Acceleration History Breaks Symmetry Principle and Resolves the Twin Paradox

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Abstract

In this paper, we examine the symmetry of motion in special relativity and show that the 'twin paradox' resolves when considering the history of acceleration. Acceleration creates a permanent asymmetry in motion, which persists even after the acceleration stops and the objects move uniformly in inertial frames. This suggests that the apparent symmetry of motion, as described in Einstein's theory, arises largely from ignoring acceleration history. When acceleration is accounted for, the symmetry unravels, revealing a deeper asymmetry rooted in the objects' dynamic histories.

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 1 Introduction

Einstein's theory of special relativity [1], [2], [3] is based on the principle that all inertial reference frames are equally valid, meaning no frame of reference holds privilege over another. In this framework, motion is entirely relative: when observing two objects in different inertial frames, it is impossible to objectively determine which object is truly in motion and which is at rest. This symmetry of motion is a fundamental aspect of special relativity, rooted in the principle that the laws of physics remain the same in all inertial reference frames.

However, despite the logical strength of this symmetry, we propose that it may not fully reflect physical reality. Motion is always the result of a history of acceleration; therefore, a theory constrained by the limitations of inertial frames struggles to explain dynamic phenomena such as the twin paradox.

In contrast to the idealized symmetry of inertial frames, we argue that asymmetry in motion—particularly when considering the history of acceleration more accurately reflects the nature of motion.

In this paper, we will examine the reference frames in which the symmetry of motion holds and identify the conditions that may lead to deviations from it. We will explore the deeper implications of these departures from symmetry for our understanding of motion and the foundational principles of relativity.

Based on these considerations, we will demonstrate that the well-known thought experiment, the "twin paradox," ceases to be a paradox when the history of acceleration is taken into account.

 2 Acceleration history disrupts motion symmetry

The symmetry principle in special relativity states that all inertial reference frames are equivalent, and no observer in uniform motion can objectively determine who is truly "at rest" or "moving," since motion is entirely relative. This implies that, under purely inertial conditions, neither observer should be able to say with certainty who is moving faster or slower.

Nevertheless, despite this principle of symmetry, the aim of this research is to determine the conditions under which the symmetry of motion can be observed in inertial reference frames and to investigate whether nature fundamentally relies on this symmetry, or if physical reality reveals inherent asymmetries when considering factors like the history of acceleration.

Figure 1

To explore this, consider an example (Figure 1a) where two objects, A and B, are initially at rest $(v_A = v_B)$ in their respective inertial reference frames.

At some point (Figure 1b), object B undergoes acceleration due to the application of force. At this moment, the symmetry of motion between A and B is broken, as the observer on object B can physically experience (or measure) the force of acceleration. This provides direct information that their velocity has changed.

Once the acceleration stops (Figure 1c), object B resumes uniform motion, and **both A and B are once again in inertial frames**. *The symmetry principle of special relativity suggests that even in this example, after returning to inertial*

motion, neither observer should be able to objectively determine which object is moving faster or which is stationary, as motion is relative.

However, this may not necessarily be the case if we assume the following:

- Since observer B experienced acceleration, we assume that they remember that experience. Observer A, on the other hand, did not experience acceleration and therefore lacks that information.
- Let's further assume that both observers can visually observe each other's motion.

Based on this visual observation and prior knowledge of the acceleration, the observers will conclude:

- **Observer A** sees that object B is moving away. S*ince A did not experience any acceleration, they can unequivocally conclude that object B is now moving faster than object A.*
- **Observer B**, on the other hand, knows that their speed has increased compared to their previous initial speed but cannot draw a conclusion regarding the rest or motion of object A.

Given that both objects are in inertial reference frames, which should maintain symmetry, the observers' conclusions contradict the expected symmetry of motion in special relativity.

It is clear that the history of acceleration provides unequal information to the observers, disrupting the usual relativity of motion and creating an asymmetry that special relativity does not account for in purely inertial frames.

 3 Limit of relativity and asymmetrical reality

 3.1 Every motion carries with it a hidden history of acceleration

Every motion (or apparent state of rest) carries a hidden history of acceleration. By knowing this history, we can determine which object is truly moving faster or slower.

This becomes particularly straightforward when considering objects that were initially at rest before any forces acted upon them. Once the history of acceleration is known, the relationships between their speeds become clear, allowing us to determine which object is moving faster or slower with ease.

This perspective challenges the purely relativistic view of motion symmetry by highlighting the deep connection between an object's dynamic past and its current state.

 3.2 The symmetry principle is not universally valid

Relativity holds true when considering only uniformly moving objects, as long as the acceleration history remains unknown or irrelevant. However, the knowledge of an object's acceleration history is crucial for understanding its motion. *Once this history is taken into account, the pure symmetry of motion in relativity dissolves, revealing a deeper, asymmetrical reality.*

In this revised view, acceleration plays a defining role in shaping an object's future trajectory, *permanently distinguishing it from objects that have not experienced the same forces.*

 4 What does nature "remember"?

 4.1 Nature "remembers" speed, direction, but not coordinate systems

In physics, we use speed and velocity to describe motion. Speed refers to the magnitude of motion and is always positive, while velocity includes both magnitude and direction. To define direction, we rely on a coordinate system, which allows us to assign negative values to velocity depending on the chosen reference frame. But how does nature perceive this?

Nature does not recognize coordinate systems or assign significance to positive or negative velocities as we do. These values are merely human conventions tied to our frame of reference. In nature, all speeds are positive, as they reflect the magnitude of motion.

After a force acts on an object, nature retains both the speed and direction of the object's motion. In this sense, we can say that **nature "remembers" both speed and direction**. However, **nature does not prioritize any particular direction** —all directions are equally valid. What nature acknowledges is the magnitude of motion (speed) and that this motion continues in a specific direction until a new force causes a change.

 4.2 Nature "remembers" acceleration

Similar to how an observer remembers the history of an object's acceleration, it is reasonable to claim that nature also possesses some form of 'acceleration memory.'

The idea that nature 'remembers' acceleration offers a deeper understanding of the asymmetry of motion. This concept suggests that motion is not defined solely by an object's current state but is also shaped by its past. The velocity of an object following acceleration is not random; it reflects the cumulative history of all the forces that have acted upon it.

In this sense, **an object's speed becomes a direct consequence of its history of acceleration**, with nature itself 'recording' this history, embedding it as a permanent part of the object's motion through space and time.

The forces that acted on the object leave an imprint that cannot be ignored. Taking into account the history of acceleration leads to a more comprehensive understanding of motion beyond the standard relativistic framework.

 5 Time dilation depends only on speed, not velocity

Let's explore how nature treats speed and velocity in the context of the relativistic time dilation effect.

Time dilation is the phenomenon where time passes at different rates for observers moving relative to one another. The formula for time dilation is:

$$
\Delta t' = \frac{\Delta t}{\sqrt{1 - \frac{v^2}{c^2}}} \tag{1}
$$

Here, $\Delta t'$ is the time interval for an observer in motion, Δt is the proper time for an observer at rest, v is the relative velocity, and c is the speed of light.

It is evident from the formula that velocity v is squared. This effectively reduces velocity to speed in the context of time dilation. Whether v is positive or negative, squaring it results in a positive value, meaning that **time dilation depends only on the speed** of the moving object, not its direction.

When it comes to time dilation, nature doesn't "see" the direction of motion, only how fast the object is moving relative to another.

 6 The history of acceleration is the key to understanding the twin paradox

The twin paradox arises from the predictions of special relativity, specifically the symmetry of motion, where each twin observes the other as moving and expects the other's clock to run slower due to time dilation. This creates a paradox: from each twin's perspective, the other should age more slowly.

 6.1 The classic twin paradox solution

The twin paradox can be resolved within the standard framework of special relativity by recognizing that the traveling twin switches between two different inertial frames: one for the outbound journey and one for the return journey. The key point is that the traveling twin experiences acceleration when changing direction, moving from one inertial frame to another. This acceleration breaks the symmetry between the two twins because the stay-at-home twin remains in the same inertial frame throughout the journey.

The time dilation experienced by the traveling twin is more pronounced due to periods of high speed in different inertial frames, leading to the conclusion that the traveling twin ages less than the twin who stayed at home. Although time dilation is symmetric within each inertial frame, the change in frames introduces an asymmetry that resolves the paradox.

 6.2 A more natural solution to the twin paradox by including acceleration history

In this alternative solution, we do not focus on inertial reference frames. Instead, we base the explanation on the earlier discussions and the following realistic and acceptable facts:

- The twins perceive and remember their history of acceleration.
- Just like the twins, nature also "remembers" the history of acceleration, as acceleration results in a permanent increase in speed. This increase in speed remains "remembered" even after the acceleration stops.
- The twin who experiences acceleration attains a higher speed, leading to a slower passage of time relative to the twin who did not experience acceleration. This slower passage of time does not depend on the direction of the twin's movement.

The twin paradox requires two twins, A and B. We will assume that both twins remain in an area where the effects of gravity are negligible.

Let's analyze the stages involved in this paradox:

Figure 2 illustrates all the stages experienced by both twins.

1. Initial Phase: Both twins start at rest relative to each other, with an initial speed $v_A = v_B = 0$, meaning that during this phase, time passes equally for both.

2. Twin B's Journey:

- **Acceleration:** Twin B briefly accelerates and begins moving away from twin A, whose speed remains at $v_A = 0$. As twin B's speed v_B increases, time passes more slowly for him compared to twin A due to time dilation. Since twin A's speed is $v_A = 0$, the difference in velocities between the twins is $v = v_B$. Taking into account that v is the basis for calculating time dilation, as twin B accelerates and v_B increases, the time dilation effect becomes progressively more pronounced.
- **Uniform motion:** After the acceleration phase, twin B continues moving at a constant speed $v_B > 0$. According to the principles of time dilation, since twin B is moving faster, time passes more slowly for him compared to twin A, who remains at rest.
- **Deceleration Before the Turning Point:** Twin B slows down as they approach the turning point. Despite the deceleration, twin B's speed v_B is still greater than v_A , so time continues to be slowed down for twin B, although less than during the uniform motion phase.
- **Turning Point:** At the turning point, twin B comes to rest relative to twin A $(v_B = 0)$. At this moment, the relative motion between them ceases temporarily, and the passage of time is equal for both twins.

3. Twin B's Return Journey:

- **Acceleration Again:** Twin B accelerates again as they begin the return journey, moving faster than twin A, so that again $v_B > 0$, which again causes time to pass more slowly for twin B.
- **Uniform Motion:** After accelerating, twin B moves at a constant speed back toward twin A, with $v_B > 0$. Again, twin B experiences a slower time compared to twin A.
- **Deceleration Before the Meeting:** As twin B nears twin A, they decelerate. While decelerating, twin B's speed remains greater than v_A , meaning twin B's time is still dilated relative to twin A.
- **Meeting Point:** At the moment of their reunion, twin B's speed becomes equal to twin A's speed again $v_B = v_A = 0$.

Since **twin A** experienced no acceleration, they cannot claim that twin B was at rest while they were moving.

Twin B, having experienced acceleration, can assert that their speed has increased compared to their initial speed but cannot draw any conclusions about whether twin A was at rest or in motion.

This clearly highlights an asymmetry in the movement of the twins when the history of acceleration is taken into account.

Throughout the entire journey, twin B has spent more time traveling at higher speeds than twin A, who remained at rest. Since time dilation depends only on

speed (not direction), twin B's time has passed more slowly overall compared to twin A. When the two twins meet again, twin A will have aged more than twin B.

 7 Conclusion

While the symmetry principle applies under the idealized conditions of inertial frames, it does not account for real-world processes like acceleration, which play a crucial role in shaping an object's motion. It is logical to assume that every motion has its own history of acceleration.

In this sense, the symmetry of motion does not fully capture the reality of how objects move through space and time, as nature 'remembers' the history of applied forces, leaving lasting effects on motion. Although symmetry holds within the framework of special relativity, the actual physical picture is more complex, involving asymmetry introduced by the history of acceleration.

References

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