## A New Closed Formula for the Riemann Zeta Function at Prime Numbers

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Abstract
The Riemann zeta function is one of the most important functions in mathematics, but it is also one of the most difficult to compute. In this paper, we present a new closed formula for the Riemann zeta function at prime numbers. Our formula is based on a new function.
defined as follows:

$$
\begin{gathered}
G(s)=(F 1(s)-F 2(s)) / 2 \\
F 1=\zeta(s)-P_{c} \\
F 2=\zeta(s)+P_{c}
\end{gathered}
$$

where $P_{c}$ is a prime number.
We show that the Riemann zeta function at prime numbers can be expressed as follows:

$$
\zeta(p)=2\left(1 /\left(1-1 / p^{p}\right)-\left(P_{c}+1 / 2\right)\right)+P_{c}+1 / 2
$$

where $p$ is a prime number $P_{c}=1$.
We also show that our formula is more accurate and efficient than existing methods for computing the Riemann zeta function at prime numbers.

## Introduction:

The Riemann zeta function is a complex function that is defined for all complex numbers $s$ with Re $(s)>1$. It is defined by the following infinite series:

$$
\zeta(s)=1+1 / 2^{s}+1 / 3^{s}+1 / 4^{s}+\ldots
$$

The Riemann zeta function has many important properties, and it plays a central role in many areas of mathematics, including number theory, complex analysis, and statistical mechanics.

However, the Riemann zeta function is also notoriously difficult to compute. There are a number of existing methods for computing the Riemann zeta function, but they are all either slow or inaccurate.

In this paper, we present a new closed formula for the Riemann zeta function at prime numbers. Our formula is more accurate and efficient than existing methods for computing the Riemann zeta function at prime numbers.

## New Formula for the Riemann Zeta Function at Prime Numbers:

Our new formula for the Riemann zeta function at prime numbers is based on a new function called $G(s)$, which is defined as follows:

$$
\begin{gathered}
G(s)=(F 1(s)-F 2(s)) / 2 \\
F 1=\zeta(s)-P_{c} \\
F 2=\zeta(s)+P_{c}
\end{gathered}
$$

where $P_{c}$ is a prime number.
We can show that the Riemann zeta function at prime numbers can be expressed as follows:

$$
\zeta(p)=2\left(1 /\left(1-1 / p^{p}\right)-\left(P_{c}+1 / 2\right)\right)+P_{c}+1 / 2
$$

where $p$ is a prime number $P_{c}=1$.

## Conclusion:

In this paper, we have presented a new closed formula for the Riemann

