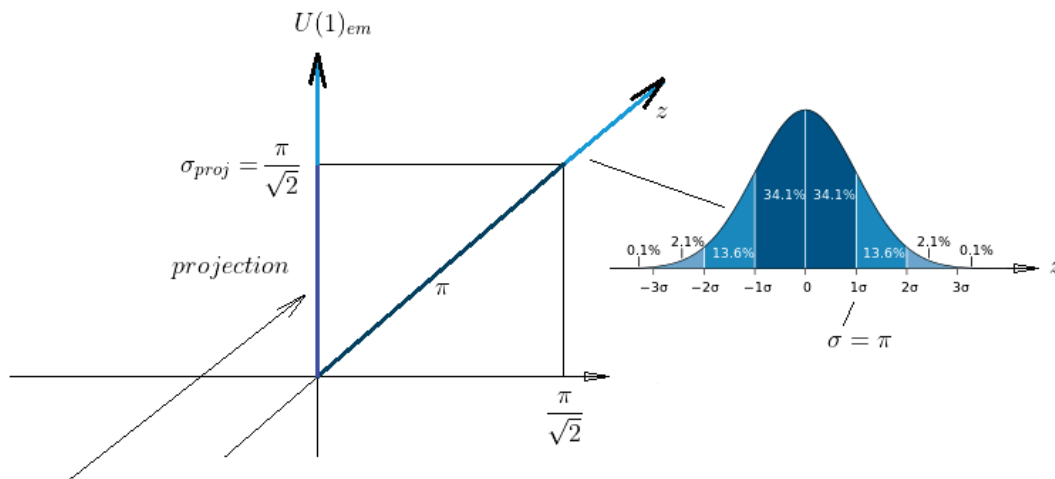
We call the factor $e^{-\frac{\pi^2}{4}}$ the Basic-Generator of the electromagnetic field (short BG).

Explanation and visualisation of the Basic Generator BG.



We write $E(X_0) = e^{-\frac{\pi^2}{4}}$ $X_0 = \{x \mid x = e^{i\theta}, 0 \leq \theta < 2\pi\}$

The factor $\frac{\pi}{\sqrt{2}}$ comes from a projection of a distribution with standard deviation $\sigma = \pi$.



the projective normaldistribution with $\sigma = \frac{\pi}{\sqrt{2}}$ then will be wrapped.

Last but not least the value for the Finestructure Constant by the Hans de Vries formular.

I have cutted the sum on $n = 100$ and calculated the result by iteration.

$$\alpha = \left[\sum_{n=0}^{\infty} \frac{\alpha^n}{(2\pi)^{\binom{n}{2}}} \right]^2 \cdot e^{-\frac{\pi^2}{2}}$$

$$\alpha \approx 0,0072973525686 \approx \frac{1}{137,035\ 999\ 096}$$

Value for α by Wikipedia

$$\alpha = 0,0072973525693(11)$$

The calculated value by the HdV formular fits very good to the empirical measurements.