MultiSet-Venn Analysis

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Abstract

This paper defines the union and intersection of multiple sets.

$$\delta_{AB}^{i} = \delta_{A}^{i} \delta_{B}^{i}$$

$$S_A \bigcup S_B = \bigcup_{i=1}^n \{ \epsilon_i \ \delta_{A \cup B}^i \}$$

$$\bigcup_{j} S_{A_{j}} = \bigcup_{i=1}^{n} \bigcup_{j=1}^{m} \left\{ \epsilon_{i} \delta_{\sum_{a=b} A_{ja} A_{jb}}^{i} + \sum_{a \neq b} \left(A_{ja} + A_{jb} \right) \right\}$$

$$S_A \cap S_B = \bigcap_{i=1}^n \{ \epsilon_i \ \delta_A^i \delta_B^i \}$$

$$S_A \cap S_B = \bigcap_{i=1}^n \left\{ \epsilon_i \delta_{AB}^i \right\}$$

$$\bigcap_{j} S_{A_{j}} = \bigcap_{i=1}^{n} \bigcap_{j=1}^{m} \left\{ \epsilon_{i} \delta_{\Pi_{j} A_{j}}^{i} \right\}$$

The top panel is the Hadamard product of a Kronecker term in Einstein notation. The middle panel is the union of two and multiple sets. Lastly, the bottom panel is the intercept of two and multiple sets.