

Jones Experiment Revisited

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Abstract

In this paper an alternative explanation of the result of the Jones experiment with a rotating glass disk has been presented.

Keyword : Jones experiment.

1 SPEED OF LIGHT IN A TRANSVERSELY MOVING BODY

Let c_2 be the speed of a light ray (or a photon) in a stationary body (medium 2) and let $c_{2,m}$ be the speed of the light ray (or a photon) in the body (medium 2) when it is moving with a velocity v . Let c_1 be the velocity of the light ray (or a photon) in medium 1 and let c_o be the speed of the light ray (or a photon) in vacuum. Now let's consider a ray of light incident perpendicularly on the interface of a body (medium 2) moving with a velocity v in a direction perpendicular to the direction of the incident light.

$$\begin{aligned} & \left| \mathbf{c}_{2,m} - \mathbf{v} \right|^2 - \left| \frac{c_o}{c_1} \mathbf{c}_1 - \mathbf{v} \right|^2 = c_2^2 - c_o^2 \\ \Rightarrow & \left[c_{2,m}^2 + v^2 - 2c_{2,m}v \cos(90^\circ - \theta) \right] - \left[c_o^2 + v^2 - 2c_o v \cos 90^\circ \right] = c_2^2 - c_o^2 \\ \Rightarrow & \left[c_{2,m}^2 + v^2 - 2c_{2,m}v \sin \theta \right] - \left[c_o^2 + v^2 \right] = c_2^2 - c_o^2 \\ \Rightarrow & c_{2,m}^2 - (2v \sin \theta)c_{2,m} - c_2^2 = 0 \quad (i) \\ \Rightarrow & c_{2,m} = \frac{2v \sin \theta + \sqrt{4v^2 \sin^2 \theta + 4c_2^2}}{2} = v \sin \theta + \sqrt{v^2 \sin^2 \theta + c_2^2} \\ \Rightarrow & c_{2,m} = v \sin \theta + c_2 \left[1 + \left(\frac{v \sin \theta}{c_2} \right)^2 \right]^{\frac{1}{2}} \end{aligned}$$

2 SPEED HYPOTHESIS

Let the speed of a light ray (or a photon), in a moving body (medium 2), along the x direction

$$c_{2,m,x} = \left(\frac{\beta_2}{\mu_2} \right)^k 2v \quad \left[\beta_2 = \frac{c_2}{c_o} ; k > 0 \right]$$

Now from (i), we have

$$c_{2,m}^2 - (2v \sin \theta) c_{2,m} - c_2^2 = 0$$

$$\Rightarrow c_{2,m}^2 = 2v c_{2,m} \sin \theta + c_2^2$$

$$\Rightarrow c_{2,m,x}^2 + c_{2,m,y}^2 = 2v c_{2,m} \sin \theta + c_2^2$$

$$\Rightarrow c_{2,m,x}^2 + c_{2,m,y}^2 = 2v c_{2,m,x} + c_2^2 \quad [c_{2,m} \sin \theta = c_{2,m,x}]$$

$$\Rightarrow \left(\frac{\beta_2}{\mu_2} \right)^{2k} 4v^2 + (c_2 + \Delta c_{2,y})^2 = \left(\frac{\beta_2}{\mu_2} \right)^k 4v^2 + c_2^2 \quad \left[c_{2,m,x} = \left(\frac{\beta_2}{\mu_2} \right)^k 2v \right]$$

$$\Rightarrow (\Delta c_{2,y})^2 + 2c_2 \Delta c_{2,y} = \left(\frac{\beta_2}{\mu_2} \right)^k \left[1 - \left(\frac{\beta_2}{\mu_2} \right)^k \right] 4v^2 = b_k^2 \quad (\text{let})$$

$$\Rightarrow (\Delta c_{2,y})^2 + 2c_2 \Delta c_{2,y} - b_k^2 = 0$$

$$\Rightarrow \Delta c_{2,y} = \frac{-2c_2 + \sqrt{4c_2^2 + 4b_k^2}}{2} = -c_2 + \sqrt{c_2^2 + b_k^2}$$

$$\Rightarrow \Delta c_{2,y} = c_2 \left[\sqrt{\left(1 + \frac{b_k^2}{c_2^2} \right)} - 1 \right]$$

$$\Rightarrow \tan \theta = \frac{c_{2,m,x}}{c_2 + \Delta c_{2,y}} = \frac{\left(\frac{\beta_2}{\mu_2} \right)^k 2v}{c_2 + c_2 \left[\sqrt{\left(1 + \frac{b_k^2}{c_2^2} \right)} - 1 \right]} = \frac{2v}{c_2} \times \frac{\left(\frac{\beta_2}{\mu_2} \right)^k}{\sqrt{\left(1 + \frac{b_k^2}{c_2^2} \right)}}$$

$$\Rightarrow c_{2,m} = \sqrt{(c_{2,m,x})^2 + (c_2 + \Delta c_{2,y})^2} = \sqrt{\left(\frac{\beta_2}{\mu_2} \right)^{2k} 4v^2 + \left(1 + \frac{b_k^2}{c_2^2} \right) c_2^2}$$

$$\Rightarrow c_{2,m} = \sqrt{\left(\frac{\beta_2}{\mu_2} \right)^{2k} 4v^2 + \left(c_2^2 + \left(\frac{\beta_2}{\mu_2} \right)^k \left[1 - \left(\frac{\beta_2}{\mu_2} \right)^k \right] 4v^2 \right)} = \sqrt{\left(\frac{\beta_2}{\mu_2} \right)^k 4v^2 + c_2^2}$$

The coefficient of restitution for the x direction

$$e_x = \frac{c_{2,m,x} - v}{v} = \frac{c_{2,m,x}}{v} - 1 = 2 \left(\frac{\beta_2}{\mu_2} \right)^k - 1$$

Now the loss in kinetic energy is given as

$$|\Delta KE| = \frac{1}{2} \frac{m_a m_b}{m_a + m_b} (u_a - u_b)^2 (1 - e^2)$$

So the loss in kinetic energy in the x direction

$$|\Delta KE_x| = \frac{1}{2} \frac{m_2 m_p}{m_2 + m_p} (v - 0)^2 (1 - e_x^2)$$

$$\Rightarrow |\Delta KE_x| = \frac{1}{2} m_p v^2 (1 - e_x^2) \quad [m_p \ll m_2]$$

So the gain in kinetic energy in the y direction

$$|\Delta KE_y| = |\Delta KE_x|$$

$$\Rightarrow \frac{1}{2} m_p [(c_2 + \Delta c_{2,y})^2 - c_2^2] = \frac{1}{2} m_p v^2 (1 - e_x^2)$$

$$\Rightarrow [(\Delta c_{2,y})^2 + 2c_2 \Delta c_{2,y}] = v^2 (1 - e_x^2)$$

$$\Rightarrow (\Delta c_{2,y})^2 + 2c_2 \Delta c_{2,y} - v^2 (1 - e_x^2) = 0$$

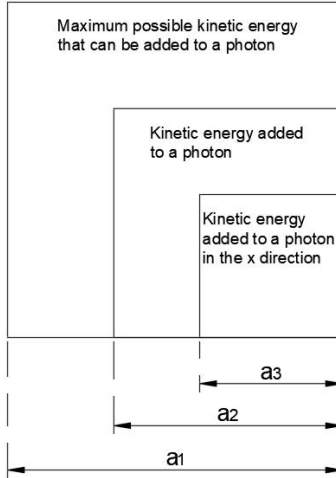
$$\Rightarrow \Delta c_{2,y} = \frac{-2c_2 + \sqrt{4c_2^2 + 4v^2(1 - e_x^2)}}{2} = -c_2 + \sqrt{c_2^2 + v^2(1 - e_x^2)}$$

$$\Rightarrow \Delta c_{2,y} = c_2 \left[\sqrt{\left(1 + \frac{v^2}{c_2^2} (1 - e_x^2) \right)} - 1 \right]$$

$$\Rightarrow \Delta c_{2,y} = c_2 \left[\sqrt{\left(1 + \frac{v^2}{c_2^2} \left(1 - \left(2 \left(\frac{\beta_2}{\mu_2} \right)^k - 1 \right)^2 \right) \right)} - 1 \right]$$

$$\Rightarrow \Delta c_{2,y} = c_2 \left[\sqrt{\left(1 + \frac{b_k^2}{c_2^2} \right)} - 1 \right]$$

3 ENERGY DIAGRAM



$$a_1 = \sqrt{\left(\frac{1}{2}m_p\right)} 2v$$

$$a_2 = \sqrt{\left(\frac{1}{2}m_p\right)} \left(\frac{\beta_2}{\mu_2}\right)^{\frac{k}{2}} 2v$$

$$a_3 = \sqrt{\left(\frac{1}{2}m_p\right)} \left(\frac{\beta_2}{\mu_2}\right)^k 2v$$

4 JONES EXPERIMENT

For light traversing a glass disk of 2.465 cm thickness and refractive index 1.524 at an operating radius of 13.75 cm, when the disk is reversed from +1501.9 to -1501.9 rev/min the displacement observed is 6.2 nm approximately, i.e., $\Delta = 6.2$ nm.

$$\Rightarrow \tan \theta = \frac{\left(\frac{\Delta}{2}\right)}{0.02465}$$

$$\Rightarrow \frac{\Delta}{2} = 0.02465 \times \tan \theta$$

$$\Rightarrow 3.1 \times 10^{-9} = 0.02465 \times \frac{2v}{c_2} \times \frac{\left(\frac{\beta_2}{\mu_2}\right)^k}{\sqrt{\left(1 + \frac{b_k^2}{c_2^2}\right)}}$$

$$\Rightarrow 3.1 \times 10^{-9} \approx 0.02465 \times \frac{2v}{c_2} \times \left(\frac{\beta_2}{\mu_2}\right)^k \quad \left[\frac{b_k^2}{c_2^2} \ll 1\right]$$

$$\Rightarrow 3.1 \times 10^{-9} \approx 0.02465 \times \frac{2 \times \left[\left(\frac{1501.9}{60}\right) \times 2\pi \times 0.1375\right]}{(\beta_2 \times 3 \times 10^8)} \times \left(\frac{\beta_2}{1.524}\right)^k$$

$$\Rightarrow 3.1 \times 10^{-9} \approx 3.55 \times 10^{-9} \times \frac{\beta_2^{k-1}}{1.524^k}$$

$$\Rightarrow \frac{\beta_2^{k-1}}{1.524^k} \approx 0.873$$

Let's assume

$$\beta_2 = \frac{1}{\mu_2} = \frac{1}{1.524}$$

$$\Rightarrow \frac{1}{1.524^{2k-1}} \approx 0.873$$

$$\Rightarrow k \approx 0.66 \approx \frac{2}{3}$$

5 CONCLUSION

Since β_2 need not be equal to $1/\mu_2$, Jones experiment needs to be performed again with water in a rotating transparent cylinder. By using $\mu_w = 4/3$ and $\beta_w = 0.7$ (as obtained via the Fizeau experiment with moving water), the precise value of k can be obtained.

References

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2. R.V. Jones, “‘*Fresnel Aether Drag’ in a Transversely Moving Medium*”, *Proceedings of the Royal Society of London, Series A, Mathematical and Physical Sciences, Vol. 328, 1972.*