Redefining of Atomic Units (au), the Exact Value of Planck’s Constant in au and Creation/Composition of the Universe

Gang Chen†, Tianman Chen, Tianyi Chen

Guangzhou Huifu Research Institute Co., Ltd., Guangzhou, P. R. China
7-20-4, Greenwich Village, Wangjianglu 1, Chengdu, P. R. China

†Correspondence to: gang137.chen@connect.polyu.hk

Abstract

Hartree atomic units or atomic units (au) are defined to be $\hbar = e = a_0 = m_e = 1$, and is supposed to be the scientific or natural units. In this paper, we redefine the atomic units to be $\hbar_{au} = e_{au} = a_0/au = 1$, $m_{e/au} = 1 + 1/c_{au}^4$, $m_{e+/au} = 1 - 1/c_{au}^4$, $\hbar_{au} = \hbar_{au}/(2\pi)_{au} = 1$ and $c_{au} = (2\pi)_{au} = 6.28$, in which $c_{au}$ is the speed of light in vacuum in atomic units and $c_{au} = 137.035999074626$. The new redefined atomic units could be called Hartree-Chen atomic unites and would be the real scientific or natural units especially in the sub-atomic world. In this new atomic units, the value of the Planck constant is demonstrated to be exactly 6.28. With the new atomic units, the frequencies of the original light and the subsequent light of the universe are calculated and hence a picture of creation and composition of the universe is depicted.

Keywords: atomic units, the Planck constant, the mass of electron, the mass of positron, the creation of the universe, the composition of the universe.

1. Introduction

Atomic units (au) are a system of units convenient for atomic physics, electromagnetism, and quantum electrodynamics, especially when the focus is on the properties of electrons [1]. There are two different kinds of atomic units, which one might name Hartree atomic units and Rydberg atomic units, which differ in the choice of the unit of mass and charge. This article deals with Hartree atomic units. In au, the numerical values of the following six physical constants are all unity (1) by definition:

Two properties of the electron, its mass and charge;
Two properties of the hydrogen atom, its Bohr radius and the absolute value of its electric potential energy in the ground state;

Two constants, Dirac's constant (reduced Planck constant) and Coulomb's constant.

<table>
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<th>Table 1. Fundamental Atomic Units</th>
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<td>Quantity</td>
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<td>length</td>
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<tr>
<td>mass</td>
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<td>charge</td>
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<td>angular momentum</td>
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<td>energy</td>
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<td>electrostatic force</td>
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These six quantities are not independent; to normalize all six quantities to 1, it suffices to normalize any four of them to 1. The normalizations of the Hartree energy and Coulomb's constant, for example, are only an incidental consequence of normalizing the other four quantities.

Hartree atomic units or atomic units (au):

$$\hbar_{\text{au}} = e_{\text{au}} = m_{e/\text{au}} = a_{0/\text{au}} = \frac{1}{(4\pi\epsilon_0)_{\text{au}}} = E_{h/\text{au}} = 1$$

It suffices to normalize any four of them to 1
So Hartree Atomic Units are usually expressed as:

$$\hbar_{\text{au}} = e_{\text{au}} = m_{e/\text{au}} = a_{0/\text{au}} = 1$$

reduced Planck’s constant: $\hbar_{\text{au}} = \frac{\hbar_{\text{au}}}{2\pi} = 1$

Planck's constant: $\hbar_{\text{au}} = 2\pi$

Some other atomic units are derived from the above four fundamental atomic units as follows (Table 2).

<table>
<thead>
<tr>
<th>Table 2. Derived Atomic Units</th>
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<tbody>
<tr>
<td>Quantity</td>
</tr>
<tr>
<td>Hartree energy</td>
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<tr>
<td>Coulomb's constant</td>
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<tr>
<td>atomic</td>
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<tr>
<td>velocity</td>
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Atomic units are derived from certain fundamental properties of the physical world, and are free of anthropocentric considerations, so atomic units should almost be scientific units or natural units.
2. Redefining of Hartree Atomic Units

Based on our previous papers [2-16], we suppose that Hartree atomic units should have some drawbacks and could be redefined to a more scientific or more natural system which we would name Hartree-Chen atomic units as follows.

Hartree Atomic Units:
\[ h_{au} = e_{au} = a_{0/au} = m_{e/au} = 1 \]
\[ \hbar_{au} = \frac{h_{au}}{2\pi} = 1, \ h_{au} = 2\pi \]

Hartree-Chen Atomic Units:
\[ h_{au} = e_{au} = a_{0/au} = 1 \]
\[ m_{e/au} = 1 + \frac{1}{c_{4/au}^4}, \ m_{e'/au} = 1 - \frac{1}{c_{4/au}^4} \]
\[ \hbar_{au} = \frac{h_{au}}{(2\pi)_{au}} = 1, \ h_{au} = (2\pi)_{au} = \frac{4 \times 157}{100} = 6.28 \]
\[ c_{au} = \frac{c}{v_e} = \sqrt{112 \times (168 - \frac{1}{3} + \frac{1}{12 \cdot 47} - \frac{1}{14 \cdot 112 \cdot (2173 + 1)}} = 137.035999074626 \]
\[ \sqrt{c} : \text{the speed of light in vacuum} \]
\[ v_e : \text{the line speed of the ground state electron of H atom in Bohr model} \]

Note: in sub-atomic world, \( \sqrt{2}, \sqrt{3} \) and \( \pi \) express as rational numbers as follows [14].
\[ (\sqrt{2})_{au} = \frac{3 \times 47}{100} = 1.41, \ (\sqrt{3})_{au} = \frac{173}{100} = 1.73, \ (\pi)_{au} = \frac{2 \times 157}{100} = 3.14 \]
\[ (\sqrt{2})_{au} + (\sqrt{3})_{au} = (\pi)_{au}, \ 1.41 + 1.73 = 3.14 \]
\[ (\sqrt{2})_{au} + (\sqrt{3})_{au} = (\pi)_{au}, \ (\sin \frac{\pi}{4})_{au} + (\sin \frac{\pi}{3})_{au} = (\frac{\pi}{2})_{au} \]
so: \( (2\pi)_{au} = \frac{4 \times 157}{100} = 6.28 \)

3. The Exact Value of Plank’s Constant in Hartree-Chen Atomic Units

The Planck constant or Planck’s constant \( h \) has the exact value of 6.62607015 J/Hz in SI units, and the reduced Planck constant, or Dirac constant \( \hbar \) is defined to be \( h/2\pi \). In Hartree atomic units (au), the reduced Planck constant \( h_{au} \) is 1, so in Hartree atomic units the Planck constant \( h_{au} \) should equal to \( 2\pi \). As atomic units should be the real scientific units, so \( h_{au} = 2\pi \) should be reasonable in sub-atomic world. According to ordinary mathematical and physical concepts, \( h_{au} = 2\pi \) should be an irrational number. However, in our previous paper [14], we define the natural number axis (NNA) and the
natural number coordinate system (NNCS), and suppose that in the world of nuclides, NNA-100 and NNCS-100 would be applicable, so in the world of nuclides the square root of 2, the square root of 3 and $\pi$ should become rational numbers of 1.41, 1.73 and 3.14 with the coincident proof of $1.41+1.73=3.14$. So we hypothesize that the value of the reduce Planck constant in Hartree-Chen atomic units should be exactly 6.28.

4. Creation of the Universe

In Hartree-Chen atomic units, the mass of electron is supposed to be $1+1/c^4_{au}$, and the mass of positron is supposed to be $1-1/c^4_{au}$. The reaction at the Big Bang of the universe and the subsequent annihilation could be expressed as follows [4].

Creation of the universe:

\[ 2\gamma_0 \rightarrow e + e^+ \]
\[ e + e^+ \rightarrow (m_e + m_d) + 2\gamma_1 \]

\[ m_{el.au} = 1 + \frac{1}{c^4_{au}}, \quad m_{e',\,au} = 1 - \frac{1}{c^4_{au}} \]

$\gamma_0$: the original light of the universe to create electron and positron in the Big Bang

$\gamma_1$: the subsequent light of the universe after annihilation of electron and positron

\[ \frac{m_e}{m_e + m_d} = \frac{1}{2(2\pi)^{\frac{1}{2}}} = 6.28 \]

$m_e$: mass of regular matter; $m_d$: mass of dark matter

According to $E = h\nu$ and $E = mc^2$:

\[ h\nu_{0/\text{au}} = \frac{m_{el.au} + m_{e',\,au}}{2} c^2_{au} = 1 \times c^2_{au}, \quad h\nu_{1/\text{au}} = (1 - \frac{1}{c^4_{au}}) c^2_{au} \]

$\nu_0$ is the frequency of $\gamma_0$, $\nu_1$ is the frequency of $\gamma_1$.

\[ c_{au} = \sqrt{112 \times (168 - \frac{1}{3} 12.47 - \frac{1}{14 \times 112 \times (2.173+1)})} = 137.035999074626 \]

\[ h_{au} = (2\pi)^{\frac{1}{2}} = 6.28 \]

\[ \nu_{0/\text{au}} = \frac{1 \times [112 \times (168 - \frac{1}{3} 12.47 - \frac{1}{14 \times 112 \times (2.173+1)})]}{4 \times 157 / 100} = 2990.26513413709 \]

Relationships with nuclides:
Other Explanations of $v_{0/au}$ and $v_{1/au}$:

\[
v_{0/au} = \left[5 \times (11 - \frac{1}{15} + \frac{1}{300} - \frac{1}{9 \cdot (2 \cdot 97 \cdot 173 + 1) - \frac{2 \cdot 5}{3 \cdot 7}})\right]^2 = 2990.26513413709
\]

\[
v_{0/au} = \left[5 \times (11 - \frac{1}{15} + \frac{1}{300} - \frac{1}{2 \cdot (90 - 1) \cdot (2 \cdot 3 \cdot (2 \cdot 47 + 1) - 1) + \frac{11}{3 \cdot 7}})\right]^2 = 2990.26513413709
\]

\[
v_{0/au} = \left[5 \times (11 - \frac{1}{15} + \frac{1}{300} - \frac{1}{9 \cdot (2 \cdot 49 - 1) \cdot 173 + 1} - \frac{2 \cdot 5}{3 \cdot 7})\right]^2 = 2990.26513413709
\]

\[
v_{0/au} = \left[5 \times (11 - \frac{1}{15} + \frac{1}{300} - \frac{1}{9 \cdot (2 \cdot 32 \cdot 3 + 1) \cdot 173 + 1} - \frac{2 \cdot 5}{3 \cdot 7})\right]^2 = 2990.26513413709
\]

\[
v_{1/au} = \frac{m \cdot c_{au}^2}{137.035999074626} \left(1 - \frac{1}{c_{au}^4}\right) \times \left[112 \times \left(\frac{1}{3} + \frac{1}{12 \cdot 47} - \frac{1}{14 \cdot 112 \cdot (2 \cdot 173 + 1)}\right)\right] = \frac{4 \cdot 157}{100} = 2990.26512565757
\]

\[
v_{1/au} = \left[5 \times (11 - \frac{1}{15} + \frac{1}{300} - \frac{1}{2 \cdot (3 \cdot 5 \cdot (2 \cdot 83 + 1) + 1) - 1) + \frac{11}{47}})\right]^2 = 2990.26512565757
\]

\[
v_{1/au} = \left[5 \times (11 - \frac{1}{15} + \frac{1}{300} - \frac{1}{47 \cdot (4 \cdot 3 \cdot 41 + 1)} + \frac{36}{47})\right]^2 = 2990.26512565757
\]
5. Composition of the Universe

In the above equations of the creation of the universe, \( m_r \) corresponds to the mass of regular matter in the universe, and \( m_d \) corresponds to the mass of dark matter in the universe [4].

\[
m_r + m_d = \frac{2}{c_{au}} \approx 5.67 \times 10^{-9}
\]

\[
\frac{m_r + m_d}{m_r} = (2\pi)_{au} = 6.28
\]

\[
\frac{m_r}{m_d} = \frac{0.90 \times 10^{-9}}{4.77 \times 10^{-9}}
\]

So in the universe after the Big Bang and subsequent annihilation of electron and positron, \( 0.90 \times 10^{-9} \) of regular matter and \( 4.77 \times 10^{-9} \) of dark matter survived (the original energy to create the universe is 2, and both electron mass and positron mass are very near to 1). This can explain the mystery of matter and antimatter imbalance in the universe, and can explain the composition of regular matter and dark matter in the universe (Fig. 1). And our results are consistent with the measurements.

Fig 1. Composition of the Universe

References

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Appendix I: Research and Writing History

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Note: date was recorded according to Beijing Time.